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# Explainable Deep Reinforcement Learning for Portfolio Optimisation of Financial Assets

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# Abstract

The dynamic and stochastic nature of financial markets together with highly non-stationary and noisy financial time series data make the task of portfolio optimisation particularly challenging. However, their nature makes them particularly well-suited for Deep Reinforcement Learning (DRL) algorithms, which can learn a trading strategy directly from the environment. Nonetheless, there are still significant challenges preventing its widespread adoption in the financial industry, such as the difficulty in finding the appropriate algorithm with a suitable reward function and their lack of transparency and interpretability. This thesis proposes an explainable DRL model for portfolio optimisation with the ability to leverage historical data to learn the optimal trading strategy that balances return maximisation and risk minimisation. Five prominent DRL algorithms are implemented and their performance is evaluated in different scenarios, including the impact of a larger environment representation, portfolio size and asset composition. Once the algorithms are trained, post-hoc explainability techniques are applied to understand which market conditions lead to a particular portfolio allocation. Although the performance of the algorithms does not generally outperform all of the benchmarks, the results show that the agents are a powerful tool in portfolio management capable of learning from high-dimensional data and adapting to changing market conditions. The crucial contribution of this research lies in the explainability framework, particularly the use of SHapley Additive exPlanations (SHAP) to provide insights into the decision-making process over the entire testing period in conjunction with interpretation for specific trading days.

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# Nomenclature

## Numbers and Arrays

|              |               |
|--------------|---------------|
| $a$          | Scalar        |
| $\mathbf{a}$ | Vector        |
| $\mathbf{A}$ | Matrix        |
| $\mathbf{1}$ | Matrix of 1's |

## Sets

|                                   |   |
|-----------------------------------|---|
| $\mathbb{A}$                      | Set   |
| $\mathbb{R}$                      | Set of real numbers                                       |
| $[a, b]$                          | Real interval including $a$ and $b$                       |
| $(a, b)$                          | Real interval excluding $a$ and $b$                       |
| $[a, b)$                          | Real interval including $a$ but excluding $b$             |
| $(a, b]$                          | Real interval excluding $a$ but including $b$             |
| $\{0, 1\}$                        | Set containing 0 and 1                                    |
| $\{0, 1, \dots, n\}$              | Set of all integers between 0 and $n$ inclusive           |
| $\emptyset$                       | Empty set   |
| $\mathbb{A} \subset \mathbb{B}$   | Set $\mathbb{A}$ is a proper subset of set $\mathbb{B}$   |
| $\mathbb{A} \subseteq \mathbb{B}$ | Set $\mathbb{A}$ is a subset or equal to set $\mathbb{B}$ |
| $\mathbb{A} \cap \mathbb{B}$      | Intersection of sets $\mathbb{A}$ and $\mathbb{B}$        |

$\mathbb{A} \cup \mathbb{B}$  Union of sets  $\mathbb{A}$  and  $\mathbb{B}$

$\mathbb{A} \setminus \mathbb{B}$  Set difference of sets  $\mathbb{A}$  and  $\mathbb{B}$

### Indexing

$a_i$  Element  $i$  of vector  $\mathbf{a}$ , with indexing start at 1

$A_{i,j}$  Element  $i, j$  of matrix  $\mathbf{A}$ , with indexing start at 1

### Algebra Operations

$\mathbf{A}^T$  Transpose of matrix  $\mathbf{A}$

$\mathbf{A}^{-1}$  Inverse of matrix  $\mathbf{A}$

### Probability

$P(x)$  Probability distribution over a random variable  $x$

$E[x]$  Expected value of random variable  $x$

$Var[x]$  Variance of random variable  $x$

$Cov[x, y]$  Covariance of random variables  $x$  and  $y$

$\mu$  Mean

$\sigma$  Standard deviation

$\sigma^2$  Variance

$\Sigma$  Covariance matrix

$\mathcal{N}(\mu, \sigma^2)$  Normal distribution with mean  $\mu$  and variance  $\sigma^2$

$\mathcal{N}(0, 1)$  Standard normal distribution

### Functions

$f : \mathbb{A} \rightarrow \mathbb{B}$  Function  $f$  with domain  $\mathbb{A}$  and range  $\mathbb{B}$

$f(x)$  Function  $f$  evaluated at  $x$

$f(x; \theta)$  Function  $f$  with parameters  $\theta$  evaluated at  $x$

$f'(x)$  Derivative of function  $f$



|                |  |
|----------------|--|
| $\int f(x) dx$ | Integral of function $f$ with respect to $x$ |
| $\min f(x)$    | Minimum of function $f$                      |
| $\min_x f(x)$  | Minimum of function $f$ with respect to $x$  |
| $\max f(x)$    | Maximum of function $f$                      |
| $\max_x f(x)$  | Maximum of function $f$ with respect to $x$  |
| $\log x$       | Natural logarithm of $x$                     |
| $x!$           | Factorial of $x$                             |

### Markov Decision Process

|               |  |
|---------------|--|
| $t$           | Time step                                    |
| $\mathcal{S}$ | State space                                  |
| $s_t$         | Observation of the state at time step $t$    |
| $\mathcal{A}$ | Action space                                 |
| $a_t$         | Action taken at time step $t$                |
| $R(s, a, s')$ | Reward function                              |
| $r_t$         | Reward received at time step $t$             |
| $T(s, a, s')$ | Transition function                          |
| $\gamma$      | Discount factor                              |
| $\pi$         | Policy                                       |
| $G$           | Long-term reward                             |
| $V^\pi$       | State Value function for policy $\pi$        |
| $Q^\pi$       | State-Action Value function for policy $\pi$ |
| $A^\pi$       | Advantage function for policy $\pi$          |

### Other Symbols

|           |         |
|-----------|---------|
| $\forall$ | For all |
|-----------|---------|

|          |                  |
|----------|------------------|
| $\in$    | Element of       |
| $\nabla$ | Gradient         |
| $\Sigma$ | Summation symbol |

# Glossary

**Advantage Actor-Critic** Algorithm that uses both an actor (policy) and a critic (value function) to learn optimal policies by estimating the advantage of actions taken.

**Algorithmic Trading** Use of computer algorithms to automate trading decisions and execute trades in financial markets.

**Artificial Intelligence** Simulation of human intelligence processes by machines enabling them to perform tasks that typically require human intelligence, such as visual perception, speech recognition, decision-making, and language translation.

**Bellman Equations** Set of equations that describe the relationship between the value of a state or action and the values of subsequent states or actions in dynamic programming and reinforcement learning.

**Black Box** Term used to describe a system or model whose internal workings are not transparent or easily understood.

**Deep Deterministic Policy Gradient** Algorithm that uses deep neural networks to learn policies for continuous action spaces.

**Deep Learning** Subset of machine learning that uses neural networks with many layers to learn from large amounts of data, enabling the model to automatically learn complex patterns and representations.

**Deep Neural Network** Type of artificial neural network with a succession of layers of non-linear transformations capable of learning a representation of the data with various levels of abstraction.

**Deep Reinforcement Learning** Combination of deep learning and reinforcement learning, where deep neural networks are used to approximate the value function or policy in reinforcement learning tasks.

**Efficient Frontier** Set of optimal portfolios that offer the highest expected return for a given level of risk, or the lowest risk for a given level of expected return, in the context of portfolio optimisation.

**Entropy** Measure of uncertainty or randomness in a system, often used in the context of information theory and reinforcement learning to encourage exploration.

**Explainable Artificial Intelligence** Methods and techniques in the application of artificial intelligence that make the results of the models understandable by humans, providing insights into how decisions are made.

**Exploitation** Process of leveraging known information to make decisions or take actions that are expected to yield the highest reward.

**Exploration** Process of investigating and experimenting with different actions or strategies to discover their effects and improve decision-making.

**Feature Importance** Technique for determining the contribution of each feature in a machine learning model to its predictions, helping to identify which features are most influential.

**Financial Markets** Marketplaces where people trade financial securities, commodities, and other fungible items of value at low transaction costs and at prices that reflect supply and demand.

**Hyper-parameter** Parameter that is set before the learning process begins and controls the learning process of a machine learning model, such as learning rate, batch size, and number of layers in a neural network.

**Local Interpretable Model-agnostic Explanations** Technique for explaining the predictions of any machine learning model its behaviour in a local region with an interpretable model, allowing users to understand the model's decisions for a specific observation.

**Machine Learning** Subset of artificial intelligence that enables systems to learn from data and improve their performance over time without being explicitly programmed.

**Markov Decision Process** Mathematical model for sequential-decision making where the outcomes are uncertain, characterised by states, actions, rewards and a transition function.

**Mean-Variance Optimisation** Investment strategy that aims to construct a portfolio of assets that maximises expected return for a given level of risk, or minimises risk for a given level of expected return.

**Modern Portfolio Theory** Investment theory that aims to construct a portfolio of assets that maximises expected return for a given level of risk, or minimises risk for a given level of expected return, through diversification.

**Portfolio Optimisation** Process of selecting the best distribution of assets in a portfolio to achieve specific investment goals, such as maximising returns or minimising risk.

**Proximal Policy Optimisation** Algorithm that optimises policies by ensuring that updates to the policy are not too large, maintaining a balance between exploration and exploitation.

**Python** Interpreted, object-oriented, high-level programming language.

**Reinforcement Learning** Subset of machine learning where an agent learns to make decisions by taking actions in an environment to maximise cumulative reward.

**Reward Function** Function that defines the feedback signal received by an agent in reinforcement learning.

**SHapley Additive exPlanations** Method based on Shapley values and cooperative game theory for interpreting machine learning models.

**Soft Actor-Critic** Algorithm that combines the benefits of off-policy learning and entropy regularisation, allowing for more exploration and better stability in learning policies for continuous action spaces.

**Supervised Learning** Machine learning task where a model is trained on labelled data to learn a mapping from inputs to outputs.

**Twin Delayed Deep Deterministic Policy Gradient** Extension of Deep Deterministic Policy Gradient that addresses the overestimation bias in value function estimation by using two critic networks and delaying policy updates.

**Unsupervised Learning** Machine learning task where a model learns patterns or structures in unlabelled data without explicit supervision.

# Acronyms

**A2C** Advantage Actor-Critic.

**A3C** Asynchronous Advantage Actor-Critic.

**ADX** Average Directional Index.

**AI** Artificial Intelligence.

**AI Act** Artificial Intelligence Act.

**ATR** Average True Range.

**AUD** Australian Dollar.

**BCS** British Computer Society.

**BXY** British Pound Currency Index.

**CAD** Canadian Dollar.

**CCI** Commodity Channel Index.

**CHF** Swiss Franc.

**CNY** Chinese Yuan.

**DDPG** Deep Deterministic Policy Gradient.

**DJIA** Dow Jones Industrial Average.

**DL** Deep Learning.

**DNN** Deep Neural Network.

**DPG** Deterministic Policy Gradient.

**DQN** Deep Q-Network.

**DRL** Deep Reinforcement Learning.

**DW30** Dow Jones 30 Index.

**DX** Directional Movement Index.

**DXY** U.S. Dollar Index.

**EMA** Exponential Moving Average.

**EU** European Union.

**EUR** Euro.

**Euro Stoxx 50** Euro Stoxx 50 Index.

**EXY** Euro Index.

**FCA** Financial Conduct Authority.

**FTSE 100** Financial Times Stock Exchange 100 Index.

**FVX** 5-Year Treasury Yield.

**GBP** British Pound.

**HKD** Hong Kong Dollar.

**HTML** HyperText Markup Language.

**IET** The Institution of Engineering and Technology.

**INR** Indian Rupee.

**IRX** 3-Month Treasury Yield.

**JPY** Japanese Yen.

**KRW** South Korean Won.



**LIME** Local Interpretable Model-agnostic Explanations.

**LLM** Large Language Model.

**LSTM** Long Short-Term Memory.

**MACD** Moving Average Convergence Divergence.

**MAPE** Mean Absolute Percentage Error.

**MDI** Negative Directional Index.

**MDP** Markov Decision Process.

**MiFID II** Markets in Financial Instruments Directive II.

**ML** Machine Learning.

**MPT** Modern Portfolio Theory.

**MSE** Mean Squared Error.

**MVO** Mean-Variance Optimisation.

**OHLCV** Open, High, Low, Close, Volume.

**PCA** Principal Component Analysis.

**PDI** Positive Directional Index.

**PPO** Proximal Policy Optimisation.

**RL** Reinforcement Learning.

**ROC** Rate of Change.

**RSI** Relative Strength Index.

**S&P 500** Standard and Poor's 500 Index.

**SAAC** Synchronous Advantage Actor Critic.

**SAC** Soft Actor-Critic.

**SHAP** SHapley Additive exPlanations.

**SMA** Simple Moving Average.

**TD3** Twin Delayed Deep Deterministic Policy Gradient.

**TNX** 10-Year Treasury Yield.

**TRPO** Trust Region Policy Optimisation.

**U.S.** United States.

**UK** United Kingdom.

**USD** United States Dollar.

**VIX** Volatility Index.

**VXD** Volatility Dow Jones 30 Index.

**XAI** Explainable Artificial Intelligence.

# Chapter 1

## Introduction

Financial markets are highly complex systems influenced by numerous factors, including economic and political events, social trends and technological advancements. Moreover, their evolving and stochastic nature requires using the most advance computational developments to model the financial environment. The tasks of financial time series prediction and portfolio optimisation are considerably intricate, due to the semi-strong form of market efficiency and the high level of noise. [7]

Algorithmic trading focuses on the application of analytical methods to automatically execute trading actions based on an algorithm without human intervention. Initially, the field mainly studied the usage of a computer program to follow a predefined strategy [8]. More recently, algorithmic trading involves environment perception by learning feature representation from highly non-stationary and noisy financial time series data, and decision-making by exploring the environment and simultaneously taking actions without supervision [9].

Machine Learning (ML) has an advantage for the task due to its ability to learn from historical data and make predictions about the future state of an environment. Research

has explored the application of Deep Learning (DL) in future price prediction of financial assets [10, 11, 7, 12]. However, its main disadvantage is the inability to directly handle trading, requiring an additional step to convert the predictions into actionable strategies. In contrast, Reinforcement Learning (RL) allows the algorithm to learn a trading strategy directly from the environment, without the need for a separate step [13, 14]. In this case, there are two main approaches: first, the algorithm can learn the amount of assets to buy, sell or hold at each time step [15], or second, the algorithm can learn the optimal portfolio allocation and automatically rebalance the portfolio weights at each time step [16].

Despite the potential of RL in portfolio optimisation, its widespread adoption in the financial industry remains limited. This is primarily due to following challenges [17]:

1. difficulty in finding the appropriate algorithm with a suitable reward function and hyper-parameters to ensure efficiency and performance,
2. challenge of testing the algorithm in a real-world environment, and
3. lack of transparency of ML models, often referred to as black boxes, making it increasingly intractable to interpret the algorithm's decisions.

In recent years, the rise in popularity of Artificial Intelligence (AI) and its widespread use have led to concerns regarding its decisions due to its black box nature [18]. The concept of explainability in AI, known as Explainable Artificial Intelligence (XAI), refers to a model's ability to provide details and reasons to make itself understandable [19]. The term was first coined in 2016 to describe the need for users to effectively understand, trust and manage artificial intelligence applications [20]. The need for explainability becomes particularly relevant within the financial domain, where the regulatory framework requires transparency and accountability in automated decision-making. Various relevant applications, including volatility models [21], credit risk assessment [22] and portfolio

construction [17], have explored the concept of explainability in financial applications.

Consequently, this thesis will focus on addressing the aforementioned challenges by exploring the application of Deep Reinforcement Learning (DRL) to portfolio optimisation and implementing explainability techniques to understand model behaviour.

## 1.1 Objectives

The objective of this thesis is to develop an explainable DRL model for portfolio optimisation. A DRL model has the ability to leverage historical financial data to learn an investment strategy that efficiently allocates financial assets while maximising expected returns and minimising risk. Moreover, the incorporation of advanced explainability techniques enhances the interpretability and transparency of the model’s decision-making. This project aims to bridge the gap between cutting-edge machine learning techniques and their practical application in finance by addressing the challenges of algorithm selection, simulation of real-world scenarios, and black box nature of ML models.

First, DRL models, namely Advantage Actor-Critic (A2C), Proximal Policy Optimisation (PPO), Deep Deterministic Policy Gradient (DDPG), Twin Delayed Deep Deterministic Policy Gradient (TD3) and Soft Actor-Critic (SAC), will be employed to learn the optimal portfolio allocation from high-dimensional environment representations. The algorithms will be trained on historical financial data, including technical and macroeconomic indicators, with the goal of capturing the complex market dynamics. Each of the algorithms is better suited to a particular scenario, for instance, DDPG encourages maximum returns [23], while A2C reduces the variance [24] and PPO is better at balancing exploration versus exploitation [25].

Second, post-hoc explainability techniques: Feature Importance, Local Interpretable Model-agnostic Explanations (LIME) and SHapley Additive exPlanations (SHAP) will

be applied to interpret the model’s decisions. The goal of these is to understand which market conditions, represented by financial data, lead to the actions/decisions, encoded as portfolio weights.

Finally, the performance of the DRL models will be analysed in different scenarios, including the impact of a larger financial environment representation, portfolio size and asset composition. The results will be compared with traditional portfolio optimisation methods to evaluate the effectiveness of the proposed approach.

## 1.2 Report Structure

This report is organised into six chapters, each of which focuses on a concrete area related to the problem. Additional material, together with source code, is included in the appendices.

The current chapter, 1, presents the motivation and the objectives of this thesis. It gives an overview of the potential of DRL in portfolio optimisation and its main challenges, particularly the lack of transparency of ML models.

Chapter 2 provides an overview of the theoretical background of the project. The problem of financial portfolio optimisation is outlined and the potential of DRL in this context is discussed. The chapter provides a comprehensive background explanation of the fundamentals of Deep Learning and Reinforcement Learning, including the main algorithms (A2C, PPO, DDPG, TD3, SAC). In addition, it gives an overview of the post-hoc explainability techniques (Feature Importance, LIME and SHAP) used to interpret the model’s decisions. Finally, it includes a comprehensive in-depth literature review on the topics of ML applied to portfolio optimisation and relevant applications of explainability techniques.

The methodology, chapter 3, describes the techniques and methods used and outlines

the implementation of the proposed solution. The chapter provides a detailed explanation of the architecture and components of the proposed DRL model, including the state representation and reward function. Furthermore, given the trained algorithms, it describes the implementation of the post-hoc explainability techniques.

The results of the experiments are presented in chapter 4, which analyses and evaluates the performance of the proposed methodology, while critically discussing the findings. It provides a detailed comparison of the DRL strategies with traditional portfolio optimisation methods. Furthermore, it consists of an analysis of the model's decisions using post-hoc explainability techniques.

Chapter 5 discusses the legal, social, ethical and professional implications within the context of the project. By addressing these issues, the project aims to ensure that the proposed solution adheres to industry standards, while considering the implications of the technology.

Finally, the report concludes with a summary of the main points of the work, the contributions made, in conjunction with potential applications and future work in chapter 6.

## Chapter 2

# Background

This chapter provides an overview of the problem of portfolio optimisation in the financial domain, followed by a comprehensive explanation of the fundamentals of Deep Learning (DL) and Reinforcement Learning (RL), and relevant algorithms in the field of Deep Reinforcement Learning (DRL). In addition, it discusses the need for explainability in Machine Learning (ML) and the relevant post-hoc explainability techniques to achieve interpretable and transparent models. Finally, it presents the state of the art in portfolio optimisation using DRL and the recent advancements in explainability techniques in the field.

### 2.1 Portfolio Optimisation

Portfolio optimisation is the process of selecting optimal weights for a portfolio of assets in order to maximise expected returns for a given level of risk, or conversely, to minimise risk for a given level of expected returns [26]. In mathematical terms, the problem requires finding a solution to the specified objective function, which is typically a function of the expected returns and the risk associated with the portfolio [27]. The task becomes



further complicated if a time dimension is introduced, as the portfolio weights need to be adjusted over time to capture the changes in market conditions and asset prices [28].

### 2.1.1 Modern Portfolio Theory

One of the most well known traditional frameworks that formalise the problem of portfolio allocation is Markowitz's Modern Portfolio Theory (MPT), proposed in 1952 [29]. It provides a mathematical framework where investors choose optimal portfolios based on risk and return, by either minimising the risk given a specified return or, maximising the return given a specified risk [30]. The theory extends the concept of diversification by suggesting that owning financial assets of different kinds is less risky than owning assets of the same kind, due to the correlations between assets.

