# Currency Relative Theory

$$CRT\sum_{k=1}^{7}\frac{1}{k!}$$

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<sup>\*</sup>This translation of: "Théorie Relative de la Monnaie" by Stéphane Laborde, http://wiki.creationmonetaire.info/index.php?title=File:LaTexTRM.zip by: Pascal J. Bourguignon <pjb@informatimago.com>

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#### 1 The Four Economic Freedoms

For the Currency Relative Theory (CRT), the definition of freedom is "what it is possible to achieve without harming yourself and others". This doesn't include unconscious possibilities.

The CRT defines four economic freedoms which are at the root of its approach. They are:

- 1. The freedom of choice of one's own monetary system.
- 2. The freedom to use resources.
- 3. The freedom to estimate and produce any economic value.
- 4. The freedom to exchange, account and display prices using this "currency".

Notably, the third freedom establishes the principle of relativity as the essence of this approach.

## 2 Principle of Economic Relativity

The CRT is based on the principle of economic relativity, which states that each human being defines a legitimate referential to estimate and produce all types of economic value, known or unknown of others.

In other words there is no absolute economic value, no human being who is legitimately able to define what is value or non-value for other human beings be it in space (between present human beings) or in time (between remote people over time).

## 3 Space-Time

The economic space-time is characterized essentially by human beings who belong to a given economic area.

The following thought experiment helps to understand this point: If we remove from a given economic area some specific economic value, there will always be an economic area. On the other hand, if we remove all the human beings from it, then there remains no observer, no actor in this economic area.

This is therefore the human being who is the only invariant basis of any economy.

But human beings are not absolute either, since they have a finite average lifespan "ev" (average life expectancy), and they're renewed in time, newborns replacing the dead.

This quantity is a finite data of the economic space-time studied by the CRT where, for each time t, the set of human beings is renewed at time t+ev.

In the following, we will call "space" the set of individuals for a given date "t", and "time" the phenomenon of successive replacement of those individuals in time. Therefore, space-time must be understood relatively to these definitions.

### 4 Free Currency

A currency is a reference economic value which gives a common metric, for a given time and a given currency area, allowing measurement in the same unit of values and exchanges, to facilitate the flow of the economy between different actors.

Note that even though people do not agree on economic values either in space or in time, they still use the same unit of individual valuation in relation to a reference value, which is called "currency".

A currency area is defined by the set, depending on time E(t), consisting of individuals I(x,t) who have adopted the same currency (a given currency area may also deal with several currencies).

A currency is said to be "free" if it's a valid reference value for a metric that respects the principle of relativity of all economic value, and the human space-time defined above, not establishing any arbitrary control on each other (which means that laws must be of the same form for all), mainly with regard to the recognition and production of any economic value.

To qualify as free, a currency, cannot be based on an arbitrary decision as to what is value or non-value, or be created preferentially for some human being in space, or in time.

It must be the accounting unit, because it is the reference of the metric (as in relativist physics, speeds are expressed in proportion of the speed of light).

Still, it must be an economic value (just like light is a physical object), because we must have an economic metric. But to be independent of the

other values, its production cost should be minimal (the mass of light is zero, which is precisely what gives it its speed invariance).

Therefore we must reconcile invariance and finiteness for the currency as well as the minimal cost of production. Since human beings are the only invariant basis, it can only be a purely numerical quantity, co-produced by human beings, a value expressed relatively to its own total.

Let's call  $\left(\frac{M}{N}\right)(t)$  the average money M for the N human beings of finite lifespan, stakeholders in this economy at time "t". The human beings must all be co-producer of this economic value, while they are being replaced in time; therefore we must define a production of our reference value M, of same form for all individuals, in space and in time.

Thus we establish an economic metric, whose reference value is produced in an way that is invariant by referential changes (change of individual, whatever the time when he's born, lives and dies).

For each of those N individuals I(x,t) in the currency area thus established, and on condition of quasi-stability (especially of N), the relative instantaneous production (differential) of a free currency, can only be identical in space (spacial symetry), and identical in time (time symetry).

