## Dr. BABASAHEB AMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE

**End Semester Examination: May 2018** 

Branch: B.Tech (Common to all)

Subject with code: Engineering Mathematics-II (MATH 201)

Marks: 60

Date: 14/05/2018

Time: 03 Hrs.

INSTRUCTION: Attempt any FIVE of the following questions. All questions carry equal marks.

## Q.1 Solve any three

(a) If 
$$arg(z+1) = \frac{\pi}{6}$$
 and  $arg(z-1) = \frac{2\pi}{3}$ , find z. [4 Marks]

(b) Solve: 
$$x^7 + x^4 + x^3 + 1 = 0$$
. [4 Marks]

(c) If 
$$\cos(\theta + i\phi) = \operatorname{Re}^{i\alpha}$$
, show that  $\phi = \frac{1}{2} \log_e \left( \frac{\sin(\theta - \alpha)}{\sin(\theta + \alpha)} \right)$ . [4 Marks]

(d) Prove that 
$$\tan \left\{ i \log \left( \frac{a - ib}{a + ib} \right) \right\} = \frac{2ab}{a^2 - b^2}$$
. [4 Marks]

## Q.2 Solve any three.

(a) Solve 
$$(4x-6y-1)dx+(3y-2x-2)dy=0$$
. [4 Marks]

(b) Solve 
$$\frac{dy}{dx} = \frac{y+1}{(y+2)e^y - x}$$
. [4 Marks]

(c) Solve 
$$(1+y^2) + (x-e^{\tan^{-1}y})\frac{dy}{dx} = 0$$
. [4 Marks]

(d) Determine the charge and current at any time 't' in a series R-C circuit with  $R = 10\Omega$ ,  $C = 2 \times 10^{-4}$  F and E = 100V, given that q(0) = 0. [4 Marks]

## Q.3. Solve any three.

(a) Solve 
$$\frac{d^2y}{dx^2} + 6\frac{dy}{dx} + 9y = 5^x - \log 2$$
. [4 Marks]

(b) Solve 
$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 5y = 25x^2$$
. [4 Marks]

(c) Solve 
$$(D^2 + 2D + 1)y = e^{-x} \log x$$
 by method of variation of parameters. [4 Marks]

(d) Solve 
$$x^2y'' - 3xy' + 5y = x^2 \sin(\log x)$$
. [4 Marks]

Q.4. (a) Obtain the Fourier series expansion of  $\sqrt{1-\cos x}$  in the interval  $0 \le x \le 2\pi$ . [6 Marks]

(b) Find the Half-range co-sine series for 
$$f(x) = \begin{cases} \frac{1}{4} - x & 0 < x < \frac{1}{2} \\ x - \frac{3}{4} & \frac{1}{2} < x < 1 \end{cases}$$
 [6 Marks]

- Q.5. (a) If a particle describes the curve  $r = 2a\cos\theta$  with constant angular speed  $\omega$ , find the [4 Marks] radial and transverse components of velocity and acceleration.
  - (b) For the curve  $x = t^3 + 1$ ,  $y = t^2$ , z = t, find the magnitude of tangential and normal components of acceleration at t = 1.
  - (c) If the particle describes the cardioid  $r = a(1 \cos \theta)$  under a force to the pole, show that the force is proportional to the inverse of the 4<sup>th</sup> power of the distance. [4 Marks]
- Q.6. (a) Find the directional derivative of  $\phi = 5x^2y 5y^2z + 2.5z^2x$  at the point p(1,1,1) in the direction of the line  $\frac{x-1}{2} = \frac{y-3}{-2} = z$ . [4 Marks]
  - (b) If  $\vec{F} = (ax+3y+4z)\hat{i} + (x-2y+3z)\hat{j} + (3x+2y-z)\hat{k}$  is solenoidal, [4 Marks] find the value of 'a'.
  - (c) Find the total work done in moving a particle in the force field,

given by 
$$\vec{F} = 3xy \hat{i} - 5z \hat{j} + 10x \hat{k}$$
 along the curve  $x = t^2 + 1$ ,  $y = 2t^2$ ,  $z = t^3$  from [4 Marks]  $t = 1$  to  $t = 2$ .

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