

101. Travelling salesman problem

AIM: to find the shortest distance.

Program:

```
from itertools import permutations
```

```
def tsp_brute_force(graph, start):
```

```
    all_cities = set(graph.keys())
```

```
    all_cities.remove(start)
```

```
    min_distance = float('inf')
```

```
    optimal_path = None
```

```
    for path in permutations(all_cities):
```

```
        path = (start,) + path + (start,)
```

```
        distance = sum(graph[path[i]][path[i + 1]] for i in range(len(path) - 1))
```

```
        if distance < min_distance:
```

```
            min_distance = distance
```

```
            optimal_path = path
```

```
    return optimal_path, min_distance
```

Example Usage

```
graph = {
```

```
    'A': {'B': 10, 'C': 15, 'D': 20},
```

```
    'B': {'A': 10, 'C': 35, 'D': 25},
```

```
    'C': {'A': 15, 'B': 35, 'D': 30},
```

```
'D': {'A': 20, 'B': 25, 'C': 30}
}
start_city = 'A'
optimal_path, min_distance = tsp_brute_force(graph, start_city)
print(f"Optimal Path: {optimal_path}, Minimum Distance: {min_distance}")
```

Output:

```
Optimal Path: ('A', 'B', 'D', 'C', 'A'), Minimum Distance: 80
=== Code Execution Successful ===
```

Time complexity:

$O(n^2 \cdot 2^n)$