

# Inferix's Proof of Rendering Algorithm

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## **Abstract**

This document presents the Active Noise Generation and Verification algorithm employed to verify image and video outputs of Inferix distributed graphics rendering service. This algorithm is the first effort introducing asymmetric watermarks into pre-rendering graphics scenes, it is different from classical watermarking method which can only work on media data.

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# Chapter 1

## Introduction

Non ministrari, sed ministrare

Matthaeus 20:28 - Biblia Vulgata

Inferix is a decentralized GPU network for visual computing and AI, it is built to bridge the needs of users and hardware owners. Its solution meets real-world problems across a range of industries, not only for the AI field but also for high-quality rendering needs. Users (e.g. 3D graphics artists, game developers, enterprises) who need GPU computing power for rendering high-quality graphics can use Inferix system to continuously access these precious resources with faster processing time and more efficient spending. Owners of

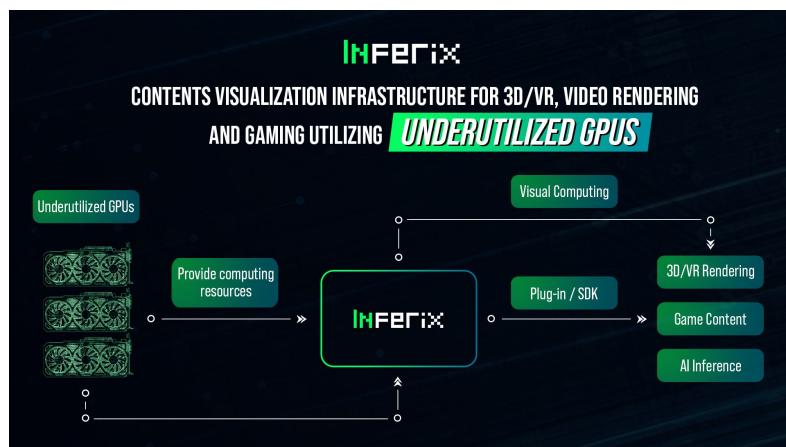


Figure 1.1: High level architecture

GPUs can share idle resources to Inferix network and earn long-term passive income while simultaneously balancing their main jobs or leisure activities.

In this document, we briefly present first the graphics rendering network of Inferix and discuss the challenge of maintaining the authenticity, then focus on the internal details of the verification procedure for rendered images.

## 1.1 Rendering network

The graphics rendering service consists in a network of decentralized machines called *nodes* which are of 3 kinds: *manager*, *worker* and *verifier*. The *managers* and *verifiers* are dedicated machines of Inferix while the *workers* are machines joined by GPU owners. The number of *workers* is normally much larger than the number of *managers* and *verifiers*. A typical rendering session contains

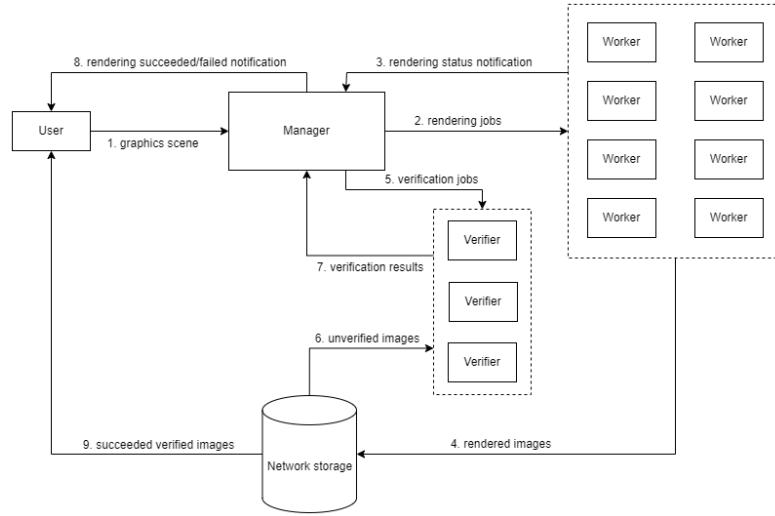


Figure 1.2: Graphics rendering flow

several steps which are shown in Figure 1.2:

1. A user submits a graphics scene to some *manager* using the Inferix plugin for client.
2. The *manager* who receives the graphics scene builds corresponding rendering jobs, each job consists of several parameters: range of images to be rendered, image format, etc. These job will be dispatched to *workers*.
3. Receiving a rendering job, a *worker* renders the graphics scene using the parameters given by the job. When it finishes, it sends the rendered images to a shared storage.
4. The *worker* then notifies a *manager* about the status of rendering job.
5. The notified manager creates a verification job and dispatches this job to some *verifier*.
6. Receiving a verification job, a *verifier* checks the authenticity of the corresponding rendered images.
7. The *verifier* then notifies the *manager* about the verification results.

8. The *manager* notifies the user about the graphics rendering result.
9. If there is no error, the user can finally download the rendered images/video from the shared storage.

The *managers* synchronize a database of rendering and verification jobs. That makes the rendering service being both logically and physically decentralized: a graphic scene can be simultaneously rendered by different *workers* and later checked by different *verifiers*, the machines of *workers* and *verifiers* can be also located at different geographical locations.

## 1.2 Rendering output verification

One of the most important problems that Inferix has to solve is to maintain the *authenticity* of rendered results. That means how to warranty that once a user submits a valid graphics scene, then after waiting for an amount of time, the user will receive authentically rendered images. The authenticity can be defined informally as if the result received from the rendering network and the result received when the scene is genuinely rendered by a graphics rendering software are human perceptual indistinguishable.

The *workers* joined the rendering network are mostly workstations<sup>1</sup> of GPU owners who want to make profit from their unused computing resources. Respecting the privacy of GPU owners and their computation resources, beside a lightweight open source software client installed to manage the communication with the network, there is completely no control on *workers*.

Consequently, there is no constraint to oblige *workers* to render the graphics scene correctly. Indeed, a malicious *worker* may receive a rendering job, but does nothing then uses some random images as results. Without rendering the graphics scene by themselves, the *managers* and users know only several superficial features of what the rendered images look like. Obviously, the *managers* and users have no interest in rendering the scene: if they can do that, there is no need to rely on *workers*. Moreover, we cannot deploy any surveillance mechanism on the machines of *worker* due to privacy reasons. Even if we try to do that, this is only a matter of time before the *worker* reverse engineers the mechanism and eventually bypass it.

The situation seems not favor us: checking the authenticity of something while only having a little knowledge about it, otherwise the attacker has complete information.

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<sup>1</sup>Except the dedicated machines of Inferix.



## Chapter 2

# Scene watermarking

Nanos gigantum humeris  
insidentes

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Bernard of Chartres

Before being sent back to the users, the output images of *workers* must be checked if they are actually the results of the corresponding submitted graphics scene. By architectural design, Inferix gains no control whatsoever on *workers* (see the discussion in section 1.2), any software installed on *workers* always suffer from risks of being completely analyzed, reversed and maliciously modified. In the long run, one cannot make any assumption about the security on the *worker* side, even worse *workers* should be considered adversaries who exhaustively try to bypass any security enforcement applied on them.

A public-key cryptography approach is using a scheme of *fully homomorphic encryption* (FHE) [Gen09]. The graphics scene is encrypted first by a private key before sending to *workers*. Given the corresponding public key, the homomorphic encryption software performs the graphics rendering on the encrypted scene without needing to decrypt it. Finally, the encrypted rendered results are returned and decrypted at the user's side using the private key. The advantage of FHE is that the *workers*, even being able to modify the FHE softwares on their side, cannot interfere the FHE graphics rendering processes without being detected. Unfortunately, this approach is impractical since all state-of-the-art implementations will make the performance of the homomorphic encryption graphics rendering become unacceptable [Mar+22].