Said otherwise, the production of a free currency can only be the same for all the stakeholder individuals for a given time "t", and this relative production is independent on time.

$$\boxed{\frac{d^2\left(\frac{M}{N}\right)}{dt\,dx} = 0 \quad and \quad \frac{d\left(\frac{M}{N}\right)}{\left(\frac{M}{N}\right)} = c\,dt}$$
 (1)

In the following, we will drop the differential "dt", since dt=1 with discrete transform.

We deduce, placing us under the assumption of continuity and differentiability, (see the chapter "Variations of N and calculation of UD"):

$$\left(\frac{M}{N}\right)(t) = \left(\frac{M}{N}\right)(t_0)e^{ct}$$
(2)

On the other hand, the individuals having a finite life expectancy "ev", the instantaneous production (derivate) being established as invariant, the relative individual sum produced during the life must not be dependent on time either.

The currency of those who go must give way to the currency of those who will replace them at the end of that period. Which is equivalent to

say that  $\left(\frac{ev}{2}\right)$  years later, the living must have co-produced their own full share of relative currency:

$$\frac{\binom{M}{N}(t)}{\binom{M}{N}(t + \frac{ev}{2})} = e^{-c(\frac{ev}{2})}$$
(3)

This symetry principle between those who go and those who arrive establishes a convergent center of symetry at the point  $\left(\frac{ev}{2}\right)$  where those who arrive at this point represent a proportion  $\frac{1 \ year}{\left(\frac{ev}{2}\right)}$  of those who go; for an other expression, see also (14):

$$\frac{\left(\frac{M}{N}\right)(t)}{\left(\frac{M}{N}\right)(t+\frac{ev}{2})} = \frac{1 \, year}{\left(\frac{ev}{2}\right)}$$
(4)

From (1) and (4) we obtain a symetric rate where he average  $\left(\frac{M}{N}\right)$  is reached for all individuals, close to  $\frac{1 \ year}{\left(\frac{ev}{2}\right)}$ , on the point  $\frac{1 \ year}{\left(\frac{ev}{2}\right)}$  of his participation in the free currency thus established, whatever the time considered.

$$c_{sym} = \frac{\ln(\frac{ev}{2})}{(\frac{ev}{2})}$$
 (5)

The rates "c" that are inferior to  $c_{sym}$  establish a metric that favours the older individuals, while the rates that are superior to  $c_{sym}$  favour the youger individuals.

This converging rate has a lower limit  $c_{min}$  obtained for a convergence reached at the end of the average life expectancy:

$$c_{min} = \frac{\ln(ev)}{ev} \tag{6}$$

Numerical application for France with a life expectancy of 80 years in 2014:

$$c_{sym} = \frac{\ln(40)}{40} = 9,22\%/an \quad et \quad c_{min} = \frac{\ln(80)}{80} = 5,48\%/an$$
 (7)

### 5 Quantitative

We will call Universal Dividend the differential invariant quantity at time "t" that we can describe either in continuous or discrete form (which will be useful to establish approximations in practice):

$$UD(t) = d\left(\frac{M}{N}\right)(t) = c\left(\frac{M}{N}\right)(t_0)e^{ct}$$

Or:

$$UD(t + dt) = UD(t) + dUD(t) = (1 + c)UD(t)$$

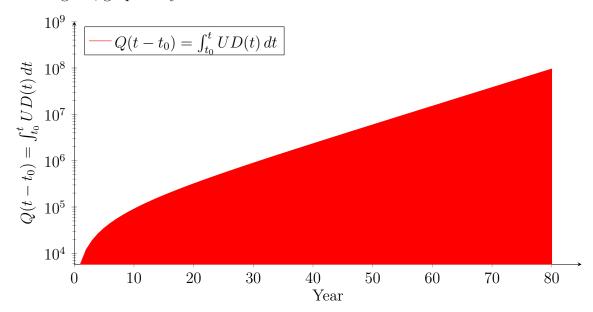
corresponding to the currency units co-created by the individuals for the yearly unit of time "t", and which will be of the form:

$$UD = c\left(\frac{M}{N}\right) \tag{8}$$

And Q(t) being the sum of the currency units co-produced by an individual between the time  $t_0$  start of his participation in the free currency, and t:

$$Q(t - t_0) = \int_{t_0}^{t} UD(t) dt = \left(\frac{M}{N}\right) (t_0) e^{ct} \left(1 - e^{-c(t - t_0)}\right)$$
(9)

