

ACS234

Maths and Data Modelling

Tutorial 5
Wednesday 1pm online

<https://github.com/ineskris/ACS234/tree/master/Tutorial5>

Done in Lecture (week 5/6)

- Polynomial Regression
- General Linear Models

Polynomial Regression

Polynomial Model $y = a_0 + a_1x + a_2x^2 + \dots + a_mx^m + e$

Estimation (least squares method) $Y = \hat{\theta}X + e \quad \hat{\theta} = (X'X)^{-1}X'Y$

General Polynomial Regression - 2 dimension $y = a_0 + a_1X_1 + a_2x_2 + a_3X_1^2 + a_4X_1X_2 + a_5X_2^2 + e$

Exercise 1

x	0	1	2	3
f(x)	2	7	14	23

Based on the data above, estimate the parameters a_0, a_1, a_2 of the **polynomial regression model**. Calculate the MSE error.

Exercise 2

X1	0	1	2	3
X2	12	12.3	12.6	12.9
f(x)	2	-3.3	-3.2	2.3

Based on the data above, estimate the parameters $a_0, a_1, a_2, a_3, a_4, a_5$ of the **general polynomial regression model**. Calculate the MSE error.

General Linear Models

There are three components to any GLM:

- *Random Component* : noise model or error model. e
- *Systematic Component* - the linear predictor $\eta = X\beta$
- *Link Function*, η or $g(\mu)$ - specifies the link between random and systematic components. $E[Y] = g^{-1}(X\beta)$

General linear model (GLM) includes multiple linear regression.

Example - logistic regression

$$X\beta = \ln\left(\frac{\mu}{1-\mu}\right) \qquad \mu = E[Y]$$