The main assumptions in MPT are:

- investors are risk-averse, rational, and seek to maximise return for a given risk;
- returns are normally distributed;
- markets are frictionless, meaning there are no transaction costs; and
- assets are infinitely divisible.

Under these assumptions, portfolio risk and return can be modelled as an optimisation problem. Let  $\mathbf{w} = (w_1, w_2, \dots, w_N)^T$  denote the portfolio weight vector, where each  $w_i$  indicates the proportion of capital allocated to asset  $i$ , subject to the budget constraint

$$\sum_{i=1}^N w_i = 1 \tag{2.1}$$

and subject to the non-negativity constraint, meaning that short-selling is not allowed:

$$w_i \geq 0 \quad \forall i = 1, 2, \dots, N. \tag{2.2}$$

Let  $\boldsymbol{\mu} = (R_1, R_2, \dots, R_N)^T$  represent the vector of expected returns, and  $\Sigma \in \mathbb{R}^{N \times N}$  the covariance matrix of asset returns. The expected return of the portfolio is then given by:

$$R_p = \mathbf{w}^T \boldsymbol{\mu}, \quad (2.3)$$

and the portfolio risk is quantified by the variance of returns:

$$\sigma_p^2 = \mathbf{w}^T \Sigma \mathbf{w}. \quad (2.4)$$

This formulation provides the foundation for solving the mean-variance optimisation problem, by either:

- minimising portfolio variance  $\sigma_p^2$  subject to a target expected return  $R_p$ , or
- maximising expected return  $R_p$  subject to a risk constraint  $\sigma_p$ .

The Markowitz mean-variance optimisation problem can be expressed as:

$$\begin{aligned} \min_{\mathbf{w}} \quad & \mathbf{w}^T \Sigma \mathbf{w} \\ \text{subject to} \quad & \begin{cases} \mathbf{w}^T \boldsymbol{\mu} = R_p \\ \mathbf{w}^T \mathbf{1} = 1 \\ \mathbf{w} \geq 0 \end{cases} \end{aligned} \quad (2.5)$$

Solving for varying levels of target return leads to a set of optimal portfolios that form the efficient frontier. It is typically visualised in a risk-return space, where the  $x$ -axis represents the risk (standard deviation) and the  $y$ -axis represents the expected return, as shown in Figure 2.1. Portfolios below the curve are sub-optimal, while those on the frontier represent the best achievable combinations of risk and return.

Despite the simplicity in the formulation of MPT, its assumptions do not reflect the

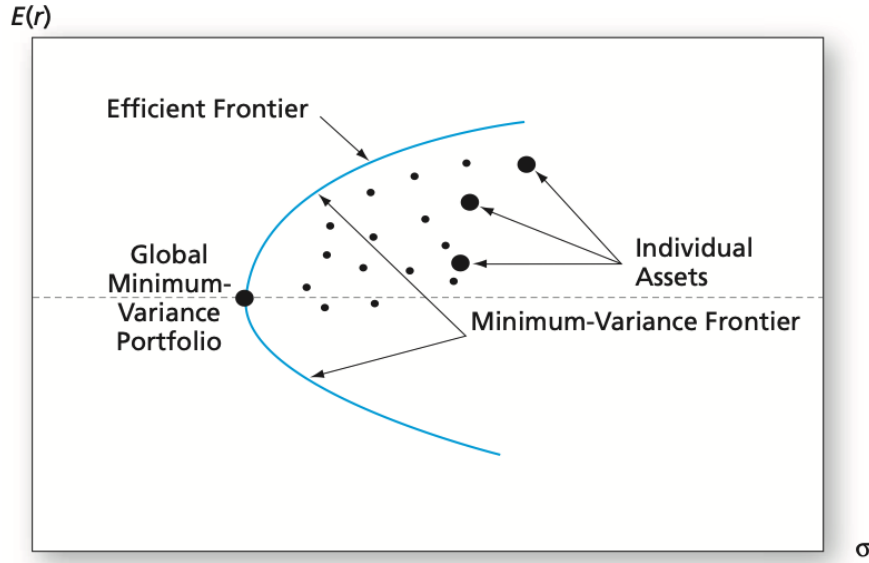


Figure 2.1: Efficient Frontier in Risk-Return Space. [1]

behaviour of real markets. Modern financial markets are dynamic, non-stationary, and feature non-linear relationships, which have driven research into other approaches better suited to capture their complexities.

## 2.2 Deep Reinforcement Learning

Machine Learning is a branch of Artificial Intelligence (AI) that focuses on the use of data and algorithms to imitate the way humans learn by gradually improving their accuracy over time [31]. There are three main tasks in ML [32]:

- **Supervised Learning:** Task of training a classification or regression model from labelled data, where the model learns to map inputs to outputs based on examples.
- **Unsupervised Learning:** Task of drawing inferences from datasets consisting of unlabelled data, where the model learns to identify patterns or structures in the data.

- **Reinforcement Learning (RL):** Task of training an agent to sequentially make decisions by taking actions in an environment with the goal of maximising cumulative reward, using feedback from the environment to learn an optimal strategy.

Deep Learning (DL) is a set of methods and techniques to solve such ML tasks, which focuses on the use of Deep Neural Networks (DNNs) [33], which are characterised by a succession of layers of non-linear transformations that allow the model to learn a representation of the data with various levels of abstraction. Therefore, Deep Reinforcement Learning (DRL) combines DL and RL to solve sequential decision-making problems with high-dimensionality in the environment representation. This approach has gained significant attention in recent years due to its success in various applications, including robotics [34] and game playing [35, 36].

### 2.2.1 Reinforcement Learning

As mentioned, RL is a type of ML that solves the problem of sequential decision-making through continuous interaction with an environment. The agent learns to take actions given an observation of the environment’s state with the goal of optimising a pre-defined notion of reward.

The RL problem can be formalised as a discrete-time stochastic control process where an agent interacts with the environment. At each time step  $t$ , the agent observes the state of the environment  $s_t \in \mathcal{S}$ , takes an action  $a_t \in \mathcal{A}$  to obtain a reward  $r_t \in \mathbb{R}$  and transition to a new state  $s_{t+1} \in \mathcal{S}$ , where  $\mathcal{S}$  is the state space and  $\mathcal{A}$  is the action space [32]. The agent’s interaction with the environment is visually represented in Figure 2.2.

A discrete-time stochastic control process can be formalised as a Markov Decision Process (MDP), if it fulfils the Markov Property.

**Definition 2.2.1** (Markov Property). A discrete-time stochastic control process satisfies

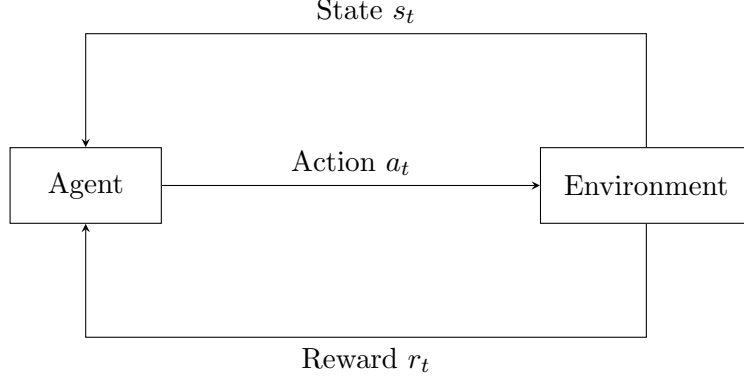


Figure 2.2: Agent interaction with environment.

the Markov Property if:

$$P(s_{t+1}|s_t, a_t) = P(s_{t+1}|s_t, a_t, s_{t-1}, a_{t-1}, \dots, s_0, a_0), \text{ and} \quad (2.6)$$

$$P(r_t|s_t, a_t) = P(r_t|s_t, a_t, s_{t-1}, a_{t-1}, \dots, s_0, a_0), \quad (2.7)$$

where  $P(s_{t+1}|s_t, a_t)$  is the transition probability of moving to state  $s_{t+1}$  given the current state  $s_t$  and action  $a_t$ , and  $P(r_t|s_t, a_t)$  is the reward function that defines the expected reward received at time  $t$  given the current state and action.

This implies that the state  $s_{t+1}$  at a future time step  $t + 1$  only depends on the current state  $s_t$  and action  $a_t$ . Similarly, the reward  $r_t$  only depends on the current state and action and not on the history of previous states and actions. Consequently, a Markov Decision Process [37] is a discrete-time stochastic control process defined as:

**Definition 2.2.2** (Markov Decision Process). An MDP is a tuple  $\mathcal{M} = (\mathcal{S}, \mathcal{A}, T, R, \gamma)$ , where:

- $\mathcal{S}$  is the state space:  $s_t \in \mathcal{S}$ ,
- $\mathcal{A}$  is the action space:  $a_t \in \mathcal{A}$ ,
- $T : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow [0, 1]$  is the transition function,

- $R : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow \mathcal{R}$  is the reward function, where  $\mathcal{R} \in [0, R_{max}]$  is the set of all possible rewards bounded by  $R_{max} \in \mathbb{R}^+$ , and
- $\gamma \in [0, 1)$  is the discount factor.

At each time step, the probability of advancing to the next state  $s_{t+1}$  is given by the transition function  $T(s_t, a_t, s_{t+1})$  and the reward  $r_t$  is given by the reward function  $R(s_t, a_t, s_{t+1})$ . This can be visualised in Figure 2.3.

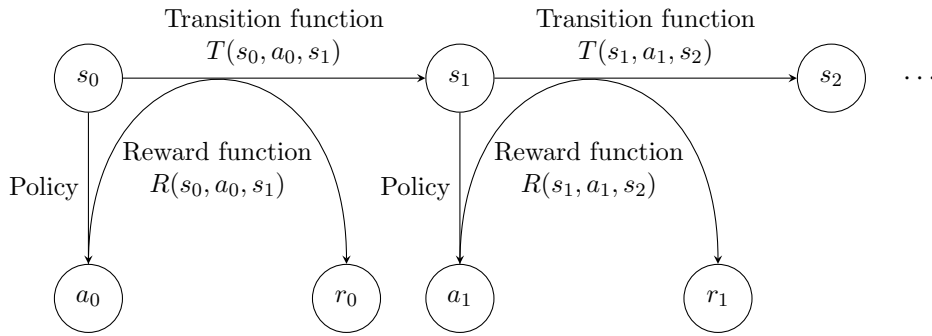


Figure 2.3: Markov Decision Process with policy, transition, and reward functions.

The agent's objective is to learn a policy  $\pi : \mathcal{S} \rightarrow \mathcal{A}$  that maps states to actions that maximises the expected cumulative reward over time. Policies can be categorised as:

- deterministic:  $\pi(s) : \mathcal{S} \rightarrow \mathcal{A}$ , at a given state  $s$ , the policy specifies the only available action to take, or
- stochastic:  $\pi(s, a) : \mathcal{S} \times \mathcal{A} \rightarrow [0, 1]$ , at a given state  $s$ , the policy specifies the probability of taking action  $a$ .

The goal of the agent is to maximise the cumulative long-term reward  $G_t$ , which is defined as the sum of discounted rewards over time:

$$G_t = r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} + \dots = r_{t+1} + \gamma G_{t+1}, \quad (2.8)$$

where  $\gamma \in [0, 1)$  is the discount factor and is used to balance the importance between immediate and future rewards. If the discount factor is set to 0, the agent is myopic and only maximises the immediate reward; whereas, as  $\gamma$  approaches 1, the agent becomes more far-sighted and places greater importance on future rewards.

The expected cumulative reward is defined as the state value function  $V^\pi(s) : \mathcal{S} \rightarrow \mathbb{R}$ , which is the expected return when starting from state  $s$  and following policy  $\pi$ :

$$V^\pi(s) = \mathbb{E}_\pi [G_t | s_t = s], \quad (2.9)$$

where  $\mathbb{E}_\pi$  denotes the expectation over the policy  $\pi$ .

Similarly, the state-action value function  $Q^\pi(s, a) : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}$  is defined as the expected return when starting from state  $s$ , taking action  $a$ , and then following policy  $\pi$ :

$$Q^\pi(s, a) = \mathbb{E}_\pi [G_t | s_t = s, a_t = a]. \quad (2.10)$$

The state value function  $V^\pi(s)$  and the state-action value function  $Q^\pi(s, a)$  are related as follows:

$$V^\pi(s) = \sum_{a \in \mathcal{A}} \pi(a|s) Q^\pi(s, a) = \mathbb{E}_\pi [Q^\pi(s, a) | s_t = s]. \quad (2.11)$$

Moreover, the advantage function  $A^\pi(s, a)$  combines both the state value function  $V^\pi(s)$  and the state-action value function  $Q^\pi(s, a)$ , and is defined as:

$$A^\pi(s, a) = Q^\pi(s, a) - V^\pi(s). \quad (2.12)$$

A policy  $\pi$  is said to be optimal if the policy's value function is the optimal value function

of the MDP, defined as:

$$V^*(s) = \max_{\pi'} V^{\pi'}(s), \forall s \in \mathcal{S}, \quad (2.13)$$

$$Q^*(s, a) = \max_{\pi'} Q^{\pi'}(s, a), \forall s \in \mathcal{S}, a \in \mathcal{A}. \quad (2.14)$$

The optimal policy  $\pi^*$  is:

$$\pi^*(s) = \arg \max_{a \in \mathcal{A}} Q^*(s, a) \quad (2.15)$$

As a result, the optimal policy is the greedy policy that performs the optimal actions at each time step as determined by the optimal value functions. This framework enables the agent to determine optimal actions that maximise long-term returns by evaluating immediate information, without requiring knowledge of the values of future states and actions.

The Bellman equations [38] provide a recursive relation between the value functions in terms of the future state/action values. There are four main Bellman equations, classified in two groups: the Bellman expectation equations and the Bellman optimality equations. The Bellman expectation equations are defined as follows:

$$V^\pi(s) = \sum_{a \in \mathcal{A}} \pi(a | s) \sum_{s' \in \mathcal{S}} T(s, a, s') [R(s, a, s') + \gamma V^\pi(s')], \quad (2.16)$$

$$Q^\pi(s, a) = \sum_{s' \in \mathcal{S}} T(s, a, s') \left[ R(s, a, s') + \gamma \sum_{a' \in \mathcal{A}} \pi(a' | s') Q^\pi(s', a') \right], \quad (2.17)$$

and the Bellman optimality equations are defined as:

$$V^*(s) = \max_{a \in \mathcal{A}} \sum_{s' \in \mathcal{S}} T(s, a, s') [R(s, a, s') + \gamma V^*(s')], \quad (2.18)$$

$$Q^*(s, a) = \sum_{s' \in \mathcal{S}} T(s, a, s') \left[ R(s, a, s') + \gamma \max_{a' \in \mathcal{A}} Q^*(s', a') \right]. \quad (2.19)$$



Although explicitly solving the Bellman equations would lead to the optimal policy, it is often intractable due to the size of the state and action spaces. Therefore, in RL algorithms, the goal is to learn an approximation of the optimal value functions, which can be used to derive the optimal policy.

Another problem that arises is that of balancing exploration and exploitation [39]. Theoretically, following the greedy action yields the optimal policy, but this is only true if all the action values are known. In practice, the agent at each time step and given state chooses either an action whose value is higher, thus exploiting its current knowledge, or picks an action at random, thus exploring the environment and gaining more information about the state-action space, leading to potentially discovering a better action than the greedy one.

### 2.2.2 Deep Reinforcement Learning Algorithms

A Reinforcement Learning (RL) agent includes one or more of the following components [32]:

- a representation of the value function that provides a prediction of the value of each state or state-action pair,
- a direct representation of the policy, or
- a model of the environment, consisting of estimates of transition and reward functions.

Depending on the components, the main RL paradigms are:

- **Model-free** algorithms do not learn a representation of the environment, but focus on the value function, the policy or both. These algorithms can be further divided into:

- **Value-based** algorithms learn an approximation of the value function, which is used to compute the state or state-action values. The policy is not learnt explicitly but can be derived from the value function. Examples include Deep Q-Network (DQN) [40] and C51 [41].
- **Policy-based** algorithms learn a direct representation of the policy, which is used to select actions. Advantage Actor-Critic (A2C), Asynchronous Advantage Actor-Critic (A3C) [24] and Proximal Policy Optimisation (PPO) [25] are examples of policy-based algorithms.
- **Actor-Critic** algorithms combine both value-based and policy-based approaches, where the actor learns the policy and the critic learns the value function. The critic provides feedback to the actor to improve the policy. Some examples are Deep Deterministic Policy Gradient (DDPG) [23], Twin Delayed Deep Deterministic Policy Gradient (TD3) [42], and Soft Actor-Critic (SAC) [43].
- **Model-based** algorithms include a model of the environment, which can be used to simulate future states and rewards. For example, World Models [44] learns a model of the environment and AlphaZero [45] has a representation of the model.

The taxonomy of the RL algorithms is shown in Figure 2.4.

The full potential of RL algorithms is achieved when leveraging the power of Deep Learning to solve dynamic stochastic control problems that have high-dimensionality in their representation of the state and action spaces. DRL algorithms use Deep Neural Networks to approximate the value functions, or use gradient ascent to find the optimal policy parameters. This thesis will focus on policy-based and actor-critic algorithms. The pseudo-code for the algorithms is provided in Appendix A.1.

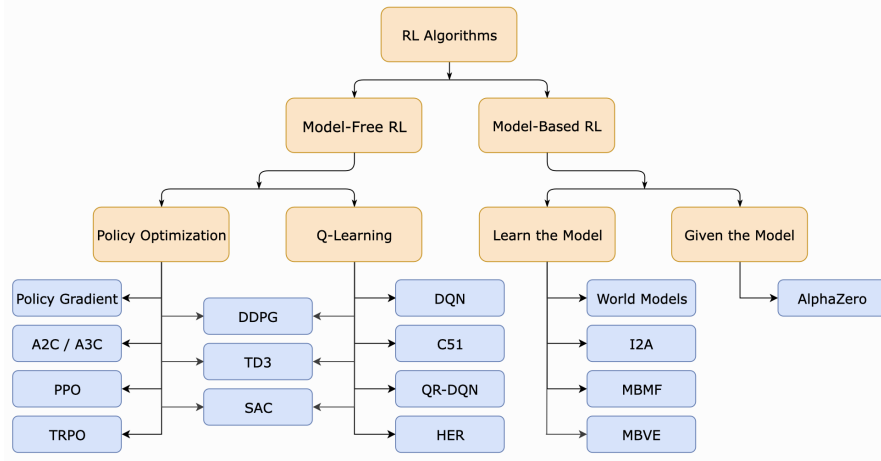


Figure 2.4: Taxonomy of Reinforcement Learning Algorithms [2].

### 2.2.2.1 Advantage Actor-Critic (A2C)

The Advantage Actor-Critic (A2C) algorithm was developed by Mnih et al. (2016) [24]. The main contribution is the usage of the advantage function to address the variance issues present in policy gradient methods. The A2C is the synchronous version of A3C, and is preferred due to its better performance in terms of training time and cost-effectiveness [46].

The algorithm consists of a dual-network architecture, where the actor network learns a stochastic policy  $\pi(a_t | s_t; \theta)$  and the critic network learns the value function  $V(s_t; \theta_v)$ . The policy and the value function are updated after every  $t_{max}$  actions or when a terminal state is reached. The advantage function is estimated as follows:

$$A(s_t, a_t; \theta, \theta_v) = \sum_{i=0}^{k-1} \gamma^i r_{t+i} + \gamma^k V(s_{t+k}; \theta_v) - V(s_t; \theta_v), \quad (2.20)$$

where  $k$  represents the  $n$ -step return and is upper-bounded by the maximum number of steps  $t_{max}$ , and  $\gamma$  is the discount factor. The algorithm's objective function is defined

as:

$$J(\theta, \theta_v) = \mathbb{E}_\pi [\log \pi(a_t | s_t; \theta) A(s_t, a_t; \theta, \theta_v)]. \quad (2.21)$$

#### 2.2.2.2 Proximal Policy Optimisation (PPO)

Proximal Policy Optimisation (PPO) is a policy gradient algorithm that was introduced by Schulman et al. (2017) [25] with the objective of constraining policy updates. The algorithm balances sufficiently large updates in order to improve the policy, while avoiding excessively large changes that could hinder performance.

