

A Series of Unfortunate Events in Complex Networks

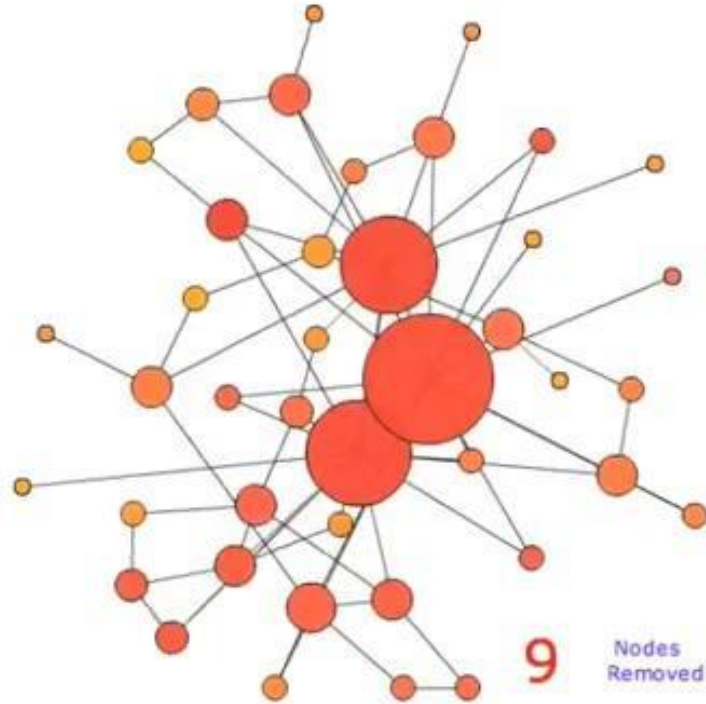
Robustness Metrics for Cascading Failures

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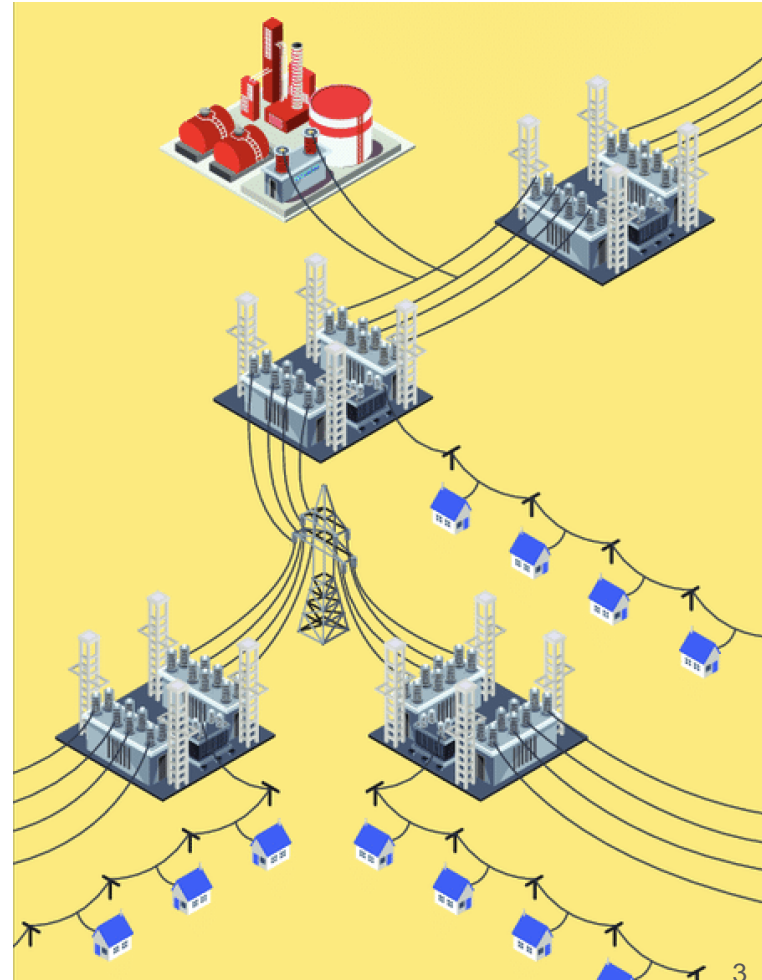
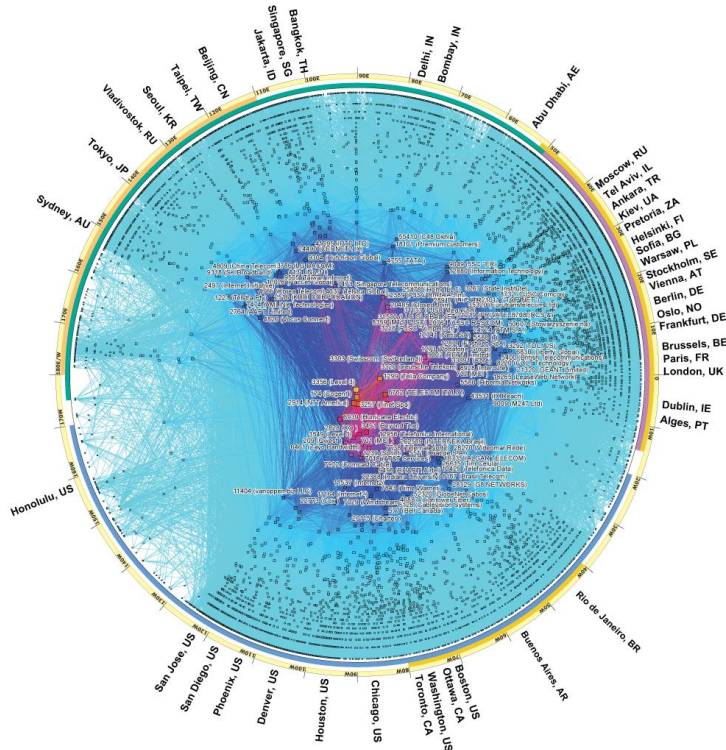
Removing nodes one by one

Real-world networks are
robust to random failures

For targeted attacks,
removing a minimal amount
of nodes cripples the
network.



