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(*FastICA Negentropy Uniform. Initial value is w=
{1,0} and w=w=RandomReal[{-Sqrt[3],Sqrt[3]},2] *)
x = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];
y = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];

A = {{5, 10}, {10, 2}};

mt = A.{x, y};

In[441]:= ma = Transpose[mt];
ListPlot[{ma[[All]]}, PlotRange -> {{-30, 30}, {-30, 30}}];

mt = mt - Mean[Transpose[mt]];

Covariance[Transpose[mt]]

{{127.846, 71.8281}, {71.8281, 103.734}}

Eigenvalues[Covariance[Transpose[mt]]]

{188.623, 42.957}

Eigenvectors[Covariance[Transpose[mt]]]

{{-0.763391, -0.645937}, {0.645937, -0.763391}}

d12 = 1 / Sqrt[Eigenvalues[Covariance[Transpose[mt]]][[1]]]
d22 = 1 / Sqrt[Eigenvalues[Covariance[Transpose[mt]]][[2]]]
dmat = DiagonalMatrix[{d12, d22}]

0.072812
0.152575

{{0.072812, 0.}, {0., 0.152575}}

emat = Transpose[Eigenvectors[Covariance[Transpose[mt]]]]
{{-0.763391, 0.645937}, {-0.645937, -0.763391}}

vmat = emat.dmat.Transpose[emat]
{{0.106092, -0.0393313}, {-0.0393313, 0.119295}}

x = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];
y = RandomReal[{-Sqrt[3], Sqrt[3]}, 1000];
mt = A.{x, y};
mt = mt - Mean[Transpose[mt]];

zmat = vmat.mt;

In[443]:= za = Transpose[zmat];
ListPlot[{za[[All]]}, PlotRange -> {{-3, 3}, {-3, 3}}];

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(*)
w=RandomReal[{-Sqrt[3],Sqrt[3]},2];
*)

w = {1, 0};

(*w={2,20};//N*)

(*w=w/Norm[w]//N*)
epsilon = 0.0001;
n = Length[x];
cnt = 1;
wbefore = w;
While[cnt < n,
  wbefore = w;
  w = (1/n) * Sum[Tanh[w.zmat[[All, i]]] * zmat[[All, i]], {i, 1, n}] -
    (1/n) * Sum[1 - (Tanh[w.zmat[[All, i]]])^2, {i, 1, n}] * w;
  w = w / Norm[w];
  Print["cnt=", cnt];
  Print["w=", w];

  If[1 - epsilon <= Abs[w.wbefore] && Abs[w.wbefore] <= 1 + epsilon,
    Print["収束した:"];
    Print["w=", w];
    Print["cnt=", cnt];
    Print["Abs[w.wbefore]=", Abs[w.wbefore]];
    cnt = n;
  ];
  ++cnt;
]
Kurtosis[w.zmat] - 3
cnt=1
w={0.997142, -0.0755494}
cnt=2
w={0.99681, -0.0798065}
収束した:
w={0.99681, -0.0798065}
cnt=2
Abs[w.wbefore]=0.999991
-1.263

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(* True Value*)
tmat = vmat.A;
truemat = {};
i = 1;
While[i ≤ 2,
  truemat = Append[truemat, tmat[[All, i]] / Norm[tmat[[All, i]]]];
  i++;
];
truemat = Transpose[truemat];
MatrixForm[truemat]

$$\begin{pmatrix} 0.13637 & 0.98782 \\ 0.990658 & -0.155599 \end{pmatrix}$$

w = RandomReal[{-Sqrt[3], Sqrt[3]}, 2];
epsilon = 0.0001;
n = Length[x];
cnt = 1;
wbefore = w;
While[cnt < n,
  wbefore = w;
  w = (1/n) * Sum[Tanh[w.zmat[[All, i]]] * zmat[[All, i]], {i, 1, n}] -
    (1/n) * Sum[1 - (Tanh[w.zmat[[All, i]]])^2, {i, 1, n}] * w;
  w = w / Norm[w];
  Print["cnt=", cnt];
  Print["w=", w];

  If[1 - epsilon ≤ Abs[w.wbefore] && Abs[w.wbefore] ≤ 1 + epsilon,
    Print["収束した:"];
    Print["w=", w];
    Print["cnt=", cnt];
    Print["Abs[w.wbefore]=", Abs[w.wbefore]];
    cnt = n;
  ];
  ++cnt;
]
Kurtosis[w.zmat] - 3
cnt=1
w={-0.9881, 0.153811}
cnt=2
w={-0.996591, 0.0824949}
cnt=3
w={-0.996786, 0.0801079}
収束した:
w={-0.996786, 0.0801079}
cnt=3
Abs[w.wbefore]=0.999997
-1.26312
MatrixForm[truemat]

$$\begin{pmatrix} 0.13637 & 0.98782 \\ 0.990658 & -0.155599 \end{pmatrix}$$


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