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Live Session Introduction

This is the live session work space for the course. Our goal with this repository, is that we're able to communicate *ahead of time* our aims for each week, and that you can prepare accordingly.

Bloom's Taxonomy

An effective rubric for student understanding is attributed to Bloom (1956). Referred to as *Bloom's Taxonomy*, this proposes that there is a hierarchy of student understanding; that a student may have one *level* of reasoning skill with a concept, but not another. The taxonomy proposes to be ordered: some levels of reasoning build upon other levels of reasoning.

In the learning objective that we present in for each live session, we will also identify the level of reasoning that we hope students will achieve at the conclusion of the live session.

- 1. **Remember** A student can remember that the concept exists. This might require the student to define, duplicate, or memorize a set of concepts or facts.
- 2. **Understand** A student can understand the concept, and can produce a working technical and non-technical statement of the concept. The student can explain why the concept *is*, or why the concept works in the way that it does.
- 3. **Apply** A student can use the concept as it is intended to be used against a novel problem.
- 4. **Analyze** A student can assess whether the concept has worked as it should have. This requires both an understanding of the intended goal, an application against a novel problem, and then the ability to introspect or reflect on whether the result is as it should be.
- 5. Evaluate A student can analyze multiple approaches, and from this analysis evaluate whether one or another approach has better succeeded at achieving its goals.
- 6. Create A student can create a new or novel method from axioms or experience, and can evaluate the performance of this new method against

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existing approaches or methods.

Chapter 1

Importance of Experimentation

Core questions for today

- Why do we conduct experiments?
- What is the value of making a causal statement?
- This is a data science program. With enough data and a savvy enough model, can't we just generate a causal statement that will be right? Can't I generate a statement that converges in probability to the *correct* value?

1.1 Learning Objectives

At the end of this live session, students will be able to

- 1. Remember (or find) the goals of the course, the assessment structure, and the learning model.
- 2. *Define*, in non-technical language, what it means for an action to cause an outcome.
- 3. *Understand* the difference between a causal statement, and an association statement.
- 4. Apply the framework of causal thinking against a series of studies to determine whether the study has achieved the goal that it intends.

1.2 Class Introductions

In no more than 2 minutes, could each student please:

• Introduce themselves, announcing their name as they would like it to be pronounced;

- Tell us where in the world they are studying;
- State what semester they are in the program;
- Any descriptive features that they would like the class to know about them (for example, gender pronouns); and,
- [Instructor's choice]

1.3 Course Plan

The course is built out into three distinct phases

- Part 1 Develops causal theory, potential outcomes, and a permutationbased uncertainty measurement
- Part 2 Further develops the idea of a treatment effect, and teaches how the careful design of experiments can improve the efficiency, and easy of analysis
- Part 3 Presents practical considerations when conducting an experiment, including problems that may arise, and how to design an experiment in anticipation of those problems.

1.4 Course Logistics

- bCourses
 - Learning Modules attached to weeks
 - Modules contain async lectures, coding exercises, and quizzes
- GitHub
 - All the course materials are available in a GitHub repository
 - We have protected the main branch, so you can't do anything destructive
 - Use that as empowerment! This is your class, propose changes that you would like to see!
- Github Classroom
 - Assignments will all be applied programming assignments against simulated and real data
 - All assignment code will be distributed through GitHub Classroom
- Gradescope
 - All assignments will be submitted to Gradescope where we'll read your solutions and provide scores and feedback

1.4.1 Learning model for the class

The course assignments are designed to put what we have learned in reading, async, and live session into practice in code. In our ideal version of your studying, we would have you working hard together with your classmates in a study group on the assignments, coming to office hours to talk candidly about what is and isn't working, and then *every single student* arriving at a full solution.

1.4.2 Feedback model for the class

We want to get you feedback very quickly after you turn your assignments.

- 1. We will release a solution set the day that you turn your assignment in
- 2. We will hold a problem set debrief office hour the Friday (i.e. next day) after the problem set it submitted
- 3. We will have light-feedback on your assignments within 7 days of when you submitted them.
- 4. You should bring your assignment to office hours after you have turned it in so that we can talk about any differences between your approach, and the instructors approach.

1.4.3 Office hour model for the class

- We will hold office hours Sunday through Thursday at 5:30.
- We will hold more than 10 hours of office hours every week; they will all be recorded, and any student is welcome in any office hour

1.5 Article Discussion

1.5.1 Predict or Cause

- What are a few examples that Athey raises of causal questions masquerading as prediction questions?
 - 1.
 - 2.
 - 3.
- Which of these examples is the most surprising to you?
- Is there something that is common to each of these examples? Is this a general phenomenon, or is Athey very clever in picking examples? Said differently, is Athey making a clever argument or is a lot of what we do as data scientists actually causal work in disguise?

1.5.2 Do the suburbs make you fat?

- 1. What is the causal claim being made in this article?
- 2. If you had to draw out this causal claim, using arrows, what would it look like?
- 3. Do you acknowledge the association that the authors present? Is there actually a difference between the BMI of people who live in cities and the suburbs?
- 4. If you acknowledge the association, does that compel you to believe the causal claim? Why or why not?
- 5. Name, and draw, five alternative *confounding* variables that might make you skeptical that the claimed relationship exists.

- 6. (Optional) Name, and draw two *mechanisms* that might exist between suburbs and BMI. Why does the existence (or not) of these mechanisms *not* pose a fundamental problem to the causal claim that the authors make?
- 7. At the conclusion of reading this paper, do you believe that there is a causal relationship between location and BMI? If so, what compels you to believe this; if not, why are you not compelled to believe this?