Networks as transportation systems



The Motter-Lai Model

$$C_i = (1 + \alpha)L_i^0, \quad i = 1, 2, \dots, N$$

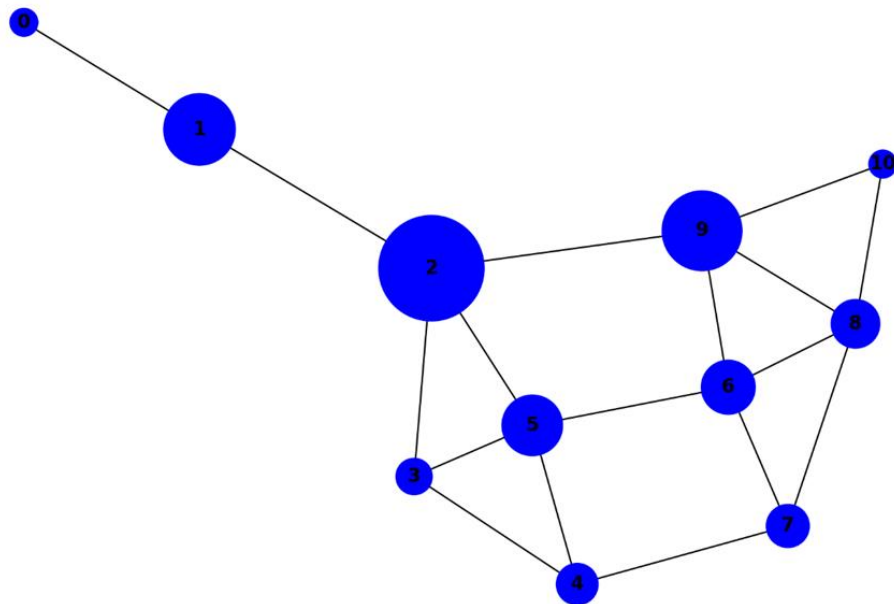
$$L_i^t > C_i \implies$$



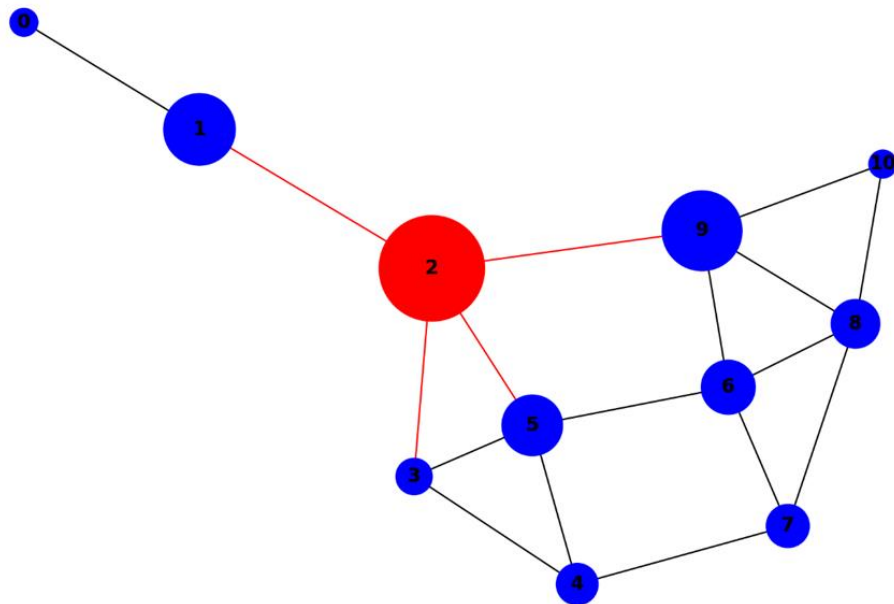
How to choose the initial node to attack?