To handle this problem, we use a watermarking [Cox+97; CMM99] method called *Active Noise Generation and Verification* (ANGV) which is a simpler variant of *proof of ownership* [WL98; YM97] schemes. *First*, the *verifier* can quickly judge that the rendered digital content is an authentic result of a rendering process whose input is the submitted graphics scene. *Second*, though ANGV needs to modify the initial submitted scene, as a sequence the rendered output will be distorted also, the distortion is regulated to below the human

perception capability, hence there is no quality degradation. *Third*, the embedded noise is robust under rendering enhancements (e.g. anti-aliasing) and post-processing operations. *Finally*, there is no need to use a special graphics rendering software on *workers* as in the case of FHE, the performance of graphics rendering is not affected.

## 2.1 Active noise generation and verification

A user submits some graphics work to a *manager* (see section 1.1), this work consists of several graphics scenes; each contains information about graphical objects, the camera, light sources and materials [Ble24]. The photorealistic rendering is a sophisticated computation process that calculate light properties at surfaces of all visible objects, results in 3D rendered images of the scene [Hug+14].

In traditional digital watermarking schemes [Cox+97; CMM99], to check the authenticity, an invisible watermark [YM97; Cra+97; WL98] will be embedded into the image needed to be protected. A detector tries to extract the watermark from a tested image then compares the extracted watermark with the original embedded one, if the comparison is passed then that the tested image is concluded as being authentic.

**Approach** In the context of Inferix’s rendering network, the *manager* has access to the image only after the graphics scene has been rendered by some *worker*. It is nonsense to embed watermark into the image at this point since the watermarking cannot help to detect any malicious manipulations which may happen before that, namely in the rendering process. Our approach is to embed watermarks into the graphics scene submitted by users before sending it to *workers*.

### High level description

The *Active Noise Generation and Verification* (ANGV) consists of two main procedures as described below.

**Noise generation** In practice, a graphics scene may contain multiple frames, each job of this scene contains some range of frames to be rendered, consequently each worker may render only a subset of these frames. For the simplification purpose, we assume in this section that a scene has only one frame, so the output image is determined uniquely by the scene. Mathematically, we denote the graphics rendering process by a function  $\mathcal{R}$ , for each input scene  $\mathcal{S}$ , the result of the rendering is an image:

$$I = \mathcal{R}(\mathcal{S})$$

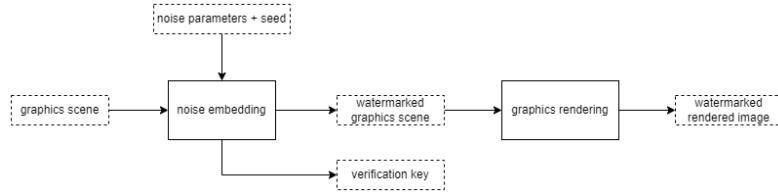


Figure 2.1: Noise generation

It is important to note that  $I$  is actually never computed, neither by the *manager* in the watermark insertion procedure nor by *workers* in rendering processes, the equation above represents only an equality.

Similar with invisible watermark schemes [YM97; Cra+97; WL98], a noise  $W$  is a sequence of atomic watermarks:

$$W = \{w_1, \dots, w_n\}$$

where  $w_i$  is chosen from some probability distribution and  $w_i$  may also depend on  $S$  (see section 2.1). Using  $W$  and  $S$ , we next generate a verification key:

$$K_{\text{verif}}(W, S) = \{k_1, \dots, k_n\}$$

that will be used later for the watermark verification procedure.