1.5.3 Nike Shoes

- 1. What is the causal claim being made in this article?
- 2. If you had to draw out this causal claim, using arrows, what would it look like?
- 3. Do you acknowledge the association that the authors present? Is there actually a difference in the finish time between people who are running with the Nike shoes vs. other shoes?
- 4. If you acknowledge the association, does that compel you to believe the causal claim? Why or why not?
- 5. What are some of the confounding relationships that the authors identify? (Can you name four?) How do they adjust their analyses once they acknowledge the confounding problem?
- 6. At the conclusion of reading this paper, do you believe that there is a causal relationship between shoes and finish time? If so, what compels you to believe this; if not, why are you not compelled to believe this?

1.5.4 What is Science: Feynman's View

In Cargo Cult Science, Richard Feynman poses a view of science that is about a seeking of the truth.

- 1. What is Feynman's view of science? What does he think makes something scientific?
- 2. What are ways that individuals fool themselves when they are working as scientists? What are ways that individuals fool themselves when they are working as data scientists?
- 3. How can we as (data) scientists, train ourselves not to be fooled?¹

 $^{^1{\}rm This}$ is a footnote, rendered into an html document.

Chapter 2

Apples to Apples

2.1 Learning Objectives

At the conclusion of this week's live session, student will be able to:

- 1. Describe, using the technical language of potential outcomes, what it means for an input to cause an output.
- 2. Describe the fundamental problem of causal inference.
- 3. Apply iid sampling as a method of producing an unbiased, consistent estimator of a population.
- 4. *Prove* that the average treatment effect estimator produces an unbiased, consistent estimator for the average treatment effect.

2.2 Revisiting Ideas of Science

Questions about epistemology are a *classic* question, and one that is particularly relevant not only at the School of Information where we have faculty and student whose work ranges from fields as diverse as computer science, psychology, sociology, law, and education – "What does it mean to *know* something?" We'll note that this question is not only an academic question, because in our workplaces we need to know how to take the best course of action. In this course, we like to think of *Science* as a method of coming to know something.

Think back to the reading and discussion from last week: For Feynman, what does it mean to be "Doing science?" Would Feynman say that data science, as we are practicing it, is a "science"? Would Feynman say that 205, or computer science is a science? Would Feynman say that 203 is a science? What about 251, 255, or 266?

For Lakatos, what does it mean for something to be a part of a science? What does it mean for something to be a part of a psuedo-science? Is it as simple a view

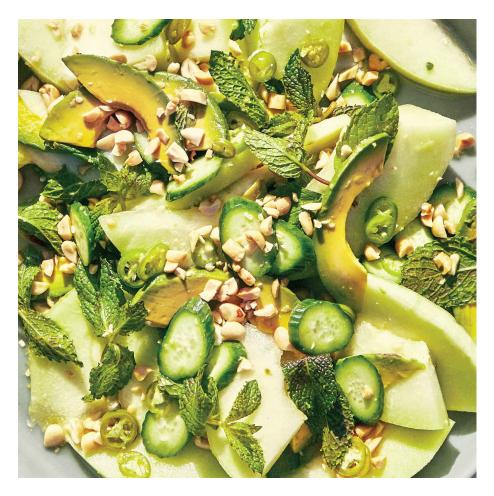


Figure 2.1: fruit salad

as Feynman espouses? Does the work that we conduct across the coursework in this program produce scientific knowledge as Lakatos see it?

What do you think produces knowledge? Can a single conversation produce knowledge? Can a non-experimental study produce knowledge about a causal effect? Can an experiment fail to produce knowledge? If an experiment fails to reject some null hypothesis, does that mean that it has not produced any knowlege?

2.3 This Causes That

What does it mean for an action to cause an outcome? Don't worry about conducting the experiment, or any measurement concerns at this point, just engage with the concepts.

2.3.1 Damn fine coffee

Suppose that you're getting ready for class, and you want to make sure that you're at your best. So, you drink a cup of water, eat a small snack, and brew a small pot of coffee for while you're in class.

Why do you do this?

Presumably, you're doing this because you like each of these things, but also because you're interested in these things causing you to have a better class. If you framed this as as causal question, you might ask:

If I drink a cup of coffee before class, will it cause me to be more alert?

What does it mean for coffee to cause alertness?

- Does coffee cause everyone to become more alert?
- Does coffee have to affect everyone equally in order for you to say it causes alertness?
- Could coffee have no effect for some people, and you would still say it causes alertness?

2.3.2 Meditation for focus

Suppose that you're getting ready for class, and you want ensure that you're at your best. So, you find a quiet place, and set your mind at ease with whatever form of meditation you think might be helpful.

If I meditate before class, will it cause me to be more focused?

What does it mean for meditation to cause focus?

- Does meditation cause everyone to become more focused?
- Does meditation have to affect everyone equally?

• Some people are frustrated by not being able to quiet their thoughts, and actually find meditation frustrating. Can this be true, and still believe that meditation causes focus?

2.3.3 Selling coffee and meditation

Suppose that you're an enterprising soul, and you want to sell a book about brewing coffee as a meditation. You reason that there must be a niche for this approach. To get the word out, you place a few flyers with tear off phone-numbers at the local yoga studios and tech incubators (good intuition to find those MIDS students).

If shown a flyer for coffee-meditation, will it cause someone to take my training?

What does it mean for for flyers to cause people to sign-up for the training?

- Does the flyer cause everyone to take the training?
- Does the flyer affect everyone equally?

One might be a radical behaviorist (Skinner is perhaps the most famous in this line of thinking) that says, "In matters of human behavior, if I cannot see it, then I cannot reason or know about." If this is your view, then you would simply stop your investigation (and reasoning) at the conclusion of your experiment.

In many ways, experiments suited only to answer empirical, observable questions. These are the questions, and lens proposed by the radical behaviorist paradigm.

2.3.4 Limits of Behaviorist Reasoning

If you accept only that coffee has this effect, and that it is measurable, are you able to translate this knowledge to a new context?

