Real-Time Systems¹

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Multiprocessor Scheduling - Day 2



Outline

- Multiprocessor scheduling
 - Global scheduling
 - Partitioned scheduling
 - Semi-partitioned scheduling



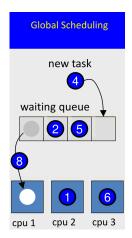
Multiprocessor Scheduling

- Global scheduling (full migration)
 - A task is allowed to execute on an arbitrary processor (sometimes even after being preempted)
- Partitioned scheduling (no migration)
 - Each instance of a task must execute on the same processor
 - Equivalent to multiple uniprocessor systems!
- Semi-partitioned scheduling
 - Static task assignment
 - Each instance (or part of it) of a task is assigned to a fixed processor
 - Task instance or part of it may migrate



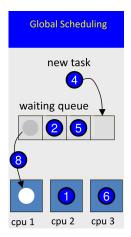


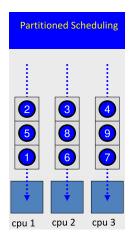
Multiprocessor Scheduling contd.





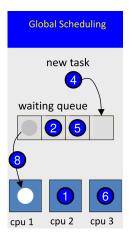
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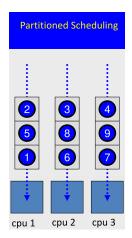


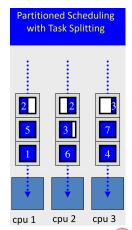




Multiprocessor Scheduling contd.

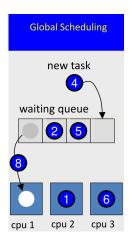








Global Scheduling



- All ready tasks are kept in a global queue
- When selected for execution, a task can be assigned to any processor, even after being preempted (task migration to another processor!)
 - Task migration may add overheads





Any algorithm for single processor scheduling may work, but schedulability analysis is non-trivial

- EDF (optimal for single processor)
 - Unfortunately EDF is not optimal for multiprocessors
 - Example: $\tau = \{(C_i, T_i)\} = \{(6, 12), (6, 12), (8, 13)\}$; Number of processors m = 2
 - No exact, but only sufficient schedulability test known
- Fixed Priority Scheduling (e.g. RM)
 - Difficult to find the optimal priority order
 - Difficult to check the schedulability
 - Suffer from the Dhall's effect



Dhall's effect (Dhall & Liu, 1978):

- With RM, DM and EDF, some low-utilization task sets can be unschedulable regardless of how many processors are used
 - Example: $\tau = \{(C_i, T_i)\} = \{(2\epsilon, 1), (2\epsilon, 1), (2\epsilon, 1), (1, 1 + \epsilon)\}$
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 - Number of processors, m
 - A set of m+1 tasks
 - m tasks each having utilization $2\epsilon/1$
 - One task has utilization $1/(1+\epsilon)$





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$$U = \frac{m \times 2\epsilon + \frac{1}{1+\epsilon}}{m} \to 0 \quad \text{(when } \epsilon \to 0 \text{ and } m \to \infty\text{)}$$





How can we avoid Dhall's effect:

- RM, DM & EDF only account for task deadlines! Actual computation demands are not accounted for
- Dhall's effect can easily be avoided by letting tasks with high utilization receive higher priority:



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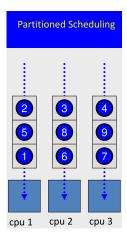
New priority assignment scheme: (Andersson, Baruah & Jonsson, 2001)

$$RM - US\{m/(3m-2)\}$$

- $RM US\{m/(3m-2)\}$ assign (static) priorities to tasks according to the following rule:
 - τ_i has highest priority if $U_i > m/(3m-2)$
 - τ_i has RM priority if $U_i ≤ m/(3m-2)$
 - Here, $U_i = C_i/T_i$, and m is the number of processor



Partitioned Scheduling



- Two steps:
 - Determine a mapping of tasks to processors
 - Perform run-time scheduling



Bin-packing Algorithms:

- Pack items of different sizes into a minimum number of bins, each with a fixed capacity
 - Solutions (Heuristics): First Fit, Next Fit, Best Fit
- Application to multiprocessor systems:
 - Bins are represented by processors and objects by tasks
 - The decision whether a processor is "fully loaded" or not is derived from a utilization-based schedulability test



Partitioned with EDF:

- Assign tasks to processors such that processor capacity does not exceeded (i.e. utilization bounded by 1)
- Schedule each processor using EDF



Partitioned with RM:

Rate-Monotonic First Fit (RMFF): (Dhall & Liu, 1978)

- First sort all tasks in non-decreasing order of their periods
- Task Assignment
 - Start from the highest priority task, and assign tasks to processors in the First Fit manner
 - A task τ_i can be assigned to a processor P_k if all the tasks assigned to P_k are RM-schedulable i.e.,
 - Total utilization of tasks assigned on P_k is bounded by $n(2^{1/n} 1)$, where n is the number of tasks assigned
 - One may also use the precise test (response time analysis) to get a better assignment!
 - Add a new processor if needed for the RM-test



Utilization bounded by 50%

- The Partitioning Problem is similar to Bin-packing problem (NP-hard)
- Limited Resource Usage, 50%
- Example:
 - Number of processors, m
 - A set of m+1 tasks each having utilization $0.5 + \epsilon$



Utilization bounded by 50%

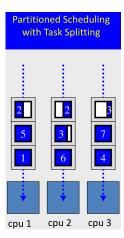
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$$U = \frac{(m+1) \times (0.5 + \epsilon)}{m} \to 0.5 \quad \text{(when } \epsilon \to 0 \text{ and } m \to \infty\text{)}$$





Semi-partitioned Scheduling



- Bin-packing with item splitting
- Resource can be "fully" (better) utilized



Semi-partitioned Scheduling contd.

Lakshmanan's Algorithm [ECRTS'09]:

- Sort all tasks in decreasing order of their utilization
- Pick up one processor, and assign as many tasks as possible from high utilization task to low utilization task
- If a task does not fit in the current processor then split the task into two
 - Assign one part of the task to the current processor
 - Pickup an empty processor, and assign another part of the task into it
- Utilization bound: 65%



Semi-partitioned Scheduling contd.

Breadth-First Partitioning Algorithms [RTAS 2010]

- Sort all tasks in increasing order of their priority
- Select the processor on which the assigned utilization is the lowest, and assign tasks from low priority to high priority
- If a task does not fit in the selected processor then split the task
- Utilization bound: 69%

