A) Zerrenden gaineko eragiketak

Jarraian aipatzen diren eragiketak definitzen dituzten ekuazioak eman. Eragiketak [Int] eta [t] datu-motentzat dira:

1) inkr --

$$inkr:: ([Int]) \rightarrow [Int]$$

$$inkr([]) = [] \tag{#1}$$

$$inkr(x:s) = (x + 1) : inkr(s)$$
 (#2)

Adibidea:

$$\begin{aligned} & \text{inkr} ([4, 8, 5]) = \\ & = & \text{inkr}(4.8:5:[]) = {}^{(\#2)} \\ & = & (4+1): & \text{inkr}(8:5:[]) = {}^{(\#2)} \\ & = & 5: (8+1): & \text{inkr}(5:[]) = {}^{(\#2)} \\ & = & 5: 9: (5+1): & \text{inkr}([]) = {}^{(\#1)} \\ & = & 5: 9: 6: [] \\ & = & [5, 9, 6] \end{aligned}$$

Adibidea garatzerakoan, urrats bakoitzean zein ekuazio erabili den adierazten da (dagokion zenbakiaren bidez) eta gainera, ekuazioa formularen zein zatiri aplikatu zaion zehaztu da koloreak erabiliz. Bi kolore erabili dira irakurgarritasuna hobetzeko. Beste ariketeran ere irizpide bera jarraitu da.

2) batu --

batu:: ([Int])
$$\rightarrow$$
 Int

$$batu([]) = 0 \tag{#1}$$

$$batu(x:s) = x + batu(s)$$
 (#2)

$$batu([4, 8, 5]) = \\ = batu(4:8:5:[]) = (#2) & x = 4, s = 8:5:[] \\ = 4 + batu(8:5:[]) = (#2) & x = 8, s = 5:[] \\ = 4 + 8 + batu(5:[]) = (#2) & x = 5, s = [] \\ = 4 + 8 + 5 + batu([]) = (#1) \\ = 4 + 8 + 5 + 0 & = 17$$

3) bikoitirik --

bikoitirik:: ([Int]) \rightarrow Bool

$$bikoitirik([]) = False$$
 (#1)

bikoitirik(x:s)

$$| bikoitia(x) = True$$
 (#2)

| bakoitia(x) = bikoitirik(s) (#3)

1. adibidea:

bikoitirik([7, 5, 9]) =
= bikoitirik(7:5:9:[]) = (#3)
= bikoitirik(5:9:[]) = (#3)
= bikoitirik(9:[]) = (#3)
= bikoitirik([]) = (#1)
= False x = 7, s = 5:9:[] x = 5, s = 9:[] x = 9, s = []

2. adibidea:

bikoitirik([7, 5, 8, 9, 12]) =
= bikoitirik(7:5:8:9:12:[]) = (x = 7, s = 5:8:9:12:[])= bikoitirik(5:8:9:12:[]) = (x = 7, s = 5:8:9:12:[])= bikoitirik(8:9:12:[]) = (x = 8, s = 9:12:[])= True

3. adibidea:

bikoitirik([4, 5, 8, 9, 12]) = = bikoitirik(4:5:8:9:12:[]) = x = 4, x = 4, x = 5:8:9:12:[] = True

4) bik_posi --

 $bik_posi:: ([Int], [Int]) \rightarrow Bool$

 $bik_posi([], \ell)$

$$| \text{ not hutsa_da}(\ell) = \text{error "Luzera desberdina"}$$
 (#1)

otherwise = True (#2)

 $bik_posi(x:s, \ell)$

```
| luzera(x:s) \neq luzera(\ell) = error "Luzera desberdina" (#3)
| (bikoitia(x) && bikoitia(leh(\ell))) || (bakoitia(x) && bakoitia(leh(\ell)))
```

 $= bik_posi(s, hond(\ell))$ (#4)

otherwise = False (#5)

1. adibidea:

$$\begin{array}{lll} bik_posi([7,4,9],[5,10,1]) = \\ &= bik_posi(7:4:9:[],5:10:1:[]) = \\ &= bik_posi(4:9:[],10:1:[]) = \\ &= bik_posi(4:9:[],10:1:[]) = \\ &= bik_posi(9:[],1:[]) = \\ &= bik_posi([],[]) = \\ &= bik_posi([],[$$

2. adibidea:

$$\begin{array}{ll} bik_posi([7, 4, 8, 9], [5, 10, 1, 15]) = \\ = bik_posi(7:4:8:9:[], 5:10:1:15:[]) = ^{(\#4)} & x = 7, s = 4:8:9:[], \\ & leh(\ell) = 5, hond(\ell) = 10:1:15:[] \\ = bik_posi(4:8:9:[], 10:1:15:[]) = ^{(\#4)} & x = 4, s = 8:9:[] \\ & leh(\ell) = 10, hond(\ell) = 1:15:[] \\ = bik_posi(9:[], 1:[]) = ^{(\#5)} & x = 8, s = 9:[] \\ & leh(\ell) = 1, hond(\ell) = 15:[] \\ = False & \end{array}$$

3. adibidea:

5) azkena --

azkena::
$$([t]) \rightarrow t$$

azkena(x:s) | hutsa_da(s) = x (#2) | otherwise = azkena(s) (#3)

$$azkena([7, 5, 9]) =$$

$$= azkena(7:5:9:[]) = (#3)$$

$$= azkena(5:9:[]) = (#3)$$

$$= azkena(9:[]) = (#2)$$

$$= 9$$

$$x = 7, s = 5:9:[]$$

$$x = 5, s = 9:[]$$

$$x = 9, s = []$$

6) azkena_kendu --

azkena_kendu:: ([t]) \rightarrow [t]

azkena_kendu(x:s)

$$| \text{hutsa_da}(s) = []$$
 (#2)

otherwise =
$$x : azkena_kendu(s)$$
 (#3)

Adibidea:

7) alder --

Bi eratara:

a) ++ erabiliz

alder:: $([t]) \rightarrow [t]$

$$alder([]) = [] \tag{#1}$$

$$alder(x:s) = alder(s) ++ (x:[])$$
(#2)

Adibidea:

$$\begin{array}{l} alder([2,5,9]) = \\ = alder(2:5:9:[]) = ^{(\#2)} & x = 2, s = 5:9:[] \\ = alder(5:9:[]) ++ (2:[]) = ^{(\#2)} & x = 5, s = 9:[] \\ = alder(9:[]) ++ (5:[]) ++ (2:[]) = ^{(\#2)} & x = 9, s = [] \\ = alder([]) ++ (9:[]) ++ (5:[]) ++ (2:[]) = ^{(\#1)} \\ = [9,5,2] & \end{array}$$

b) azkena eta azkena_kendu erabiliz

alder::
$$([t]) \rightarrow [t]$$

$$alder([]) = [] \tag{#1}$$

$$alder(x:s) = azkena(x:s) : alder(azkena_kendu(x:s))$$
 (#2)

```
 alder([2, 5, 9]) = \\ = alder(2:5:9:[]) = (**2) \\ = azkena(2:5:9:[]) = 9, azkena_kendu(2:5:9:[]) = 2:5:[] \\ = 9: alder(2:5:[]) = (**2) \\ = 2: azkena(2:5:[]) = 5, azkena_kendu(2:5:[]) = 2:[] \\ = 2: 5: alder(2:[]) = (**2) \\ = 2: 5: 2: alder([]) = (**1) \\ = 3: 5: 2: alder([]) = (**1) \\ = 3: 5: 2: [] \\ = [9, 5, 2]
```