- Suppose that your experiments finds an effect of coffee on alertness: those who drink a cup of coffee are more alert in class.
- Suppose, though, that you're out of coffee *tonight*. A radical behaviorist would simply say, "I know not what to drink then to increase my alertness."

2.3.5 Reflecting on Causes

Does anything unify questions of causes?

When you think about {this} causing {that}, do you think about it at a population level, a smaller group level, or at the individual level?

2.3.6 Evaluating Value

Is this an entirely academic exercise, the discussion of {this} causing {that}? Or, is there some value to thinking about things in these terms? Susan Athey, whom we read last week, seems to think that there is value in distinguishing

between associations and causes. However, here is a view that is generated by an academic; much like the views of David and David, and all of the live session instructors. We're all academics, so maybe we're being *typical* academic pedants.

What is a case, perhaps that you read or wrote about for your first essay, mistakenly believing they had measured a causal effect? What would happen if they implemented the policy that is implicated in their study? Or, what would happen if they took action consonant with what their study purports to find?

2.3.7 Value of Theory

- Can you produce several theories (some of them might be silly) about why coffee might increase alertness in class?
 - Proposed theory #1:
 - Proposed theory #2:
 - Proposed theory #3:
- Does Feynman's approach to *Science* provide a method to adjudicate which of these theories is consonant with the evidence, and which are not consonant with the evidence?
- Does Lakatos' approach to *Science* provide such a method?

2.3.8 Evaluating Theories

- What data might you be able to produce that would allow you to "drive a wedge" between the different theories?
- This ability to proactively deign an experiment to distinguish between theories is the goal you're striving to achieve, and it is very hard to accomplish.

2.4 Reading Discussion: The Power of Experiments

The Power of Experiments starts the discussion of experimentation in the workplace with what is, for the course instructors, a uniquely pedestrian example, increasing contributions to taxes. In particular, Her Majesty's Revenue and Customs sends different versions of a letter to British taxpayers, and observes that different language leads to different amounts of taxes being paid.

2.4.1 Chapter One: The Power of Experiments

- 1. Is it *actually* a "big-deal" to increase tax compliance by 2 percentage points?
- 2. On page five, the book identifies five "one-liners" that HMRC chose to send to taxpayers:
- 3. Nine out of ten people pay their tax on time."

- 4. Nine out of ten people in the UK pay their tax on time.
- 5. Nine out of ten people in the UK pay their tax on time. You are currently in the very small minority of people who have not paid us yet."
- 6. Paying tax means we all gain from vital public services like the NHS, roads and schools.
- 7. Not paying tax means we all lose out on vital public services like the NHS, roads, and schools.
- 8. Which of these sentences would be the most effective at getting you to pay your taxes? Which do you think will be most effective, overall, at generating tax compliance? Why? How willing are you to make a million pound bet that you're correct?
- 9. Some of your instructors are vegetarians. None of them, however, has previously made an argument for why everyone should be vegetarian based on the example of Daniel and his study of diet and divine intervention. What about the study that Daniel conducted produces evidence that you think is useful for evaluating diet? What are the limitations that you see in this study? The book lists several, but there are other issues, along the lines of the exclusion restriction that Field Experiments identifies.
- 10. In order for Pasteur to be declared the winner of the vaccine argument, the observers said that every control group sheep had to die and every treatment group (i.e. vaccine-receiving) sheep had to live. Is this a fair burden of proof? Do the frequentest tests that we developed in 203 and are going to use here in 241 set a higher or lower bar than Pasteur faced? What are the merits of a relatively higher or lower bar?

2.4.2 Chapter Two: The Rise of Experimetrts in Psychology and Economics

Freud is noted as being specifically against experimentation. But, PoE then goes on to write, "[Freud's] big ideas inspired entire fields of psychological research. Including the notion that unconscious processes shape our judgement and behavior, psychological disorders are rooted in the mind rather than the body; and that sexual urges and behavior are worthy of study" (p. 19). Some of the theories that Freud promulgated were found to have evidence that was consistent with the theory; some of these theories could not produce evidence to support the theory; and many were outright contradicted by the evidence.

- 1. Is there value in being an "idea person"? How would you ever know if your ideas were actually right if you're unwilling to evaluate them?
- 2. What, if any, are the limitations of experimenting without any "big ideas" to ground your experiments?

Behaviorists (Skinner is the leading behaviorist) make a compelling argument: "One cannot directly observe what is happening in the mind of a person." A classic implication of this argument for behaviorists is that only that which is empirically observable is reasoned about. "Why does the rat avoid getting shocked? Does it really matter?" "Why does the child want a cookie? Does it

really matter why?"

1. Is this position reasonable for you to take as you navigate your own life? If you spoke with a therapist or a coach and said, "I've been feeling stressed over the past several weeks," would be satisfied with a *mindful* answer like, "Well, let's acknowledge those feelings and hold them for a moment" or would you want to reason further about why you feel stressed? What are the types of things in people's heads that you think we can profitably reason about; what are the types of things in people's heads that we cannot reason about? Is there something that is common to those that we can or cannot work with?

The experiments of Milgram and Zimbardo are widely identified as the reason that human-subjects review boards no exist. These review boards serve as an external review that keeps researchers from inflicting harm to individuals that is not outweighed by societal or scientific benefits.

- 1. What did Milgram and Zimbardo do to their subjects?
- 2. By talking continuing to talk about these experiments nearly fifty years after they were conducted even if we are talking about them negatively are we adding to the fame of these researchers? (For those interested in inside baseball, Zimbardo was the president of the American Psychology Association in 2002, and was awarded a lifetime achievement award from his discipline.) How should we learn and react to work that shouldn't have been conducted in the first place?

Kahneman and Tversky propose that individuals think about expected values differently depending on whether they are thinking in the domain of gains or the domain of losses. They come to this theory through the, now cringe-worthy, *Asian Disease Problem*:

In the positive frame, they ask the question:

Imagine that the US is preparing for the outbreak of an unusual Asian disease that is expected to kill 600 people. Two alternative programs to combat the disease have been proposed.