Which gives, graphically:



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#### 6 Relative

Given the previous, we also have the following relative expression for the reference currency of the global economic metric, under the immutable form in space-time:

$$\boxed{\frac{M}{N} = \frac{1}{c}UD} \tag{10}$$

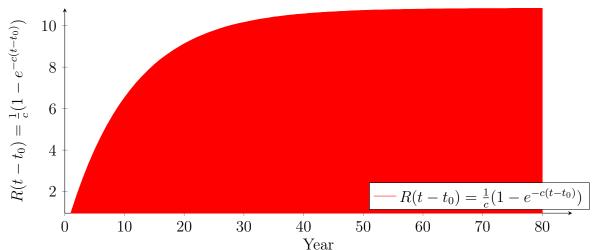
And

$$UD(t) = d\left(\frac{M}{N}\right)(t) = c\left(\frac{M}{N}\right)(t_0)e^{ct}$$

So we can also transform our metric based on the relative unit "UD" well established. Let's call now  $R = \frac{Q}{UD}$  the number of relative units coproduced by an individual between  $t_0$  and t:

$$R(t - t_0) = \frac{\int_{t_0}^t UD(t) dt}{UD(t)} = \frac{1}{c} (1 - e^{-c(t - t_0)})$$
(11)

This gives, graphically:



In the relative referential, the share of currency co-produced by any individual participating in this metric converges asymptotically and consistently (in space-time) toward:

$$\lim_{t \to +\infty} R(t - t_0) = \frac{1}{c}$$
 (12)

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And more specifically, for  $t = t_0 + \frac{ev}{2}$  with  $c = \frac{\ln(\frac{ev}{2})}{(\frac{ev}{2})}$ :

$$R\left(\frac{ev}{2}\right) = \frac{1}{c}\left(1 - e^{-c\frac{ev}{2}}\right) = \frac{1}{c}\left(1 - \frac{1}{\left(\frac{ev}{2}\right)}\right)$$
(13)

Given (10), (11) and (13), we can express the fundamental expression (4) as:

$$\frac{\int_{t_0}^{t_0 + \frac{ev}{2}} UD(t) dt}{\left(\frac{M}{N}\right) \left(t_0 + \frac{ev}{2}\right)} = \left(1 - \frac{1}{\left(\frac{ev}{2}\right)}\right) \tag{14}$$

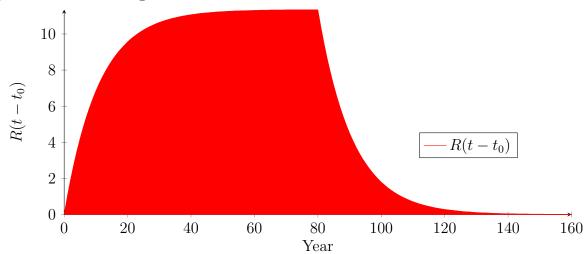
which we may express, according to (14) as:

"The sum of the UD produced by an individual participating in a free currency, during  $\left(\frac{ev}{2}\right)$  converges toward the average money supply at approximatively  $\frac{1\,year}{\left(\frac{ev}{2}\right)}$ , whoever this individual is and whatever the time considered."

Or also, according to (13) as:

"The sum of the relative UD produced by an individual participating of a free currency, during  $\left(\frac{ev}{2}\right)$  converges toward  $\frac{1}{c}$  at approximately  $\frac{1\,year}{\left(\frac{ev}{2}\right)}$  whoever this individual is, and whatever the time considered."

Relative graph of the share of currency generated by an individual during and after his leaving:



#### 7 Initial Asymetries

Let's consider the specific case of an individual starting his participation in the metric with an initial share of currency (gift, inheritance or any economic exchange)  $Q_s(t_0)$  and having exchanges with the exterior that are balanced (monetary purchases are always equal to the monetary sales). This individual, called pseudo-autonomous, will see his share of currency  $Q_s(t)$  evolve as:

Quantitatively:

$$Q_s(t) = Q_s(t_0) + \int_{t_0}^t UD(t) dt = Q_s(t_0) + \left(\frac{M}{N}\right) (t_0) e^{ct} \left(1 - e^{-c(t - t_0)}\right)$$