- Random
- Degree
- Betweenness Centrality (Load)
- Clustering Coefficient

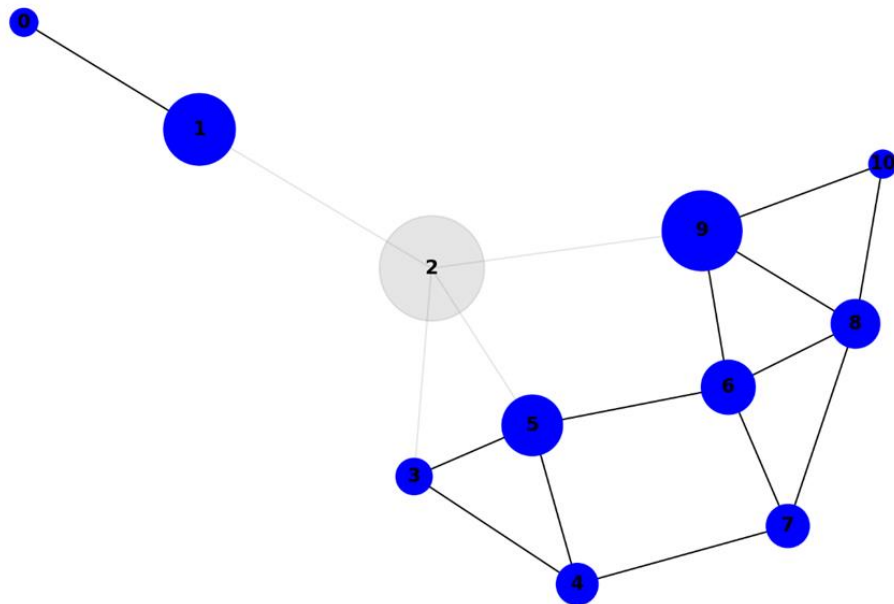
Algorithm



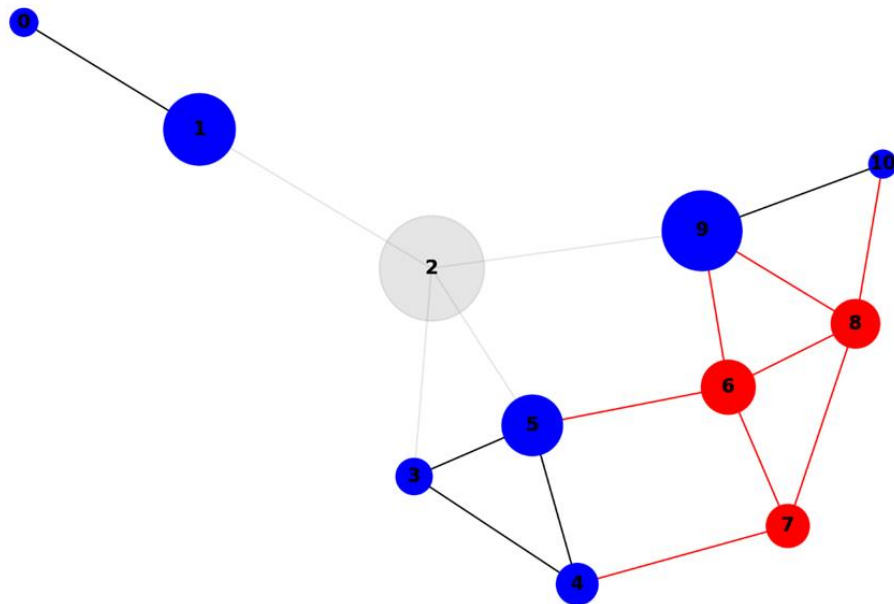
Algorithm



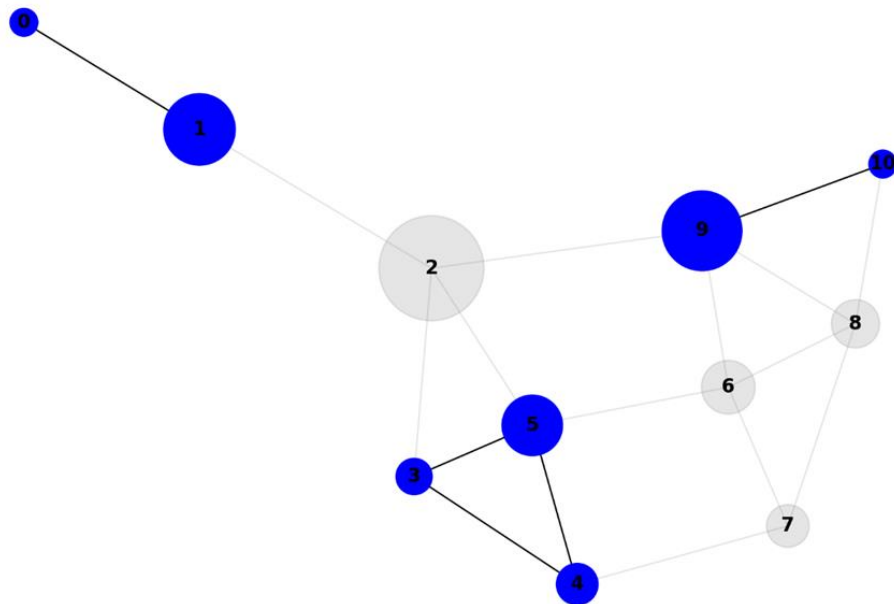
Algorithm



Algorithm



Algorithm



The Giant Component Metric

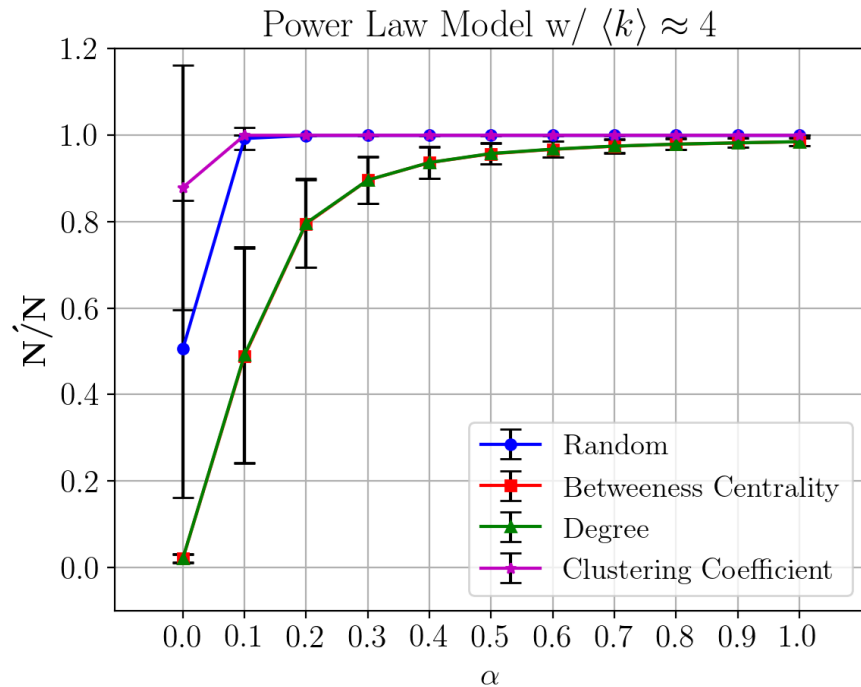
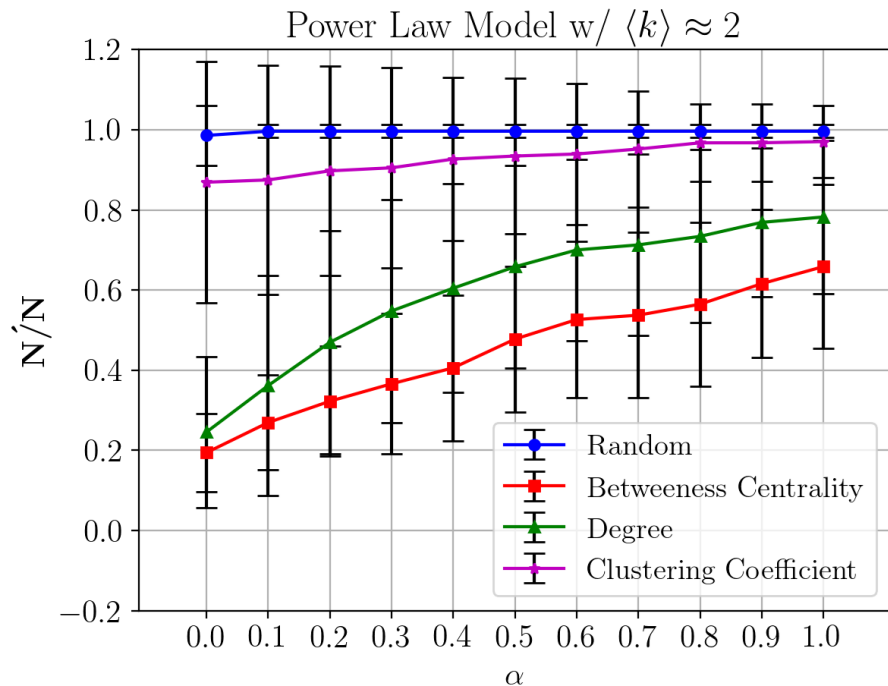
How to evaluate the robustness of a network?