8) alder_dira --

Bi eratara:

a) alder erabiliz

$$\begin{aligned} & \text{alder_dira:: ([t], [t])} \rightarrow \text{Bool} \\ & \text{alder_dira(s, r)} \\ & | \text{s} == \text{alder(r)} & = \text{True} \\ & | \text{otherwise} & = \text{False} \end{aligned} \tag{\#1}$$

1. adibidea:

alder_dira([2, 5, 9], [9, 5, 2]) =
= alder_dira(2:5:9:[], 9:5:2:[]) =
$$s = 2:5:9:[], r = 9:5:2:[]$$

= True

2. adibidea:

alder_dira funtzioaren definizio honetan ez dago errekurtsibitaterik eta, horregatik, adibideak urrats bakar batean ebazten dira.

b) azkena, azkena_kendu, luzera eta hutsa_da erabiliz

$$\begin{array}{l} \text{alder_dira:: ([t], [t])} \rightarrow \text{Bool} \\ \\ \text{alder_dira([], ℓ)} \\ \mid \text{not hutsa_da(ℓ)} = \text{False} & (\#1) \\ \mid \text{otherwise} & = \text{True} & (\#2) \\ \\ \text{alder_dira(x:s, ℓ)} \\ \mid \text{luzera(x:s)} /= \text{luzera(ℓ)} & = \text{False} & (\#3) \\ \mid \text{x /= azkena(ℓ)} & = \text{False} & (\#4) \\ \mid \text{otherwise} & = \text{alder_dira(s, azkena_kendu(ℓ))} & (\#5) \\ \end{array}$$

1. adibidea:

$$\begin{array}{l} alder_dira([2,5,9],[9,5,2]) = \\ = alder_dira(2:5:9:[],9:5:2:[]) = \\ & azkena(\ell) = 2, \ azkena_kendu(\ell) = 9:5:[] \\ = alder_dira(5:9:[],9:5:[]) = \\ & x = 5, \ s = 9:[], \ \ell = 9:5:[] \\ & azkena(\ell) = 5, \ azkena_kendu(\ell) = 9:[] \\ = alder_dira(9:[],9:[]) = \\ & x = 9, \ s = [], \ \ell = 9:[] \\ & azkena(\ell) = 9, \ azkena_kendu(\ell) = [] \\ = alder_dira([],[]) = \\ & azkena(\ell) = 9, \ azkena_kendu(\ell) = [] \\ = alder_dira([],[]) = \\ & azkena(\ell) = 9, \ azkena_kendu(\ell) = [] \\ & azkena(\ell) = [] \\ & azkena(\ell) = [] \\ & azkena(\ell) = [] \\ & azkena($$

2. adibidea:

$$\begin{aligned} & \text{alder_dira}([2,5,9],[9,8,2]) = \\ & = & \text{alder_dira}(2:5:9:[], 9:8:2:[]) = \\ & = & \text{azkena}(\ell) = 2, \text{azkena_kendu}(\ell) = 9:8:[] \\ & = & \text{alder_dira}(5:9:[], 9:8:[]) = \\ & = & \text{azkena}(\ell) = 2, \text{azkena_kendu}(\ell) = 9:8:[] \\ & = & \text{azkena}(\ell) = 8, \text{azkena_kendu}(\ell) = 9:[] \end{aligned}$$

= False

alder_dira funtzioaren bigarren definizio honetan errekurtsibitatea erabili da eta, ondorioz, adibideak ebazteko orokorrean urrats bat baino gehiago behar dira.

9) aldiz --

$$\begin{aligned} &\text{aldiz:: } (t, [t]) \rightarrow \text{Int} \\ &\text{aldiz}(x, [t]) = 0 \end{aligned} \tag{\#1} \\ &\text{aldiz}(x, y:s) \\ &| x == y \\ &| \text{otherwise} \end{aligned} = 1 + &\text{aldiz}(x, s) \\ &\text{aldiz}(x, s) \end{aligned} \tag{\#2}$$

$$\begin{array}{ll} \text{aldiz}(8, [7, 8, 5, 9, 8]) = \\ = & \text{aldiz}(8, 7.8:5:9:8:[]) = ^{(\#3)} \\ = & \text{aldiz}(8, 8:5:9:8:[]) = ^{(\#2)} \\ = & 1 + & \text{aldiz}(8, 5:9:8:[]) = ^{(\#3)} \\ = & 1 + & \text{aldiz}(8, 9:8:[]) = ^{(\#3)} \\ = & 1 + & \text{aldiz}(8, 9:8:[]) = ^{(\#3)} \\ = & 1 + & \text{aldiz}(8, 8:[]) = ^{(\#2)} \\ = & 1 + 1 + & \text{aldiz}(8, []) = ^{(\#1)} \\ = & 1 + 1 + 0 = 2 \end{array}$$

$$\begin{array}{ll} x = 8, \ y = 7, \ s = 8:5:9:8:[] \\ x = 8, \ y = 8, \ s = 5:9:8:[] \\ x = 8, \ y = 9, \ s = 8:[] \\ x = 8, \ y = 8, \ s = [] \\ x = 8, \ y = 8, \ s =$$

10)erre --

erre:: $([t]) \rightarrow Bool$

$$erre([]) = False$$
 (#1)

erre(x:s)

$$| badago(x, s) = True$$
 (#2)

= erre(s) (#3)

1. adibidea:

$$erre([7, 5, 8, 9, 8]) =$$
 $= erre(7:8:5:9:8:[]) = (#3)$
 $= erre(5:8:9:8:[]) = (#3)$
 $= erre(8:9:8:[]) = (#2)$
 $= True$
 $x = 7, s = 5:8:9:8:[]$
 $x = 5, s = 8:9:8:[]$
 $x = 8, s = 9:8:[]$

2. adibidea:

$$\begin{array}{ll} \operatorname{erre}([7,5,8,9,1]) = \\ = \operatorname{erre}(7:8:5:9:1:[]) = ^{(\#3)} & x = 7, s = 5:8:9:1:[] \\ = \operatorname{erre}(5:8:9:1:[]) = ^{(\#3)} & x = 5, s = 8:9:1:[] \\ = \operatorname{erre}(8:9:1:[]) = ^{(\#3)} & x = 8, s = 9:1:[] \\ = \operatorname{erre}(9:1:[]) = ^{(\#3)} & x = 1, s = [] \\ = \operatorname{erre}([]) = ^{(\#1)} & x = 1, s = [] \end{array}$$