PPO improves the performance of Trust Region Policy Optimisation (TRPO) [47] by using a clipped surrogate objective function that ensures that the probability ratio  $r_t$  is bounded within a range of  $[1 - \epsilon, 1 + \epsilon]$ , where  $\epsilon$  is a hyperparameter that controls the clipping range. The objective function is defined as:

$$L_t^{CLIP}(\theta) = \mathbb{E}_t \left[ \min \left( r_t(\theta) \hat{A}_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right) \right], \quad (2.22)$$

where

$$r_t(\theta) = \frac{\pi_\theta(a_t | s_t)}{\pi_{\theta_{old}}(a_t | s_t)} \quad (2.23)$$

is the probability ratio between the current policy  $\pi_\theta$  and the old policy  $\pi_{\theta_{old}}$ .

Another improvement with respect to TRPO is the use of simple first-order optimisation methods as opposed to the second-order methods used in TRPO. Consequently, PPO maintains the stability and reliability of other trust-region methods, while being easier to implement and more computationally efficient.

### 2.2.2.3 Deep Deterministic Policy Gradient (DDPG)

Deep Deterministic Policy Gradient (DDPG) is an off-policy actor-critic algorithm that was introduced by Lillicrap et al. (2015) [23]. The algorithm arises to solve the challenges of applying Deep Q-Network [40] to continuous action spaces by applying Deterministic Policy Gradient (DPG), which enables the efficient computation of the policy gradient without the need to integrate over the action space.

The algorithm uses the following networks: the actor network  $\mu(s_t; \theta_\mu)$ , which learns a deterministic policy; the critic network  $Q(s_t, a_t; \theta_Q)$ , which learns the state-action value function; and the actor's and critic's target networks. The actor network is updated using DPG:

$$\nabla_{\theta_\mu} J \approx \mathbb{E}_{s_t \sim \mathcal{D}} [\nabla_a Q(s_t, a_t; \theta_Q) \nabla_{\theta_\mu} \mu(s_t; \theta_\mu)] , \quad (2.24)$$

where  $\mathcal{D}$  is the replay buffer that stores the agent's experiences,  $\theta_\mu$  are the parameters of the actor network, and  $\theta_Q$  are the parameters of the critic network, and the critic network is updated using the Bellman equations:

$$\nabla_{\theta_Q} J \approx \mathbb{E}_{s_t \sim \mathcal{D}} [(r_t + \gamma Q(s_{t+1}, \mu(s_{t+1}; \theta_\mu); \theta'_Q) - Q(s_t, a_t; \theta_Q)) \nabla_{\theta_Q} Q(s_t, a_t; \theta_Q)] , \quad (2.25)$$

where  $\theta'_Q$  are the parameters of the target critic network.

From Deep Q-Network, the algorithm incorporates a replay buffer to store the agent's experiences, which allows the agent to learn from past experiences and improve its performance over time. Moreover, DDPG incorporates noise, typically Ornstein-Uhlenbeck noise [48], to the actions taken by the actor network to encourage exploration of the action space.

#### **2.2.2.4 Twin Delayed Deep Deterministic Policy Gradient (TD3)**

Twin Delayed Deep Deterministic Policy Gradient (TD3) is an extension of DDPG introduced by Fujimoto et al. (2018) [42]. The proposal addresses the hyper-parameter sensitivity and overestimation bias present in the critic network of DDPG by proposing three main improvements. First, clipped double Q-learning, where the algorithm employs two critic networks and uses their minimum value to compute the target value for the actor network, which reduces the overestimation bias. Second, by introducing delayed policy updates, the actor and critic networks' updates are performed at different frequencies. The critic networks are updated every time step, whereas the actor and target networks are updated less frequently. The main benefit is that it allows the critic to improve the accuracy of the value estimates before the actor updates its policy. Third, to perform target policy smoothing, the algorithm adds noise to the target action during the critic updates to smooth the value function over similar actions, resulting in a lower impact of approximation errors and more robust policies.

#### **2.2.2.5 Soft Actor-Critic (SAC)**

Soft Actor-Critic (SAC), despite being an off-policy actor-critic algorithm, represents a paradigm shift in RL. The algorithm was presented by Haarnoja et al. (2018) [43] and is based on the maximum entropy framework, which aims to maximise both the expected return and the entropy of the policy, encouraging the agent to succeed at the task while acting as randomly as possible.

The algorithm uses two critic networks to estimate the state-action value function, and a stochastic actor network that learns a policy that maximises the expected return while also maximising the entropy of the policy. The objective function for the actor network,

which is updated using the policy gradient method, is defined as:

$$J(\theta) = \mathbb{E}_{s_t \sim \mathcal{D}} [\mathbb{E}_{a_t \sim \pi_\theta} [\alpha \log \pi_\theta(a_t | s_t) + Q(s_t, a_t; \theta_Q)]] , \quad (2.26)$$

where  $\alpha$  is a temperature parameter that controls the trade-off between exploration and exploitation, and  $\mathcal{D}$  is the replay buffer that stores the agent’s experiences. The critic networks are updated using the Bellman equations:

$$J(\theta_Q) = \mathbb{E}_{s_t \sim \mathcal{D}} \left[ \left( r_t + \gamma \min_{i=1,2} Q(s_{t+1}, \mu_\theta(s_{t+1}) + \mathcal{N}(0, \sigma); \theta_{Q_i}) - Q(s_t, a_t; \theta_{Q_i}) \right)^2 \right] , \quad (2.27)$$

where  $\mathcal{N}(0, \sigma)$  is the noise added to the action to encourage exploration, and  $\theta_{Q_i}$  are the parameters of the two critic networks. The temperature parameter  $\alpha$  is learned automatically by maximising the entropy of the policy, which is defined as:

$$J(\alpha) = \mathbb{E}_{s_t \sim \mathcal{D}} [\alpha \log \pi_\theta(a_t | s_t)] . \quad (2.28)$$

This parameter is used to control the trade-off between the entropy and the reward terms, effectively controlling the stochasticity of the policy.

#### 2.2.2.6 Algorithm comparison

The five algorithms presented above are among the most widely used in the field of DRL, each addressing specific challenges in policy estimation and value function approximation. A2C is an on-policy actor-critic method that reduces variance through advantage estimation, while PPO changed on-policy learning by introducing a clipped surrogate objective that ensures stable policy updates. Although DDPG pioneered continuous control through deterministic policies, TD3 addressed the overestimation bias of its predecessor via twin critics and delayed updates. SAC revolutionised the field of DRL by

incorporating maximum entropy principles.

An overview of the algorithms and their key characteristics is summarised in Table 2.1.

Table 2.1: Comparison of Deep Reinforcement Learning Algorithms.

| Algorithm | Policy Type   | On/Off Policy | Key Idea                         |
|-----------|---------------|---------------|----------------------------------|
| A2C       | Stochastic    | On            | Advantage Function Estimation    |
| PPO       | Stochastic    | On            | Clipped Policy Updates           |
| DDPG      | Deterministic | Off           | Actor-Critic + Replay buffer     |
| TD3       | Deterministic | Off           | Double critics + Delayed updates |
| SAC       | Stochastic    | Off           | Max-entropy RL                   |

## 2.3 Explainable Artificial Intelligence

Explainable Artificial Intelligence (XAI) refers to a set of processes, methods and techniques that enable human users to comprehend and trust the outcomes and decisions made by Artificial Intelligence (AI) systems. The goal is to make AI algorithms more transparent, interpretable, and accountable, allowing end-users to understand the outputs of the models. This is particularly important in Deep Learning (DL) where the models are often considered black boxes due to their complexity, non-linearity and high-dimensionality, making it difficult to understand how they arrive at their decisions. With explainable systems, the benefits are numerous ranging from informed decision making to increased user adoption and better governance [49].

Although there are many possible classifications of XAI methods, they can be broadly categorised into two main categories. First, transparent algorithms are inherently understandable and interpretable, such as linear regression, decision trees and rule-based systems. Second, post-hoc explanations are methods that require the usage of an ad-



ditional algorithm to clarify the decisions made by a model. Examples include saliency maps [50] and interaction data [51].

Another classification relates to whether the explanation method depends on the type of model it is being applied to. On the one hand, model-agnostic methods work with any model regardless of its internal architecture, effectively treating all types of models as black boxes. The analysis is conducted by understanding the input-output behaviour and how small perturbations to the input impact the output. These methods can be further sub-divided between global explanations, which provide an understanding of the model’s overall behaviour across an entire dataset, and local techniques, which focus on explaining the individual predictions. SHapley Additive exPlanations (SHAP) [52] is an example of a global method, while Local Interpretable Model-agnostic Explanations (LIME) [53] provides local interpretations. On the other hand, model-specific methods are tailored to a particular architecture and leverage its components as part of the explanation process. In the case of neural networks, this can be achieved by analysing the learned features or by incorporating attention mechanisms [54].

The taxonomy of the XAI methods is shown in Figure 2.5.

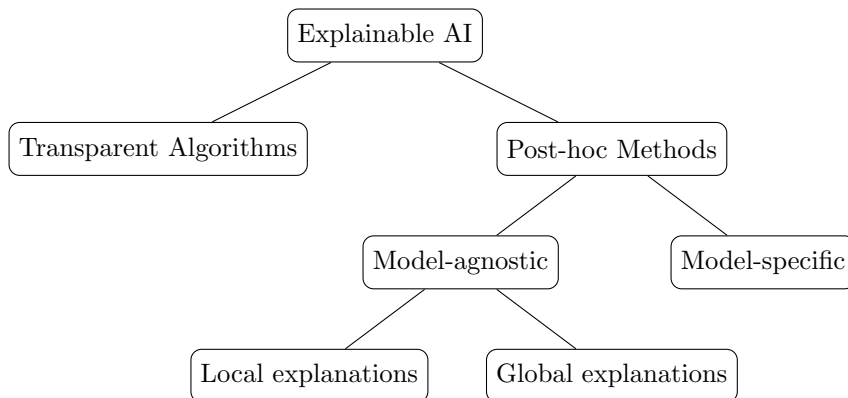


Figure 2.5: Taxonomy of Explainable Artificial Intelligence Methods [3].

### 2.3.1 Feature Importance

Feature Importance is a global model-specific method that quantifies the contribution of each feature to the model’s predictions. In particular, permutation feature importance measures the contribution of each feature by evaluating the model’s performance on the original dataset and comparing it to the performance on a permuted version of the dataset, where a specific feature is randomly shuffled [55]. The process allows to understand how much the model’s relies on a particular feature for its prediction, by measuring the decrease in predictive power if the input feature’s values vary.

An alternative method, well-suited for tree-based models, is impurity-based feature importance. Random forests split their features with the goal of reducing an impurity measure at each node, normally Gini impurity for classification tasks or Mean Squared Error (MSE) for regression [56]. As such, a variable responsible for a split with a large decrease in impurity is considered important [57]. As a result, the impurity importance of a feature is the sum of all impurity reductions across all nodes and trees in the forest where the particular feature was used to split the data. While powerful, this method suffers from bias towards features with high cardinality and they do not necessarily reflect the ability of a feature to make useful predictions on the test set, given that importance is computed on the training set [55].

### 2.3.2 Local Interpretable Model-agnostic Explanations

Local Interpretable Model-agnostic Explanations (LIME) is a model-agnostic explanation method that interprets individual predictions of a Machine Learning model by analysing the model locally around the prediction of interest. The method, introduced by Ribeiro et al. (2016) [53], utilises the black box model to understand what happens to the outputs when the input data is slightly modified, then fits a simpler, interpretable

model to the perturbed data to approximate its behaviour in that local region.

For a more rigorous definition, let  $\mathcal{L}(f, g, \pi_x)$  be a measure of how unfaithful an explanation model  $g$  is in approximating the model  $f : \mathbb{R}^d \rightarrow \mathbb{R}$  in the neighbourhood of the instance  $x$  defined as  $\pi_x$ . The goal is to find an interpretable model  $g \in G$ , where  $G$  is the space of all interpretable models, that minimises the following objective function:

$$\xi(x) = \mathcal{L}(f, g, \pi_x) + \Omega(g) \quad (2.29)$$

where  $\Omega(g)$  is a regularisation term that penalises the complexity of the explanation model  $g$ . This encourages interpretability, meaning a qualitative understanding of the relationship between inputs and outputs, and promotes local fidelity, ensuring the explanation accurately approximates the model's behaviour in that region.

The method works as follows:

- **Instance Selection:** Start with a specific prediction instance that requires explanation.
- **Perturbation:** Generate synthetic data points by perturbing the original instance.
- **Model Querying:** Obtain predictions from the black box model for these perturbed instances.
- **Weighting:** Assign weights to the synthetic data points based on their proximity to the original instance.
- **Surrogate Training:** Train a simple, interpretable model (typically linear regression) on the weighted synthetic dataset.
- **Explanation:** Use the surrogate model to explain the original prediction by interpreting its coefficients or structure.

Its main advantages are its ability to work across different types of data and models, due to its model-agnostic nature, and the fact that its explanations are human-friendly and include a fidelity measure that indicates how well the explanation approximates the black box model’s local behaviour. Nonetheless, the method offers only local explanations, which may not generalise well to the entire dataset; it relies on the choice of neighbourhood; and the complexity of the surrogate model needs to be defined in advance and can compromise the interpretability of the explanation [3].

### 2.3.3 Shapley Additive Explanations

Another model-agnostic technique is SHapley Additive exPlanations (SHAP), which was introduced by Lundberg and Lee (2017) [52]. The method is based on cooperative game theory and the concept of Shapley values [58].

The Shapley value arises in cooperative game theory to answer the question of how to fairly distribute the contribution of each player in a coalition. In this framework, a coalitional game is represented as a tuple  $(N, v)$ , where  $N = \{1, 2, \dots, n\}$  is the set of players and  $v : 2^N \rightarrow \mathbb{R}$  is the characteristic function that assigns a value  $v(S)$  to each possible coalition  $S \subseteq N$ , with the convention that  $v(\emptyset) = 0$ . The characteristic function  $v(S)$  represents the total value that coalition  $S$  can achieve through cooperation.

Mathematically, the Shapley value for a feature  $i$  is defined as:

$$\phi_i = \sum_{S \subseteq N \setminus \{i\}} \frac{|S|!(|N| - |S| - 1)!}{|N|!} [v_{S \cup \{i\}}(x_{S \cup \{i\}}) - v_S(x_S)] \quad (2.30)$$

where  $S \subseteq N$  is a subset of all features  $N$ ,  $v_{S \cup \{i\}}$  is marginal contribution of player  $i$  to coalition  $S$ , and  $v_S$  is the value of coalition  $S$  without player  $i$ . This formula can be understood as computing the weighted average of marginal contributions of feature  $i$  across all possible coalitions.

The advantage of Shapley values is that it is the only attribution method that results in a fair payout. In particular, it satisfies the four fundamental properties that define a fair allocation:

- **Efficiency:** The sum of all Shapley values equals the value of the grand coalition:

$$\sum_{i \in N} \phi_i = v(N)$$

- **Symmetry:** The contributions of two players  $i$  and  $j$  should be equal if they make identical marginal contributions to all possible coalitions:

$$v(S \cup \{i\}) = v(S \cup \{j\}), \forall S \subseteq N \setminus \{i, j\} \implies \phi_i = \phi_j$$

- **Dummy:** If a player contributes nothing to any coalition they join, their Shapley value should be zero:

$$v(S \cup \{i\}) = v(S), \forall S \subseteq N \setminus \{i\} \implies \phi_i = 0$$

- **Additivity:** For two games  $(N, v_1)$  and  $(N, v_2)$ , the Shapley value of the combined game  $(N, v_1 + v_2)$  equals the sum of individual Shapley values:

$$\phi_i(v_1 + v_2) = \phi_i(v_1) + \phi_i(v_2)$$

The algorithm for approximating Shapley values is outlined in Appendix 6. However, the method is computationally expensive, as it requires evaluating the model for all possible coalitions of features.

The use of Shapley values in ML was not introduced until 2011, when Štrumbelj and Kononenko [59] proposed it as a method for explaining black box regression models.

However, it was popularised in 2017 by Lundberg and Lee [52], who introduced the SHAP framework. Although their proposal relies on the principles of Shapley values, their main contribution is to represent the Shapley value as an additive feature attribution method given as:

$$g(\mathbf{z}') = \phi_0 + \sum_{j=1}^M \phi_j z'_j \quad (2.31)$$

where  $g$  is the explanation model,  $\mathbf{z}' \in \{0, 1\}^M$  is the coalition vector,  $M$  is the maximum coalition size,  $\phi_0$  is the bias term, and  $\phi_j$  is the feature attribution for feature  $j$ .

### 2.3.3.1 KernelSHAP

The KernelSHAP algorithm builds on the SHAP framework by using a kernel-based approach to estimate Shapley values. It approximates the Shapley value by sampling different coalitions and using a weighted linear regression model to fit the contributions of each feature. The method relies on not all coalitions contributing equally to the final Shapley value and as such uses kernel weights to identify the most important coalitions. The main steps of the KernelSHAP algorithm are:

- sample a set of coalitions from the feature space:  $\mathbf{z}'_k \in \{0, 1\}^M, k \in \{1, \dots, K\}$ , where  $K$  is the total number of samples;
- for each coalition  $\mathbf{z}'_k$ , compute the model's prediction by first converting  $\mathbf{z}'_k$  to the original feature space and then applying the model  $\hat{f} : \hat{f}(h_{\mathbf{x}}(\mathbf{z}'_k))$ ;
- compute the weight for each coalition with the SHAP kernel:  $\pi_{\mathbf{x}}(\mathbf{z}')$ ;
- fit a weighted linear regression model to the sampled coalitions and their corresponding predictions; and
- return Shapley values  $\phi_k$  as the coefficients of the fitted model.

The sample coalitions are generated by randomly selecting subsets of the features, or equivalently, a vector of 0s and 1s indicating whether a feature is included in the coalition. The sampled coalitions represent the dataset for the regression model whose target is the prediction for a coalition. However, the sampled coalitions are not on the target feature space and, as such, it is necessary to implement another function  $h_{\mathbf{x}}(\mathbf{z}') = \mathbf{z}$  that maps the sampled coalitions to the original feature space. In the case of tabular data, this is done by replacing the features that are not included in the coalition with their mean value or a random sample from its possible values. As a result, sampling from the marginal distribution ignores the dependence structure between features.

Although there are similarities between KernelSHAP and LIME, their main difference lies in feature weighting in the regression model. The SHAP weighting assumes that small and large coalitions provide the most information about its isolated effects or its total effects, respectively; whereas coalitions with half the features add little information about a specific feature's contributions [52]. The proposed weighting function for KernelSHAP is:

$$\pi_{\mathbf{x}}(\mathbf{z}') = \frac{(M - 1)}{\binom{M}{|\mathbf{z}'|} |\mathbf{z}'| (M - |\mathbf{z}'|)}, \quad (2.32)$$

where  $M$  is the maximum coalition size and  $|\mathbf{z}'|$  is the number of features in the coalition  $\mathbf{z}'$ .

In addition, since the coalitions with the smallest and the largest number of features are the most informative, the sampling process is biased towards coalitions of size 1 and  $M - 1$ , resulting in  $2M$  possible coalitions. Then, the remaining budget  $K - 2M$  is used to sample coalitions of size 2 to  $M - 2$ . This process continues until the sampled coalitions reach the desired number of samples.

Consequently, given the samples, the KernelSHAP algorithm fits a weighted linear re-

gression model to estimate the Shapley values. The model is defined as:

$$g(\mathbf{z}') = \phi_0 + \sum_{j=1}^M \phi_j z'_j. \quad (2.33)$$

The goal is to minimise the following loss function:

$$\mathcal{L}(\hat{f}, g, \pi_{\mathbf{x}}) = \sum_{\mathbf{z}' \in \mathbf{Z}} \left[ \hat{f}(h_{\mathbf{x}}(\mathbf{z}')) - g(\mathbf{z}') \right]^2 \pi_{\mathbf{x}}(\mathbf{z}'), \quad (2.34)$$

where  $\mathbf{Z}$  is the dataset of sampled coalitions.

### 2.3.3.2 TreeSHAP

A variant of their original proposal is TreeSHAP [60], designed specifically for tree-based models. In this case, the method is model-specific and by leveraging the structure of the tree, it improves the computational efficiency by reducing computation time from exponential for KernelSHAP to polynomial.

The method works by exploiting the tree structure and the main steps of the algorithm are as follows.