$$G = \frac{N'}{N}$$

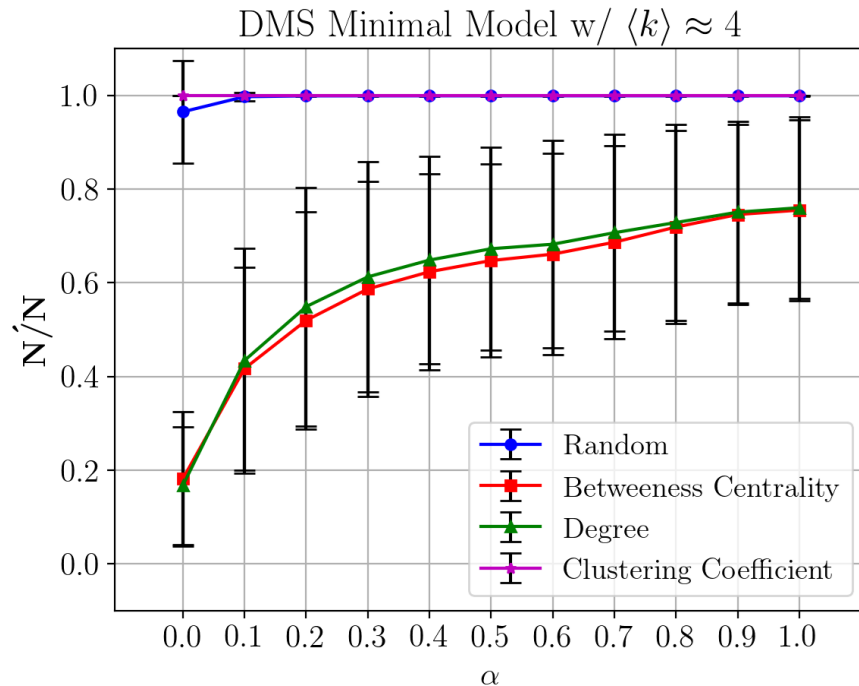
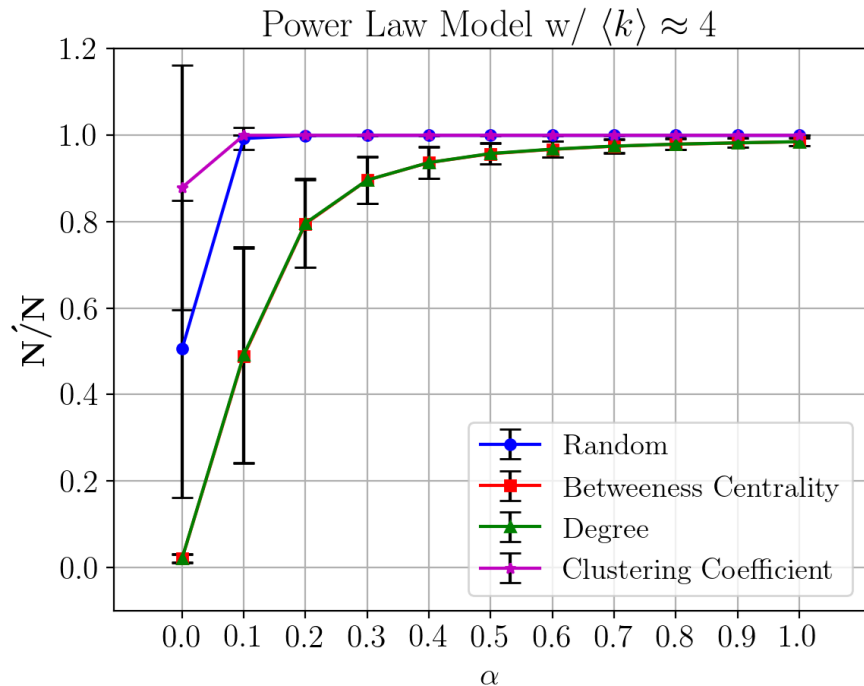
What models to use for testing?

$$P(k) \sim k^{-\gamma}$$

Power Law Avg. Degree 2 VS 4 (N = 5000)



Power Law VS DMS (Avg. Degree 4, N = 5000)



Power Law VS DMS (Avg. Degree 4)

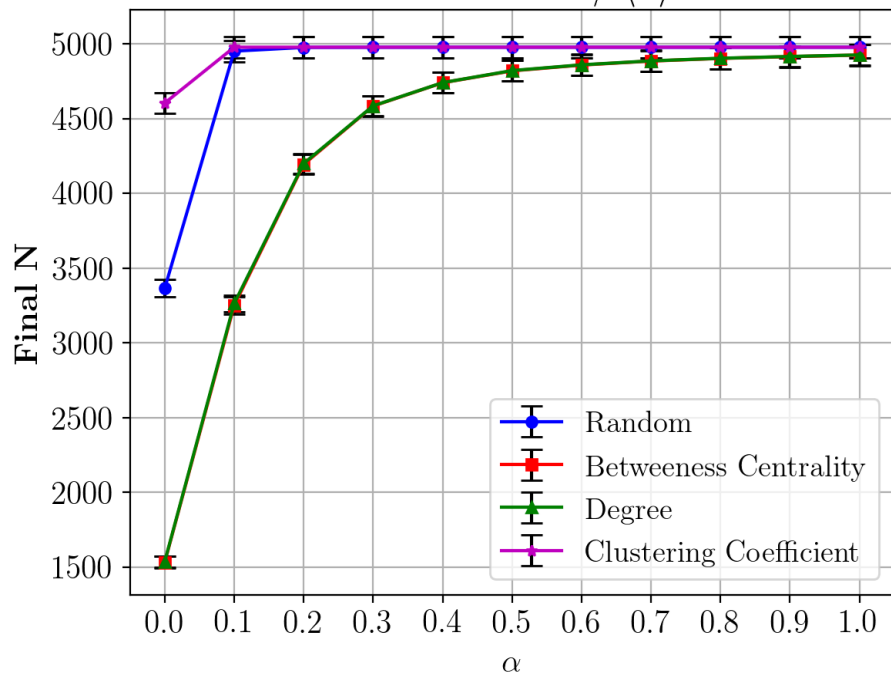
The DMS Model seems less robust to targeted attacks...

What about if we use a different metric?

