

106. optimal binomial search tree

Program:

```
def optimal_bst(keys, freq):  
    n = len(keys)  
    cost = [[0 for _ in range(n)] for _ in range(n)]  
  
    for i in range(n):  
        cost[i][i] = freq[i]  
  
    for L in range(2, n+1):  
        for i in range(n-L+1):  
            j = i + L - 1  
            cost[i][j] = float('inf')  
            for r in range(i, j+1):  
                c = cost[i][r-1] if r > i else 0  
                c += cost[r+1][j] if r < j else 0  
                c += sum(freq[i:j+1])  
                if c < cost[i][j]:  
                    cost[i][j] = c  
  
    return cost[0][n-1]  
  
keys = [10, 12, 20]  
freq = [34, 8, 50]  
print("Cost of optimal BST:", optimal_bst(keys, freq))  
OUTPUT:
```

```
Cost of optimal BST: 142
```

```
=== Code Execution Successful ===
```

Time complexity: $O(N*N)$