11)kendu --

 $kendu:: (t, [t]) \rightarrow [t]$

$$kendu(x, []) = [] \tag{#1}$$

kendu(x, y:s)

$$| x == y = kendu(x, s)$$
 (#2)
 $| otherwise = y: kendu(x, s)$ (#3)

12)bik kendu --

```
bik\_kendu:: ([Int]) \rightarrow [Int]
bik\_kendu([]) = [] \qquad (#1)
bik\_kendu(x:s)
| bikoitia(x) = bik\_kendu(s) \qquad (#2)
| bakoitia(x) = x:bik\_kendu(s) \qquad (#3)
```

Adibidea:

```
\begin{array}{lll} bik\_kendu([7, 5, 8, 9, 12]) = \\ &= bik\_kendu(7:5:8:9:12:[]) = (\#3) \\ &= 7:bik\_kendu(5:8:9:12:[]) = (\#3) \\ &= 7:5:bik\_kendu(8:9:12:[]) = (\#2) \\ &= 7:5:bik\_kendu(9:12:[]) = (\#3) \\ &= 7:5:9:bik\_kendu(12:[]) = (\#2) \\ &= 7:5:9:bik\_kendu(12:[]) = (\#2) \\ &= 7:5:9:[] = [7, 5, 9] \end{array} \qquad \begin{array}{ll} x = 7, \ s = 5:8:9:12:[] \\ x = 8, \ s = 9:12:[] \\ x = 9, \ s = 12:[] \\ x = 12, \ s = [] \end{array}
```

13)pos_bik_kendu --

pos_bik_kendu:: ([t]) \rightarrow [t]

```
pos_bik_kendu([]) = [] (#1)
```

```
pos_bik_kendu(x:s)

| hutsa_da(s) = x:s (#2)

| otherwise = x:pos_bik_kendu(hond(s)) (#3)
```

1. adibidea:

```
\begin{array}{l} pos\_bik\_kendu([7,5,8,9,12]) = \\ = pos\_bik\_kendu(7:5:8:9:12:[]) = ^{(\#3)} \\ & x = 7, \ s = 5:8:9:12:[], \ hond(s) = 8:9:12:[] \\ = 7:pos\_bik\_kendu(8:9:12:[]) = ^{(\#3)} \\ = 7:8:pos\_bik\_kendu(12:[]) = ^{(\#2)} \\ = 7:8:12:[] = [7,8,12] \end{array} \quad \begin{array}{l} x = 8, \ s = 9:12:[], \ hond(s) = 12:[] \\ x = 8, \ s = [] \end{array}
```

```
\begin{array}{ll} pos\_bik\_kendu([7, 5, 8, 9]) = \\ = pos\_bik\_kendu(7:5:8:9:[]) = \\ = 7:pos\_bik\_kendu(8:9:[]) = \\ = 7:8:pos\_bik\_kendu([]) = \\ = 7:8:[] = [7, 8] \end{array} \qquad \begin{array}{ll} x = 7, s = 5:8:9:[], \ hond(s) = 8:9:[] \\ x = 8, s = 9:[], \ hond(s) = [] \end{array}
```

14)pos_bak_kendu --

```
pos_bak_kendu:: ([t]) \rightarrow [t]
                                                               (#1)
pos_bak_kendu([]) = []
pos_bak_kendu(x:s)
   | hutsa_da(s)
                                                                       (#2)
                      = []
   otherwise
                      = leh(s):pos bak kendu(hond(s))
                                                                       (#3)
1. adibidea:
pos_bak_kendu([7, 5, 8, 9, 12]) =
= pos_bak_kendu(7:5:8:9:12:[]) = (#3)
                  x = 7, s = 5:8:9:12:[], leh(s) = 5, hond(s) = 8:9:12:[]
= 5:pos_bak_kendu(8:9:12:[]) = (#3)
                          x = 8, s = 9:12:[], leh(s) = 9, hond(s) = 12:[]
= 5:9:pos bak kendu(12:[]) = (*2)
                                   x = 8, s = []
= 5:9:[] = [5, 9]
2. adibidea:
pos_bak_kendu([7, 5, 8, 9]) =
= pos_bak_kendu(7:5:8:9:[]) = (#3)
```

x = 7, s = 5:8:9:[], leh(s) = 5, hond(s) = 8:9:[]

x = 8, s = 9:[], leh(s) = 9, hond(s) = []

15)erre_kendu --

= 5:9:[] = [5, 9]

erre_kendu:: ([t]) \rightarrow [t]

= 5:pos_bak_kendu(8:9:[]) =

 $= 5:9:pos_bak_kendu([]) = (#1)$

$$erre_kendu([]) = [] (#1)$$

```
erre_kendu([7, 5, 8, 5, 2, 8, 8]) =
= erre_kendu(7:5:8:5:2:8:8:[]) = (x = 7, s = 5:8:5:2:8:8:[])
= 7:erre_kendu(5:8:5:2:8:8:[]) = (x = 7, s = 5:8:5:2:8:8:[])
= 7:5:erre_kendu(8:2:8:8:[]) = (x = 7, s = 5:8:5:2:8:8:[])
= 7:5:8:erre_kendu(8:2:8:8:[]) = (x = 7, s = 5:8:5:2:8:8:[])
= 7:5:8:erre_kendu(2:[]) = (x = 7, s = 6:8:5:2:8:8:[])
= 7:5:8:2:erre_kendu([]) = (x = 7, s = 6:8:5:2:8:8:[])
= 7:5:8:2:erre_kendu([]) = (x = 7, s = 6:8:5:2:8:8:[])
= 7:5:8:2:erre_kendu([]) = (x = 7, s = 6:8:5:2:8:8:[])
= 7:5:8:2:erre_kendu([]) = (x = 7, s = 6:8:5:2:8:8:[])
= 7:5:8:2:erre_kendu([]) = (x = 7, s = 6:8:5:2:8:8:[])
```

16)erre_kendu2 --

erre_kendu2:: ([t]) \rightarrow [t]

$$erre_kendu2([]) = [] (#1)$$

erre_kendu2(x:s)

$$| badago(x, s) = erre_kendu2(s)$$
 (#2)

$$= x:erre \ kendu2(s)$$
 (#3)