- If **Program A** is adopted, 200 people will be saved.
- If **Program B** is adopted, with a 1/3 probability 600 will be saved and with a 2/3 probability nobody will be saved.

The authors also present a countervailing pair of scenarios framed in terms of losses

- If **Program C** is adopted, 400 people will die.
- If **Program D** is adopted, there is a one-third probability that no one will die, and a 2/3 probability that everyone will die.

Clearly, all these programs have the same expected number of deaths; but, people can disagree about which of these is the program that we should pursue. Just ask as a poll in the class; and, ask people to justify their beliefs.

2.4.3 The Rise of Behavioral Experiments in Policymaking

PoE points out that experiments abound in policy making. Part of this stems from a truthful ignorance of the optimal policy to pursue. Another part of this stems from the ability of policy makers to make decisions by fiat that affect a large number of people.

1. Does this justification for experiments align with your current understeanding of the landscape in human-facing data science?

In a section titled **The nuance behind behavioral insights** the authors state a series of three caveats:

- 1. Context matters
- 2. Design choices matter
- 3. Unintended consequences abound
- 1. What do they mean when they raise the three points?
- 2. We are going to ask you to justify conducting experiments by staking out an extreme point of view, and asking you to convince us that this point of view is so extreme that it cannot be justified. "Writing that context matters, design choices matter, and unanticipated consequences abound is little more than writing that experiments cannot produce any more useful insights than the theories of Freud. As a result, there is little reason to conduct any experiments because what we learn will be highly contextualized, affected by very small implementation choices, and may generate as many (or more) negative outcomes as positive outcomes."

2.5 Potential Outcomes

Potential outcomes are a system of reasoning, and a corresponding notation, that allow us to talk about observable and un-observable characteristics of the world.

What is your position on *ontology*? What does it mean for something to exist?

- Does Field Experiments, as a textbook, exist?
- Do Don Green and Alan Gerber, the authors of the textbook that we're reading, exist?
- Does David Reiley, the slower-talking Davids in the async, exist?
- Do I, your section, instructor, exist (or am I a deep fake in this room with you)?
- Can a concept exist, even if you can't hold it? Even if you haven't seen it?

2.5.1 Defining Potential Outcomes

For each of the following sets of notation: (1) Read the notation aloud, not as "Y sub i zero", but instead as "The potential outcome to control ...".

- $Y_i(0)$:
- $Y_i(1)$:
- $E[Y_i(0)]$:
- $E[Y_i(1)]$:
- $E[Y_i(0)|D_i=0]$:
- $E[Y_i(1)|D_i=1]$:
- $E[Y_i(0)|D_i=1]$:
- $E[Y_i(1)|D_i=0]$:
- Which of these concepts that you have just read aloud exist?
- Can a concept exist, even if you can't hold it? Even if you can't see it?

2.6 Using Independence

Suppose that you have a random variable that is defined as the function,

$$Y = \begin{cases} \frac{1}{10} &, 0 \le y \le 10\\ 0 &, \text{ otherwise} \end{cases}$$

• What is the expected value of this function?

$$E[Y] = \int_0^{10} y \cdot f_y(y) \, dy$$

$$= \int_0^{10} y \cdot \frac{1}{10} \, dy$$

$$= \frac{1}{10} \int_0^{10} y \, dy$$

$$= \frac{1}{10} \cdot \frac{1}{2} y^2 \Big|_0^{10}$$

$$= \frac{1}{20} y^2 \Big|_0^{10}$$

$$= \frac{1}{20} \cdot [(100) - (0)]$$

$$= \frac{1}{20} \cdot 100$$

$$= \mathbf{5}$$

• Why is the expected value a good characterization of a random variable?

- If you wanted to write down an estimator to produce a summary statistic for Y given a sample of data, what properties do the following estimators possess:
- $\hat{\theta}_1 = y_1$

$$\bullet \quad \hat{\theta}_2 = \frac{1}{2} \sum_{i=1}^2 y_i$$

$$\bullet \ \hat{\theta}_3 = \frac{1}{n-1} \sum_{i=1}^N y_i$$

$$\bullet \ \hat{\theta}_4 = \frac{1}{n} \sum_{i=1}^N y_i$$

conduct_sample <- function(size) {
 runif(n=size, min=0, max=10)</pre>

```
}
theta_1 <- function(data) {</pre>
  # take the first element
}
theta_2 <- function(data) {</pre>
  # sum the first two elements and divide by two
}
theta_3 <- function(data) {</pre>
  # sum the sample, and divide by 1 less than the sample size
}
theta_4 <- function(data) {</pre>
  # sum the sample, and divide by the sample size
  # honestly, just use the mean call.
  # clearly, this is a silly function to write, since you're just
  # providing an alias, without modification, to an existing function.
  mean(data)
```

[1] 5.271191

theta_4(conduct_sample(size=100))

• Just to put a fine point on it: **What estimator properties does the sample average provide, and why are these desirable?"

2.7 Use Randomization to Produce Independence

How can we use the independence that is induced by "random **assignment** to treatment" combined with the sample average estimator to produce an estimate of an otherwise very difficult concept to measure?

2.8 Theoretical Justification

Before we show that this very simple ATE estimator work against a sample of data, it is worth reasoning about whether we can guarantee that it works in a general case. If we can show that it works in a general case, then any specific case inherits that guarantee. However, if we can only reason thorugh the existence of a single examlpe, it is not a sufficient argument to compell us to believe that it must hold for all cases.

Here's an example, "Behold! I see a black sheep! Therefore all sheep are black." This doesn't make sense, and it is not a logically sound argument. However, if you say, "All sheep say, 'Baaah!' This is a black sheep, so it must say 'Baah!' " is a logically sound arugment, so long as the antecedent is, in fact true. When we're proving something, we're proving that the antecedent to this statement is generally true. For anyone who took a symbolic logic course in, this method of argument might be marked down as $\forall X \implies \exists X$, whereas $\exists Y \not\Rightarrow \forall Y$.