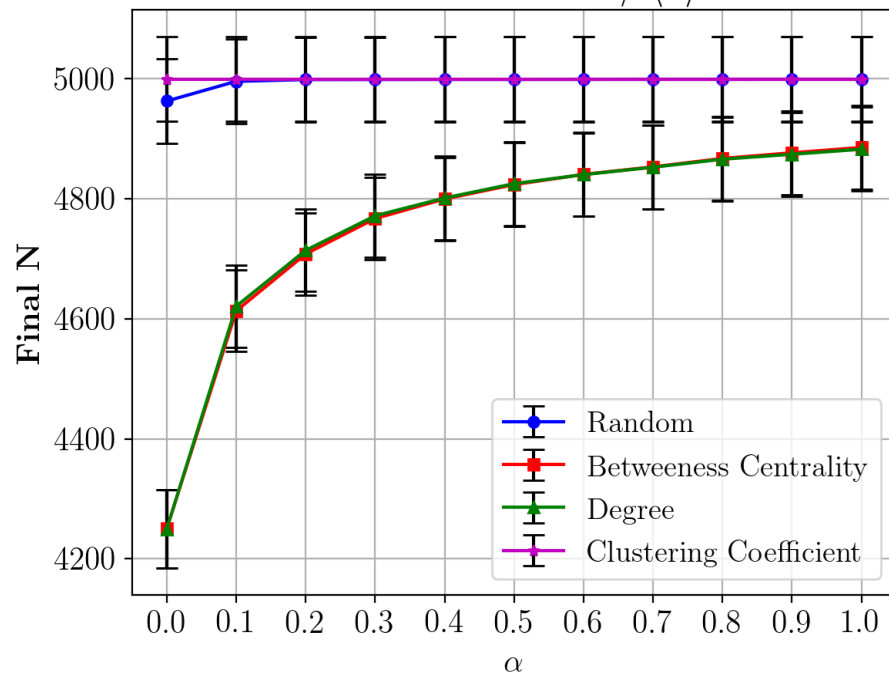
Will the results be the same?

Power Law VS DMS (Avg. Degree 4)

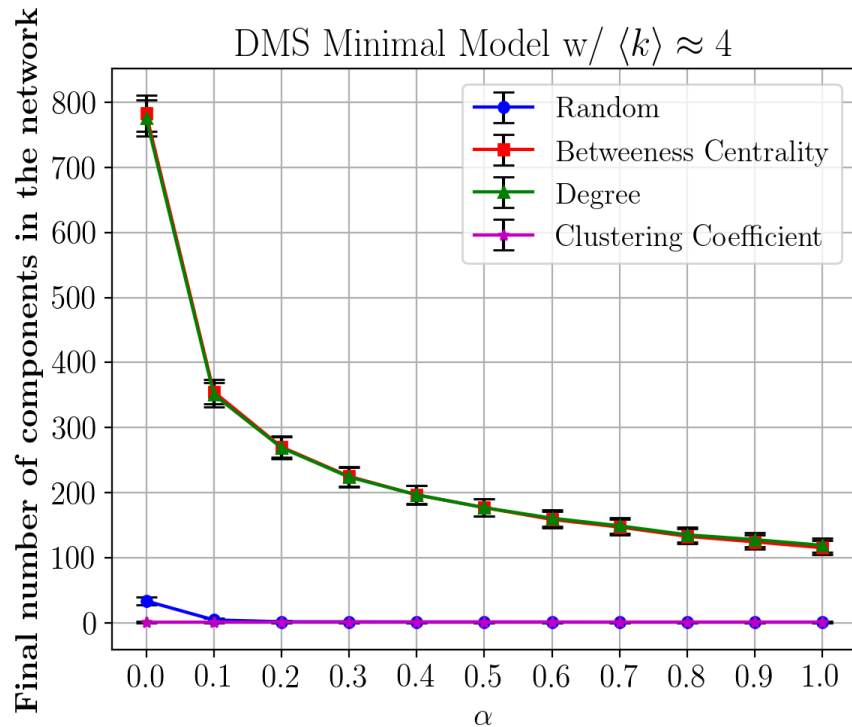
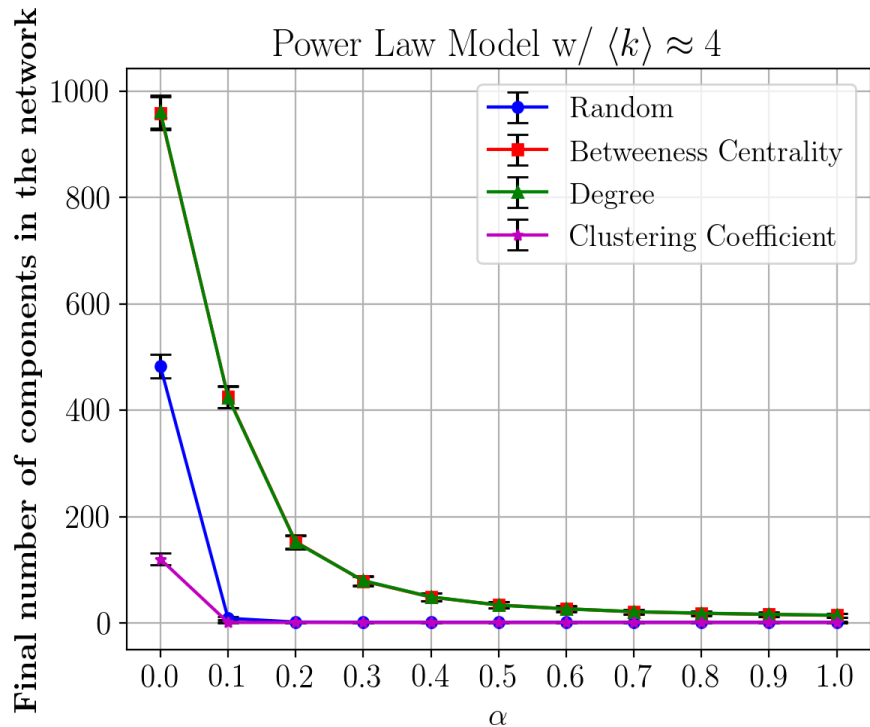
Power Law Model w/ $\langle k \rangle \approx 4$