Adibidea:

```
erre_kendu2([7, 5, 8, 5, 2, 8, 8]) =
= erre_kendu2(7:5:8:5:2:8:8:[]) = (#3)
                                                  x = 7, s = 5:8:5:2:8:8:[]
= 7:erre kendu2(5:8:5:2:8:8:[]) =
                                                  x = 5, s = 8:5:2:8:8:[]
= 7:erre_kendu2(8:5:2:8:8:[]) =
                                                  x = 8, s = 5:2:8:8:[]
= 7:erre_kendu2(5:2:8:8:[]) =
                                                  x = 5, s = 2:8:8:[]
= 7:5:erre kendu2(2:8:8:[])=
                                                  x = 2, s = 8:8:[]
= 7:5:2:erre_kendu2(8:8:[]) =
                                                  x = 8, s = 8:[]
= 7:5:2:erre_kendu2(8:[])=^{(#3)}
                                                   x = 8, s = []
= 7:5:2:8:erre_kendu2([])=^{(#1)}
= 7:5:2:8:[] = [7, 5, 2, 8]
```

17)bikote_berdin --

bikote_berdin:: ([t]) \rightarrow Bool

$$bikote_berdin([]) = False$$
 (#1)

bikote berdin(x:s)

$$| hutsa_da(s) | = False$$
 (#2)

$$| x == leh(s)$$
 = True (#3)

$$| otherwise = bikote_berdin(s)$$
 (#4)

1. adibidea:

```
bikote_berdin([7, 5, 8, 8, 6, 5]) =
= bikote_berdin(7:5:8:8:6:5:[]) = (x = 7, s = 5:8:8:6:5:[], leh(s) = 5
= bikote_berdin(8:8:6:5:[]) = (x = 7, s = 5:8:8:6:5:[], leh(s) = 5
= bikote_berdin(8:8:6:5:[]) = (x = 7, s = 5:8:8:6:5:[], leh(s) = 5
= True

(x = 7, s = 5:8:8:6:5:[], leh(s) = 8
= (x = 8, s = 8:6:5:[], leh(s) = 8
= True
```

18)aurrizkia --

aurrizkia:: ([t], [t]) \rightarrow Bool

aurrizkia([],
$$\ell$$
) = True (#1)

aurrizkia(x:s, ℓ)

$$| \text{hutsa_da}(\ell) | = \text{False}$$
 (#2)

$$| x / = leh(\ell)$$
 = False (#3)

otherwise =
$$\operatorname{aurrizkia}(s, \operatorname{hond}(\ell))$$
 (#4)

1. adibidea:

2. adibidea:

$$\begin{aligned} & \text{aurrizkia}([1,2,3], [1,2,3,5,6]) = \\ & = \underset{\text{aurrizkia}(1:2:3:[], 1:2:3:5:6:[])}{\text{x} = 1, \text{s} = 2:3:[], \ell = 1:2:3:5:6:[], \text{leh}(\ell) = 1, \text{hond}(\ell) = 2:3:5:6:[]} \\ & = \underset{\text{aurrizkia}(2:3:[], 2:3:5:6:[])}{\text{aurrizkia}(2:3:[], 2:3:5:6:[])} = \\ & \quad \text{x} = 2, \text{s} = 3:[], \ell = 2:3:5:6:[], \text{leh}(\ell) = 2, \text{hond}(\ell) = 3:5:6:[]} \\ & = \underset{\text{aurrizkia}(3:[], 3:5:6:[])}{\text{aurrizkia}(3:[], 3:5:6:[])} = \\ & \quad \text{x} = 3, \text{s} = [], \ell = 3:5:6:[], \text{leh}(\ell) = 3, \text{hond}(\ell) = 5:6:[]} \\ & = \underset{\text{aurrizkia}([], 5:6:[])}{\text{aurrizkia}([], 5:6:[])} = \\ \end{aligned}$$

= True

```
\begin{aligned} & \text{aurrizkia}([1,2,3],[1,2]) = \\ & = \underset{\text{aurrizkia}(1:2:3:[], 1:2:[])}{\text{x}} = \underset{\text{aurrizkia}(2:3:[], 2:[])}{\text{(}} = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 1; \text{hond}(\ell) = 2:[]; \\ & = \underset{\text{aurrizkia}(2:3:[], 2:[])}{\text{(}} = \underset{\text{(}}{\text{(}} = 2:[], \text{leh}(\ell) = 2; \text{hond}(\ell) = []; \\ & = \underset{\text{aurrizkia}(3:[], [])}{\text{(}} = \underset{\text{(}}{\text{(}} = 2:[], \text{leh}(\ell) = 2; \text{hond}(\ell) = []; \\ & = \underset{\text{(}}{\text{True}} = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \text{leh}(\ell) = 2; \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & = \underset{\text{(}}{\text{(}} = 1;2:[], \text{leh}(\ell) = 2; \\ & =
```

19)azpizer --

azpizer::
$$([t], [t]) \rightarrow Bool$$

$$azpizer([], \ell) = True$$
 (#1)

 $azpizer(x:s, \ell)$

$$| \text{hutsa_da}(\ell) | = \text{False}$$
 (#2)

$$| \operatorname{aurrizkia}(x:s, \ell) | = \operatorname{True}$$
 (#3)

otherwise =
$$azpizer(x:s, hond(\ell))$$
 (#4)

1. adibidea:

$$\begin{aligned} & \text{azpizer}([4,5],[1,2,5,6]) = \\ & = \text{azpizer}(4:5:[],1:2:5:6:[]) =^{(\#4)} \\ & \qquad \qquad x = 4, \, s = 5:[], \, \ell = 1:2:5:6:[], \, \text{hond}(\ell) = 2:5:6:[] \\ & = \text{azpizer}(4:5:[],2:5:6:[]) =^{(\#4)} \\ & \qquad \qquad x = 4, \, s = 5:[], \, \ell = 2:5:6:[], \, \text{hond}(\ell) = 5:6:[] \\ & = \text{azpizer}(4:5:[],5:6:[]) =^{(\#4)} \\ & \qquad \qquad x = 4, \, s = 5:[], \, \ell = 5:6:[], \, \text{hond}(\ell) = 6:[] \\ & = \text{es_sublista}(4:5:[],6:[]) =^{(\#4)} \\ & \qquad \qquad x = 4, \, s = 5:[], \, \ell = 6:[], \, \text{hond}(\ell) = [] \\ & = \text{es_sublista}(4:5:[],[]) =^{(\#2)} \end{aligned}$$

 $x = 4, s = 5:[], \ell = []$

= False

20)elem_pos --

elem_pos:: (Int, [t]) \rightarrow t

elem_pos(pos, x:s)

$$|pos| <= 0 ||pos| > luzera(x:s)$$
 = error "Ez da egokia" (#2)

$$|pos == 1 = x \tag{#3}$$

$$| otherwise = elem_pos(pos - 1, s)$$
 (#4)

Adibidea:

21)sartu --

sartu:: (Int, t, [t]) \rightarrow [t]

$$sartu(pos, x, [])$$

| $pos /= 1$ = error "Ez da egokia" (#1)

$$| pos == 1$$
 $= x:[]$ (#2)

sartu(pos, x, y:s)

$$|pos| <= 0 ||pos| > (luzera(x:s) + 1) = error "Ez da egokia" (#3)$$

$$|pos == 1 = x:y:s$$
 (#4)

otherwise =
$$y:sartu(pos - 1, x, s)$$
 (#5)