- For each feature, traverse the tree and compute the contribution of the feature to the prediction at each node.
- For each node, compute the contribution of the feature to the prediction by considering the difference between the prediction at the node and the prediction at the parent node.
- For each feature, compute the Shapley value by averaging the contributions across all nodes in the tree.



## 2.4 State of the Art of Deep Learning and Explainability for Portfolio Optimisation

The emergence of Machine Learning (ML) and its rise in popularity have led to a new research direction in various financial applications, due to its ability to learn complex patterns from high-dimensional data and adapt to changing market conditions. Particularly, the main approaches in the financial field include the use of Deep Learning and Reinforcement Learning (RL) for price trend prediction [61] and portfolio optimisation [62].

The topic of portfolio optimisation with multiple risky financial assets has been extensively studied and it still poses a challenging task due to the complex and stochastic nature of financial markets. Traditional approaches to portfolio optimisation, such as Mean-Variance Optimisation (MVO) [29], have been widely used, but often rely on assumptions that do not hold in practice, such as the normality of returns and the stability of the covariance matrix. As a result, these methods can lead to suboptimal portfolios and poor performance in real-world scenarios.

The use of Deep Learning architectures is particularly prominent in the context of price prediction, where deep neural networks are employed to learn complex patterns in historical price data. For instance, Long Short-Term Memory (LSTM) architectures are particularly well-suited for financial time series forecasting due to their ability to capture long-term dependencies and temporal patterns in the data [63]. The performance of these architectures can lead to a Mean Absolute Percentage Error (MAPE) as low as 2.72%, as demonstrated by Chaudhary (2025) [64]. Shen et al. (2020) [7] also propose an LSTM architecture for short-term trend prediction with the main contribution being the feature engineering process. The proposal incorporates feature extension, followed by recursive feature elimination and, finally, performs Principal Component Analysis

(PCA) to reduce the dimensionality of the input data for the LSTM model. The use of PCA improves the training time of the architecture by 36.8% [7].

Ensemble methods are also prominent for price prediction, where techniques such as stacking, blending, boosting and bagging are employed to combine the predictions of multiple models. For example, Nti et al. (2020) [11] explore twenty-five different ensemble classifiers and regressors based on Decision Trees, Support Vector Machines and Neural Networks. Their research shows that although stacking and boosting ensemble algorithms provide better results in terms of accuracy, they are the most computationally expensive.

When it comes to portfolio optimisation, DRL algorithms are particularly better suited as they address the sequential decision making nature of portfolio management. Unlike traditional Supervised Learning approaches that require labelled data, DRL enables agents to learn optimal investment strategies through direct interaction with market environments. This paradigm allows for the dynamic adjustment of portfolio weights without the need for predefined rules, making it suitable to capture market non-linearities and adapt to changing conditions. There are numerous DRL algorithms, as outlined in Section 2.2.2, with each particularly befitting to different aspects of the portfolio management process.

Liu et al. (2018) [15] propose the use of DDPG for profitable stock trading, where the agent learns to buy, hold and sell stocks based on the historical price data with the goal of maximising the investment return. Their proposal outperforms the Dow Jones Industrial Average (DJIA) and the min-variance portfolio allocation strategies, achieving an annualised return of 25.86% and a Sharpe ratio of 1.79. Their work is further extended by proposing a Python library, FinRL, which provides a comprehensive framework for developing and evaluating DRL algorithms in the context of financial trading [65]. Although the library provides implementation for numerous DRL algorithms in-

cluding DQN, A2C and SAC, they only evaluate the performance of TD3 and DDPG on the Dow Jones Industrial Average (DJIA) constituents for the tasks of multiple stock trading and portfolio allocation. Notwithstanding, an interesting aspect of their work is the incorporation of the turbulence index, that measures extreme asset price fluctuations, to control portfolio risk. Beyond traditional assets, optimal portfolio allocation has also been explored in the context of cryptocurrencies [66] and future contracts [67].

Despite the significant applications of DRL in portfolio optimisation, the field still faces significant challenges that prevent its widespread adoption. When it comes to market conditions, identifying the correct objective function that guarantees both efficiency and accuracy remains an open research question. Finally, one of the most significant concerns is the lack of transparency of ML models. If there is to be general acceptance of these models in the financial field, great strides must be made in the area of explainability.

Barriedo et al. (2020) [19] provide a comprehensive overview of Explainable Artificial Intelligence (XAI) methods and their need in different fields. Given the regulatory requirements, it is crucial for financial institutions to adopt techniques that enhance the interpretability and traceability of ML models [68].

The application of XAI methods has gained traction in the financial domain, with notable use cases including stock market trend prediction [69] and auditing [70]. However, despite examples of XAI methods in finance, there is still a lack of research in DRL. An interesting study was conducted by González Cortés et al. (2024) [17], whose authors address the black box behaviour of DRL models by proposing an intrinsically transparent algorithm. They use Advantage Actor-Critic (A2C) <sup>1</sup> enhanced with an attention-layered LSTM to determine the importance of the input features. Although their results show an improvement in performance compared against two variants of the Markowitz model, their implementation does not scale well with the number of assets in

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<sup>1</sup>In the paper [17], they refer to A2C as Synchronous Advantage Actor Critic (SAAC)

the portfolio, as the attention mechanism is independent for each stock.

Another recent study by de-la-Rica-Escudero et al. (2025) [71] proposes post-hoc explainability methods to interpret the decisions of PPO agent optimised for portfolio management. They implement three model-agnostic explainability techniques: SHAP, LIME and feature importance analysis. Despite their proposal’s ability to provide insights into the model’s decision-making process, they do not use the model prediction function directly but instead implement a surrogate model to approximate the decision boundary of the PPO agent, effectively adding an additional layer to the model.

Given the lack of research in the area of explainability for DRL models that perform automated portfolio allocation and the current limitations of existing methods, this thesis proposes to provide a comprehensive study of DRL techniques tailored for portfolio optimisation in financial markets, by exploring the potential of five prominent algorithms (A2C, PPO, DDPG, TD3 and SAC) across various market conditions and asset classes. Moreover, due to the complex and hidden nature of those algorithms, their decision-making process will be explained using XAI methods. The objective is to bridge the gap between the performance of DRL and algorithmic transparency.

## Chapter 3

# Methodology

This chapter covers the methodology and framework established to provide an explainable Deep Reinforcement Learning (DRL) model capable of optimising a portfolio of financial assets. The chapter is structured as follows: first, it describes the architecture and components of the proposed DRL model, including the state representation, reward function and training process and second, it outlines the implementation of the explainability techniques used to interpret the model's decisions.

### 3.1 Problem Definition

The problem of portfolio optimisation is the task of finding an optimal allocation of financial assets in a portfolio to maximise expected returns while minimising risk. Thus, it is necessary to decide how to rebalance the portfolio at each time step in a highly stochastic and complex financial market. This can be formulated using a Markov Decision Process (MDP) framework, where the agent interacts with the environment by deciding the optimal allocation based on the state of the environment at each time step to maximise the expected cumulative reward over time. Deep Reinforcement Learning

(DRL) gives the agent the ability to learn the optimal policy directly from the environment by taking actions and receiving rewards.

## 3.2 Markov Decision Process Model

Due to the dynamic, stochastic and interactive nature of financial markets, a Markov Decision Process is a suitable framework to model the problem. The main elements of the MDP model are defined as follows:

- state space  $\mathcal{S}$ ,
- action space  $\mathcal{A}$ ,
- reward function  $R : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow \mathbb{R}$ ,
- transition function  $T : \mathcal{S} \times \mathcal{A} \rightarrow \mathcal{S}$ , and
- discount factor  $\gamma \in [0, 1)$ .

The state space  $\mathcal{S}$  is a vector representation of the financial environment. For a portfolio of  $D$  assets, the features that describe the state include asset prices, technical indicators and macroeconomic indicators.

- Close price  $\mathbf{p}_t \in \mathbb{R}^D$ : Adjusted close prices of the assets at time  $t$ .
- Open price  $\mathbf{o}_t \in \mathbb{R}^D$ : Opening prices of the assets at time  $t$ .
- High price  $\mathbf{h}_t \in \mathbb{R}^D$ : Highest prices of the assets at time  $t$ .
- Low price  $\mathbf{l}_t \in \mathbb{R}^D$ : Lowest prices of the assets at time  $t$ .
- Volume  $\mathbf{v}_t \in \mathbb{R}^D$ : Trading volume of the assets at time  $t$ .

- Technical indicators  $\mathbf{I}_t \in \mathbb{R}^{D \times I}$ : For each of the  $D$  assets, a vector  $\mathbf{i}_t$  of  $I$  technical indicators, such as moving averages, relative strength index (RSI), and Bollinger Bands, calculated from the asset prices.
- Macroeconomic indicators  $\mathbf{M}_t \in \mathbb{R}^{D \times M}$ : For each of the  $D$  assets, a vector  $\mathbf{m}_t$  of  $M$  macroeconomic indicators, such as volatility index and interest rates, which provide additional context about the financial environment.
- Covariance matrix  $\mathbf{C}_t \in \mathbb{R}^{D \times D}$ : For each of the  $D$  assets, a vector of  $D$  values representing the covariance between the assets in the portfolio at time  $t$ .

The description of technical and macroeconomic indicators is provided in more detail in Appendix B.

The action space  $\mathcal{A}$  is the set of possible actions that the agent can take at each time step. For the portfolio optimisation problem, the actions correspond to portfolio weights and are defined as follows:

$$\mathbf{a}_t = \mathbf{w}_t : w_{t,d} \in [0, 1] \quad \forall d \in \{1, \dots, D\}, \quad (3.1)$$

where  $\mathbf{w}_t$  is a vector of portfolio weights at time  $t$ , representing the allocation of the portfolio to each asset. The weights are constrained to be non-negative and sum to one:

$$\sum_{d=1}^D w_{t,d} = 1, \quad w_{t,d} \geq 0 \quad \forall d \in \{1, \dots, D\}. \quad (3.2)$$

Moreover, they are initialised to be equal for all assets, meaning that the agent starts with an equal allocation to each asset in the portfolio. The reason behind this is to avoid an initial bias and allow the agent to learn an allocation from the environment rather than favour any particular asset.

The transition function  $T$  describes how the state of the environment changes in response

to the action taken. It is defined as:

$$s_{t+1} = T(s_t, a_t), \quad (3.3)$$

where  $s_{t+1}$  is the new state of the environment after taking action  $a_t$  in state  $s_t$ . The transition function is determined by the dynamics of the financial market, which are influenced by the asset prices, trading volume and other factors. The trading dynamics assume that the agent does not have an impact on the market.

The reward function  $R$  models the direct reward of taking an action  $a_t$  in state  $s_t$  and transitioning to a new state  $s_{t+1}$ . It is defined as the change in the portfolio value from time  $t$  to time  $t + 1$ :

$$R_{t+1} = R(s_t, a_t, s_{t+1}) = V_{t+1} - V_t, \quad (3.4)$$

where the value of the portfolio at time  $t$  is given by the dot product of the portfolio weights and the asset close prices:

$$V_t = \mathbf{w}_t \cdot \mathbf{p}_t. \quad (3.5)$$

The goal of the agent is to learn a policy  $\pi : \mathcal{S} \rightarrow \mathcal{A}$  that maximises the expected cumulative reward over time, which can be expressed as:

$$J(\pi) = \mathbb{E} \left[ \sum_{t=0}^T \gamma^t R(s_t, a_t, s_{t+1}) \right], \quad (3.6)$$

where  $T$  is the time horizon and  $\gamma$  is the discount factor that determines the importance of future rewards.

The environment is implemented in Python <sup>1</sup> using the `Gym` library [72], which provides a standard interface for reinforcement learning environments.

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<sup>1</sup><https://www.python.org/>



### 3.3 Deep Reinforcement Learning Algorithms

The proposed solution is based on the DRL framework, which allows the agent to learn the optimal policy directly from the environment by taking actions and receiving rewards. The algorithms used are Advantage Actor-Critic (A2C), Proximal Policy Optimisation (PPO), Deep Q-Network (DQN), Deep Deterministic Policy Gradient (DDPG), Twin Delayed Deep Deterministic Policy Gradient (TD3) and Soft Actor-Critic (SAC).

The implementation is done using the **Stable Baselines3** library [73], which provides a set of state-of-the-art DRL algorithms with a consistent interface and easy-to-use API. The pseudo-code for each algorithm is provided in Appendix A.1.

#### 3.3.1 Hyper-parameter tuning

Hyper-parameter tuning [74] is a crucial step in the training process of DRL models, as the right choice of hyper-parameters can significantly impact the model’s performance. In this thesis, hyper-parameter tuning refers to the process of optimising the training parameters of the DRL algorithms to maximise their performance in the task of portfolio optimisation. The hyper-parameters tuned include the learning rate, batch size, number of training steps, and other algorithm-specific parameters, which are summarised in Appendix C.

To implement hyper-parameter tuning in Python, the **wandb** [75] library is used, which provides a simple and efficient way to track experiments, visualise results, and manage hyper-parameter sweeps. A sweep is defined as a search for hyper-parameters that optimises a cost function, in our case, the Sharpe ratio [76]. Given that the models were implemented using the **Stable Baselines3** library, the integration with **wandb** allows for seamless tracking of hyper-parameter configurations and their corresponding performance metrics [77].

As mentioned above, sweeps can optimise a cost function to avoid naively testing every possible combination. Using `wandb`, a Bayesian optimisation approach is taken [78], which uses a probabilistic model to estimate the performance of different hyper-parameter configurations and selects the next configuration to test based on the expected improvement over the current best configuration. This allows for a more efficient search of the hyper-parameter space and reduces the number of configurations that need to be tested. Another option to reduce the time taken to find the optimal hyper-parameters is to use early termination. This method will stop a poorly performing run before it has fully completed, saving computational resources [79].

### 3.4 Post-hoc Explainability

Given the goal of improving the explainability of the DRL models, this thesis adopts explainability techniques to interpret the model’s decision-making process in a transparent manner. By using post-hoc methods, rather than modifying each individual model’s architecture to enhance their transparency, the proposal is model-agnostic and can be applied to any DRL model. Consequently, it combines the ability to find the most suitable architecture while maintaining the interpretability. The explainability techniques implemented are Feature Importance, Local Interpretable Model-agnostic Explanations (LIME), and SHapley Additive exPlanations (SHAP).

Following the work from de-la-Rica-Escudero et al. (2025) [71], the implementation of these techniques follows two directions. First, as in their paper, a surrogate model maps the state space to the action space as a proxy for the model’s decisions. The second direction uses the LIME and SHAP techniques directly on the DRL model to interpret its decisions.

### 3.4.1 Surrogate Model Explainability

The surrogate model is trained to approximate the behaviour of the DRL model by learning the mapping from its inputs, the environment representation, to its outputs, the portfolio weights. In the paper [71], the authors do not explicitly acknowledge the use of a surrogate model, even though their code implementation does so. A potential reason behind not explaining the model’s actions directly could be the code complexity in using SHAP with a DL model.

Given that the action space is continuous, the surrogate model is implemented using a `RandomForestRegressor` [80], which is a non-parametric model that can capture complex relationships between the inputs and outputs. The model is trained on the state-actions pairs of the test data, which is the object of the explanations. However, since the model has a number of hyper-parameters, it requires careful tuning to achieve optimal performance. Consequently, hyperparameter tuning was used to find the optimal architecture using `HalvingGridSearchCV` [81], which is a method that iteratively narrows down the search space by evaluating a subset of hyper-parameters and discarding the less promising ones. The use of grid search rather than Bayesian Optimisation, as was done for DRL hyper-parameter tuning in Section 3.3.1, is to replicate the approach taken in [71]. Once the optimal hyper-parameters have been found and the surrogate model has been trained, its prediction function is used as a proxy to interpret the original model’s decisions.

Feature importance is built-in for Random Forest Regressors, and can be easily accessed with the built-in property `feature_importances_` [82]. This method provides the importance of each feature in the state representation by using a combination of the fraction of the samples a feature contributes to and the mean decrease in impurity.

LIME and SHAP are then applied to the surrogate model via the predict function to

provide local explanations for individual predictions. Both of these techniques provide insights into the model’s decisions by perturbing the input data and observing the changes in the output. The LIME implementation is done using the `LimeTabularExplainer` [83], which is designed to work with tabular data and provides a way to explain individual predictions by approximating the model’s behaviour locally with a linear model. Similarly, for SHAP, the `TreeExplainer` [84] provides a particular implementation for tree-based models used to compute the SHAP values efficiently by exploiting the model’s inherent structure.

### 3.4.2 Direct Model Explainability

Undoubtedly, a surrogate model adds an additional layer of complexity and may obscure the understanding of the original model’s decisions. Therefore, the LIME and SHAP techniques are also applied directly to the prediction function of DRL model. This approach allows for a more direct interpretation of the model’s decision-making process, without the need of a supplementary level.

For LIME, the implementation is again done using `LimeTabularExplainer`, but the prediction function is now obtained from the relevant DRL algorithm. For SHAP, the `KernelExplainer` is used, which is a model-agnostic method that randomly samples feature coalitions to approximate SHAP values to reduce computation [85].

## Chapter 4

# Results

This chapter presents the results of conducting experiments under the methodology proposed in Chapter 3. The experiments were designed to evaluate the performance of the implemented DRL models for portfolio optimisation in changing environment representations and market conditions. Moreover, to enable the interpretability of the model’s decisions, a framework using post-hoc explainability techniques is explored.

### 4.1 Dataset

Given the general difficulty in finding the appropriate DRL algorithm with a suitable reward function for portfolio optimisation, the five implemented algorithms were tested on five different datasets. Each dataset consists of a different set of financial assets, ranging from three different asset classes. First, three datasets were constructed using the stock constituents of three renowned indexes:

- Dow Jones Industrial Average (DJIA) with 30 stocks,
- Euro Stoxx 50 Index (Euro Stoxx 50) with 50 stocks, and

- Financial Times Stock Exchange 100 Index (FTSE 100) with 100 stocks.

The constituents of each of the indexes were retrieved in April 2025 and can be found in Appendix D.1. It is important to note that the datasets were chosen to illustrate different currencies, as this introduces another factor of changing market conditions.

Additionally, two datasets were constructed using commodities and currencies, respectively. The commodities dataset includes six different commodities, which are listed in Appendix D.2. These are a sample of the most traded commodities in the market and were chosen by their availability in the `Yahoo! Finance API`<sup>1</sup>. With regard to the currencies dataset, it includes ten different currency pairs, listed in Appendix D.3. These were selected based on their trading volume and liquidity, with all pairs quoted in United States Dollar (USD).

The datasets are constructed using daily data from January 2016 to July 2025 downloaded using the Python `yfinance` library [86]. The dataset is partitioned into two disjoint sets: training and testing, with the training set containing data from January 2016 to December 2023, and the testing set starting on January 2024 until July 2025. For hyper-parameter tuning, the training set is further split into a training and validation set, with the validation sets corresponding to the period between January 2023 and December 2023.

## 4.2 Experiment Design

To address the challenge of finding a suitable algorithm for portfolio optimisation, the five implemented DRL algorithms were tested on the five datasets described in Section 4.1, with the goal of evaluating the performance of each algorithm in different scenarios and market conditions. Moreover, the environment representation will also be varied to

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<sup>1</sup><https://uk.finance.yahoo.com>

assess the impact of more information on the model’s performance. Four environment representations were considered, each with a different number of features.

- Simple dataset: Open, High, Low, Close, Volume (OHLCV) of the assets.
- Covariance dataset: To the simple dataset, the covariance matrix of the assets is added to explicitly model the relationships between the assets.
- Indicators dataset: Technical and macroeconomic indicators are added to the simple dataset.
- Complete dataset: The complete dataset includes the OHLCV, the covariance matrix and the technical and macroeconomic indicators.

The strength of DRL algorithms lies in their ability to learn from high-dimensional data, which is why the goal is to evaluate whether a more exhaustive environment representation leads to better performance, despite the higher computational cost.

Finally, the performance of the algorithms is closely related to the choice of hyper-parameters. Ideally, the hyper-parameters should be tuned to find the optimal configuration for each algorithm and dataset combination. However, it was not feasible to perform tuning for all combinations of algorithms, datasets and environment representations. Consequently, the default hyper-parameters for all the experiments were chosen based on a testing run that was done on a small dataset of five tickers with indicators as environment representation. Those results can be seen in Appendix E and the default hyper-parameters are summarised in Table C.2.