- What concepts compose τ_{David} ?
- What concepts compose τ_i ?
- Is there any reason to believe that $\tau_{David\ Reiley} = \tau_{David\ Broockman}$?
- Is there any reason to believe that $\tau_i = \tau_j$, where $j \neq i$?
- Could $\tau_i = \tau j$?
- What is the fundamental problem of causal inference?

The proof for this argument is also made in *Field Experiments*, on or about page 30 of the text. However, in our view, the authors don't give enough room to fully develop this proof, and so we skipped right past it the first time that we read the chapter.

Begin our proof with the statement for what a treatment effect is, τ_i .

2.9 Simulation Example

Now, let's work through an example that shows this works not only in the math, but also in the realized, i.e. sampled, world.

To begin with, lets work with a *very* simple sample that has 100 observations, potential outcomes to control are uniformly distributed between 0 and 1 and every single unit has a potential outcome to treatment that is 0.25 units larger than their potential outcomes to control.

```
make_simple_data <- function(size=100) {
    require(data.table)

d <- data.table(id = 1:100)

d[ , y0 := runif(.N, min = 0, max = 1)]
    d[ , y1 := y0 + .25]

return(d)
}

d <- make_simple_data(size=100)</pre>
```

```
d[1:5]
```

```
## id y0 y1

## 1: 1 0.6220411 0.8720411

## 2: 2 0.1397788 0.3897788

## 3: 3 0.1595309 0.4095309

## 4: 4 0.8757292 1.1257292

## 5: 5 0.2374063 0.4874063
```

In this world, we've taken a sample of 100 individuals, and at this point, each of those individuals that we've sampled has both a potential outcome to control and also a potential outcome to treatment. We haven't talked at all about measurement yet; we're just asserting that both of these potential outcomes exist for each person.

Essentially, this stage of creating the sample is the same as bringing people in the door to your experiment. If you were running this in the laboratory, you'd literally think of this as sitting your subjects down at their chairs, getting ready to begin their task.

Is randomly sampling people to be a part of your experiment sufficient to ensure that your experiment produces an unbiased, consistent estimate of the true treamtent effect?

Suppose that for each unit, you then toss a coin, placing the subject either into treatment or control based on the result of that coin flip.

- Does this coin flip ensure that you have the same number of units in treatment as control? Does this matter to you? Why or why not?
- Are there other ways that you could assign individuals to treatment an control, rather than through a simple-randomization process?
- What are the relative merits or limitations of each of the methods?
- Are some of these methods *more random* than others? Or, are all things that are random equal in their randomness?

2.9.1 Assign to Treatment and Control

```
d[ , experimental_assignment := sample(0:1, size = .N, replace = TRUE)]
d[1:5]
```

```
## id y0 y1 experimental_assignment
## 1: 1 0.6220411 0.8720411 0
## 2: 2 0.1397788 0.3897788 1
## 3: 3 0.1595309 0.4095309 0
## 4: 4 0.8757292 1.1257292 0
## 5: 5 0.2374063 0.4874063
```

As as comparison, suppose that instead of randomly assigning individuals into

treatment and control we allowed individuals to select into treatment and control. And suppose that people with the lowest potential outcomes to control opt to take the treatment. You might think of this as being something like, "The people who are the most tired are the most likely to drink a cup of coffee before they start class," if an example helps you ground this.

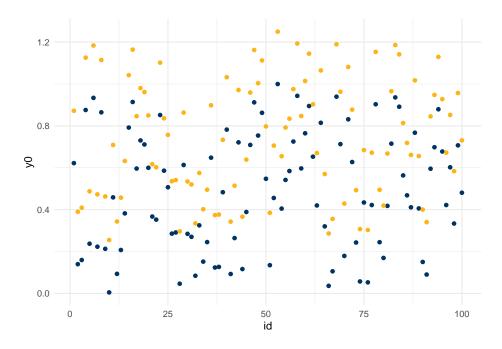
Specifically, suppose that any unit that has a potential outcome lower that 0.33 opts to take the treatment.

```
d[ , observational_selection := ifelse(y0 < .33, 1, 0)]
d[1:5]</pre>
```

```
## id y0 y1 experimental_assignment observational_selection
## 1: 1 0.6220411 0.8720411 0 0
## 2: 2 0.1397788 0.3897788 1 1 1
## 3: 3 0.1595309 0.4095309 0 1
## 4: 4 0.8757292 1.1257292 0 0
## 5: 5 0.2374063 0.4874063 0 1
```

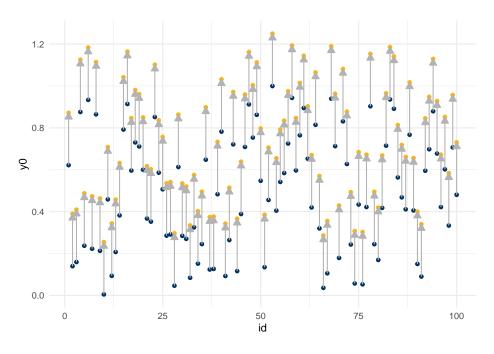
These represent two different ways that you might conduct your research, each time with the same subject pool. Of course, in reality you probably would not be able to run these two studies at the same time, but since this is a simulation, we can stretch the confines of reality just a little bit.

```
first_plot <- ggplot(data=d) +
  geom_point(aes(x = id, y = y0), color = blue) +
  geom_point(aes(x = id, y = y1), color = gold)
first_plot</pre>
```