Adibidea:

22)lehen_bik_pos --

lehen_bik_pos:: (Int, [t])
$$\rightarrow$$
 t

$$lehen_bik_pos([]) = 1 (#1)$$

$$lehen_bik_pos(x:s) | x \mod 2 == 0$$
 = 1 (#2)

otherwise = $1 + lehen_bik_pos(s)$ (#3)

1. adibidea:

lehen_bik_pos([5, 9, 8, 6]) =
= lehen_bik_pos(5:9:8:6:[]) = (s = 1 + 1 + 1 + 1 = 3) x = 5, s = 9:8:6:[] x = 5, s = 9:8:6:[] x = 9, s = 8:6:[] x = 8, s = 6:[]

2. adibidea:

23)azken_pos --

 $azken_pos:: (Int, [Int]) \rightarrow Int$

$$azken_pos(x, []) = 0 (#1)$$

 $azken_pos(x, y:s)$ | $x \neq y & not badago(x, s) = 0$ (#2) | otherwise = 1 + $azken_pos(x, s)$ (#3)

1. adibidea:

 $azken_pos(8, [8, 6, 8, 5]) =$ $= azken_pos(8, 8:6:8:5:[]) =$ $= 1 + azken_pos(8, 6:8:5:[]) =$ $= 1 + 1 + azken_pos(8, 8:5:[]) =$ $= 1 + 1 + 1 + azken_pos(8, []) =$ = 1 + 1 + 1 + 0 = 3 x = 8, y = 8, s = 6:8:5:[] x = 8, y = 8, s = 5:[] x = 8, y = 8, s = 5:[]

2. adibidea:

 $azken_pos(8, [3, 2]) =$ $= azken_pos(8, 3:2:[]) = {}^{(#2)}$ = 0 x = 8, y = 3, s = 2:[]

Funtzioa definitzeko beste aukera bat:

 $azken_pos:: (Int, [Int]) \rightarrow Int$

$$azken_pos(x, []) = 0 (#1)$$

azken_pos(x, y:s)

$$| x == y$$
 = 1 + azken_pos(x, s) (#2)

$$| badago(x, s) = 1 + azken_pos(x, s)$$
 (#3)

| otherwise = 0 (#4)

1. adibidea:

$$\begin{array}{l} azken_pos(8, [8, 6, 8, 5]) = \\ = \underbrace{azken_pos(8, 8:6:8:5:[])}_{=} = \underbrace{(\#2)}_{=} \\ = 1 + \underbrace{azken_pos(8, 6:8:5:[])}_{=} = \underbrace{(\#3)}_{=} \\ = 1 + 1 + \underbrace{azken_pos(8, 8:5:[])}_{=} = \underbrace{(\#2)}_{=} \\ = 1 + 1 + 1 + \underbrace{azken_pos(8, [])}_{=} = \underbrace{(\#1)}_{=} \\ = 1 + 1 + 1 + 0 = 3 \end{array}$$

$$x = 8, y = 8, s = 6:8:5:[]$$

$$x = 8, y = 8, s = 5:[]$$

$$x = 8, y = 8, s = 5:[]$$

2. adibidea:

$$azken_pos(8, [3, 2]) =$$
 $= azken_pos(8, 3:2:[]) = (#4)$
 $= 0$
 $x = 8, y = 3, s = 2:[]$

24)hand --

hand:: ([Int]) \rightarrow Int

hand(x:s)

$$| hutsa_da(s) = x$$
 (#2)

$$| x >= leh(s) = hand(x:hond(s))$$
 (#3)

$$| otherwise = hand(s)$$
 (#4)

```
\begin{array}{ll} \text{hand}([5,3,8,7,8]) = \\ = & \text{hand}(5:3:8:7:8:[]) = \\ = & \text{hand}(5:3:8:7:8:[]) = \\ = & \text{hand}(5:8:7:8:[]) = \\ = & \text{hand}(5:8:7:8:[]) = \\ = & \text{hand}(8:7:8:[]) = \\ = & \text{hand}(8:7:8:[]) = \\ = & \text{hand}(8:8:[]) = \\ = & \text{hand}(8:8:[]) = \\ = & \text{hand}(8:[]) = \\ = & \text{hand}(8:[
```

25)elkartu --

a) Aurretik definituta dagoen beste funtziorik erabili gabe

elkartu::
$$([t], [t]) \rightarrow [t]$$

$$elkartu([], \ell) = \ell \tag{#1}$$

$$elkartu(x:s, \ell) = elkartu(s, x: \ell)$$
 (#2)

Adibidea:

elkartu([5, 3, 8], [7, 9]) =
= elkartu(5:3:8:[], 7:9:[]) =
$$(\#2)$$
= elkartu(3:8:[], 5:7:9:[]) = $(\#2)$
= elkartu(8:[], 3:5:7:9:[]) = $(\#2)$
= elkartu([], 8:3:5:7:9:[]) = $(\#2)$
= 8:3:5:7:9:[] = $(\#3)$
 $\ell = 8:3:5:7:9:[]$

b) Aurretik definituta dauden beste funtzio hauek erabiliz: alder eta ++

elkartu:: ([t], [t])
$$\rightarrow$$
 [t]
elkartu($\ell 1$, $\ell 2$) = alder($\ell 1$) ++ $\ell 2$ (#1)

Kasu honetan *elkartu* funtzioaren definizioa ez da errekurtsiboa.

Adibidea:

elkartu([5, 3, 8], [7, 9]) =
= elkartu(5:3:8:[], 7:9:[]) =
$$\ell = 0$$
= 8:3:5:[] ++ 7:9:[]
= 8:3:5:7:9:[] = [8,3,5,7,9]

Beste aukera bat:

elkartu:: ([t], [t])
$$\rightarrow$$
 [t]

$$elkartu([], \ell) = \ell \tag{#1}$$

$$elkartu(x:s, \ell) = alder(s) ++ (x:\ell)$$
 (#2)

elkartu([5, 3, 8], [7, 9]) =
= elkartu(5:3:8:[], 7:9:[]) =
$$(x = 5, s = 3:8:[], \ell = 7:9:[]$$

= 8:3:[] ++ 5:7:9:[] = [8,3,5,7,9]