Overall, the experiments were designed to evaluate the performance of the implemented DRL algorithms in different scenarios, with the goal of finding the most suitable algorithm for portfolio optimisation. However, testing five algorithms on five distinct datasets with four possible environment representations would result in a total of twenty

different experiments per algorithm. Additionally, optimising the parameters for each experiment further expands the experimental space and significantly increases the computational time required.

Due to limited computational resources<sup>2</sup>, the scope of experiments was adjusted as follows. Firstly, hyper-parameter tuning was performed only for the Dow Jones 30 dataset with simple and indicators environment representation, as it is the smallest equities dataset and requires less computational time. Second, since the covariance matrix increases the dimensionality of the environment representation, it was only included in the experiments with the Dow Jones 30, the currencies and the commodities datasets.

## 4.3 Evaluation

As outlined in the previous section, the experiments are designed to evaluate the performance of the implemented DRL algorithms in different scenarios and market conditions. The evaluation will focus on key performance metrics, as well as benchmarking against traditional portfolio optimisation techniques.

### 4.3.1 Performance Metrics

The performance metrics are provided through the `pyfolio` library [87], which includes a `perf_stats` method to calculate various performance metrics of a strategy.

The main metrics for comparison are:

- The cumulative return is the total change in investment price over a period of time, representing the overall percentage gain or loss from the initial investment value.

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<sup>2</sup>The university did not provide access to a computing cluster; therefore, all experiments were conducted on a personal computer.



The formula is given by:

$$\text{Cumulative return} = \frac{\text{Final portfolio value} - \text{Initial portfolio value}}{\text{Initial portfolio value}}. \quad (4.1)$$

- The annualised return is the geometric average of the amount of money earned by an investment each year over a given period of time, providing a standardised measure of annual performance. It is calculated as follows:

$$\text{Annualised Return} = \left( \frac{\text{Final portfolio value}}{\text{Initial portfolio value}} \right)^{\frac{1}{\text{Number of years}}} - 1. \quad (4.2)$$

- The annualised volatility is the standard deviation of returns annualised to provide a measure of investment risk on a yearly basis and can be computed with the following formula:

$$\text{Annualised Volatility} = \text{Standard Deviation of Returns} \times \sqrt{\text{Yearly trading days}}, \quad (4.3)$$

where the number of trading days per year is typically assumed to be 252.

- The Sharpe ratio is a measure of risk-adjusted performance that compares the excess return of an investment to a risk-free asset against its volatility. The ratio is given by:

$$\text{Sharpe Ratio} = \frac{R_p - R_f}{\sigma_p}, \quad (4.4)$$

where  $R_p$  is the annualised return of the portfolio,  $R_f$  is the annualised risk-free rate, and  $\sigma_p$  is the annualised volatility of the portfolio.

- The max drawdown is the maximum percentage loss from a peak to a trough during a specified period, indicating the worst-case scenario for portfolio decline.

Its formula is:

$$\text{Max Drawdown} = \frac{\text{Peak Value} - \text{Trough Value}}{\text{Peak Value}}. \quad (4.5)$$

### 4.3.2 Benchmark Strategies

Aside from computing relevant performance metrics, the algorithms will be benchmarked against traditional portfolio optimisation methods. These are designed to provide a baseline for comparison and to evaluate the performance of the DRL algorithms in relation to established methods. The following benchmark strategies were considered.

- Equal-weighted portfolio: A simple strategy that allocates an equal weight to each asset in the portfolio.
- Mean-variance optimisation: A classic portfolio optimisation method that aims to maximise Sharpe ratio.
- Min-variance portfolio: Another classic portfolio optimisation method that seeks to minimise the portfolio's volatility.
- Momentum portfolio: A strategy that invests in assets with positive momentum, i.e. those that have performed well in the previous time step, and avoids those with negative momentum.

The implementation of the mean-variance and the min-variance portfolio allocation strategies has been done using the `PyPortfolioOpt` Python library [88], whereas the equal-weighted and momentum strategies have been implemented using custom code.

Finally, if the portfolio is made up of equities of a relevant index, the benchmark will also include the index itself, which serves as a reference point for the performance of the portfolio.

## 4.4 Deep Reinforcement Learning Algorithm Experiments

### 4.4.1 Algorithm Comparison

In this section, the results of the experiment to identify the suitability of the implemented DRL algorithms for portfolio optimisation under different market conditions are presented. The algorithms are trained on data with a simple environment representation, which only includes the OHLCV prices of the assets, and evaluated on the five datasets. The table 4.1 summarises the results of the experiment for the A2C algorithm, where each row corresponds to a different dataset and each column to a different performance metric. The results for the other algorithms are presented in Appendix F.1.

Table 4.1: Algorithm comparison results for the A2C implementation.

| <b>Dataset</b>       | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|----------------------|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>Dow Jones 30</b>  | 0.2165                       | 0.3387                       | 0.1579                           | 1.3203                  | -0.1649                 |
| <b>Euro Stoxx 50</b> | 0.1467                       | 0.2293                       | 0.1549                           | 0.9617                  | -0.1667                 |
| <b>FTSE 100</b>      | 0.1052                       | 0.1623                       | 0.1268                           | 0.8520                  | -0.1409                 |
| <b>Commodities</b>   | 0.2353                       | 0.3694                       | 0.2041                           | 1.1372                  | -0.1512                 |
| <b>Currencies</b>    | -0.0011                      | -0.0017                      | 0.0462                           | -0.0018                 | -0.0665                 |

For the case of A2C, the algorithm demonstrates competitive performance particularly for the DowJones30 dataset, achieving a cumulative return of 21.65% and a Sharpe ratio of 1.32. Positive results are also obtained with the commodities dataset, which demonstrates the highest cumulative return of 23.53% and a Sharpe ratio of 1.14. Despite being of the same asset class, the EuroStoxx50 and the FTSE100 datasets show relatively lower performance, with cumulative returns of 14.67% and 10.52%, respectively, most likely due to the higher number of assets. With regard to the currencies dataset, the

performance of the algorithm is less impressive, with near-zero cumulative returns and Sharpe ratios, indicating that the algorithm struggles to learn a profitable strategy in this asset class.

Although similar observations can be made for the other algorithms, the performance varies significantly across different datasets, as outlined in Appendix F.1. Regarding PPO, better performance is achieved in the commodities dataset, with a cumulative return of 25.31% and a Sharpe ratio of 1.26. which is slightly more than 0.1 higher than that of the A2C algorithm. DDPG performs the best in the DowJones30 dataset, achieving similar performance to that of A2C, with a 22.06% cumulative return and a Sharpe ratio of 1.38. However, TD3 surpasses all other algorithms for the DowJones30 dataset and the Commodities datasets, achieving 24.78% and 27.68% in cumulative return, respectively. Finally, SAC demonstrates a strong performance in the EuroStoxx50 dataset, with a cumulative return of 17.61% and a Sharpe ratio of 1.14, but it does not outperform the other algorithms in the DowJones30 and Commodities datasets. The algorithm that performs better in the FTSE100 dataset is DDPG, with a cumulative return of 13.36% and a Sharpe ratio of 1.08.

Taking the DowJones30 dataset with an environment representation made up of the OHLCV prices and the indicators, the performance of the algorithms can be benchmarked against traditional strategies and the DJIA Index. The evolution of the cumulative returns over the testing period is shown in Figure 4.1 and the corresponding performance metrics are summarised in Table 4.2.

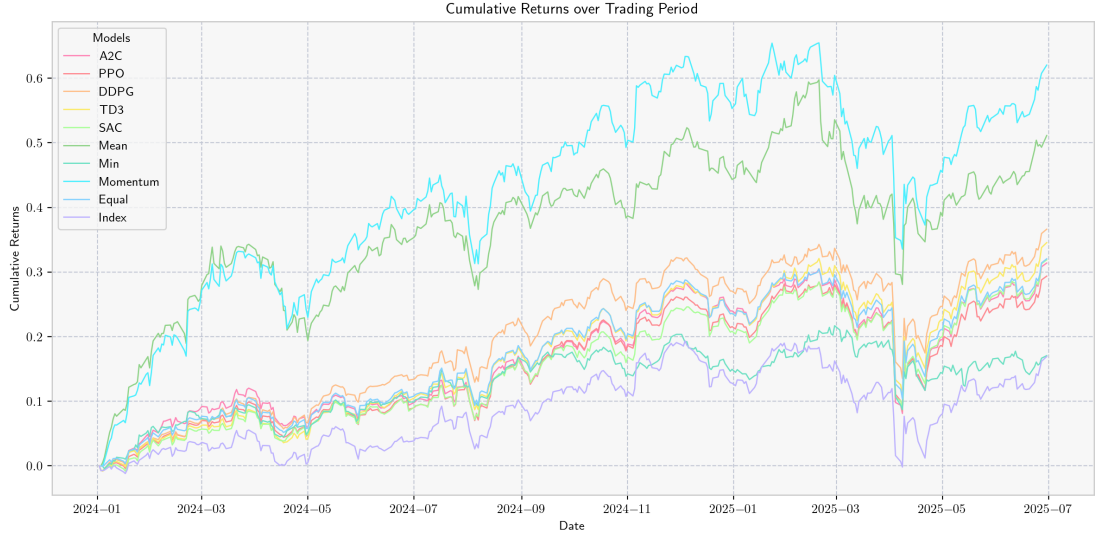


Figure 4.1: Evolution of the Cumulative Returns for the DowJones30 dataset with the OHLCV prices and indicators environment representation.

Table 4.2: Algorithm comparison results for the DowJones30 dataset. The colours correspond to the best performing configurations, with blue for the best performing DRL algorithm and green for the best benchmark.

| Algorithm<br>/<br>Bench-<br>mark | Cumulative<br>return | Annualised<br>return | Annualised<br>volatility | Sharpe<br>ratio | Max<br>drawdown |
|----------------------------------|----------------------|----------------------|--------------------------|-----------------|-----------------|
| <b>A2C</b>                       | 0.2020               | 0.3139               | 0.1559                   | 1.2575          | -0.1716         |
| <b>PPO</b>                       | 0.1895               | 0.2937               | 0.1487                   | 1.2407          | -0.1556         |
| <b>DDPG</b>                      | 0.2341               | 0.3663               | 0.1486                   | 1.4896          | -0.1546         |
| <b>TD3</b>                       | 0.2214               | 0.3456               | 0.1517                   | 1.3938          | -0.1609         |
| <b>SAC</b>                       | 0.2050               | 0.3189               | 0.1480                   | 1.3340          | -0.1538         |
| <b>Mean</b>                      | 0.3218               | 0.5114               | 0.1839                   | 1.6096          | -0.1983         |
| <b>Min</b>                       | 0.1123               | 0.1705               | 0.1157                   | 0.9777          | -0.1066         |
| <b>Momentum</b>                  | 0.3855               | 0.6204               | 0.1990                   | 1.7388          | -0.1929         |

| <b>Algorithm<br/>/<br/>Bench-<br/>mark</b> | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|--|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>Equal</b>                               | 0.2066                       | 0.3205                       | 0.1476                           | 1.3461                  | -0.1541                 |
| <b>Index</b>                               | 0.1110                       | 0.1692                       | 0.1532                           | 0.7635                  | -0.1637                 |

The results show that all the algorithms outperform the index for all the considered metrics, as well as the min-variance portfolio. Out of all the DRL algorithms, DDPG achieves the highest cumulative return of 23.41% and a Sharpe ratio of 1.49, followed by TD3 with a cumulative return of 22.14% and a Sharpe ratio of 1.39, while PPO has the worst performance of the five with a cumulative return of 18.95% and a Sharpe ratio of 1.24. However, none of these outperform the mean-variance and momentum benchmark strategies, with the latter achieving a Sharpe ratio of 1.74 and a cumulative return of 38.55%, which is significantly higher than the performance of the DRL algorithms.

#### 4.4.2 Environment Representation

Another source of variability in the performance of the algorithms is the environment representation. In this section, the results of comparing the DRL algorithms on different environment representations are presented. For the experiment to be meaningful, it has been performed on the DowJones30 dataset, the currencies and the commodities datasets. This choice provides the ability to compare the performance of the algorithms across different asset classes, while also allowing for a more manageable computational cost. The table 4.3 compares the performance according to the Sharpe ratio and, in Appendix F.2, according to the cumulative return.

Table 4.3: Environment representation experiment comparison according to the Sharpe ratio. The colours correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset.

| Algorithm   | Dataset     | Simple  | Indicators | Covariance | Complete |
|-------------|-------------|---------|------------|------------|----------|
| <b>A2C</b>  | DowJones30  | 1.3203  | 1.2575     | 1.3615     | 1.3929   |
|             | Commodities | 1.1373  | 1.2881     | 1.0273     | 1.2079   |
|             | Currencies  | -0.0018 | -0.0571    | -0.0674    | -0.0053  |
| <b>PPO</b>  | DowJones30  | 1.3410  | 1.2407     | 1.3524     | 1.1890   |
|             | Commodities | 1.2600  | 1.1256     | 1.1559     | 1.2015   |
|             | Currencies  | 0.0014  | 0.0699     | 0.0652     | 0.1399   |
| <b>DDPG</b> | DowJones30  | 1.3826  | 1.4896     | 1.3562     | 1.3261   |
|             | Commodities | 1.1745  | 0.9871     | 1.0731     | 1.1612   |
|             | Currencies  | 0.0528  | 0.0689     | 0.0200     | 0.0115   |
| <b>TD3</b>  | DowJones30  | 1.4911  | 1.3938     | 1.1792     | 1.2084   |
|             | Commodities | 1.4537  | 0.9776     | 1.0462     | 1.2388   |
|             | Currencies  | 0.0807  | -0.0088    | -0.0086    | -0.0436  |
| <b>SAC</b>  | DowJones30  | 0.9769  | 1.3340     | 1.4670     | 1.3017   |
|             | Commodities | 1.3727  | 1.1973     | 1.1773     | 1.0500   |
|             | Currencies  | 0.0806  | 0.1771     | -0.1441    | 0.2550   |

The results show that the performance of the algorithms varies significantly across different environment representations. For the DowJones30 dataset, the OHLCV prices representation achieves the highest Sharpe ratio of 1.49 for TD3, closely followed by the OHLCV prices with indicators. The OHLCV prices with covariance representation achieves 1.47 for SAC. For the complete feature set, only the A2C algorithm achieves a higher Sharpe ratio of 1.39 than the other algorithms.

For the commodities dataset, the results are completely different to those of the DowJones30. The only coincidence is that TD3 achieves the highest Sharpe ratio and highest cumulative return in the simple feature set. Moreover, when looking at this dataset, explicitly adding the covariance to the environment representation does not lead to better performance in terms of Sharpe ratio.

Finally, for the currencies dataset, the performance of the algorithms is significantly lower, going negative in some cases. A possible reason is the particular set of hyper-parameters used.

#### 4.4.3 Hyper-parameter Tuning

As has been mentioned in the above experiments, the performance of the algorithms is substantially influenced by the choice of hyper-parameters. Ideally, a systematic approach should be employed to find the optimal hyper-parameters for each algorithm, dataset and environment representation combination. However, due to the computational cost of hyper-parameter tuning, it was only performed for the DowJones30 dataset with the OHLCV and indicators environment representations over five trials. The results for each of the algorithms with the default hyper-parameters versus the tuned hyper-parameters are compared in Table 4.4 and Table 4.5 for the two features sets: simple and with indicators, respectively.

Table 4.4: Hyper-parameter tuning experiment results for the DowJones30 dataset with simple environment representation.

| Algorithm  | Metric            | Default parameters | Tuned parameters |
|------------|-------------------|--------------------|------------------|
| <b>A2C</b> | Cumulative Return | 0.3387             | 0.3491           |
|            | Sharpe ratio      | 1.3203             | 1.4307           |
| <b>PPO</b> | Cumulative Return | 0.3174             | 0.2844           |



| Algorithm | Metric            | Default parameters | Tuned parameters |
|-----------|-------------------|--------------------|------------------|
|           | Sharpe ratio      | 1.3410             | 1.1939           |
| DDPG      | Cumulative Return | 0.3454             | 0.27404          |
|           | Sharpe ratio      | 1.3826             | 1.2088           |
| TD3       | Cumulative Return | 0.3902             | 0.2974           |
|           | Sharpe ratio      | 1.4911             | 1.2354           |
| SAC       | Cumulative Return | 0.2243             | 0.3703           |
|           | Sharpe ratio      | 0.9769             | 1.4521           |

Table 4.5: Hyper-parameter tuning experiment results for the DowJones30 dataset with indicators environment representation.

| Algorithm | Metric            | Default parameters | Tuned parameters |
|-----------|-------------------|--------------------|------------------|
| A2C       | Cumulative Return | 0.3139             | 0.3573           |
|           | Sharpe ratio      | 1.2575             | 1.3994           |
| PPO       | Cumulative Return | 0.2937             | 0.3134           |
|           | Sharpe ratio      | 1.2407             | 1.3679           |
| DDPG      | Cumulative Return | 0.3663             | 0.4086           |
|           | Sharpe ratio      | 1.4896             | 1.5597           |
| TD3       | Cumulative Return | 0.3456             | 0.2891           |
|           | Sharpe ratio      | 1.3938             | 1.2332           |
| SAC       | Cumulative Return | 0.3189             | 0.2646           |
|           | Sharpe ratio      | 1.3340             | 1.1688           |

By looking at the data presented in these tables, it is clear that finding the optimal

configuration can have a significant impact on the performance of the algorithms. For instance, although the cumulative return for A2C in the simple feature set only improves by 1%, the Sharpe ratio increases from 1.32 to 1.43, meaning that the algorithm learns to better balance risk while maximising returns. Another example is the SAC algorithm, which achieves a better performance than that of the default configuration. However, for the PPO, DDPG and TD3 algorithms, there are no improvements and the default hyper-parameters perform better. Similarly, when looking at the indicators feature set, not all the algorithms show sign of improvements. These means that, for that particular algorithm, dataset and environment representation combination, the optimal hyper-parameter configuration has not been found. Understandably, due to the limited computational resources, the hyper-parameter search was very limited to only five runs, which is not sufficient for a thorough search.

## 4.5 Explainability Results

A main objective of this thesis is to be able to interpret the decisions made by the DRL algorithms. The following explainability framework is designed to provide insights into the decision-making process of the algorithms and present the most relevant features that influence the portfolio allocation decision in a visual and human-readable manner. As described in Section 3.4, two approaches were employed: a surrogate model and direct explanations.

For the purposes of visualisation, the results are shown for a sample dataset of five tickers (AAPL, CSCO, HON, MSFT, V) from the DJIA and using only the open, close, high, and low prices as the environment representation. This choice is made because explanations are more easily visualised when the number of assets and features is small. However, the explainability framework itself is general and can be applied to any number of assets and any environment representation. In practice, to support larger portfolios

and more complex feature sets, an interactive dashboard could be developed, allowing users to select the relevant assets in the portfolio for which explanations are required. Moreover, only the explanations of the A2C algorithm are presented, as it serves as a representative example of the framework’s capabilities.

The surrogate model was implemented following the proposal by de-la-Rica-Escudero et al. (2025) [71]. Although their paper does not explicitly acknowledge the use of a surrogate model nor outline the reasons for its use, it can be inferred that using a simpler transparent algorithm as a proxy provides built-in feature importance, which is a global explainability method. However, there does not seem to be any added value when using LIME and SHAP as they are both model-agnostic methods capable of providing explanations for any black-box model.

#### 4.5.1 Feature Importance Results

The feature importance results from the surrogate model are shown in Figure 4.2, where the top 20 features are ranked according to the importance measure. The ranking shows that the low price of CSCO and the close price of MSFT are the two most important features, followed by the open price of CSCO. At the bottom section of the ranking, HON and AAPL features have a lower importance.

This trend is further confirmed by looking at the mean importance of the features for each asset, as shown in Figure 4.3. This indicates that the agent heavily relied on the performance of MSFT and CSCO to guide its portfolio allocation decisions, while the other assets played a less significant role.