Relatively let's call  $R_s(t)$  the evolution of his share of currency:

$$R_s(t) = \frac{Q_s(t_0) + \int_{t_0}^t UD(t) dt}{UD(t)} = \frac{Q_s(t_0)}{UD(t)} + \frac{1}{c} (1 - e^{-c(t - t_0)})$$

And we have:

$$UD(t) = UD(t_0) e^{c(t-t_0)} \text{ and also } R_s(t_0) = \frac{Q_s(t_0)}{UD(t_0)}$$

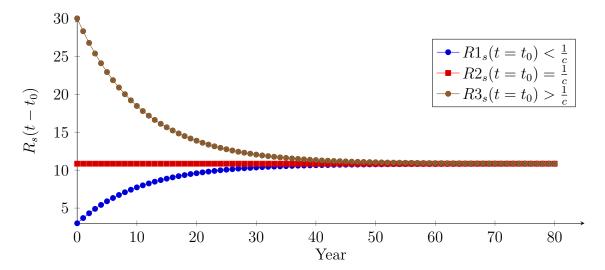
Thus, factorizing we obtain finally the relative form:

$$R_s(t) = \frac{1}{c} \left[ 1 - e^{-c(t-t_0)} \left( 1 - cR_s(t_0) \right) \right]$$
 (15)

Where we see directly that if  $R_s(t_0) = \frac{1}{c}$  which is equivalent to  $Q_s(t_0) = \left(\frac{M}{N}\right)(t_0)$ , then for all t we will have:

$$R_s(t) = \frac{1}{c}$$

Now, depending on the three cases,  $R_s(t=t_0)<\frac{1}{c}$ ,  $R_s(t=t_0)=\frac{1}{c}$  or  $R_s(t=t_0)>\frac{1}{c}$ , we have, under condition of balanced exchanges, the following three evolutions in the relative referential:



This evolution is only valid in this specific case studied here.

#### 8 The four referentials

We've seen previously two metric referentials, quantitative and relative, whose transformation law is given by:

$$R_s(t - t_0) = \frac{Q_s(t - t_0)}{UD(t)}$$

We may also establish the quantitative referential with zero-sum of accounts, with the transformation:

$$Z_q(t - t_0) = Q_s(t - t_0) - \left(\frac{M}{N}\right)(t)$$

and also the relative referential with zero-sum of accounts:

$$Z_r(t-t_0) = \frac{Z_q(t-t_0)}{UD(t)} = R_s(t-t_0) - \frac{1}{c}$$

All individuals being perfectly able to switch to the referential that seems best adapted. The same free currency system can propose at least four distinct referentials for each individual participating in it, this choice being purely personal:

- 1. The quantitative referential.
- 2. The quantitative referential with zero-sum.

- 3. The relative referential.
- 4. The relative referential with zero-sum.

# 9 Variation for a pseudo-autonomous individual

Let's study here the variation of a monetary account for a pseudo-autonomous individual. First, in quantitative:

$$dQ_s(t) = UD(t)$$

And in relative:

$$dR_s(t) = e^{-c(t-t_0)} \left( 1 - cR_s(t_0) \right) = 1 - cR_s(t)$$

This let us affirm the following conclusions (a) and (b), perfectly equivalent:

- (a) "In the quantitative referential, the account of a pseudo-autonomous individual appears as if a Universal Dividend is added between two time units."
- (b) "In the relative referential, the account of a pseudo-autonomous individual appears as if between two units of time, one Universal Dividend was added, and at the same time, a proportion equal to c was removed."

Understanding that these points are only appearance, an individual participating in a free currency chooses the referential of his choice in terms of his monetary accounts, quantitative, relative, quantitative zero-sum, relative zero-sum, or another referencial he deems most consistent with his experience, this in no way affecting the free currency established.

### 10 Variations of N and calculation of UD

Given the above it should be borne in mind that it is the convergence at half-life which is the goal sought by a free currency, new entrants replacing the dead (see in this connection forms (4) and (14) concerning the time condition valid for any individual).

When looking for a practical calculation method of UD, we must not make an estimation using only the local differential calculus. We must keep in mind the fundamental behavior of a free currency, which is to ensure for each human being, during his life, and particularly at the center of the temporal symetry, at half-life, the same relative share of currency as his predecessors and successors at the same point.