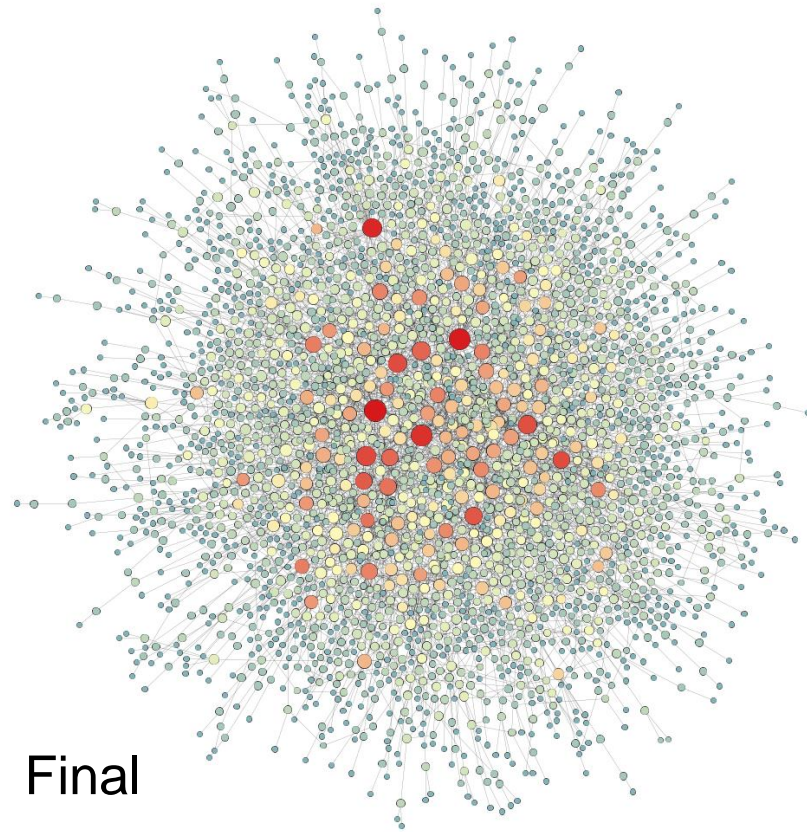
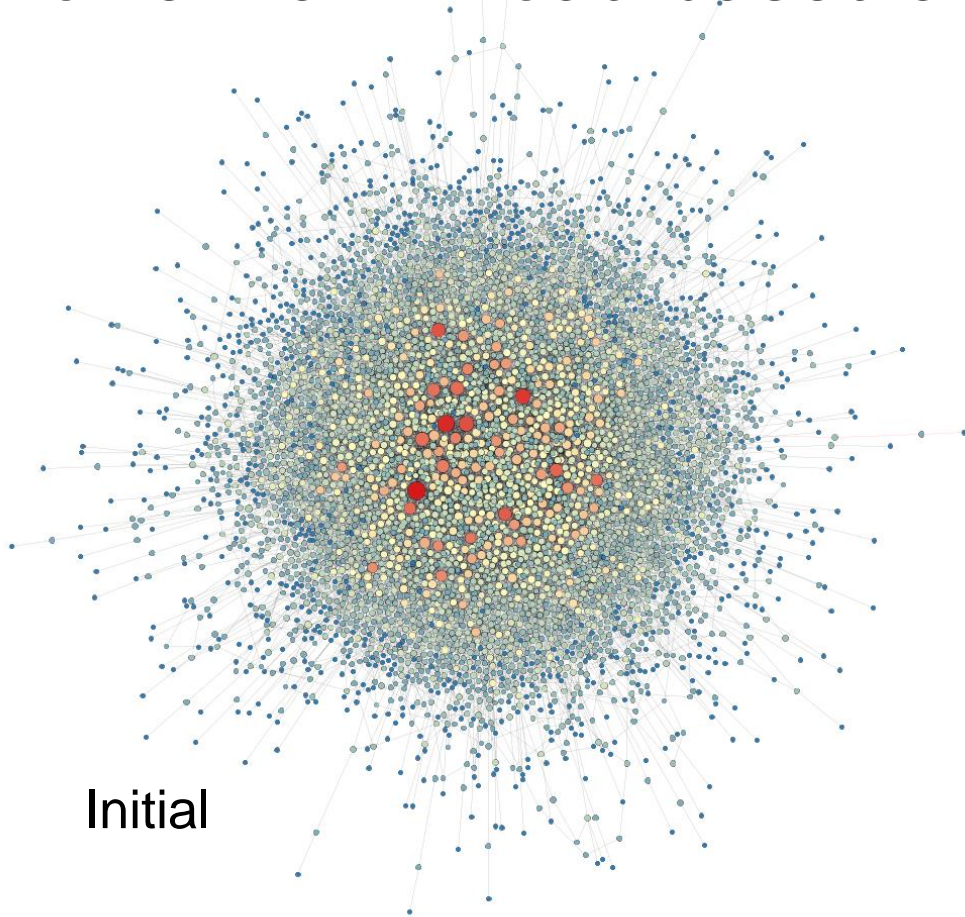
DMS Minimal Model w/ $\langle k \rangle \approx 4$



Power Law VS DMS (Avg. Degree 4)

