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In[443]:= (*FastICA Negentropy Uniform. Initial value is w=
          {1,0} and w=w=RandomReal[{-Sqrt[3],Sqrt[3]},2] *)
          x = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];
          y = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];

In[445]:= A = {{5, 10}, {10, 2}};

In[446]:= mt = A.{x, y};

In[447]:= ma = Transpose[mt];
          ListPlot[{ma[[All]]}, PlotRange -> {{-30, 30}, {-30, 30}}];

In[449]:= mt = mt - Mean[Transpose[mt]];

In[450]:= Covariance[Transpose[mt]]

Out[450]= {{121.312, 69.521}, {69.521, 104.655}}

In[451]:= Eigenvalues[Covariance[Transpose[mt]]]

Out[451]= {183.002, 42.9654}

In[452]:= Eigenvectors[Covariance[Transpose[mt]]]

Out[452]= {{-0.74798, -0.663721}, {0.663721, -0.74798}}

In[453]:= d12 = 1 / Sqrt[Eigenvalues[Covariance[Transpose[mt]]][[1]]]
          d22 = 1 / Sqrt[Eigenvalues[Covariance[Transpose[mt]]][[2]]]
          dmat = DiagonalMatrix[{d12, d22}]

Out[453]= 0.0739218

Out[454]= 0.15256

Out[455]= {{0.0739218, 0.}, {0., 0.15256}}

In[456]:= emat = Transpose[Eigenvectors[Covariance[Transpose[mt]]]]

Out[456]= {{-0.74798, 0.663721}, {-0.663721, -0.74798}}

In[457]:= vmat = emat.dmat.Transpose[emat]

Out[457]= {{0.108564, -0.0390399}, {-0.0390399, 0.117918}}

In[458]:= x = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];
          y = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];
          mt = A.{x, y};
          mt = mt - Mean[Transpose[mt]];

In[462]:= zmat = vmat.mt;

In[463]:= za = Transpose[zmat];
          ListPlot[{za[[All]]}, PlotRange -> {{-3, 3}, {-3, 3}}];

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In[465]:= (*
w=RandomReal[{-Sqrt[3],Sqrt[3]},2];
*)

w = {1, 0};

(*w={2,20};//N*)

(*w=w/Norm[w]//N*)
epsilon = 0.0001;
n = Length[x];
cnt = 1;
wbefore = w;
While[cnt < n,
  wbefore = w;
  w = (1/n) * Sum[Tanh[w.zmat[[All, i]]] * zmat[[All, i]], {i, 1, n}] -
    (1/n) * Sum[1 - (Tanh[w.zmat[[All, i]]])^2, {i, 1, n}] * w;
  w = w / Norm[w];
  Print["cnt=", cnt];
  Print["w=", w];

  If[1 - epsilon <= Abs[w.wbefore] && Abs[w.wbefore] <= 1 + epsilon,
    Print["収束した:"];
    Print["w=", w];
    Print["cnt=", cnt];
    Print["Abs[w.wbefore]=", Abs[w.wbefore]];
    cnt = n;
  ];
  ++cnt;
]
Kurtosis[w.zmat] - 3
cnt=1
w={0.968458, -0.249176}
cnt=2
w={0.974443, -0.224635}
cnt=3
w={0.974017, -0.226477}
収束した:
w={0.974017, -0.226477}
cnt=3
Abs[w.wbefore]=0.999998

Out[471]= -1.22385

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In[472]:= (* True Value*)
tmat = vmat.A;
truemat = {};
i = 1;
While[i ≤ 2,
  truemat = Append[truemat, tmat[[All, i]] / Norm[tmat[[All, i]]]];
  i++;
];
truemat = Transpose[truemat];
MatrixForm[truemat]

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Out[477]/MatrixForm=

$$\begin{pmatrix} 0.153076 & 0.988437 \\ 0.988214 & -0.15163 \end{pmatrix}$$


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In[478]:= w = RandomReal[{-Sqrt[3], Sqrt[3]}, 2];
epsilon = 0.0000000001;
n = Length[x];
cnt = 1;
wbefore = w;
While[cnt < n,
  wbefore = w;
  w = (1 / n) * Sum[Tanh[w.zmat[[All, i]]] * zmat[[All, i]], {i, 1, n}] -
    (1 / n) * Sum[1 - (Tanh[w.zmat[[All, i]]])^2, {i, 1, n}] * w;
  w = w / Norm[w];
  Print["cnt=", cnt];
  Print["w=", w];

  If[1 - epsilon <= Abs[w.wbefore] && Abs[w.wbefore] <= 1 + epsilon,
    Print["収束した:"];
    Print["w=", w];
    Print["cnt=", cnt];
    Print["Abs[w.wbefore]=", Abs[w.wbefore]];
    cnt = n;
  ];
  ++cnt;
]
Kurtosis[w.zmat] - 3

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cnt=1
w={0.924872, -0.380278}

cnt=2
w={0.976089, -0.217372}

cnt=3
w={0.973884, -0.227046}

cnt=4
w={0.97406, -0.22629}

cnt=5
w={0.974046, -0.226349}

cnt=6
w={0.974047, -0.226344}

収束した:

w={0.974047, -0.226344}

cnt=6

Abs[w.wbefore]=1.

Out[484]= -1.22391

In[485]:= MatrixForm[truemat]

Out[485]/MatrixForm=

$$\begin{pmatrix} 0.153076 & 0.988437 \\ 0.988214 & -0.15163 \end{pmatrix}$$


In[486]:= Transpose[vmat.A].w

Out[486]= {-0.0742533, 1.0164}

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