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In[388]:= (*FastICA Negentropy Laplace *)
          x = RandomVariate[LaplaceDistribution[0, 1], 10 000];
          y = RandomVariate[LaplaceDistribution[0, 1], 10 000];
          A = {{5, 10}, {10, 2}};
          mt = A.{x, y};

In[437]:= ma = Transpose[mt];
          ListPlot[{ma[[All]]}, PlotRange → {{-50, 50}, {-50, 50}}];

In[394]:= mt = mt - Mean[Transpose[mt]];

In[395]:= Covariance[Transpose[mt]]

Out[395]= {{248.34, 141.216}, {141.216, 215.299}}

In[396]:= Eigenvalues[Covariance[Transpose[mt]]]

Out[396]= {373.998, 89.641}

In[397]:= Eigenvectors[Covariance[Transpose[mt]]]

Out[397]= {{-0.74706, -0.664757}, {0.664757, -0.74706}}

In[398]:= d12 = Eigenvalues[Covariance[Transpose[mt]]][[1]]^(-1/2)
          d22 = Eigenvalues[Covariance[Transpose[mt]]][[2]]^(-1/2)
          dmat = DiagonalMatrix[{d12, d22}]

Out[398]= 0.0517089

Out[399]= 0.10562

Out[400]= {{0.0517089, 0.}, {0., 0.10562}}

In[401]:= emat = Transpose[Eigenvectors[Covariance[Transpose[mt]]]]

Out[401]= {{-0.74706, 0.664757}, {-0.664757, -0.74706}}

In[402]:= vmat = emat.dmat.Transpose[emat]

Out[402]= {{0.0755323, -0.026773}, {-0.026773, 0.0817967}}

In[403]:= x = RandomVariate[LaplaceDistribution[0, 1], 10 000];
          y = RandomVariate[LaplaceDistribution[0, 1], 10 000];
          mt = A.{x, y};
          mt = mt - Mean[Transpose[mt]];

In[407]:= zmat = vmat.mt;

In[439]:= za = Transpose[zmat];
          ListPlot[{za[[All]]}, PlotRange → {{-3, 3}, {-3, 3}}];

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In[410]:= w = {1, 0};
w = w / Norm[w];
epsilon = 0.0001;
n = Length[x];
cnt = 1;
wbefore = w;
While[cnt < n,
  wbefore = w;
  w = (1 / n) * Sum[Tanh[w.zmat[[All, i]]] * zmat[[All, i]], {i, 1, n}] -
    (1 / n) * Sum[1 - (Tanh[w.zmat[[All, i]]])^2, {i, 1, n}] * w;
  w = w / Norm[w];
  Print["cnt=", cnt];
  Print["w=", w];
  ++cnt;
  If[1 - epsilon <= Abs[w.wbefore] && Abs[w.wbefore] <= 1 + epsilon,
    Print["収束した:"];
    Print["w=", w];
    Print["Abs[w.wbefore]=", Abs[w.wbefore]];
    cnt = n;
  ]
]
Kurtosis[w.zmat] - 3

cnt=1
w={-0.98548, 0.169793}

cnt=2
w={0.976347, -0.216212}

cnt=3
w={-0.973826, 0.227295}

収束した:
w={-0.973826, 0.227295}

Abs[w.wbefore]=0.999935

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Out[417]= 2.1857

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In[423]:= (* True Value*)
tmat = vmat.A;
truemat = {};
i = 1;
While[i ≤ 2,
  truemat = Append[truemat, tmat[[All, i]] / Norm[tmat[[All, i]]]];
  i++;
];
MatrixForm[truemat]

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Out[427]/MatrixForm=

$$\begin{pmatrix} 0.158659 & 0.987333 \\ 0.989169 & -0.146783 \end{pmatrix}$$

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In[428]:= w = RandomReal[{-1 / 2, 1 / 2}, 2];
w = w / Norm[w];
epsilon = 0.0001;
n = Length[x];
cnt = 1;
wbefore = w;
While[cnt < n,
  wbefore = w;
  w = (1 / n) * Sum[Tanh[w.zmat[[All, i]]] * zmat[[All, i]], {i, 1, n}] -
    (1 / n) * Sum[1 - (Tanh[w.zmat[[All, i]]])^2, {i, 1, n}] * w;
  w = w / Norm[w];
  Print["cnt=", cnt];
  Print["w=", w];
  ++cnt;
  If[1 - epsilon <= Abs[w.wbefore] && Abs[w.wbefore] <= 1 + epsilon,
    Print["収束した:"];
    Print["w=", w];
    Print["Abs[w.wbefore]=", Abs[w.wbefore]];
    cnt = n;
  ]
]
Kurtosis[w.zmat] - 3

cnt=1
w={0.974672, -0.223641}

cnt=2
w={-0.973367, 0.229253}

収束した:
w={-0.973367, 0.229253}

Abs[w.wbefore]=0.999983

Out[435]= 2.18498

In[436]:= MatrixForm[truemat]

Out[436]/MatrixForm=

$$\begin{pmatrix} 0.158659 & 0.987333 \\ 0.989169 & -0.146783 \end{pmatrix}$$


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