In particular we will be convinced by the reflection of the need to address the practical solution by considering extreme cases, such as the case of a sharp rise in the number of participants in a free currency (equivalent to a pseudo-initialization of money), where UD calculated in relative  $(UD(t) = c\left(\frac{M}{N}\right)(t))$  suffer a strong discontinuity, destroying the continuity of the progression, and would become extremely low with respect to the initial participants, few, and who possess in this case a monetary share extremely strong compared to new entrants, unrelated to the computed UD.

Said otherwise, in a more mathematical way, the fundamental equations (1) and (4) expressed in the analysis of the form of a free currency, have identified solutions only for a continuous and derivable  $\binom{M}{N}$  (or quasicontinuous and quasi-derivable), which we'll have to approximate to the best in case of discontinuous variations.

In this reflection we need to have initially a UD(t=0) not relative, since to establish a monetary amount, it is still necessary that the currency exists first. We understand that in this case there is a convergence of phenomenon between the initialization of a free currency and the huge increase in the number of members of an installed currency. The solution complying with the CRT having to be independent of time (principle of relativity), we now understand that we must in these cases establish a non-relative amount of UD(t), that is, a fixed and stable amount, until the relative area is reached.

N(t) is unknown, so to evaluate the shape of a general and practical method of generation, we must establish a most simple and readable method, which we can approximate thru the modelization of the variation of N as  $dN(t) = \alpha N(t)$  or also  $N(t+dt) = N(t) + dN(t) = (1+\alpha)N(t)$  and we take an approximation for M conform to  $M(t+dt) \approx (1+c)M(t)$ .

It should be noted that  $\alpha$  must be understood as being in general "small" on durations on the order of  $\left(\frac{ev}{2}\right)$ , and even compared to c. Indeed, to take the example of France between 1950 and 1999, the population went from 41 to 56 millions, which corresponds to  $\alpha = \frac{ln(\frac{56}{41})}{40} = 0,78\%/\text{year}$  while  $c = \frac{ln(40)}{40} = 9,22\%/\text{year}$ .

We obtain an approximation of the differential variation of the Dividend:

$$UD(t+dt) = c \frac{M(t+dt)}{N(t+dt)} \approx c \frac{(1+c)M(t)}{(1+\alpha)N(t)}$$

From which we deduct this first form:

$$UD(t+dt) \approx \frac{(1+c)}{(1+\alpha)}UD(t)$$

As well as a second form approximated to the first order ("c" being small):

$$UD(t+dt) \approx \frac{(c+c^2)M(t)}{N(t+dt)} \approx c \frac{M(t)}{N(t+dt)}$$

A simple lower bound appears for  $\alpha$  positive, if  $\alpha \approx c$  we have  $UD(t+dt) \approx UD(t)$ , and another simple minimal bound appears for  $\alpha$  small and negative, that we are happy to find under this form, since it is very close to the definition:  $UD(t) = c \frac{M(t)}{N(t)}$ .

From these two minimum bounds revealed by this approximation we can derive a simple practical calculation of UD, showing a quantitative form and another relative, adapting flexibly to changes in N:

$$UD(t+dt) = Max \left[ UD(t); c \frac{M(t)}{N(t+dt)} \right]$$
(16)

In particular, we recognize that for a stable N, the form will converge quickly toward its relative fundamental expression (which is absolutely necessary):

$$UD = c \, \frac{M}{N}$$

This form is notably extremely practical for the development of an independent free currency from scratch, but also equivalently, to manage in a flexible way the imprevisible variations of N, while having an invariant law in space and time, and without moving away from the basic form.

While being simple, easy to understand, and reassuring from a quantitative point of view, this form appears as the best we may find.

We may summary the behavior thus:

"The UD never drops in quantitative, and is always at least equal to a relative proportion c of the money supply."

Other forms are of course possible, given the uncertainty of N(t), the simpliest forms being better...

In general, to ensure the relevance of this form, and possibly to compare it with others, such as the trivial but dangerous theorical form UD(t+dt) = (1+c)UD(t), it is necessary to simulate random N(t) and to test the different forms, keeping in mind that to do that, we must use individuals with limited lifespan, while simulating operations for larger periods than ev, and evaluating if for all of these individuals, the fundamental principles are respected, almost all the time.