Another interesting result about the feature importance shown in Figure 4.2 is that the different assets have a different OHLCV feature importance distribution, which suggests that the agent may have developed distinct strategies for each asset. Figure G.1 in Appendix G.1 shows the top features grouped by asset, where it can be seen more

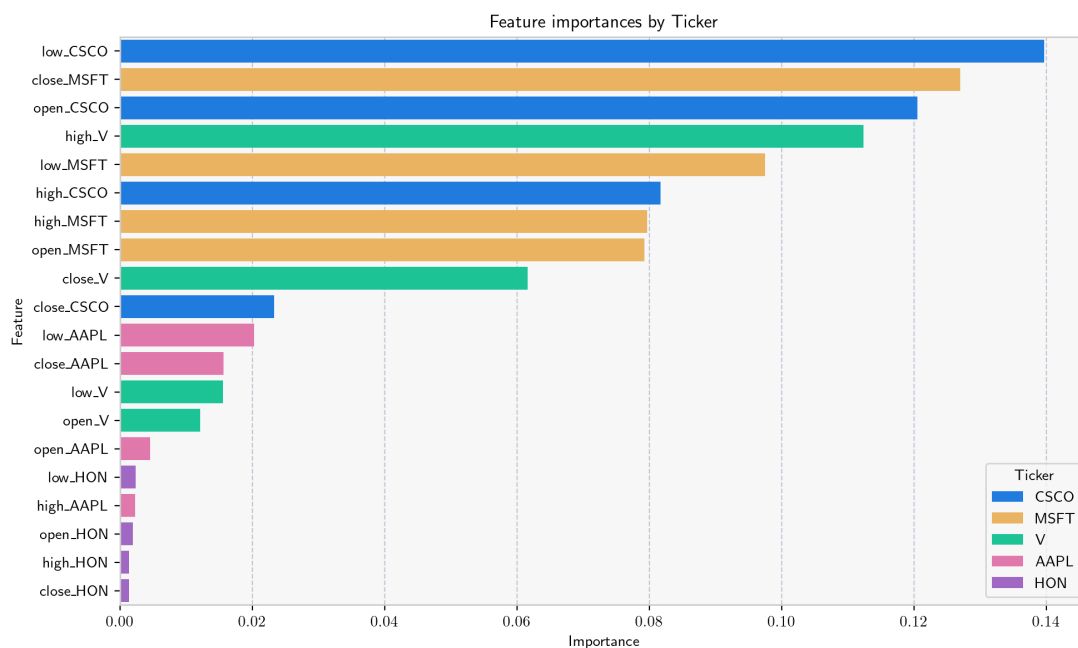


Figure 4.2: Top features from the surrogate model according to feature importance.

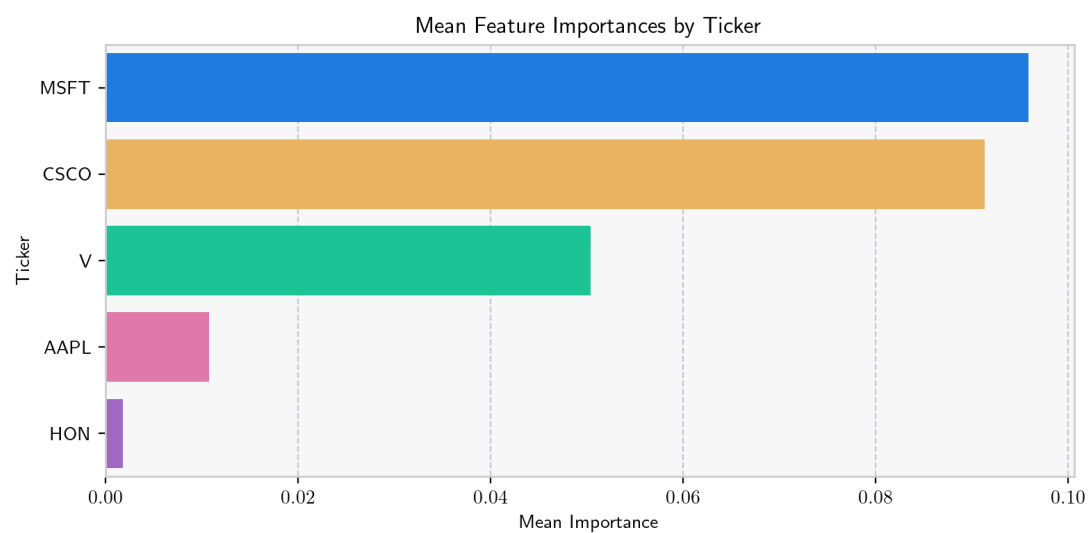


Figure 4.3: Mean feature importance per asset from the surrogate model.

clearly how each asset has a different most important feature. In the case of AAPL, HON and CSCO, the low price played a more critical role in informing the agent’s decisions, showing how extreme price changes lead the agent to adjust the portfolio allocation. In contrast, for MSFT, the close price is the most important feature, which might imply the agent is more focused on the end of day activities of this asset. Finally, looking over all the assets, Figure G.2 in Appendix G.1 shows how features corresponding to low and high prices contributed the most to the agent’s decisions. This again indicates that the agent is sensitive to price extremes of the assets.

### 4.5.2 Local Interpretable Model-agnostic Explanations Results

Moving on to the local explanations of LIME, the direct explanations for the A2C algorithm are provided. The benefit of LIME is its ability to provide explanations at a particular point in time. In this case, the local explanations are provided for an instance of the test dataset, i.e. a specific trading day. In this section, Figure 4.4 illustrates the local explanations for the MSFT asset, whilst the other assets are found in Appendix G.2. This particular instance is affected by V’s low price in the positive terms, meaning that it pushes the price higher, whilst the high price of CSCO and the open of V negatively affect the prediction by pushing it lower. Looking at these explanations over a number of days can help an investor decide whether there exist particular features that consistently contribute to the portfolio allocation decision.

### 4.5.3 Shapley Additive Explanations Results

Finally, the results of the SHAP analysis provide a global view of the feature importance across all time steps and assets, as well as a local interpretation for individual predictions. As with the case of LIME, instead of using a surrogate model, the explanations are extracted from the A2C model directly. Since the predictions of the output are

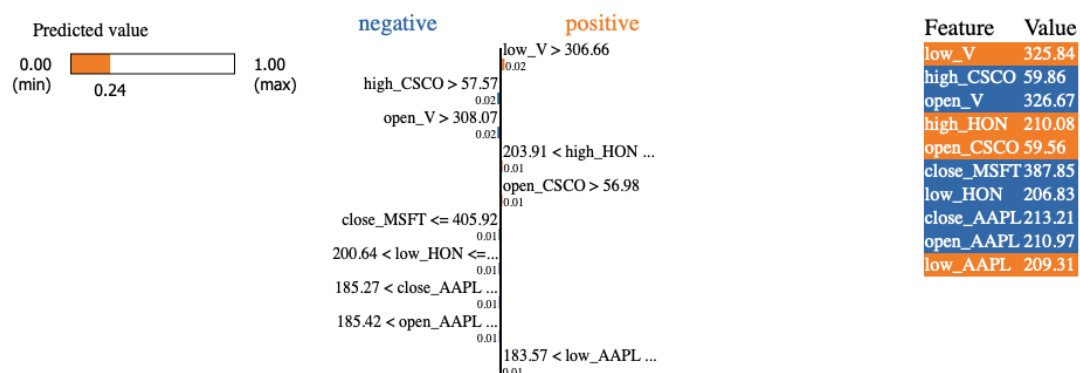


Figure 4.4: LIME explanations for the A2C algorithm for a specific observation in the test dataset for the MSFT asset. The orange bars indicate features that contribute positively to the prediction, while the blue bars indicate features that contribute negatively.

weight allocations across all portfolio assets, the SHAP values presented in this section correspond only to AAPL, but the interpretations can be generalised to other assets and algorithms.

Figure 4.5 depicts a beeswarm plot, where the x-axis represents the SHAP value, which measures the impact of a feature on the model's output; while the y-axis displays the top features. Each point in the beeswarm plot represents a single prediction, with the point's colour indicating whether its corresponding feature value is low, coloured in blue, or high, coloured in magenta. The beeswarm plot provides a visual representation of the distribution of SHAP values for each feature, allowing for an easy comparison of their importance. Surprisingly, the most important feature for the AAPL asset is the low price of the MSFT asset and, by visual inspection, the high values of the low price of MSFT push the AAPL allocation lower, while the low values of the low price of MSFT push the AAPL allocation higher. However, this is not quite significant as there is a cluster of data points around the zero, indicating that, for a number of trading days, the low price of MSFT does not have an impact on AAPL's allocation.

The `shap` Python library provides numerous visualisations to explain the prediction of

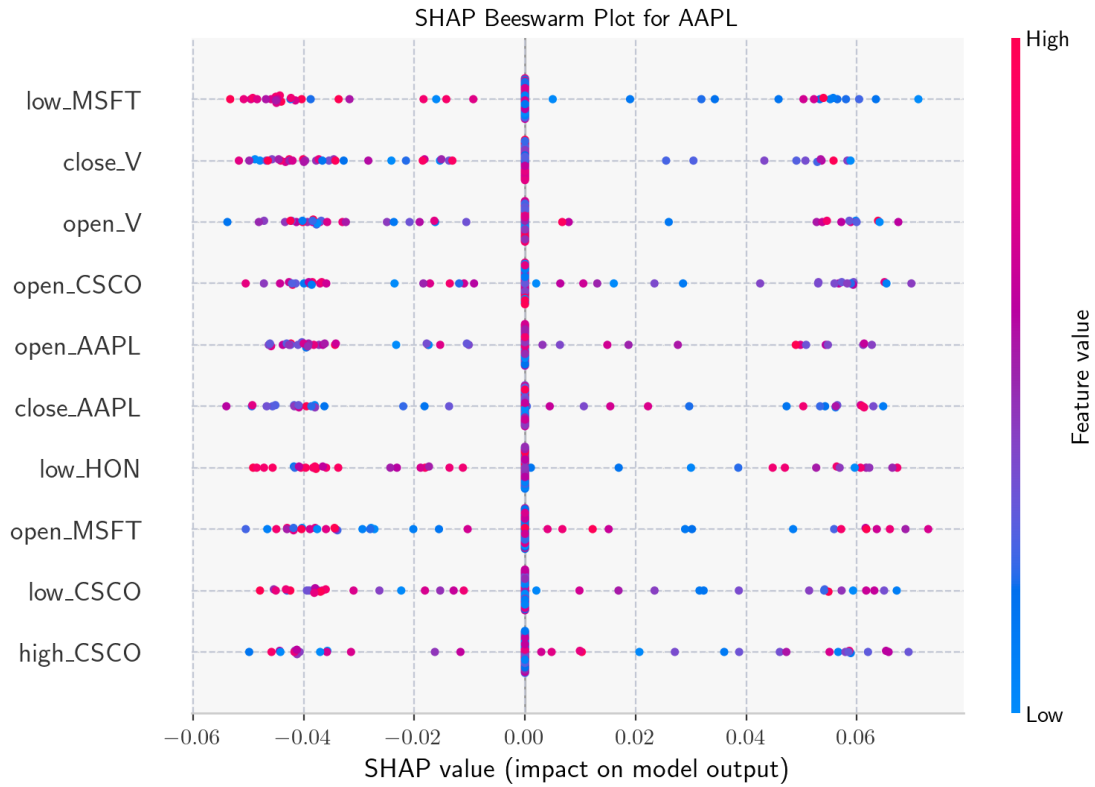


Figure 4.5: Beeswarm SHAP explanations for the A2C algorithm for the AAPL asset. The x-axis represents the SHAP values, whilst the y-axis represents the top features. The colour indicates the feature value, with magenta being high and blue being low.

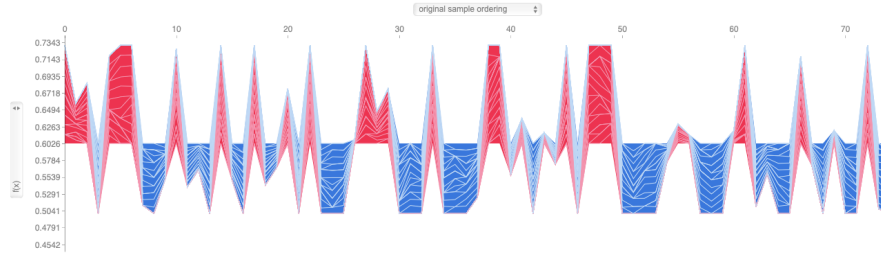


Figure 4.6: SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm.

a model. An interesting one is the force plot, shown in Figure 4.6, for the AAPL weight allocation and the contribution of all features. The force plot visualises the impact of each feature on the model’s weight allocation over the entire test dataset ordered by time. Positive values, visualised in magenta, show feature contributions that push the allocation higher, while negative values, in blue, push it lower. The baseline is the average weight allocation across all time steps.

The `shap` library provides the output in an interactive HyperText Markup Language (HTML) format that allows us to interact with the visualisation and gain deeper insights into the model’s behaviour. Using the force plot, it is possible to single out the effects of AAPL’s most important feature over the test period, as shown in Figure 4.7, as well as its isolated effect in one specific prediction. Its impact is very well-defined as for approximately the first 30 samples, it has a positive contribution, increasing the allocation, while for the rest of the time steps, it has a negative contribution, decreasing it.

Lundberg and Lee (2017) [52] showed that LIME is a subset of SHAP and, as a consequence, it is possible to obtain local explanations using the `shap` library. Figure 4.8 shows the local explanation for the AAPL asset at a single observation of the test dataset. Although the visualisation is different, the information it provides is similar to that of LIME. Shown horizontally, the features in magenta push the allocation higher, while



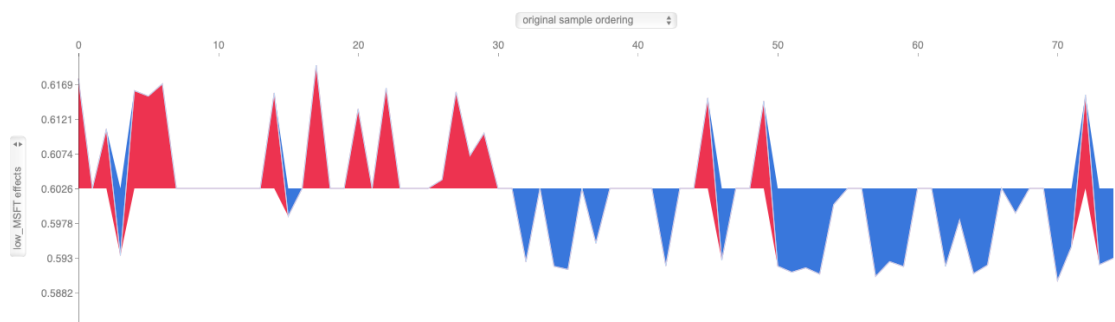


Figure 4.7: SHAP force plot for the impact of MSFT low price feature in the weight allocation of the AAPL asset for the A2C algorithm.

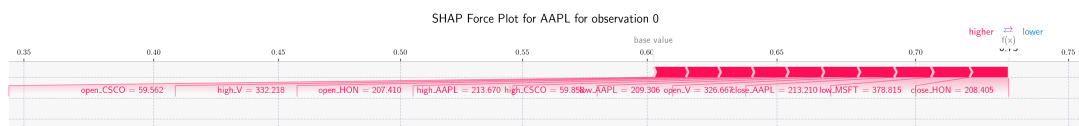


Figure 4.8: SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm at the first time step of the test dataset.

those in blue push it lower. In this case, the most important features that contribute to the allocation weight of AAPL are only features that increase the allocation and, as such, no blue features are present.

## Chapter 5

# Legal, Social, Ethical and Professional Issues

The development and deployment of Deep Reinforcement Learning (DRL) algorithms to perform profitable portfolio allocation raises several legal, social, ethical and professional issues that must be considered. The incorporation of post-hoc explainable techniques to understand, interpret and clarify the decision-making process of these algorithms is a crucial step towards addressing these concerns. This chapter explores them in detail, referencing relevant regulatory frameworks and professional codes of conducts, and highlights potential mitigation strategies.

### 5.1 Legal Issues

When deploying Machine Learning (ML) algorithms in finance, the European Union (EU)'s Artificial Intelligence Act (AI Act) [68] classifies them as high-risk under Article 6 due to their potential impact on an individual's economic well-being. Consequently, high-risk systems must comply with Chapter 3 - Section 2, Articles 9-15, which include

the obligations for risk management, data governance, documentation, transparency and human supervision. In particular, Article 13 requires that high-risk AI systems's outputs are interpretable. The use of explainability techniques ensures that the decision-making process of the algorithm can be understood and justified, thus adhering to the legal requirements set forth by the AI Act.

In addition, algorithmic trading systems must adhere to the European Union directive on Markets in Financial Instruments Directive II (MiFID II) [89] and the United Kingdom (UK) Financial Conduct Authority (FCA) guidance on *Algorithmic Trading Compliance in Wholesale Markets* [90]. These regulations require robust governance and oversight frameworks, risk controls and thorough testing infrastructure. In this project, back-testing has been carried out to assess the algorithm's performance under varying market conditions followed by explainability techniques to enable the auditability of the system.

## 5.2 Social Issues

Despite the growing exposure to Artificial Intelligence (AI) systems with the rise of Large Language Models (LLMs), there is still a significant lack of understanding and trust in these systems. Some of the reasons behind this mistrust include the black box nature of models, making outputs hard to interpret, lack of human-like qualities in the models, and perceived limitations to adapt to new situations and learn from previous mistakes.

In the context of this work, the integration of explainability techniques addresses the black box behaviour of the implemented technology by offering clear, data-driven justifications. However, transparency must also be accessible. It is essential to provide a user-friendly interface to easily access the explanations and generate plain language descriptions for non-technical audiences.

### 5.3 Ethical Issues

The ethical implications of DRL in portfolio optimisation are multifaceted. The primary concern is the potential for these systems to make decisions that may not align with human values or ethical standards. For instance, if the algorithm prioritises profit maximisation without considering the social or environmental impact of its investment choices, it could lead to unethical outcomes, such as supporting companies with poor labour practices or those contributing to environmental degradation. To address this concern, the following practices can be put in place:

1. the end-user should have full control over the assets included in their portfolio, allowing them to exclude companies that do not meet their ethical standards; or
2. the environment’s representation can be expanded to include ethical dimensions, like social impact or environmental sustainability metrics.

Regarding the environment representation, it was not possible to incorporate such data as it is not readily available nor in a standardised format. This is why, although there was an interest to broaden the environment representation to include other sources outside of the financial domain, it was not feasible to do so given the available resources.

A critical point in portfolio allocation is risk management. In this research, a performance metric that balances return maximisation and risk minimisation is used for hyper-parameter tuning, ensuring that the agent learns to avoid overly risky investments. Additionally, the inclusion of a risk-free asset enables a safe-guard mechanism. The agent can be implemented to allocate all the resources to cash when market volatility exceeds a pre-defined threshold and resume only when said volatility decreases.

Finally, potential biases in the training data or model structure could result in allocations favouring certain industries or assets classes. This thesis mitigates such biases by

constructing a portfolio from diversified indices (Appendix D.1) and using explainability techniques to audit the decisions for systematic biases.

## 5.4 Professional Issues

This work has been conducted in accordance with the British Computer Society (BCS) Code of Conduct [91] and the The Institution of Engineering and Technology (IET) Rules of Conduct [92]. All the work in this report is original unless stated otherwise, and all external contributions are explicitly acknowledged, following the principles of the BCS Code of Conduct [91]. Moreover, all third-party libraries, datasets and code have been explicitly acknowledged and their use complies with the respective licences and guidelines.

Most importantly, the project has been conducted within my own area of expertise: computational finance, Reinforcement Learning, and Explainable Artificial Intelligence. If any aspects of the project were beyond these, proper academic sources have been consulted to ensure the integrity and quality of the work.

## Chapter 6

# Conclusion

This thesis has explored the application of Deep Reinforcement Learning (DRL) algorithms for optimal portfolio allocation in dynamic financial markets. The primary objective was to develop an explainable model-agnostic framework capable of enhancing the understanding of any DRL algorithm's predictions. Such a tool would provide insights into the decision-making process of these complex models and facilitate auditability.

Five state-of-the-art DRL algorithms were implemented and evaluated on a portfolio management task. To assess the behaviour of these algorithms in different market conditions, a comprehensive experimental setup was designed, involving various datasets and environment representations. The datasets ranged from equities to commodities and currencies, each presenting unique challenges and opportunities for the DRL algorithms. The results demonstrated that DRL algorithms can effectively learn and adapt to dynamic market conditions, achieving competitive performance compared to traditional portfolio management strategies. However, the challenge remains in finding the optimal hyper-parameters, uniquely suited to each algorithm and dataset combination, in order to be able to fully exploit their potential.