The noise  $W$  is not embedded into the image  $I$  but into the scene  $S$  (see Figure 2.1). We use an encoding function  $\mathcal{E}$  to create a watermarked scene:

$$\hat{S} = \mathcal{E}(S, W)$$

Finally  $\hat{S}$  is sent to *workers* for rendering, that results in a watermarked image:

$$\hat{I} = \mathcal{R}(\hat{S})$$

In case of being accepted, the rendered image sent back to the original user (i.e. the owner of the graphics scene  $S$ ) is  $\hat{I}$  but not  $I$ . The encoding function  $\mathcal{E}$  and the watermark  $W$  are designed so that the distortion of  $\hat{I}$  against  $I$  is under human perception capability, then  $\hat{I}$  can be authentically used as a result of the graphics rendering.

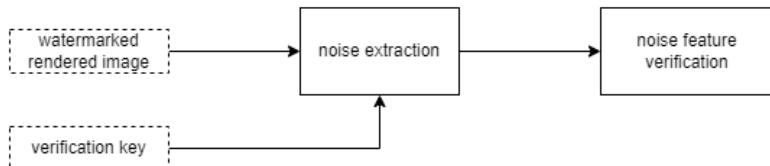


Figure 2.2: Noise verification

**Noise verification** Given an image  $J$  and a verification key  $K_{\text{repr}}$ , we first try to recover a watermark  $\hat{W}$  from  $\hat{I}$  using a decoding function  $\mathcal{D}$ :

$$\hat{W} = \mathcal{D}(J, K_{\text{repr}})$$

Next  $\hat{W}$  is compared against  $W$ , if the difference is above some threshold  $T$

$$\|\hat{W} - W\| \geq T$$

then  $J$  will be accepted otherwise rejected.

**Performance** The functions  $\mathcal{E}$  and  $\mathcal{D}$  are designed so that their computation resource consumption is negligible in comparison with the graphics rendering function  $\mathcal{R}$ ; and the watermark verification does not require  $I$ , only  $\hat{I}$  is rendered. That means the only overhead caused by ANGV is by  $\mathcal{E}$  and  $\mathcal{D}$ , hence there is no significant effect on the performance of the graphics rendering.

## Deployment

To apply ANGV into the rendering network (see Figure 1.2)

## Implementation

In this section, we present in detail the current Inferix's implementation of watermark insertion and verification.

**Structure of watermark** As described above, a watermark  $W$  consists of a sequence of  $n$  atomic watermarks, each watermark  $w_i$  is a rectangle image of special pattern (see Figure 2.3) of noise chosen from a normal distribution  $w_i \sim \mathcal{N}(0, \sigma_i^2)$ . The number  $n$  is one of the factors decides the robustness of

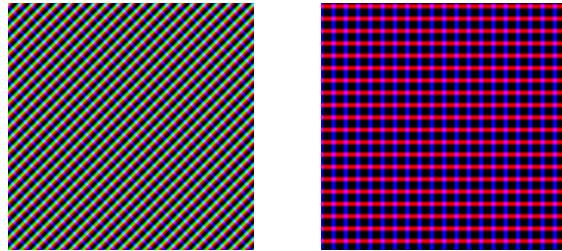


Figure 2.3: Some atomic watermark patterns

watermark, the higher this number the lower the false positive of watermark verification. Experimentally,  $W$  contains about 8 to 10 atomic watermarks.

**Watermark insertion** Given some graphics scene  $S$ , we embed the watermark  $W$  into  $S$  by wrapping each atomic watermark as a graphics objects, then insert these objects into  $S$  so that they contribute to the result rendered image (i.e. they distort this image).

By the nature of the graphics rendering, an object in the scene will not be visible if there is no light scattered from the surface of the object to the camera. This may be caused by several reasons: the object is not located in the frustum of the camera, is hidden by some other objects, or the material of the object is transparent, etc. The watermark insertion must satisfy first several constraints:

- there are no collisions between watermark objects,
- all watermark objects are located completely in the camera frustum,
- no watermark object is hidden by another object (including both watermark objects and existing objects of the scene).

