Lecture

```
In [1]: using JuMP
         m = Model()
         @variables m begin
             r>=0
             g>=0
         end
         Oconstraints m begin
             r + g <= 8
             r >= 1
             g >= 1
             r <= 5
             g <= 6
         end
         @objective(m, Max, 3r+2g)
         solve(m)
         println(getobjectivevalue(m))
writeLP(m, "costs.lp")
```

21.0

```
In [2]: ;less "costs.lp"
        Maximize
         obj: 3 VAR1 + 2 VAR2
        Subject To
         c1: 1 VAR1 + 1 VAR2 <= 8
         c2: 1 VAR1 >= 1
         c3: 1 VAR2 >= 1
         c4: 1 VAR1 <= 5
         c5: 1 VAR2 <= 6
        Bounds
         0 <= VAR1 <= +inf
         0 <= VAR2 <= +inf
        General
        End
In [3]: | ;qlpsol --cpxlp costs.lp --ranges costs.sen
        GLPSOL: GLPK LP/MIP Solver, v4.60
        Parameter(s) specified in the command line:
         --cpxlp costs.lp --ranges costs.sen
        Reading problem data from 'costs.lp'...
        5 rows, 2 columns, 6 non-zeros
        13 lines were read
        GLPK Simplex Optimizer, v4.60
        5 rows, 2 columns, 6 non-zeros
        Preprocessing...
        1 row, 2 columns, 2 non-zeros
        Scaling...
         A: min|aij| = 1.000e+00 max|aij| = 1.000e+00 ratio = 1.000e+00
        Problem data seem to be well scaled
        Constructing initial basis...
        Size of triangular part is 1
             2: obj = 2.1000000000e+01 inf = 0.000e+00 (0)
        OPTIMAL LP SOLUTION FOUND
        Time used: 0.0 secs
        Memory used: 0.0 Mb (40416 bytes)
        Write sensitivity analysis report to 'costs.sen'...
```

In [4]: ;less "costs.sen"

GLPK 4.60 - SENSITIVITY ANALYSIS REPORT

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Problem:

Objective: obj = 21 (MAXimum)

No. Row name	St	Activity	Slack Marginal	Lower bound Upper bound	Activity range	Obj coef range	Obj value at Limiting break point variable
1 c1	NU	8.00000	2.00000	-Inf 8.00000	6.00000 11.00000	-2.00000 +Inf	17.00000 c3 27.00000 c5
2 c2	BS	5.00000	-4.00000 •	1.00000 +Inf	2.00000 5.00000	-1.00000 +Inf	16.00000 c4 +Inf
3 c3	BS	3.00000	-2.00000	1.00000 +Inf	6.00000	-2.00000 1.00000	15.00000 c1 24.00000 c4
4 c4	NU	5.00000	1.00000	-Inf 5.00000	2.00000 7.00000	-1.00000 +Inf	18.00000 c5 23.00000 c3
5 c5	BS	3.00000	3.00000	-Inf 6.00000	1.00000 7.00000	-2.00000 1.00000	15.00000 c1 24.00000 c4

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Problem:

Objective: obj = 21 (MAXimum)

No. Column name	St	Activity	Obj coef Marginal	Lower bound Upper bound	Activity range	Obj coef range	Obj value at Limiting break point variable
1 VAR1	BS	5.00000	3.00000	+Inf	2.00000 5.00000	2.00000 +Inf	16.00000 c4 +Inf
2 VAR2	BS	3.00000	2.00000	+Inf	1.00000 6.00000	3.00000	15.00000 c1 24.00000 c4

End of report

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