26)ezabatu --

```
ezabatu:: (Int, [t]) \rightarrow [t]
ezabatu(zenbat, [])
   | zenbat /= 0
                                   = error "Ez da egokia"
                                                                  (#1)
   otherwise
                                   =[]
                                                                  (#2)
ezabatu(zenbat, x:s)
   | zenbat < 0 || zenbat > luzera (x:s)
                                          = error "Ez da egokia"
                                                                          (#3)
   | zenbat == 0
                                          = x:s
                                                                          (#4)
   otherwise
                                           = ezabatu(zenbat -1, s)
                                                                          (#5)
Adibidea:
ezabatu(3, [7, 6, 8, 5, 9]) =
= ezabatu(3, 7:6:8:5:9:[]) = (#5
                                           zenbat = 3, x = 7, s = 6.8.5.9.
= ezabatu(2, 6:8:5:9:[]) =
                                           zenbat = 2, x = 6, s = 8:5:9:[]
= ezabatu(1, 8:5:9:[]) =
                                           zenbat = 1, x = 8, s = 5:9:[]
= ezabatu(0, 5:9:[]) =
                                           zenbat = 0, x = 5, s = 9:[]
= 5:9:[] = [5, 9]
```

27)hartu --

```
hartu:: (Int, [t]) \rightarrow [t]
hartu(zenbat, [])
   | zenbat /= 0
                                    = error "Ez da egokia"
                                                                    (#1)
   otherwise
                                    =[]
                                                                    (#2)
hartu(zenbat, x:s)
   | zenbat < 0 || zenbat > luzera (x:s)
                                            = error "Ez da egokia"
                                                                            (#3)
   | zenbat == 0
                                            = []
                                                                            (#4)
```

= x:hartu(zenbat - 1, s)

Adibidea:

otherwise

```
hartu(3, [7, 6, 8, 5, 9]) =
= hartu(3, 7:6:8:5:9:[]) = (#5)
                                                 zenbat = 3, x = 7, s = 6:8:5:9:[]
= 7:hartu(2, 6:8:5:9:[]) =
                                                 zenbat = 2, x = 6, s = 8:5:9:[]
=7:6:\frac{\text{hartu}(1, 8:5:9:[])}{\text{hartu}(1, 8:5:9:[])}
                                                 zenbat = 1, x = 8, s = 5:9:[]
= 7:6:8:hartu(0, 5:9:[]) =
                                                 zenbat = 0, x = 5, s = 9:[]
= 7:6:8:[] = [7, 6, 8]
```

(#5)

28)kolapsatu --

a)

kolapsatu:: ([Int]) \rightarrow [Int]

$$kolapsatu([]) = []$$
 (#1)

kolapsatu(x:s)

$$| \text{hutsa_da}(s) = x:s$$
 (#2)

$$| x == leh(s) = kolapsatu(s)$$
 (#3)

| otherwise = x:kolapsatu(s) (#4)

b)

Adibidea:

```
kolapsatu([3, 9, 9, 3]) =
= kolapsatu(3:9:9:3:[]) = (#4)
= 3:kolapsatu(9:9:3:[]) = (#4)
= 3:y:kolapsatu(3:[]) = (#4)
= 3:9:3:[] = [3, 9, 3]

x = 3, s = 9:9:3:[], leh(s) = 9
x = 9, s = 3:[], leh(s) = 9
x = 9, s = 3:[], leh(s) = 3
x = 3, s = []
```

29)hedatu --

a)

hedatu:: ([Int]) \rightarrow [Int]

$$hedatu([]) = [] \tag{#1}$$

hedatu(x:s)

$$| hutsa_da(s) = x:s$$
 (#2)

$$| x \mod 2 == 0$$
 = $x:hedatu((x + leh(s)):hond(s))$ (#3)

$$= x:hedatu(s)$$
 (#4)

b)

$$\begin{array}{l} \text{hedatu}([8,7,2]) = \\ = \frac{\text{hedatu}(8:7:2:[])}{\text{e}^{\#3}} \\ = 8:\frac{\text{hedatu}(15:2:[])}{\text{e}^{\#4}} \\ = 8:15:\frac{\text{hedatu}(2:[])}{\text{e}^{\#2}} \\ = 8:15:2:[] = [8,15,2] \end{array} \qquad \begin{array}{l} x = 8, \text{ s} = 7:2:[], \text{ leh(s)} = 7, \text{ hond(s)} = 2:[] \\ x = 15, \text{ s} = 2:[], \text{ leh(s)} = 2, \text{ hond(s)} = [] \\ x = 2, \text{ s} = [] \end{array}$$

30)zapaldu --

a) $zapaldu:: ([Int]) \rightarrow [Int]$

$$zapaldu([]) = [] \tag{#1}$$

zapaldu(x:s)

$$| \text{hutsa_da}(s) = x:s$$
 (#2)

$$|x\rangle = leh(s)$$
 = x:zapaldu(x:hond(s)) (#3)

$$| otherwise = x:zapaldu(s)$$
 (#4)

b)

```
\begin{aligned} &\text{zapaldu}([3, 9, 9, 3]) = \\ &= &\text{zapaldu}(3:9:9:3:[]) = {}^{(\#4)} \\ &= &3: &\text{zapaldu}(9:9:3:[]) = {}^{(\#3)} \\ &= &3:9: &\text{zapaldu}(9:3:[]) = {}^{(\#3)} \\ &= &3:9:9: &\text{zapaldu}(9:[]) = {}^{(\#3)} \\ &= &3:9:9: &\text{zapaldu}(9:[]) = {}^{(\#2)} \\ &= &3:9:9:9:[] = [3, 9, 9, 9] \end{aligned} \qquad \begin{aligned} &x = 3, s = 9:9:3:[], \text{ leh}(s) = 9, \text{ hond}(s) = 9:3:[] \\ &x = 9, s = 3:[], \text{ leh}(s) = 3, \text{ hond}(s) = [] \\ &x = 9, s = [] \end{aligned}
```

31)hondoratu --

a)

hondoratu:: ([Int]) \rightarrow [Int]

$$hondoratu([]) = [] \tag{#1}$$

hondoratu(x:s)

$$| \text{hutsa_da}(s) = x:s$$
 (#2)

$$|x> leh(s)| = leh(s):hondoratu(x:hond(s))|$$
 (#3)

$$= x:s$$
 (#4)

b)

```
\begin{array}{l} \mbox{hondoratu}([8,3,2,9]) = \\ = \mbox{hondoratu}(8:3:2:9:[]) = (\#3) \\ = 3:\mbox{hondoratu}(8:2:9:[]) = (\#3) \\ = 3:2:\mbox{hondoratu}(8:2:9:[]) = (\#3) \\ = 3:2:8:9:[] = [3,2,8,9] \end{array} \quad \begin{array}{l} x = 8, \ s = 3:2:9:[], \ leh(s) = 3, \ hond(s) = 2:9:[] \\ x = 8, \ s = 2:9:[], \ leh(s) = 2, \ hond(s) = 9:[] \\ x = 8, \ s = 9:[], \ leh(s) = 9, \ hond(s) = [] \end{array}
```