**Representative key generation** An atomic watermark  $w_i$  contributes to the image  $\hat{I}$  as a rectangular region at the location  $k_i$  (for that, the rotation vector of the graphics object  $w_i$  is kept to be equal with the one of the camera in  $S$ ). The location  $k_i$  on  $\hat{I}$  can be precisely calculated without rendering:

$$k_i = (x_i^{\text{ul}}, y_i^{\text{ul}}, x_i^{\text{lr}}, y_i^{\text{lr}})$$

where  $(x_i^{\text{ul}}, y_i^{\text{ul}})$  (resp.  $x_i^{\text{lr}}, y_i^{\text{lr}}$ ) are the upper left (resp. lower right) coordinates of the region. So the insertion of  $W$  into  $S$  generates a key

$$K_{\text{repr}} = \{k_1, \dots, k_n\}$$

**Distortion constraint** It might be worth noting that  $k_i$  represents the distortion caused by the atomic watermark  $w_i$  to the rendered image, normally  $k_i$  is much smaller than the original size of  $w_i$ . On the one hand  $k_i$  must not be negligible otherwise the watermark verification is not possible. On the other hand,  $k_i$  must be kept under the human perception capability. Experimentally we keep a trade-off:

$$\begin{aligned} 2 \leq x_i^{\text{lr}} - x_i^{\text{ul}} &\leq 3 \\ 2 \leq y_i^{\text{lr}} - y_i^{\text{ul}} &\leq 3 \end{aligned} \tag{2.1}$$

for all  $1 \leq i \leq n$  (see Figure 2.4 and Figure 2.5).

**Watermark verification** The verification procedure needs only the representative key  $K_{\text{repr}}$  and the rendered image  $\hat{I}$ . It is not always possible to restore the atomic watermark  $w_i \in W$  since most information of  $w_i$  is lost

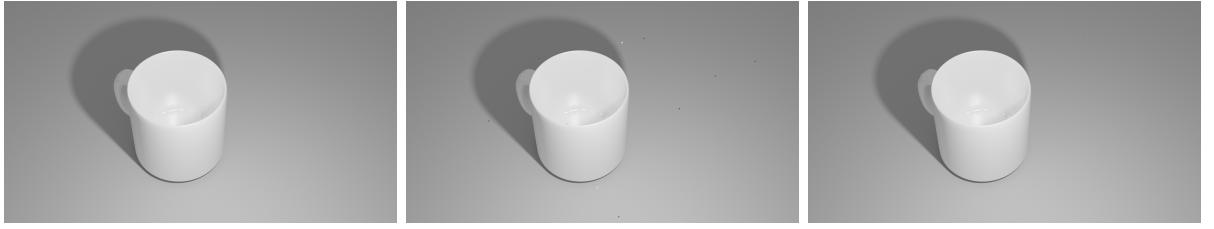


(a) Original

(b) Watermarked with atomic wa-  
termark size = 5

(c) Atomic watermark size = 2

Figure 2.4: Scene watermarked with different size of atomic watermarks: the distortion is observable when the width and the height of an atomic watermark are about 5, but unobservable when these lengths are 2.



(a) Original

(b) Atomic watermark size = 7

(c) Atomic watermark size = 3

Figure 2.5: Another scene watermarked with different sizes of atomic watermarks

after the graphics rendering process (note that  $k_i$  is much smaller than the size of  $w_i$ ). However, it is neither necessary to restore  $w_i$ , instead to verify the existence of  $W$ , checking the existence of  $w_i$  on the image region determined by  $k_i$  on  $\hat{I}$  for  $1 \leq i \leq n$  is sufficient.