Regarding the explainability aspect, the framework developed in this thesis successfully enhances the interpretability, transparency and auditability of these black box models. The incorporation of feature importance through a surrogate model, Local Interpretable Model-agnostic Explanations (LIME) analysis and SHapley Additive ex-Planations (SHAP) values provides an exhaustive methodology for understanding both individual predictions and the overall decision-making process of the models. However, the results highlight the superiority of the SHAP technique, which is capable of providing global explanations and feature importance without the need for an additional layer, in conjunction with local explanations.

## 6.1 Future Work

Despite the comprehensive and exhaustive nature of this report, there are several areas where future research could enhance this work. Indisputably, the main limitation of this thesis has been the lack of computational resources. Any future work should aim to fully explore the hyper-parameter space for each of the DRL algorithms, datasets and environment representations. In a similar vein, current research in price prediction has investigated the impact of a smaller feature representation by performing feature engineering techniques, such as feature selection and dimensionality reduction. Such measures might not only improve model performance and reduce over-fitting, but could also reduce computational requirements.

Moreover, even in the case of optimal hyper-parameter configuration, comparing the performance of the models to those of traditional methods left room for improvement. Exploring alternative reward functions, such as Sharpe ratio, incorporating additional constraints, such as transaction costs, or explicitly handling periods of high volatility could lead to more robust and effective trading strategies. Another possibility that led to reduced performance against the benchmarks was the exclusion of a risk-free asset in

the portfolio. Future work could include a risk-free asset in the portfolio, which would result in a more diversified and potentially less risky portfolio. In terms of real-world scenarios, portfolios tend to be composed of different asset classes. Although this thesis explored the performance of the algorithms in different classes, forthcoming research could investigate the performance of these algorithms in multi-asset class portfolios.

Lastly, for the explainability aspect, the current framework would benefit from a more user-friendly interface that allows users to provide their dataset and prediction function easily and explore the model’s explanations interactively. Another direction is to add intrinsic interpretability methods directly within the DRL algorithms, such as attention-based mechanisms [17], reducing the need for post-hoc explanation techniques.



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# Appendix A

## Algorithms

### A.1 Deep Reinforcement Learning Algorithms

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**Algorithm 1** Advantage Actor-Critic (A2C) Pseudo-code

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**Initialise:**Global shared policy parameters  $\theta$  and value parameters  $\theta_v$ Number of parallel workers  $N$ Global step counter  $T \leftarrow 0$ Hyper-parameters: discount  $\gamma$ , max steps per update  $t_{\max}$ , max total steps  $T_{\max}$ , learning rates  $\alpha_\pi, \alpha_v$ **repeat**Reset gradients:  $d\theta \leftarrow 0, d\theta_v \leftarrow 0$ 

Initialise empty batch storage for all workers

**for** worker  $i = 1$  to  $N$  **do** $t_{\text{start}} \leftarrow t$ Get initial state  $s_t^{(i)}$  from worker  $i$ **repeat**Select action  $a_t^{(i)} \sim \pi_\theta(\cdot | s_t^{(i)})$ Execute  $a_t^{(i)}$ , observe reward  $r_t^{(i)}$  and next state  $s_{t+1}^{(i)}$ Store  $(s_t^{(i)}, a_t^{(i)}, r_t^{(i)})$  in worker  $i$ 's trajectory $t \leftarrow t + 1$ **until** terminal  $s_t^{(i)}$  or  $t - t_{\text{start}} == t_{\max}$ 

$$R^{(i)} = \begin{cases} 0 & \text{if terminal } s_t^{(i)} \\ V_{\theta_v}(s_t^{(i)}) & \text{otherwise} \end{cases}$$

**for**  $j \in \{t-1, \dots, t_{\text{start}}\}$  **do**

$$R^{(i)} \leftarrow r_j^{(i)} + \gamma R^{(i)}$$

Accumulate gradients w.r.t.  $\theta$ :

$$d\theta \leftarrow d\theta + \nabla_\theta \log \pi_\theta(a_j^{(i)} | s_j^{(i)})(R^{(i)} - V_{\theta_v}(s_j^{(i)}))$$

Accumulate gradients w.r.t.  $\theta_v$ :

$$d\theta_v \leftarrow d\theta_v + \nabla_{\theta_v}(R^{(i)} - V_{\theta_v}(s_j^{(i)}))^2$$

**end for****end for**

// Synchronous update: wait for all workers to complete

Average gradients:  $d\theta \leftarrow \frac{1}{N}d\theta, d\theta_v \leftarrow \frac{1}{N}d\theta_v$ Update  $\theta \leftarrow \theta + \alpha_\pi d\theta, \theta_v \leftarrow \theta_v + \alpha_v d\theta_v$  $T \leftarrow T + N \times t_{\max}$ **until**  $T > T_{\max}$ 

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**Algorithm 2** Proximal Policy Optimisation (PPO) Pseudo-code

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**Initialise:**Policy parameters  $\theta_0$  and value function parameters  $\phi_0$ Global step counter  $T \leftarrow 0$ Hyper-parameters: discount  $\gamma$ , GAE parameter  $\lambda$ , clipping parameter  $\epsilon$ , learning rates  $\alpha_\pi, \alpha_v$ , epochs per update  $K_{\text{epochs}}$ , minibatch size  $N_{\text{minibatch}}$ , loss coefficients  $c_1, c_2$ **for**  $k = 0, 1, 2, \dots$  **do**Collect set of trajectories  $\mathcal{D}_k = \{\tau_i\}$  by running policy  $\pi_{\theta_k}$  in environmentStore transitions:  $\{(s_t, a_t, r_t, s_{t+1}, \text{done}_t)\}$ **for** each trajectory  $\tau$  in  $\mathcal{D}_k$  **do**Compute value estimates:  $V_t = V_{\phi_k}(s_t)$ Compute TD residuals:  $\delta_t = r_t + \gamma V_{t+1}(1 - \text{done}_t) - V_t$ Compute GAE advantages:  $\hat{A}_t = \sum_{l=0}^{\infty} (\gamma\lambda)^l \delta_{t+l}$ Compute returns:  $\hat{R}_t = \hat{A}_t + V_t$ **end for****for** epoch  $e = 1$  to  $K_{\text{epochs}}$  **do**Shuffle dataset  $\mathcal{D}_k$ **for** each minibatch  $\mathcal{B}$  in  $\mathcal{D}_k$  **do**

$$r_t(\theta) = \frac{\pi_\theta(a_t|s_t)}{\pi_{\theta_k}(a_t|s_t)}$$

$$L^{\text{CLIP}}(\theta) = \frac{1}{|\mathcal{B}|} \sum_{t \in \mathcal{B}} \min \left( r_t(\theta) \hat{A}_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right)$$

$$L^{VF}(\phi) = \frac{1}{|\mathcal{B}|} \sum_{t \in \mathcal{B}} \left( V_\phi(s_t) - \hat{R}_t \right)^2$$

$$L(\theta, \phi) = L^{\text{CLIP}}(\theta) - c_1 L^{VF}(\phi) + c_2 S[\pi_\theta]$$

$$\theta \leftarrow \theta + \alpha_\pi \nabla_\theta L^{\text{CLIP}}(\theta)$$

$$\phi \leftarrow \phi - \alpha_v \nabla_\phi L^{VF}(\phi)$$

**end for****end for**Update policy:  $\theta_{k+1} = \theta$ Update value function:  $\phi_{k+1} = \phi$  $T \leftarrow T + |\mathcal{D}_k|$ **end for**

---

---

**Algorithm 3** Deep Deterministic Policy Gradient (DDPG) Pseudo-code

---

**Initialise:**

Critic network  $Q_{\theta^Q}(s, a)$  and actor  $\mu_{\theta^\mu}(s)$  with random weights  $\theta^Q, \theta^\mu$

Target networks:  $\theta^{Q'} \leftarrow \theta^Q, \theta^{\mu'} \leftarrow \theta^\mu$

Replay buffer  $\mathcal{B}$

Hyper-parameters: discount  $\gamma$ , soft update rate  $\tau$ , batch size  $N$ , exploration noise process  $\mathcal{N}$ , learning rates  $\alpha_Q, \alpha_\mu$ , total episodes  $M$ , steps per episode  $T$

**for** episode = 1 to  $M$  **do**

    Initialise random process  $\mathcal{N}$  for action exploration

    Receive initial state  $s_1$

**for**  $t = 1$  to  $T$  **do**

        Select action  $a_t = \mu_{\theta^\mu}(s_t) + \mathcal{N}_t$

        Execute  $a_t$ , observe reward  $r_t$  and next state  $s_{t+1}$

        Store  $(s_t, a_t, r_t, s_{t+1})$  in  $\mathcal{B}$

        Sample mini-batch  $\{(s_i, a_i, r_i, s_{i+1})\}_{i=1}^N$  from  $\mathcal{B}$

        Compute target:  $y_i = r_i + \gamma Q_{\theta^{Q'}}(s_{i+1}, \mu_{\theta^{\mu'}}(s_{i+1}))$

        Update critic by minimising:  $L(\theta^Q) = \frac{1}{N} \sum_i (y_i - Q_{\theta^Q}(s_i, a_i))^2$

        Update actor by policy gradient:

$$\nabla_{\theta^\mu} J \approx \frac{1}{N} \sum_i \nabla_a Q_{\theta^Q}(s_i, a)|_{a=\mu_{\theta^\mu}(s_i)} \nabla_{\theta^\mu} \mu_{\theta^\mu}(s_i)$$

        Update target networks:

$$\theta^{Q'} \leftarrow \tau \theta^Q + (1 - \tau) \theta^{Q'}$$

$$\theta^{\mu'} \leftarrow \tau \theta^\mu + (1 - \tau) \theta^{\mu'}$$

**end for**

**end for**

---

---

**Algorithm 4** Twin Delayed Deep Deterministic Policy Gradient (TD3) Pseudo-code

---

**Initialise:**

Critic networks  $Q_{\theta_1}(s, a)$  and  $Q_{\theta_2}(s, a)$  with random weights  $\theta_1, \theta_2$

Actor policy  $\mu_\phi(s)$  with random weights  $\phi$

Target networks:  $\theta'_1 \leftarrow \theta_1, \theta'_2 \leftarrow \theta_2, \phi' \leftarrow \phi$

Replay buffer  $\mathcal{B}$

Hyper-parameters: discount  $\gamma$ , target policy noise  $\tilde{\sigma}$ , noise clip  $c$ , policy delay  $d$ , exploration noise  $\sigma$ , update rate  $\tau$ , batch size  $N$ , total steps  $T$

**for**  $t = 1$  to  $T$  **do**

Observe state  $s_t$

Sample action with exploration:  $a_t = \mu_\phi(s_t) + \epsilon, \epsilon \sim \mathcal{N}(0, \sigma)$

Execute  $a_t$ , observe reward  $r_t$  and next state  $s_{t+1}$

Store  $(s_t, a_t, r_t, s_{t+1})$  in  $\mathcal{B}$

Sample mini-batch  $\{(s_i, a_i, r_i, s_{i+1})\}_{i=1}^N$  from  $\mathcal{B}$

Sample clipped noise:  $\tilde{\epsilon} \sim \text{clip}(\mathcal{N}(0, \tilde{\sigma}), -c, c)$

Compute target action:  $\tilde{a}_{i+1} = \mu_{\phi'}(s_{i+1}) + \tilde{\epsilon}$

Compute target Q-value:  $y_i = r_i + \gamma \min_{j=1,2} Q_{\theta'_j}(s_{i+1}, \tilde{a}_{i+1})$

Update each critic by minimising  $L(\theta_j) = \frac{1}{N} \sum_i (y_i - Q_{\theta_j}(s_i, a_i))^2$

**if**  $t \bmod d = 0$  **then**

Update actor by policy gradient:  $\nabla_\phi J \approx \frac{1}{N} \sum_i \nabla_a Q_{\theta_1}(s_i, a) |_{a=\mu_\phi(s_i)} \nabla_\phi \mu_\phi(s_i)$

Update target networks:

$\theta'_j \leftarrow \tau \theta_j + (1 - \tau) \theta'_j$  for  $j = 1, 2$

$\phi' \leftarrow \tau \phi + (1 - \tau) \phi'$

**end if**

**end for**

---

---

**Algorithm 5** Soft Actor-Critic (SAC) Pseudo-code

---

**Initialise:**Actor network  $\pi_\theta(a|s)$  with parameters  $\theta$ Two critic networks  $Q_{\phi_1}(s, a)$  and  $Q_{\phi_2}(s, a)$  with parameters  $\phi_1, \phi_2$ Target critic networks:  $\phi'_1 \leftarrow \phi_1, \phi'_2 \leftarrow \phi_2$ Replay buffer  $\mathcal{D}$ Hyper-parameters: discount  $\gamma$ , temperature  $\alpha$  (fixed or learnable), target entropy  $\mathcal{H}$  (if  $\alpha$  is learnable), batch size  $N$ , learning rates  $\lambda_Q, \lambda_\pi, \lambda_\alpha$ , soft update rate  $\tau$ **for** each training step **do**Observe state  $s_t$ Sample action:  $a_t \sim \pi_\theta(\cdot|s_t)$ Execute  $a_t$ , observe reward  $r_t$  and next state  $s_{t+1}$ Store  $(s_t, a_t, r_t, s_{t+1})$  in  $\mathcal{D}$ **if** time to update **then**Sample mini-batch  $\{(s_i, a_i, r_i, s_{i+1})\}_{i=1}^N$  from  $\mathcal{D}$ **Update Critics:****for**  $j = 1, 2$  **do**Sample next actions:  $\tilde{a}_{i+1} \sim \pi_\theta(\cdot|s_{i+1})$ 

Compute target Q-values:

$$y_i = r_i + \gamma \left( \min_{k=1,2} Q_{\phi'_k}(s_{i+1}, \tilde{a}_{i+1}) - \alpha \log \pi_\theta(\tilde{a}_{i+1}|s_{i+1}) \right)$$

Update critic:  $\phi_j \leftarrow \phi_j - \lambda_Q \nabla_{\phi_j} \frac{1}{N} \sum_i (Q_{\phi_j}(s_i, a_i) - y_i)^2$ **end for****Update Actor:**Sample actions with reparametrisation:  $\tilde{a}_i = f_\theta(\epsilon_i; s_i)$  where  $\epsilon_i \sim \mathcal{N}(0, I)$ 

Compute policy loss:

$$J(\theta) = \frac{1}{N} \sum_i [\alpha \log \pi_\theta(\tilde{a}_i|s_i) - \min_{j=1,2} Q_{\phi_j}(s_i, \tilde{a}_i)]$$

Update actor:  $\theta \leftarrow \theta - \lambda_\pi \nabla_\theta J(\theta)$ **if**  $\alpha$  is learnable **then****Update Temperature:**

$$J(\alpha) = \frac{1}{N} \sum_i \alpha (\log \pi_\theta(\tilde{a}_i|s_i) + \mathcal{H})$$

Update temperature:  $\alpha \leftarrow \alpha - \lambda_\alpha \nabla_\alpha J(\alpha)$ **end if****Update Target Networks:** $\phi'_j \leftarrow \tau \phi_j + (1 - \tau) \phi'_j$  for  $j = 1, 2$ **end if****end for**

---



## A.2 Explainability Algorithms

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**Algorithm 6** Shapley Value Approximation

---

**Initialise:**

Number of iterations  $M$

Instance of interest  $\mathbf{x}$

Feature index  $j$

Data matrix  $\mathbf{X}$

Model  $\hat{f}$

**for**  $m = 1$  to  $M$  **do**

    Draw a random instance  $\mathbf{z}$  from data matrix  $\mathbf{X}$

    Choose a random permutation  $\mathbf{o}$  of the feature indices

    Order  $\mathbf{x}$  according to  $\mathbf{o}$ :  $\mathbf{x}_{\mathbf{o}} = (x_{(1)}, \dots, x_{(j)}, \dots, x_{(p)})$

    Order  $\mathbf{z}$  according to  $\mathbf{o}$ :  $\mathbf{z}_{\mathbf{o}} = (z_{(1)}, \dots, z_{(j)}, \dots, z_{(p)})$

    Construct two new instances:

$\mathbf{x}_{+j} = (x_{(1)}, \dots, x_{(j-1)}, x_{(j)}, z_{(j+1)}, \dots, z_{(p)})$

$\mathbf{x}_{-j} = (x_{(1)}, \dots, x_{(j-1)}, z_{(j)}, z_{(j+1)}, \dots, z_{(p)})$

    Compute marginal contribution:

$$\phi_j^{(m)} = \hat{f}(\mathbf{x}_{+j}) - \hat{f}(\mathbf{x}_{-j})$$

**end for**

Compute average Shapley value:

$$\phi_j(\mathbf{x}) = \frac{1}{M} \sum_{m=1}^M \phi_j^{(m)}$$

---

## Appendix B

# State Representation

### B.1 Technical Indicators

The following technical indicators are used to represent the state of the financial environment. They are calculated based on the historical price data of the assets in the portfolio.

- Simple Moving Average (SMA): Lagging indicator that smooths the price over a period of time. It is the unweighted mean of the previous  $k$  data points and is computed following:

$$\text{SMA}_t^k = \frac{1}{k} \sum_{i=t-k+1}^t p_i, \quad (\text{B.1})$$

where  $t$  is the current time step,  $k$  is the look-back period and  $p_i$  is the close price at time  $i$ . In this thesis, the SMA is calculated for 5, 10 and 20 days.

- Exponential Moving Average (EMA): Weighted moving average that gives more importance to recent prices with the goal of making it more responsive to new

information. It is calculated using the formula:

$$\text{EMA}_t^k = \begin{cases} p_t & \text{if } t = 0 \\ \frac{2}{k+1}p_t + \left(1 - \frac{2}{k+1}\right) \text{EMA}_{t-1}^k & \text{if } t > 0 \end{cases}, \quad (\text{B.2})$$

where  $k$  is the look-back period,  $p_t$  is the close price at time  $t$  and  $\frac{2}{k+1}$  is the smoothing factor. In this thesis, the EMA is calculated for 5 and 10 days.

- Moving Average Convergence Divergence (MACD): Momentum indicator that shows the relationship between two moving average of an asset's price. The formula is:

$$\text{MACD}_t = \text{EMA}_t^{k_1} - \text{EMA}_t^{k_2}, \quad (\text{B.3})$$

where  $k_1$  and  $k_2$  are the look-back periods for the short-term (12 periods) and long-term (26 periods) EMAs, respectively, and  $p_t$  is the close price at time  $t$ .