32)elem_kendu --

```
a)
   elem_kendu:: ([Int], Int) \rightarrow [Int]
   elem_kendu([], pos) = error "Zerrenda hutsa"
                                                                              (#1)
   elem_kendu(x:s, pos)
       \mid pos \le 0 \mid pos > luzera(x:s)
                                              = error "Ez da egokia"
                                                                              (#2)
       | pos == luzera(x:s)
                                              = s
                                                                              (#3)
       otherwise
                                              = x:elem_kendu(s, pos)
                                                                              (#4)
b)
   elem_kendu([1, 7, 5, 8], 2) =
   = elem_kendu(1:7:5:8:[], 2) = (#4)
                                              x = 1, s = 7:5:8:[], pos = 2
   = 1:elem_kendu(7:5:8:[], 2)
                                              x = 7, s = 5:8:[], pos = 2
                                              x = 5, s = 8:[], pos = 2
   = 1:7:elem_kendu(5:8:[], 2)
   = 1:7:8:[] = [1, 7, 8]
```

33)garbitu (2008ko apirila #1) --

```
a)
garbitu:: ([Int]) \rightarrow [Int]
garbitu([]) = error "Zerrenda hutsa" \qquad (#1)
garbitu(x:s) \qquad = x:s \qquad (#2)
| hutsa_da(s) \qquad = garbitu(x:hond(s)) \qquad (#3)
| otherwise \qquad = leh(s):garbitu(x:hond(s)) \qquad (#4)
```

```
b)
    garbitu([5, 8, 4, 1, 9]) =
    x = 5, s = 8:4:1:9:[],
                                                 leh(s) = 8, hond(s) = 4:1:9:[]
    = 8:garbitu(5:4:1:9:[]) =
                                         x = 5, s = 4:1:9:[],
                                                 leh(s) = 4, hond(s) = 1:9:[]
    = 8: garbitu(5:1:9:[]) = {}^{(#3)}
                                         x = 5, s = 1:9:[],
                                                 leh(s) = 1, hond(s) = 9:[]
                                         x = 5, s = 9:[], leh(s) = 9, hond(s) = []
    = 8:garbitu(5:9:[]) =
    = 8:9: \frac{\text{garbitu}(5:[])}{\text{garbitu}(5:[])} =
                                         x = 5, s = []
    = 8:9:5:[] = [8, 9, 5]
```

34)zeharkatu (2008ko apirila #2) --

zeharkatu:: ([Int]) \rightarrow [Int]

a)

```
zeharkatu([]) = [] 		(#1)
```

b) $\begin{array}{l} zeharkatu([5,8,4]) = \\ = zeharkatu(5:8:4:[]) = (\#4) \\ = 8: zeharkatu(5:4:[]) = (\#4) \\ = 8:4: zeharkatu(5:4:[]) = (\#2) \\ = 8:4:5:[] = [8,4,5] \\ \end{array} \qquad \begin{array}{l} x = 5, \ s = 8:4:[], \ leh(s) = 8, \ hond(s) = 4:[] \\ x = 5, \ s = 4:[], \ leh(s) = 4, \ hond(s) = [] \\ x = 5, \ s = [] \\ \end{array} \qquad \begin{array}{l} x = 5, \ s = 5:4:[], \ leh(s) = 5, \ hond(s) = 4:[] \\ zeharkatu([5,5,4]) = (\#3) \\ = zeharkatu(5:5:4:[]) = (\#3) \\ = 0:0:4:[] = [0,0,4] \end{array} \qquad \begin{array}{l} x = 5, \ s = 5:4:[], \ leh(s) = 5, \ hond(s) = 4:[] \\ \end{array}$

35)zatitu (2008ko ekaina) --

otherwise

a)

zatitu:: ([Int])
$$\rightarrow$$
 [Int]
zatitu([]) = error "Zerrenda hutsa" (#1)

 $\begin{array}{lll} zatitu(x:s) & & = error \text{ "Lehenengoa zero da"} & \text{ (#2)} \\ | \text{ hutsa_da(s)} & = s & \text{ (#3)} \\ | \text{ leh(s) `mod` x == 0} & = (\text{leh(s) `div` x}):zatitu(x:\text{hond(s))} & \text{ (#4)} \end{array}$

= leh(s):zatitu(x:hond(s))

b)

$$\begin{array}{l} \text{zatitu}([5, 20, 6, 15]) = \\ = \text{zatitu}(5:20:6:15:[]) = \\ & \\ \text{leh(s)} = 20, \text{ hond(s)} = 6:15:[] \\ = 4: & \\ \text{zatitu}(5:6:15:[]) = \\ & \\ \text{zatitu}(5:15:[]) = \\ & \\ \text{zati$$

(#5)

36)superbik (2008ko iraila) --

b)

37)metatu (2009ko apirila #1) --

```
a)
                                          metatu:: ([Int]) \rightarrow ([Int])
                                          metatu([]) = []
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (#1)
                                           metatu(x:s)
                                                 hutsa da(s)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (#2)
                                                                                                                                                                                                                                                                                                                                          = x:[]
                                                 otherwise
                                                                                                                                                                                                                                                       = x: metatu((x + leh(s)):hond(s))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (#3)
b)
                                          metatu([10, 8, 15]) = \frac{\text{metatu}(10:8:15:[])}{\text{metatu}(10:8:15:[])} = \frac{\text{metatu}(10:8:15:[])}{\text{metatu}(10:8:[])} = \frac{\text{metatu}(10:8:[])}{\text{metatu}(10:[])} = \frac{\text{metatu}(10:[])}{\text{metatu}(10:[])} = \frac{\text{metatu}(10:[])}{\text{m
                                           = 10:metatu(18:15:[]) =<sup>(#3)</sup>
                                           = 10:18:33:[]
```

Adibidea garatzerakoan, urrats bakoitzean lerroaren eskuineko ertzean zehazten den ekuazioa formularen zein zatiri aplikatu zaion garbiago ikusteko koloreak erabili dira. Irakurgarritasunagatik bi kolore desberdin erabili dira baina kolore desberdinek ez dute inolako esanahi berezirik.

38)aurreratu (2009ko apirila #2) --

```
a)
    aurreratu :: ([Bool], [Int]) \rightarrow [Int]
    aurreratu([], r)
    | luzera(r) \neq 0
                                       = error "Luzera desberdina"
                                                                               (#1)
    otherwise
                                       =[]
                                                                               (#2)
    aurreratu(x:s, r)
                                       = error "Luzera desberdina"
    | luzera(x:s) \neq luzera(r)
                                                                               (#3)
    hutsa_da(s)
                                       = r
                                                                               (#4)
    | x == False
                                       = leh(r):aurreratu(s, hond(r))
                                                                               (#5)
    | x == True
                                                                               (#6)
                       = leh(hond(r)): aurreratu(s, leh(r):hond(hond(r)))
b)
    aurreratu([True, False, True, True], [8, 3, 9, 5, 2]) = (#6)
    = 3: aurreratu([False, True, True, True], [8, 9, 5, 2]) =
    = 3: 8: aurreratu([True, True, True], [9, 5, 2]) = (^{\#6}
    = 3: 8: 5: aurreratu([True, True], [9, 2]) = (#6)
    = 3: 8: 5: 2: aurreratu([True], [9]) = (#4)
    = 3: 8: 5: 2: 9: [] = [3, 8, 5, 2, 9]
```