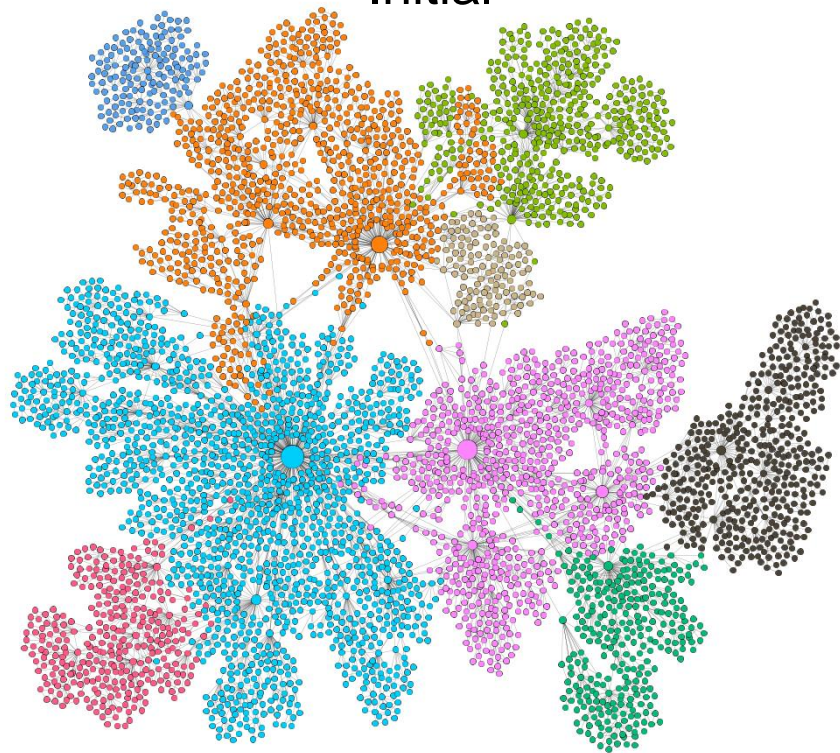


Power Law - Load-based attack - $\alpha = 0.2$ - $N = 5000$

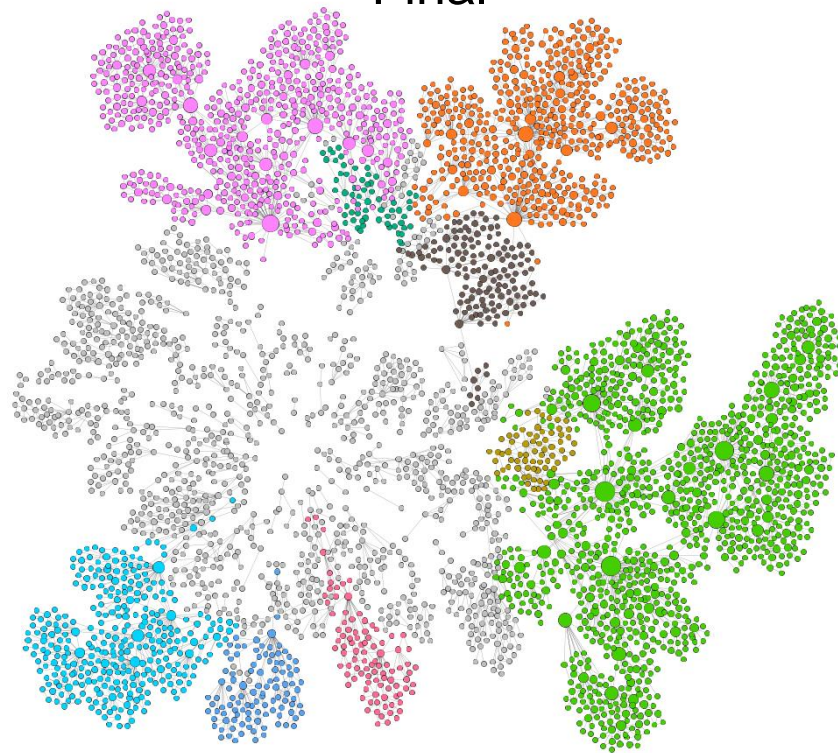


DMS - Load-based attack - $\alpha = 0.2$ - $N = 5000$

Initial



Final

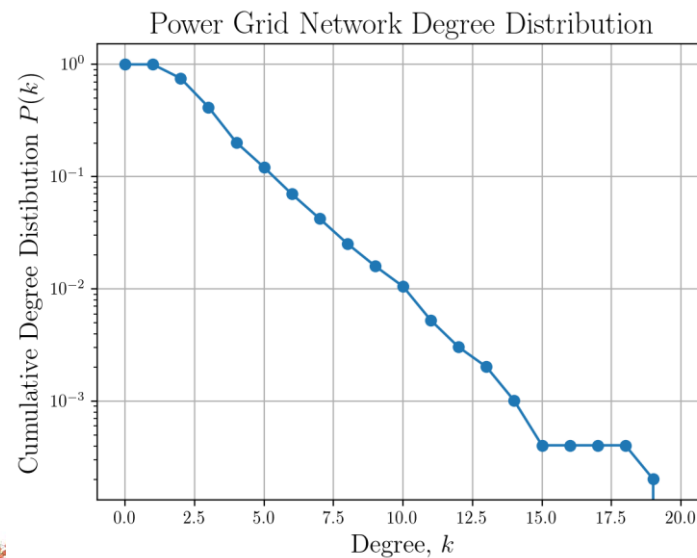
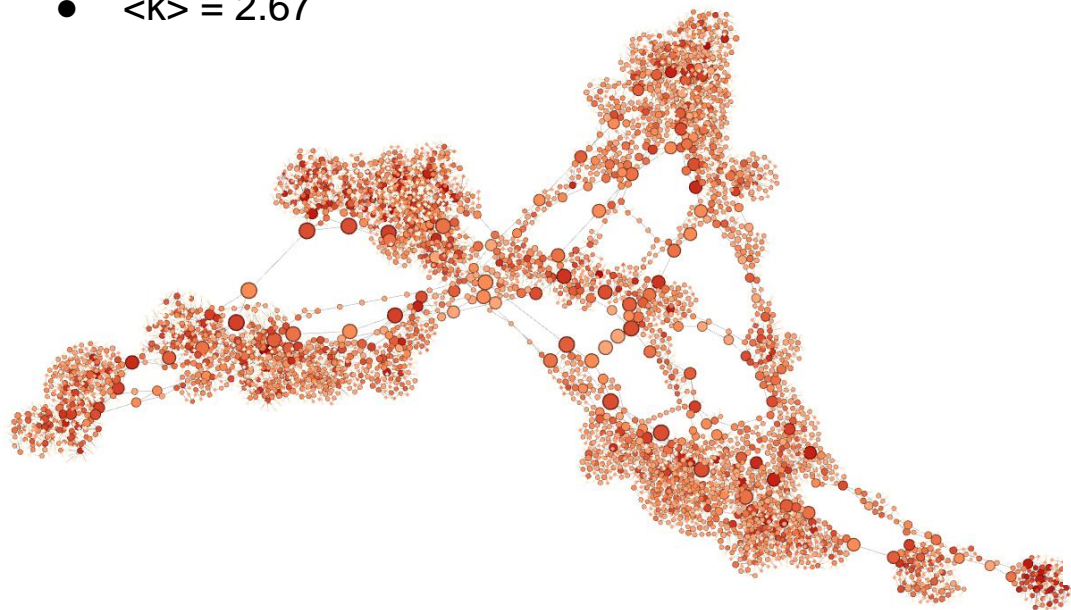


