

Mixed strategies

Matching pennies

		Player Odd	
		↓ Heads	↓ Tails
Player Even	$\begin{matrix} 0.5 & p \\ \hline \end{matrix}$ Heads	1, <u>-1</u>	<u>-1, 1</u>
	$\begin{matrix} 0.5 & (1-p) \\ \hline \end{matrix}$ Tails	-1, <u>1</u>	1, <u>-1</u>

$$E_{\text{Odd}}(\text{Heads}) = (1-p) - p = \underline{1-2p}$$

$$E_{\text{Odd}}(\text{Tails}) = p + -1(1-p) = \underline{2p-1}$$

Indifference

$$E_{\text{Odd}}(H) = E_{\text{Odd}}(T)$$

$$1-2p = 2p-1$$

$$2 = 4p$$

$$\frac{2}{4} = p$$

$$\frac{1}{2}$$

Mixed strategy

$$p = \frac{1}{2} \quad H: 0.5, T: 0.5$$

Security games

		Adversary	
		Terminal 1	Terminal 2
Defender	$\begin{matrix} \frac{2}{5} & p \\ \hline \end{matrix}$ Terminal 1	5, <u>-3</u>	-1, <u>1</u>
	$\begin{matrix} \frac{2}{5} & (1-p) \\ \hline \end{matrix}$ Terminal 2	-5, <u>5</u>	2, <u>-1</u>

$$E_{\text{Adv}}(T1) = E_{\text{Adv}}(T2)$$

$$5-3p = 2p-1$$

$$6 = 5p$$

$$p = \frac{6}{5}$$

$$1-p = \frac{2}{5}$$

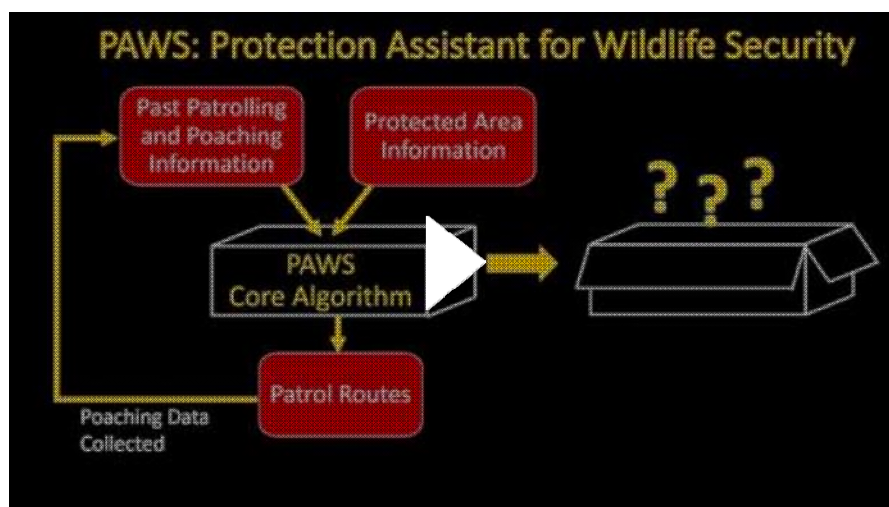
$$E_{\text{Adv}}(T1) = 5(1-p) - 3p = \underline{5-8p}$$

$$E_{\text{PAWS}}(\tau) = p^{-1} / (1-p) = 2p^{-1}$$

[Ferry escort](#)



[Save the Wildlife, Save the Planet: Protection Assistant for Wildlife Security \(PAWS\)](#)



Pure and mixed equilibria

		Player 2	
		$\downarrow \frac{3}{4}$ Left	$\frac{1}{4}$ Right
Player 1	$\rightarrow \frac{3}{4} \quad p$ Up	<u>3, 1</u>	0, 0
	$\rightarrow \frac{1}{4} \quad (1-p)$ Down	0, 0	<u>1, 3</u>

$$E_{P_2}(L) = E_{P_2}(R)$$

$$p = 3 - 3p$$

$$4p = 3$$

$$p = \frac{3}{4}$$

$$E_{P_2}(L) = p$$

$$E_{P_2}(R) = 3(1-p)$$

Assumptions

		Player Odd	
		Heads	Tails
Player Even	Heads	1, -1	<u>-1, 1</u>
	Tails	<u>-1, 1</u>	1, -1

- ① Rational
- ② Self interested
- ③ Perfect information
- ④ Pay-offs are known
- ⑤ Simultaneous moves