39)kendubikpos (2009ko ekaina) --

```
a)
   kendubikpos:: ([Int], Int) \rightarrow [Int]
   kendubikpos([], pos) = error "Zerrenda hutsa"
                                                                              (#1)
    kendubikpos(x:s, pos)
    \mid pos < 1 \mid \mid pos > luzera(x:s)
                                      = error "Posizioa ez da egokia"
                                                                              (#2)
    | pos == 1 \&\& x mod 2 == 0
                                              = s
                                                                              (#3)
    | pos == 1 \&\& x mod 2 /= 0
                                                                              (#4)
                                              = x:s
    otherwise
                                              = x:kendubikpos(s, pos -1) (#5)
b)
   kendubikpos([8, 5, 16, 7, 10, 4], 3) =
    = kendubikpos(8:5:16:7:10:4:[], 3) = (#5)
    = 8:kendubikpos(5:16:7:10:4:[], 2) =
    = 8: 5:kendubikpos(16:7:10:4:[], 1) =
    = 8: 5: 7:10:4:[] =
   = [8, 5, 7, 10, 4]
```

40)azk_lehena (2009ko iraila) --

```
azk\_lehena:: ([Int]) \rightarrow Int
azk_lehena([]) = -1
                                                                         (#1)
azk_lehena(x:s)
| not lehena_da(x)
                                  = azk_lehena(s)
                                                                         (#2)
| hutsa da(s)
                                                                         (#3)
                                  = x
| lehena_da(leh(s))
                                  = azk_lehena (s)
                                                                         (#4)
                                  = azk_lehena(x:hond(s))
| not lehena_da(leh(s))
                                                                         (#5)
```

(#3), (#4) eta (#5) ekuazioetan $lehena_da(x)$ betetzen da. (#4) eta (#5) ekuazioetan $not\ hutsa_da(s)$ betetzen da. (#5) ekuazioan otherwise ipini daiteke $not\ lehena_da(leh(s))$ baldintzaren ordez.

```
b)
azk_lehena([8, 11, -7, 9, 3, 6]) =
azk_lehena(8:11:-7:9:3:6:[]) = (#2)
azk_lehena(11:-7:9:3:6:[]) = (#5)
azk_lehena(11:9:3:6:[]) = (#5)
azk_lehena(11:3:6:[]) = (#4)
azk_lehena(3:6:[]) = (#5)
azk_lehena(3:6:[]) = (#5)
azk_lehena(3:6:[]) = (#5)
= 3
```

41)azpiluzbikgehi (2010eko apirila #1) --

```
a)
        azpiluzbikgehi:: ([t]) \rightarrow ([t])
        azpiluzbikgehi([]) = []
                                                                                     (#1)
        azpiluzbikgehi(x:s)
        | hutsa_da(s)
                                    = x:x:[]
                                                                                     (#2)
        | x == leh(s)
                                    = x:x:azpiluzbikgehi(hond(s))
                                                                                     (#3)
        | x /= leh(s)
                                    = x:x: azpiluzbikgehi(s)
                                                                                     (#4)
   b)
        azpiluzbikgehi([10, 10, 10, 8, 8, 15, 8]) =
        = \frac{\text{azpiluzbikgehi}(10:10:10:8:8:15:8:[])}{\text{azpiluzbikgehi}(10:10:10:8:8:15:8:[])}
        = 10:10:azpiluzbikgehi(10:8:8:15:8:[]) =
        = 10:10:10:10:azpiluzbikgehi(8:8:15:8:[]) = (#3)
        = 10:10:10:10:8:8:azpiluzbikgehi(15:8:[])
        = 10:10:10:10:8:8:15:15:azpiluzbikgehi(8:[]) = (*2)
        = 10:10:10:10:8:8:15:15:8:8:[] =
        = [10, 10, 10, 10, 8, 8, 15, 15, 8, 8]
42)handibik (2010eko apirila #2) -- #
        handibik:: ([Int]) \rightarrow ([Int])
        handibik([]) = []
                                                                                     (#1)
        handibik(x:s)
                                    = error "Luzera bakoitia"
        | luzera(x:s) mod 2 /= 0
                                                                                     (#2)
        |x\rangle = leh(s)
                                            = x: x: handibik(hond(s))
                                                                                     (#3)
        | x < leh(s)
                                            = leh(s):leh(s):handibik(hond(s))
                                                                                     (#4)
   b)
```

```
handibik([10, 8, 5, 7, 7, 20, 5, 5]) =
= handibik (10:8:5:7:7:20:5:5:[]) = (#3)
= 10:10:handibik(5:7:7:20:5:5:[]) = (#4)
= 10:10:7:7:handibik(7:20:5:5:[]) = (#4)
= 10:10:7:7:20:20:handibik(5:5:[]) = (#3)
= 10:10:7:7:20:20:5:5:handibik([]) = (#1)
= 10:10:7:7:20:20:5:5:[] =
= [10, 10, 7, 7, 20, 20, 5, 5]
```

43)kokatu (2010eko ekaina) --

kokatu([8, 0, 0, 7], [3, 20, 12, 28])
= kokatu(8:0:0:7:0:6:[], 3:20:12:28:[]) = (#4)
= 8: kokatu(0:0:7:[], 3:20:12:45:28:[]) = (#3)
= 8: 0: 3: kokatu(0:7:[], 20:12:45:28:[]) = (#3)
= 8: 0: 3: 0: 20: kokatu(7:[], 12:45:28:[]) = (#4)
= 8: 0: 3: 0: 20: 7: kokatu([], 12:45:28:[]) = (#4)
= 8: 0: 3: 0: 20: 7: [] = [8, 0, 3, 0, 20, 7]

44) azpiluzbikken (2010eko iraila) --

```
a) azpiluzbikken:: ([t]) \rightarrow ([t]) azpiluzbikken([]) = []
```

azpiluzbikken(x:s) | hutsa_da(s) = [] (#2) | x == leh(s) = x:x:azpiluzbikken(hond(s)) (#3)

| x /= leh(s) = azpiluzbikken(s) (#4)

b)

azpiluzbikken([10, 10, 10, 8, 8, 15, 8]) =

= azpiluzbikken(10:10:10:8:8:15:8:[]) = (#3)

= 10:10:azpiluzbikken(10:8:8:15:8:[]) = (#4)

= 10:10:azpiluzbikken(8:8:15:8:[]) = (#4)

= 10:10:8:8:azpiluzbikken(15:8:[]) = (#4)

= 10:10:8:8:azpiluzbikken(8:[]) = (#2)

= 10:10:8:8:[] =

= [10, 10, 8, 8]

(#1)