For each region of coordinates  $k_i = (x_i^{\text{ul}}, y_i^{\text{ul}}, x_i^{\text{lr}}, y_i^{\text{lr}})$ , we pick a bound region of coordinates:

$$b_i = (x_i^{\text{ul}} - \delta_i^x, y_i^{\text{ul}} - \delta_i^y, x_i^{\text{lr}} + \delta_i^x, y_i^{\text{lr}} + \delta_i^y)$$

where  $\delta_i^x$  and  $\delta_i^y$  are the width and the height of  $k_i$  (see Figure 2.6a):

$$\delta_i^x = x_i^{\text{lr}} - x_i^{\text{ul}} \quad \delta_i^y = y_i^{\text{lr}} - y_i^{\text{ul}}$$

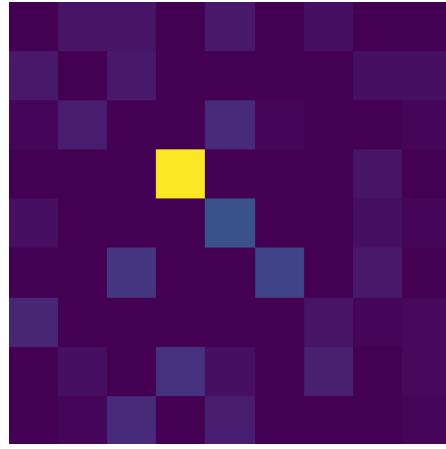
To check the contribution of the atomic watermark at the region of coordinates  $k_i$ , we apply an edge detection filter (see Figure 2.6b) on the bound region,

then compare the mean  $m_b$  of the bound region against the mean  $m_k$  of the atomic watermark located inside. Experimentally, we will check if

$$m_k - m_b \geq 5 \quad (2.2)$$

to validate the existence of the atomic watermark. This check is proceeded for all  $n$  atomic watermarks, if all of them are validated then the rendered image  $\hat{I}$  is accepted otherwise rejected.

	0	1	2	3	4	5	6	7	8	9
0	168	170	170	166	169	167	169	167	165	165
	165	168	169	164	163	165	166	165	162	162
	144	162	149	143	145	153	156	144	142	142
1	170	168	170	167	167	168	167	168	168	168
	168	166	168	165	165	165	165	166	166	166
	145	145	146	144	145	144	144	145	144	144
2	169	171	170	168	168	168	168	169	167	169
	157	168	168	168	170	166	164	165	165	166
	145	146	148	146	145	144	143	143	145	145
3	157	168	167	159	165	167	167	169	169	169
	143	152	159	160	165	155	155	156	156	156
	143	145	149	146	148	144	144	145	145	145
4	168	166	164	183	173	169	167	170	170	170
	165	164	166	180	172	169	167	167	167	166
	144	142	143	155	147	145	144	146	145	145
5	166	166	170	166	169	172	166	169	168	168
	164	164	168	164	168	169	164	167	165	165
	143	143	144	143	145	148	148	146	144	144
6	169	167	168	169	168	167	169	169	169	169
	167	165	166	166	166	165	167	167	167	167
	146	144	146	144	145	144	145	145	146	146
7	166	166	168	171	170	168	170	169	170	170
	163	166	166	169	168	166	168	165	170	170
	143	145	144	147	146	145	146	144	146	146
8	167	169	171	167	170	167	167	168	169	169
	165	167	167	167	168	168	168	166	167	167
	144	145	147	144	146	144	145	145	145	145
9										



(a) Pickup bound region of size  $9 \times 9$  pixels, the atomic watermark region of size  $3 \times 3$  located at the center of the bound (numbers on each pixel are RGB color values)

(b) Pickup bound region after an edge detection filter

Figure 2.6: Watermark verification

**Robustness** We now discuss several details about the contribution of the watermark on the rendered image. There are two related constraints:

- the side trade-off in Equation 2.1 is used to keep the rendering distortion under the human perception capability, and
- the mean difference in Equation 2.2 is used to validate the existence of an atomic watermark

which are unfortunately disproportional: if the side is too small

## Performance

### 2.2 Threat analysis



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