**Batez besteko aritmetikoa:**  $\overline{x} = \left(\sum_{i=1}^{k} x_i f_i\right)/n$ ; **Mediana:** kasu jarraituan  $M_e = l_i + \frac{\frac{n}{2} - F_{i-1}}{f_i} \cdot d_i$ ; **Heina**  $R = max(x_i) - \frac{n}{2} \cdot d_i$ 

 $\min(x_i) \; ; \; \textbf{Bariantza:} \; \; V(x) = \frac{\displaystyle\sum_{i=1}^n x_i^2 f_i}{2} - (\overline{x})^2 \; ; \; \textbf{Desbideratze tipikoa:} \; \; s(x) = \sqrt{V(x)} \; ; \; \textbf{Aldakuntza koefizientea:} \; \; CV_x = s/\overline{x} \; ;$ 

**k. ordenako pertzentila:** kasu jarraituan  $P_k = l_i + \left(\frac{kn}{100} - F_{i-1}\right)d_i / f_i$ ; **Moda** kasu jarraituan  $M_o = l_i + \frac{\Delta_1}{\Delta_1 + \Delta_2} \cdot d_i$ ,

$$\Delta_1 = \frac{f_i}{d_i} - \frac{f_{i-1}}{d_{i-1}} \; , \; \Delta_2 = \frac{f_i}{d_i} - \frac{f_{i+1}}{d_{i+1}}$$

 $P(\overline{A}) = 1 - P(A); A \subseteq B \Rightarrow P(A) \le P(B); P(A \cup B) = P(A) + P(B) - P(A \cap B); P(A \cup B) \le P(A) + P(B)$ 

 $P(A|B) = P(A \cap B)/P(B)$ , P(B) > 0

 $P(A \cap B) = P(A) P(B|A), P(A) \neq 0$ edo  $P(A \cap B) = P(B) P(A \mid B)$ ,  $P(B) \neq 0$ 

 $P(A \cap B) = P(A) P(B|A), \quad P(A) \neq 0 \quad \text{edo} \quad P(A \cap B) = P(B) P(A|B), \quad P(B) \neq 0$   $P(A_1 \cap A_2, \cap ... \cap A_n) = P(A_1)P(A_2|A_1)...P(A_n|A_1 \cap ... \cap A_{n-1})$   $A \text{ eta } B \text{ bateraezinak} \Leftrightarrow P(A \cap B) = 0 \quad A \text{ eta } B \text{ independenteak} \Leftrightarrow P(A \cap B) = P(A)P(B).$   $P(B) = P(B|A_1) P(A_1) + P(B|A_2) P(A_2) + ... + P(B|A_n) P(A_n), \quad \{A_1, A_2, ..., A_n\} \text{ gertaera-sistema osoa, } P(A_i) > 0$ 

$$P(A_r|B) = \frac{P(B|A_r)P(A_r)}{P(B|A_1)P(A_1) + \dots + P(B|A_n)P(A_n)}, \qquad r = 1, 2, \dots, n, \qquad " \qquad " \qquad " \qquad " \qquad "$$

X a.a. diskretuaren  $P(X = x_i) = f(x_i) = p_i$  probabilitate-funtzioa baldin (i)  $f(x_i) \ge 0$ , i = 1, ..., n eta (ii)  $\sum_{i=1}^{n} f(x_i) = 1$ , F(x)

**banaketa-funtzioa**  $F(x) = P(X \le x) = \sum_{x_i \le x} f(x_i)$ . Propietatea:  $f(x_i) = F(x_i) - F(x_{i-1})$ , i = 1, 2, ..., n;  $\mu = E(x) = \sum_{i=1}^{n} x_i f(x_i)$ ;

 $E(k_1X_1 + k_2X_2 + ... + k_nX_n) = k_1E(X_1) + k_2E(X_2) + ... + k_nE(X_n); \ \sigma_x^2 = Var(X) = \sum_{i=1}^n x_i^2 p_i - \mu^2; \ Var(kX) = k^2Var(X), \ \mathbf{Tchebychev}$ 

 $P(|X-\mu| \le k\sigma) \ge 1 - \frac{1}{k^2}, \forall k > 0;$  Teorema:  $Bin(n,p) \cong Pois(np), p \le 0, 1, np < 5.$  Teorema:  $H(N,n,p) \cong Bin(n,p), n/N < 0, 1$ 

$$X: Bin(n,p), \qquad P(X=x) = \binom{n}{x} p^{x} (1-p)^{n-x}, \qquad F(x) = P(X \le x) = \sum_{k \le x} \binom{n}{k} p^{k} (1-p)^{n-k} ., E(X) = np, \ Var(X) = npq$$

X: Pois(
$$\lambda$$
),  $P(X = x) = \frac{e^{-\lambda} \lambda^x}{x!}$ ,  $F(x) = P(X \le x) = \sum_{k \le x} (e^{-\lambda} \lambda^k) / k!$ ,  $E(X) = \lambda$ ,  $Var(X) = \lambda$ 

X:H(N, n, r/N), 
$$P(X = x) = {r \choose x} {N-r \choose n-x} / {n \choose n} , \qquad E(X) = np, \quad Var(X) = npq(N-n)/(N-1).$$

*X* a.a.jarraituaren F(x) banaketa-funtzioak  $F(x) = P(X \le x)$ ; f(x) funtzioa dentsitate-funtzioa baldin (i)  $f(x) \ge 0$ ,  $\forall x \in \square$  eta

(ii) 
$$\int_{-\infty}^{+\infty} f(x)dx = 1$$
;  $P(x_1 \le X \le x_2) = F(x_2) - F(x_1)$ ;  $F(x) = \int_{-\infty}^{x} f(t)dt$ ;  $E(X) = \int_{-\infty}^{+\infty} xf(x)dx$ ;  $Var(X) = \int_{-\infty}^{+\infty} x^2 f(x)dx - \mu^2$ 

**Teorema:**  $Bin(n,p) \cong N(np, \sqrt{npq})$ , np>5 eta nq>5. **Teorema:**  $Pois(\lambda) \cong N(\lambda, \sqrt{\lambda})$ ,  $\lambda>18$ ; **Tchebychev** (berdin)

$$X: Unif(a,b), . \ f(x) = \begin{cases} \frac{1}{b-a}, & a \le x \le b \\ 0, & \text{beste} \end{cases}, \ F(x) = \begin{cases} 0, & x < a \\ \frac{x-a}{b-a}, & a \le x < b \end{cases}, \ E(X) = \frac{a+b}{2}, \quad Var(X) = (b-a)^2/12$$

$$X: exp(\beta) \ f(x) = \begin{cases} \frac{1}{\beta} e^{-\frac{x}{\beta}}, & x > 0 \\ 0, & x \le 0 \end{cases}, \quad F(x) = \begin{cases} 1 - e^{-\frac{x}{\beta}}, & x > 0 \\ 0, & x \le 0 \end{cases}, E(X) = \beta, \ Var(X) = \beta^2$$

**Teorema**. Biz X:  $N(\mu, \sigma)$ ,  $\sigma$  ezagunekoa. Orduan,  $\overline{X}$  aldagaiak  $N(\mu, \sigma/\sqrt{n})$  banaketa du.