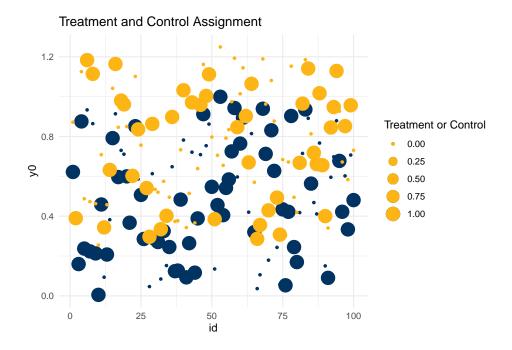
What's actually happening in this? It might be more clear if we add arrows to this plot to show.

```
first_plot +
  geom_segment(
   aes(x = id, xend = id, y = y0, yend = y1),
   arrow = arrow(ends = 'last', length = unit(0.1, "inches"), type = 'closed'),
   color = 'grey70'
)
```



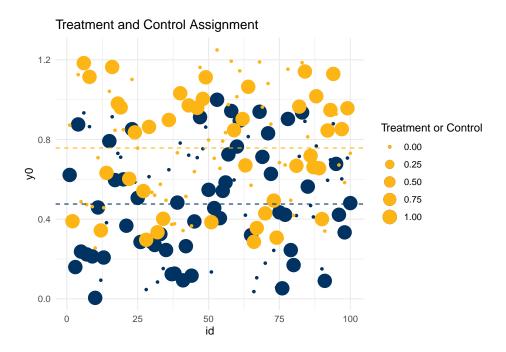
Even though these potential outcomes exist for all the units, is it possible to actually see them for all the units? How do we go about showing, and then measuring the potential outcomes to control for a set of units? How about the potential outcomes to treatment?

```
second_plot <- ggplot(data = d) +
  geom_point(
    aes(x = id, y = y0, size = 1 - experimental_assignment),
    color = blue) +
  geom_point(
    aes(x = id, y = y1, size = 0 + experimental_assignment),
    color = gold) +
  labs(
    title = 'Treatment and Control Assignment',
    size = 'Treatment or Control'
)</pre>
```



What are the averages of these samples that have been assigned to treatment?

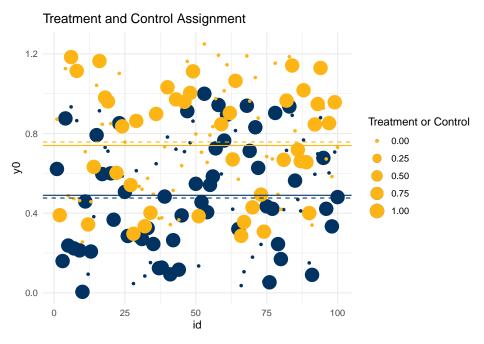
```
third_plot <- second_plot +
  geom_hline(
    yintercept = mean(d[experimental_assignment==0, y0]),
    color = blue,
    linetype = 2) +
  geom_hline(
    yintercept = mean(d[experimental_assignment==1, y1]),
    color = gold,
    linetype = 2)
third_plot</pre>
```



Even though we aren't able to see it, can we reason about what the sample average would be if we could see both of an individual's potential outcome to treatment and control?

- Is there a guarantee that the sample should be the same as the feasible realization?
- Should they be close? What property from 203 provides this guarantee?

```
third_plot +
  geom_hline(yintercept = mean(d[, y0]), color = blue, linetype = 1) +
  geom_hline(yintercept = mean(d[, y1]), color = gold, linetype = 1)
```



Put it all together, what has this little demo shown?

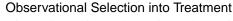
2.9.2 What if there is selection?

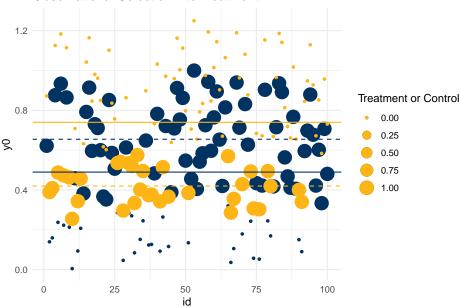
What if, rather than being assigned to treatment and control, instead individuals had been able to opt into treatment and control?

Produce only the last plot, but this time for the observational, or selected data.

```
selection_plot <- ggplot(d) +</pre>
  geom_point(
    aes(x = id, y = y0, size = 1 - observational_selection),
    color = blue) +
  geom_point(
    aes(x = id, y = y1, size = 0 + observational_selection), color = gold) +
  geom_hline(
    yintercept = mean(d[, y0]),
    color = blue,
    linetype = 1) +
  geom_hline(
    yintercept = d[observational_selection == 0, mean(y0)],
    color = blue,
    linetype = 2) +
  geom_hline(
    yintercept = mean(d[, y1]),
    color = gold,
```

```
linetype = 1) +
geom_hline(
    yintercept = d[observational_selection == 1, mean(y1)],
    color = gold,
    linetype = 2) +
labs(
    title = 'Observational Selection into Treatment',
    size = 'Treatment or Control'
)
selection_plot
```





2.10 Requirements of An Experiment

David Reiley makes the case that an experiment is something where we intervene in the world to produce knowledge. This is essentially providing a definition and making an argument that this is the correct definition. One difficulty with argument through definitions is that reasonable people can disagree because their definitions, through their lived experience, just disagree.

Here's the demonstrated proof:

Who in class is from the "midwest" broadly defined? Is Chicagostyle pizza, pizza per se? Who in class is from the east coast? Is Chicago-style pizza, pizza per se? Try not to make deep character judgments about your classmates.

Green and Gerber, in *Field Experiments* make additional requirements of experiments. As they argue on page 45 of the textbook, in their view, experiments require:

- 1. Random Assignment
- 2. Excludability
- 3. Non-interference

What do each of these terms mean? Why is each necessary?