Power Law and DMS comparison for $\alpha = 0.2$

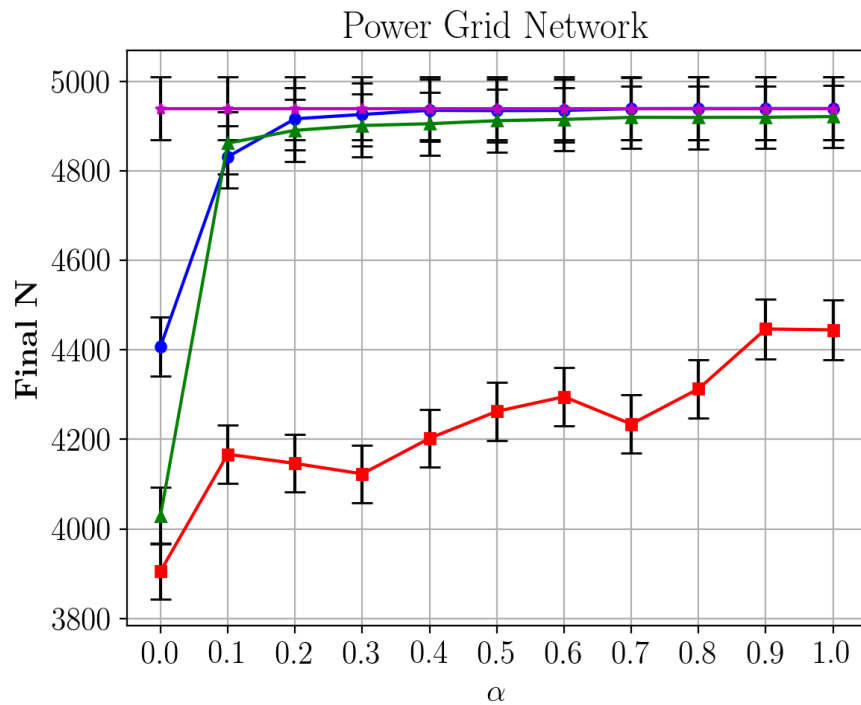
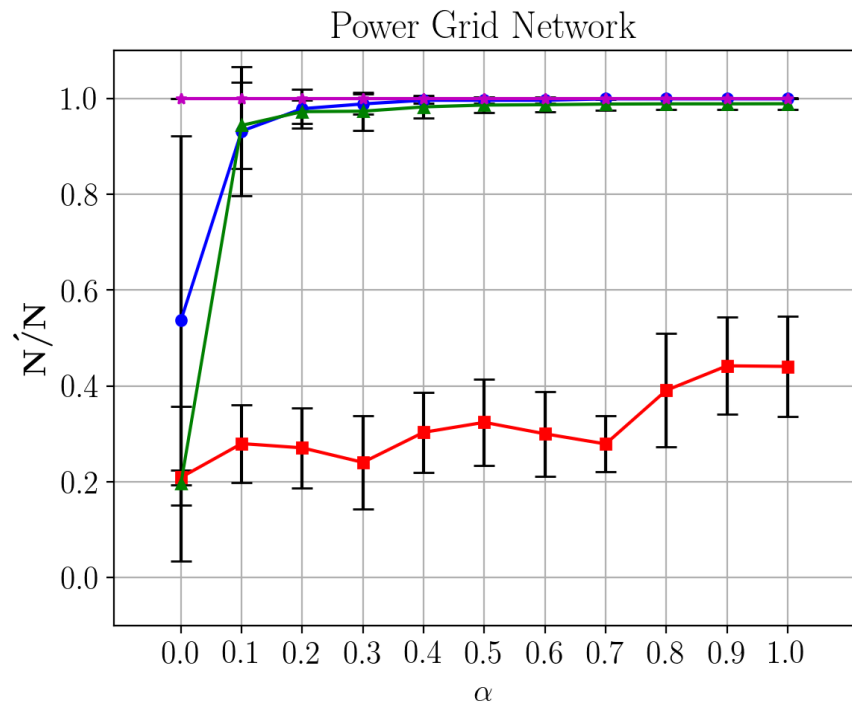
Final values	Power Law	DMS
# of Nodes	3193	4483
# of Nodes w/ $k > 0$	2995 (94%)	4125 (92%)
# of Nodes in biggest comp.	2751 (86%)	1095 (24%)
# of Components	83	175
Average Degree	2.695	3.411

Power Grid

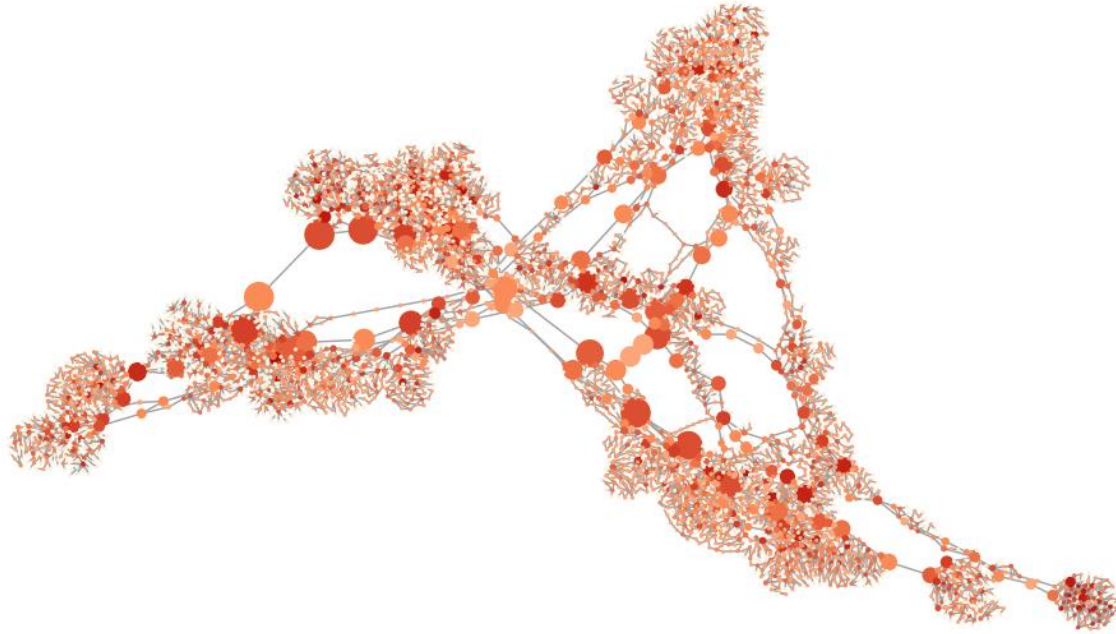
- $N = 4941$
- $\langle k \rangle = 2.67$



Power Grid



Power Grid - Load-based attack - $\alpha = 0.2$



Conclusion

How to attack a network?

- Degree
- Betweenness Centrality

Higher degree \Rightarrow More robustness

- Robustness \Leftrightarrow Number of nodes \Rightarrow Choose a DMS Model
- Robustness \Leftrightarrow Size of the giant component \Rightarrow Choose a Power Law Model

Thank you!