- Did the experiment that Daniel conducted, described in *Power of Experiments* satisfy these three requirements? For any of these requirements that David's experiment did not satisfy, what are the consequences for the scientific knowledge that the experiment generated?
- Did the Nurses Health Study, described in the async, satisfy all these three requirements? For any that this experiment did not satisfy, what are the consequences for the scientific knowledge that the experiment generated?

2.10.1 Meta-Questions

- Can an experiment generate scientific knowledge about a causal effect, even without satisfying all of these requirements? Is it guaranteed to produce scientific knowledge about a causal effect?
- What then, justifies the use of experiments to measure causal effects?

Chapter 3

Quantifying Uncertainty

When we are working with a sample of data, estimates produced by an estimator might change – sometimes being higher than the *true* value, other times lower than the *true* value.

In Frequentist inference, we understand the variance in these estimates as sampling based variance of the sample estimator. In this week, we present a different inferential paradigm, Randomization Inference.

In randomization inference, there is no uncertainty about the parameter estimate that is generated in the experiment: The estimate that we observe is the estimate that we observe. Uncertainty, instead, comes from the acknowledgment that different *randomization* could have been realized, even from within the same sample.

3.1 Learning Objectives

At the end of this week's live session, students will be able to

- 1. *Understand* the sharp null, and how to apply it in an argument using randomization inference.
- 2. Describe how randomization creates uncertainty, and assess how this uncertainty differs from that in Frequentist paradigm
- 3. Apply the sharp null and randomization inference to data
- 4. Assess the assumptions necessary for Frequentist inference to produce nominal coverage on confidence intervals; assess the assumptions necessary for randomization inference to produce nominal coverage on confidence intervals; and, evaluate which of the two approaches is appropriate given a set of data.
- 5. Describe the concept of statistical power and what it means in the context of conducting an experiment.

3.2 Value of Theory

Suppose that you are evaluating the effect of coffee on students' alertness in class. You reason that drinking coffee will increase students' alertness in class.



Figure 3.1: "Damn Fine Coffee."

3.3 Stating the sharp null

Continue with our idea of an experiment to evaluate if coffee produces alertness in class. Here, we are going to further develop this notional experiment into something that we might actually be able to conduct.

- What is the *sharp null* hypothesis that is at risk in this investigation?
- How, if at all, does this sharp null differ from the null hypothesis you might be more familiar with?
- Is the sharp null hypothesis a concept that ever makes sense? Is the sharp null hypothesis a concept that is ever, actually, true?

3.4 Randomization Inference

3.4.1 Stating the process of Randomization Inference

Randomization inference is a method of understanding the variability of results in an experiment that you have conducted. It specifically acknowledges several facts:

- 1. The sample of data that you collected or used in your experiment is, quite simply, the sample of data that you collected for your experiment. There might be a larger population; there might be an infinite population; or, there might not.
- 2. The observed outcomes that you observe are, quite simply, the outcomes that you observed. There is no uncertainty about having seen these.
- 3. When the experiment assigned some units to treatment and others to the control, it revealed some outcomes, for some people. Specifically, it revealed the potential outcomes to treatment, denoted $Y_i(1)$ for those who were assigned to the treatment group and the potential outcomes to control, denoted $Y_i(0)$ for those who were assigned to the control group.
- 4. The experimenter chose one out of many possible treatment assignments.
- 5. If the sharp null hypothesis were to be true (note the subjunctive verb tense there) then, the particular revelation of potential outcomes to treatment and control are inconsequential. Despite seeing only half the data (referred to as the **Fundimental Problem of Causal Inference**) we actually posess all the data. After all, if the sharp null were true, $Y_{Alex}(1) = Y_{Alex}(0)$, and $Y_{David}(1) = Y_{David}(0)$, $Y_i(1) = Y_i(0)$ for all of the i = 1, ..., N people who are a part of the experiment.

3.4.2 Questions about Randomization Inference

- Where does uncertainty come from in an experiment that is evaluated using randomization inference?
- How is the ATE estimand defined?
- What is the feasible method that we use to write down an estimator (call it θ) for this quantity?
 - Which of the following properties does this feasible method possess?
 - a. Unbiasedness: $E[\theta] = ATE$
 - b. Convergence: $\theta \xrightarrow{p} ATE$, where \xrightarrow{p} means converges in probabilty
 - c. Efficiency: The mean squared error of θ is either (i) smaller than some other estimator, or (ii) as small is theoretically possible.

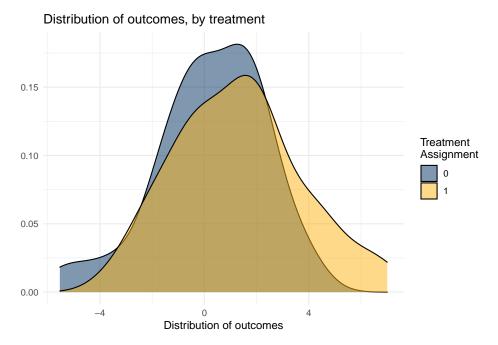
3.5 Applying Randomization Inference

3.5.1 Make Data

```
set.seed(1)
d <- data.table(
  id = 1:100,
  D = rep(0:1, each = 50),
  Y = c(rnorm(n=50, mean=0, sd=2.5), rnorm(n=50, mean=1, sd=2.5))
)</pre>
```

3.5.2 Plot Data

In the following plot, are you able to assess whether there is a treatment effect simply by looking at the distributions?



3.5.3 Classic Test

If you were to write a *classic* test against this data, given what you know about how it was generated, what would be the classic test? What do you learn from this test, and what is the interpretation?

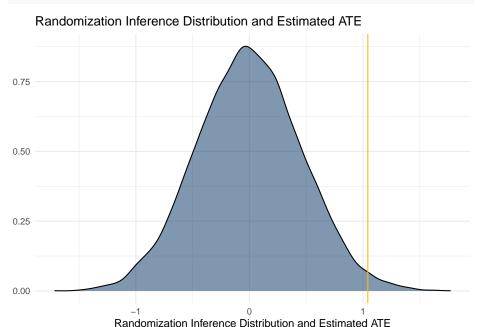
```
##
## Welch Two Sample t-test
##
## data: Y by D
## t = -2.309, df = 95.793, p-value = 0.02309
## alternative hypothesis: true difference in means between group 0 and group 1 is not equal to 0
## 95 percent confidence interval:
## -1.9381728 -0.1462181
## sample estimates:
## mean in group 0 mean in group 1
## 0.2511207 1.2933161
```

3.5.4 Randomization Inference Test

Now, instead suppose that you were to conduct the randomization inference. What are the steps to the algorithm for producing a result using randomization?

- 1. State the null hypothesis
- 2. Compute the statistic of interest using the observed data
- 3. Fill in data, under the statement of the null hypothesis
- 4. Permute the treatment assignment labels to generate a new sample of the treatment assignment vector, and then estimate the statistic of interest
- 5. Repeat the permutation and estimation (step 4) process repeatedly to sample from the randomization inference distribution of the statistic
- 6. Examine randomization inference distribution

```
x = 'Randomization Inference Distribution and Estimated ATE',
y = NULL,
title = 'Randomization Inference Distribution and Estimated ATE')
```



How much of the randomization inference is more extreme than the treatment effect?

```
ri_p_value <- mean(abs(ri_distribution) > abs(true_ate))
ri_p_value
```

[1] 0.0226

Notice that 0.023 of the randomization inference distribution is more extreme than the observed treatment effect. How does this compare to the t-test p-value that we calculated above?

3.6 Comparing Randomization Inference and Frequentist Inference

If both Randomization Inference and Frequentist Inference produce similar p-values, what is utility in learning another set of methods for communicating estimator-based uncertainty?

What are the requirements (frequently referred to as "assumptions") that are necessary for the Frequentist paradigm to provide guarantees? What happens if

these guarantees are not, in fact, satisfied or true in the data generating process? How do you react, respond, or address those problems?

- If data is not sampled *iid*, is it sufficient to simply note that limitation (frequently referred to as an "assumption violation") and report whatever p-value you report?
- How affected is this p-value by the violation? How do you know this?
- What does it mean for the p-value to be affected by this violation? (Recall that a p-value is just a random variable that is produced through a series of summarizing transformations and then a comparison against a reference distribution.)

3.6.1 Donations to a political campaign

In *Field Experiments* Green and Gerber provide some useful (hypothetical) data about donations to a political campaign. The data is defined in the following way, D is an indicator for whether the potential donor is assigned to treatment or control, and Y is the outcome of how much the potential donor actually gave.

Let us provide a little bit more back story, that is necessary for the example to work, fully. Suppose that a progressive political candidate was hosting a fundraiser in Berkeley and has to make a choice about what to serve the attendees at the fundraiser.

In the D=0 group, suppose that the candidate elects to serve a hippie-vegetarian staple, to fu sauteed in Bragg's liquid aminos. (It is Berkeley after all.) In the D=1 group, suppose that the candidate decides to be a little more, well, progressive in their vegetarian food offerings and instead serves Gado-Gado from Katzen's The Enchanted Broccoli Forest. (Still Berkeley.....)

After dinner, and the requisite drum-circle, attendees to this shin-dig are asked to donate to the candidates re-election efforts. Every attendee is expected to contribute something – social norms rule out failing to donate when the collection plate is passed – but the amount donated is at the discretion of the attendee.

1. With this data, conduct a t.test to assess whether the choice of dinner affects the amount donated to the campaign. What is your null-hypothesis (be specific), what is your rejection criteria, and do you reject or fail to reject this null hypothesis under the t-test framework.

```
## Null Hypothesis:
## Rejection Criteria:
```

```
## Conduct the Test Here:
## Conclusion:
```

2. With this data, use randomization inference to assess whether the choice of dinner affects the amount donated to the campaign. What is your null-hypothesis (be specific), what is your rejection criteria, and do you reject or fail to reject this null hypothesis under the t-test framework.

```
## Null Hypothesis:
## Rejection Criteria:
## Conduct the Test Here:
## Conclusion
```

- 1. Characterize the distribution of the sharp-null distribution of treatment effects. Talk about what, if anything, is notable about it, and what components of the data might be leading to any patterns that you note.
- 2. How many of the randomization inference loops are larger than the treatment effect that you calculated? How would you use this statement to construct a one-sided test, and an associated p-value?
- 3. How many of the randomization inference loops are *more extreme* (:metal:) than the treatment effect that you calculated? How would you use this statement to construct a two-sided test, and an associated p-value?
- 4. Compare the two-sided p-value against the p-value that you generate from a two-tailed t-test. If these p-values are the same, would this be a positive or a negative characteristic of randomization inference? If these p-values are different, why would they be different? Don't go looking all over hill-and-dale for the call for a t-test, it is at t.test.
- 5. Which of the two of these inferrential methods do you prefer, randomization inference or a t-test, and why? Ease of use is not an acceptable answer.

3.7 Statistical Power

Blocking and Clustering

4.1 Learning Objectives

1.

2.

Covariates and Regression

5.1 Learning Objectives

1.

2.

Regression and Multifactor Experiments

6.1 Learning Objectives

1.

Heterogeneous Treatment Effects

7.1 Learning Objectives

1.

2.

Treatment Noncompliance

Learning Objectives 8.1

1.

Spillover and Interference

9.1 Learning Objectives

1.

2.

Causality from Observational Data

10.1 Learning Objectives

1.

Problems and Diagnostics

11.1 Learning Objectives

1.

2.

Attrition, Mediation, and Generalizability

12.1 Learning Objectives

1.

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Applications of Experiments

Learning Objectives 13.1

1.

Review of the Course

14.1 Learning Objectives

1.

2.