- Relative Strength Index (RSI): Momentum indicator that measures the magnitude of recent changes to identify overbought or oversold conditions in the market. It is computed using smoothed moving averages for the upward change in closing price  $p_t$ , defined as  $u_t = \max\{p_t - p_{t-1}, 0\}$ :

$$\text{SMMA}_t^k(u_t) = \frac{1}{k}u_t + \left(1 - \frac{1}{k}\right) \text{SMMA}_{t-1}^k(u_{t-1}) \quad (\text{B.4})$$

and for the downward change, defined as  $d_t = \max\{p_{t-1} - p_t, 0\}$ :

$$\text{SMMA}_t^k(d_t) = \frac{1}{k}d_t + \left(1 - \frac{1}{k}\right) \text{SMMA}_{t-1}^k(d_{t-1}). \quad (\text{B.5})$$

Then, the Relative Strength Index (RSI) is given by:

$$\text{RSI}_t = 100 - \frac{100}{1 + \text{RS}_t}, \quad (\text{B.6})$$

where the relative strength  $RS_t$  is defined as:

$$RS_t = \frac{SMMA_t^k(u_t)}{SMMA_t^k(d_t)}. \quad (B.7)$$

- Commodity Channel Index (CCI): Momentum indicator that measures the deviation of the price from its historical average price over a period of time. It is calculated as:

$$CCI_t^k = \frac{TP_t^k - MA_t^k}{0.015 \cdot MD_t}, \quad (B.8)$$

where  $k$  is the number of periods (14 days), the typical price  $TP_t$  is:

$$TP_t = \sum_{i=t-k+1}^t \frac{p_i + h_i + l_i}{3}, \quad (B.9)$$

with  $p_t$ ,  $h_t$  and  $l_t$  being the close, high and low prices at time step  $t$ , respectively, and the moving average  $MA_t^k$  is:

$$MA_t^k = \frac{1}{k} \sum_{i=t-k+1}^t TP_i \quad (B.10)$$

and the mean deviation  $MD_t$  is:

$$MD_t = \frac{1}{k} \sum_{i=t-k+1}^t |TP_i - MA_i^k|. \quad (B.11)$$

- Bollinger Bands: Volatility indicator that defines the trend-line for high and low prices based on the deviation of the asset from the moving average. The upper bands is calculated as:

$$BOLLUB_t^k = MA_t^k + m \cdot SD_t^k, \quad (B.12)$$

where  $k$  is the number of periods (20 days),  $m$  is the number of standard deviations

away from the moving average (2 standard deviations) and  $SD_t^k$  is the standard deviation of the typical price over the same period. Similarly, the lower band is calculated as:

$$\text{BOLLDB}_t^k = \text{MA}_t^k - m \cdot \text{SD}_t^k. \quad (\text{B.13})$$

- Average True Range (ATR): Volatility indicator that measures the average range of price movement over a period of time, usually 14 days. It is calculated as:

$$\text{ATR}_t^k = \frac{1}{k} \sum_{i=t-k+1}^t \text{TR}_i, \quad (\text{B.14})$$

where the true range  $\text{TR}_i$  is defined as:

$$\text{TR}_i = \max \{h_i - l_i, |h_i - p_{i-1}|, |l_i - p_{i-1}|\}, \quad (\text{B.15})$$

where  $h_i$  and  $l_i$  are the high and low prices of the asset at time  $i$ , respectively, and  $p_{i-1}$  is the close price of the asset at time  $i - 1$ . The true range finds the maximum of the following three:

- most recent period high minus most recent period low,
  - absolute value of the most recent period high minus the previous close, and
  - absolute value of the most recent period low minus the previous close.
- Average Directional Index (ADX): Trend indicator used to measure the strength of a trend by quantifying the price movement. It is calculated as:

$$\text{ADX}_t^k = \frac{1}{k} \sum_{i=t-k+1}^t \text{DX}_i, \quad (\text{B.16})$$

where the Directional Movement Index (DX) is defined as:

$$DX_t = \frac{100 \cdot |PDI_t - MDI_t|}{PDI_t + MDI_t} \quad (B.17)$$

with the Positive Directional Index (PDI) and Negative Directional Index (MDI) calculated as

$$PDI_t = \frac{100 \cdot SMMA_t^k(DM^+)}{ATR_t^k} \quad (B.18)$$

and

$$MDI_t = \frac{100 \cdot SMMA_t^k(DM^-)}{ATR_t^k}, \quad (B.19)$$

where  $DM^+$  and  $DM^-$  are the positive and negative directional movements, respectively, calculated as:

$$DM^+ = \max(0, h_t - h_{t-1}) \quad (B.20)$$

and

$$DM^- = \max(0, l_{t-1} - l_t), \quad (B.21)$$

where  $h_t$  and  $l_t$  are the high and low prices of the asset at time  $t$ , respectively.

- Rate of Change (ROC): Momentum indicator that measures the percentage change in price between the current price  $p_t$  and the price  $p_{t-k}$  periods ago. It is given by the formula:

$$ROC_t^k = \frac{p_t - p_{t-k}}{p_{t-k}} \cdot 100. \quad (B.22)$$

In this thesis, the ROC is calculated for  $k = 10$  days.

## B.2 Macroeconomic Indicators

The following macroeconomic indicators are used to represent the state of the financial environment. They provide additional context about the market conditions and are calculated based on external data sources.

- Volatility Index (VIX) measures the market's expectation of future volatility based on options prices. This is only available for US markets.
  - VIX is calculated using the implied volatility of Standard and Poor's 500 Index (S&P 500) options.
  - VXD is calculated using the implied volatility of Dow Jones 30 Index (DW30) options.
- Currency index captures the impact from the monetary market on the stock market.
  - U.S. Dollar Index (DXY): United States (U.S.) dollar's value relative to a basket of foreign currencies.
  - Euro Index (EXY): Euro's value relative to a basket of foreign currencies.
  - British Pound Currency Index (BXY): British pound's value relative to a basket of foreign currencies.
- Interest rates reflect the cost of borrowing money and the return on savings. This is only available for US markets.
  - 3-Month Treasury Yield (IRX): Reflects the return on investment for a 3-month government bond.
  - 5-Year Treasury Yield (FVX): Reflects the return on investment for a 5-year government bond.

- 10-Year Treasury Yield (TNX): Reflects the return on investment for a 10-year government bond.



## Appendix C

# Hyper-parameter tuning

For the five implemented Deep Reinforcement Learning algorithms, the following table summarises the hyper-parameters that were tuned during the training process.

Table C.1: Hyper-parameter tuning configurations for different RL algorithms.

| Model       | Hyperparameter      | Values / Range                                     |
|-------------|---------------------|--|
| <b>A2C</b>  | Number of steps     | {5, 10, 20, 30, 40}                                |
|             | Entropy coefficient | Uniform[ $1 \times 10^{-8}$ , $1 \times 10^{-3}$ ] |
|             | Learning rate       | Uniform[ $1 \times 10^{-5}$ , $1 \times 10^{-2}$ ] |
| <b>PPO</b>  | Number of steps     | {128, 256, 512, 1024, 2048}                        |
|             | Entropy coefficient | Uniform[ $1 \times 10^{-8}$ , $1 \times 10^{-3}$ ] |
|             | Learning rate       | Uniform[ $1 \times 10^{-5}$ , $1 \times 10^{-2}$ ] |
|             | Batch size          | {32, 64, 128, 256, 512}                            |
| <b>DDPG</b> | Batch size          | {64, 128, 256}                                     |
|             | Buffer size         | {50000, 100000, 200000, 500000}                    |
|             | Learning rate       | Uniform[ $1 \times 10^{-5}$ , $1 \times 10^{-2}$ ] |
| <b>TD3</b>  | Batch size          | {64, 100, 128, 256}                                |

| Model      | Hyperparameter      | Values / Range                                     |
|------------|---------------------|--|
|            | Buffer size         | {500000, 1000000, 2000000}                         |
|            | Learning rate       | Uniform[ $1 \times 10^{-5}$ , $1 \times 10^{-2}$ ] |
| <b>SAC</b> | Batch size          | {32, 64, 128}                                      |
|            | Buffer size         | {100000, 500000, 1000000, 2000000}                 |
|            | Learning rate       | Uniform[ $1 \times 10^{-5}$ , $1 \times 10^{-2}$ ] |
|            | Learning starts     | {500, 1000, 2000, 5000}                            |
|            | Entropy coefficient | {"auto", "auto_0.1", "auto_0.01"}                  |

Table C.2: Default hyper-parameter configurations.

| Model       | Hyperparameter      | Values / Range |
|-------------|---------------------|----------------|
| <b>A2C</b>  | Number of steps     | 40             |
|             | Entropy coefficient | 0.0003         |
|             | Learning rate       | 0.003          |
| <b>PPO</b>  | Number of steps     | 512            |
|             | Entropy coefficient | 0.0005         |
|             | Learning rate       | 0.0015         |
|             | Batch size          | 64             |
| <b>DDPG</b> | Batch size          | 256            |
|             | Buffer size         | 200000         |
|             | Learning rate       | 0.005          |
| <b>TD3</b>  | Batch size          | 128            |
|             | Buffer size         | 500000         |
|             | Learning rate       | 0.001          |
| <b>SAC</b>  | Batch size          | 64             |
|             | Buffer size         | 500000         |

| Model | Hyperparameter      | Values / Range |
|-------|---------------------|----------------|
|       | Learning rate       | 0.001          |
|       | Learning starts     | 2000           |
|       | Entropy coefficient | auto_0.1       |

# Appendix D

## Datasets

### D.1 Equities

#### D.1.1 Dow Jones 30

The Dow Jones Industrial Average (DJIA) is a stock market index with 30 companies listed on United States (U.S.) stock exchanges. The trading symbol is DJI and as of April 2025, its constituents are:

Table D.1: Constituents of the Dow Jones Industrial Average index as of April 2025. [4]

| Symbol | Name              | Sector             | Industry                     |
|--------|-------------------|--------------------|------------------------------|
| AXP    | American Ex-press | Financial Services | Credit Services              |
| AMGN   | Amgen             | Healthcare         | Drug Manufacturers - General |
| AAPL   | Apple             | Technology         | Consumer Electronics         |
| AMZN   | Amazon            | Consumer Cyclical  | Internet Retail              |

| Symbol | Name              | Sector                 | Industry                            |
|--------|-------------------|------------------------|-------------------------------------|
| BA     | Boeing            | Industrials            | Aerospace & Defense                 |
| CAT    | Caterpillar       | Industrials            | Farm & Heavy Construction Machinery |
| CRM    | Salesforce        | Technology             | Software - Application              |
| CSCO   | Cisco             | Technology             | Communication Equipment             |
| CVX    | Chevron           | Energy                 | Oil & Gas Integrated                |
| DIS    | Walt Disney       | Communication Services | Entertainment                       |
| GS     | Goldman Sachs     | Financial Services     | Capital Markets                     |
| HD     | Home Depot        | Consumer Cyclical      | Home Improvement Retail             |
| HON    | Honeywell         | Industrials            | Conglomerates                       |
| IBM    | IBM               | Technology             | Information Technology Services     |
| JNJ    | Johnson & Johnson | Healthcare             | Drug Manufacturers - General        |
| JPM    | JP Morgan Chase   | Financial Services     | Banks - Diversified                 |
| KO     | Coca-Cola         | Consumer Defensive     | Beverages - Non-Alcoholic           |
| MCD    | McDonald's        | Consumer Cyclical      | Restaurants                         |
| MMM    | 3M                | Industrials            | Conglomerates                       |
| MRK    | Merck             | Healthcare             | Drug Manufacturers - General        |

| <b>Symbol</b> | <b>Name</b>      | <b>Sector</b>          | <b>Industry</b>                 |
|---------------|------------------|------------------------|---------------------------------|
| MSFT          | Microsoft        | Technology             | Software - Infrastructure       |
| NKE           | Nike             | Consumer Cyclical      | Footwear & Accessories          |
| NVDA          | NVIDIA           | Technology             | Semiconductors                  |
| PG            | Procter & Gamble | Consumer Defensive     | Household & Personal Products   |
| SHW           | Sherwin-Williams | Basic Materials        | Specialty Chemicals             |
| TRV           | Travelers        | Financial Services     | Insurance - Property & Casualty |
| UNH           | UnitedHealth     | Healthcare             | Healthcare Plans                |
| V             | Visa             | Financial Services     | Credit Services                 |
| VZ            | Verizon          | Communication Services | Telecom Services                |
| WMT           | Walmart          | Consumer Defensive     | Discount Stores                 |

### D.1.2 Euro Stoxx 50

The Euro Stoxx 50 Index (Euro Stoxx 50) is a stock market index that represents 50 of the largest companies in the Eurozone. The trading symbol is ST0XX50E and as of April 2025, its constituents are:

Table D.2: Constituents of the Euro Stoxx 50 index as of April 2025[5].

| <b>Symbol</b> | <b>Name</b> | <b>Sector</b>     | <b>Industry</b>        |
|---------------|-------------|-------------------|------------------------|
| ADS.DE        | adidas      | Consumer Cyclical | Footwear & Accessories |

| <b>Symbol</b> | <b>Name</b>                   | <b>Sector</b>      | <b>Industry</b>                     |
|---------------|-------------------------------|--------------------|-------------------------------------|
| ADYEN.AS      | Adyen                         | Technology         | Software - Infrastructure           |
| AD.AS         | Koninklijke<br>Ahold Delhaize | Consumer Defensive | Grocery Stores                      |
| AI.PA         | L’Air Liquide                 | Basic Materials    | Specialty Chemicals                 |
| AIR.PA        | Airbus                        | Industrials        | Aerospace & Defense                 |
| ALV.DE        | Allianz                       | Financial Services | Insurance - Diversified             |
| ABI.BR        | Anheuser-Busch<br>InBev       | Consumer Defensive | Beverages - Brewers                 |
| ASML.AS       | ASML Holding                  | Technology         | Semiconductor Equipment & Materials |
| CS.PA         | AXA                           | Financial Services | Insurance - Diversified             |
| BAS.DE        | BASF                          | Basic Materials    | Chemicals                           |
| BAYN.DE       | Bayer                         | Healthcare         | Drug Manufacturers - General        |
| BBVA.MC       | BBVA                          | Financial Services | Banks - Diversified                 |
| SAN.MC        | Banco Santander               | Financial Services | Banks - Diversified                 |
| BMW.DE        | BMW                           | Consumer Cyclical  | Auto Manufacturers                  |
| BNP.PA        | BNP Paribas                   | Financial Services | Banks - Regional                    |
| BN.PA         | Danone                        | Consumer Defensive | Packaged Foods                      |
| DB1.DE        | Deutsche Börse                | Financial Services | Financial Data & Stock Exchanges    |
| DHL.DE        | Deutsche Post                 | Industrials        | Integrated Freight & Logistics      |

| Symbol  | Name                               | Sector                 | Industry                       |
|---------|------------------------------------|------------------------|--------------------------------|
| DTE.DE  | Deutsche Telekom                   | Communication Services | Telecom Services               |
| ENEL.MI | Enel                               | Utilities              | Utilities - Diversified        |
| ENI.MI  | Eni                                | Energy                 | Oil & Gas Integrated           |
| EL.PA   | EssilorLuxottica                   | Healthcare             | Medical Instruments & Supplies |
| RACE.MI | Ferrari                            | Consumer Cyclical      | Auto Manufacturers             |
| FLTR.L  | Flutter Entertainment              | Consumer Cyclical      | Gambling                       |
| RMS.PA  | Hermès International               | Consumer Cyclical      | Luxury Goods                   |
| IBE.MC  | Iberdrola                          | Utilities              | Utilities - Diversified        |
| ITX.MC  | Industria de Diseño Textil         | Consumer Cyclical      | Apparel Retail                 |
| IFX.DE  | Infineon Technologies              | Technology             | Semiconductors                 |
| INGA.AS | ING Groep                          | Financial Services     | Banks - Diversified            |
| ISP.MI  | Intesa Sanpaolo                    | Financial Services     | Banks - Regional               |
| KER.PA  | Kering                             | Consumer Cyclical      | Luxury Goods                   |
| OR.PA   | L'Oréal                            | Consumer Defensive     | Household & Personal Products  |
| MC.PA   | LVMH Moët Hennessy - Louis Vuitton | Consumer Cyclical      | Luxury Goods                   |



| <b>Symbol</b> | <b>Name</b>                              | <b>Sector</b>          | <b>Industry</b>                     |
|---------------|--|------------------------|-------------------------------------|
| MBG.DE        | Mercedes-Benz Group AG                   | Consumer Cyclical      | Auto Manufacturers                  |
| MUV2.DE       | Münchener Rückversicherungs-Gesellschaft | Financial Services     | Insurance - Reinsurance             |
| NOKIA.HE      | Nokia                                    | Technology             | Communication Equipment             |
| NDA-FI.HE     | Nordea Bank                              | Financial Services     | Banks - Regional                    |
| RI.PA         | Pernod Ricard                            | Consumer Defensive     | Beverages - Wineries & Distilleries |
| PRX.AS        | Prosus                                   | Communication Services | Internet Content & Information      |
| SAF.PA        | Safran                                   | Industrials            | Aerospace & Defense                 |
| SGO.PA        | Compagnie de Saint-Gobain                | Industrials            | Building Products & Equipment       |
| SAN.PA        | Sanofi                                   | Healthcare             | Drug Manufacturers - General        |
| SAP.DE        | SAP                                      | Technology             | Software - Application              |
| SU.PA         | Schneider Electric                       | Industrials            | Specialty Industrial Machinery      |
| SIE.DE        | Siemens                                  | Industrials            | Specialty Industrial Machinery      |
| STLAM.MI      | Stellantis                               | Consumer Cyclical      | Auto Manufacturers                  |
| TTE.PA        | TotalEnergies                            | Energy                 | Oil & Gas Integrated                |

| Symbol | Name       | Sector             | Industry                   |
|--------|------------|--------------------|----------------------------|
| DG.PA  | Vinci      | Industrials        | Engineering & Construction |
| UCG.MI | UniCredit  | Financial Services | Banks - Regional           |
| VOW.DE | Volkswagen | Consumer Cyclical  | Auto Manufacturers         |

### D.1.3 FTSE 100

The Financial Times Stock Exchange 100 Index (FTSE 100) is a stock market index that represents 100 of the largest companies listed on the London Stock Exchange. The trading symbol is FTSE and as of April 2025, its constituents are:

Table D.3: Constituents of the FTSE100 index as of April 2025. [6]

| Symbol | Name                     | Industry                        |
|--------|--------------------------|---------------------------------|
| III.L  | 3i Group                 | Financial Services              |
| ADM.L  | Admiral Group            | Insurance                       |
| AAF.L  | Airtel Africa            | Telecommunications Services     |
| ALW.L  | Alliance Witan           | Investment Trusts               |
| AAL.L  | Anglo American           | Mining                          |
| ANTO.L | Antofagasta              | Mining                          |
| AHT.L  | Ashtead Group            | Support Services                |
| ABF.L  | Associated British Foods | Food & Tobacco                  |
| AZN.L  | AstraZeneca              | Pharmaceuticals & Biotechnology |
| AUTO.L | Auto Trader Group        | Media                           |
| AV.L   | Aviva                    | Life Insurance                  |

| <b>Symbol</b> | <b>Name</b>                    | <b>Industry</b>                     |
|---------------|--------------------------------|-------------------------------------|
| BAB.L         | Babcock International Group    | Aerospace & Defence                 |
| BA.L          | BAE Systems                    | Aerospace & Defence                 |
| BARC.L        | Barclays                       | Banks                               |
| BTRW.L        | Barratt Redrow                 | Household Goods & Home Construction |
| BEZ.L         | Beazley                        | Insurance                           |
| BKG.L         | The Berkeley Group Holdings    | Household Goods & Home Construction |
| BP.L          | BP                             | Oil & Gas Producers                 |
| BATS.L        | British American Tobacco       | Tobacco                             |
| BT-A.L        | BT Group                       | Telecommunications Services         |
| BNZL.L        | Bunzl                          | Support Services                    |
| CNA.L         | Centrica                       | Multiline Utilities                 |
| CCEP.L        | Coca-Cola Europacific Partners | Beverages                           |
| CCH.L         | Coca-Cola HBC                  | Beverages                           |
| CPG.L         | Compass Group                  | Support Services                    |
| CTEC.L        | ConvaTec Group                 | Health Care Equipment & Services    |
| CRDA.L        | Croda International            | Chemicals                           |
| DCC.L         | DCC                            | Support Services                    |
| DGE.L         | Diageo                         | Beverages                           |
| DPLM.L        | Diploma                        | Industrial Support Services         |
| EDV.L         | Endeavour Mining               | Precious Metals and Mining          |

| <b>Symbol</b> | <b>Name</b>                                  | <b>Industry</b>                      |
|---------------|--|--------------------------------------|
| ENT.L         | Entain                                       | Travel & Leisure                     |
| EZJ.L         | easyJet                                      | Travel & Leisure                     |
| EXPN.L        | Experian                                     | Support Services                     |
| FCIT.L        | F&C Investment Trust                         | Collective Investments               |
| FRES.L        | Fresnillo                                    | Mining                               |
| GAW.L         | Games Workshop<br>Group                      | Leisure Goods                        |
| GLEN.L        | Glencore                                     | Mining                               |
| GSK.L         | GSK  | Pharmaceuticals & Biotechnology      |
| HLN.L         | Haleon                                       | Pharmaceuticals & Biotechnology      |
| HLMA.L        | Halma  | Electronic Equipment & Parts         |
| HIK.L         | Hikma Pharmaceuticals                        | Pharmaceuticals & Biotechnology      |
| HSX.L         | Hiscox                                       | Non-life insurance                   |
| HWDN.L        | Howden Joinery Group                         | Homebuilding & Construction Supplies |
| HSBA.L        | HSBC Holdings                                | Banks                                |
| IHG.L         | InterContinental Hotels<br>Group             | Travel & Leisure                     |
| IMI.L         | IMI  | Industrial Engineering               |
| IMB.L         | Imperial Brands                              | Tobacco                              |
| INF.L         | Informa                                      | Media                                |
| ICG.L         | ICG  | Financial Services                   |
| IAG.L         | International Consolidated<br>Airlines Group | Travel & Leisure                     |
| ITRK.L        | Intertek Group                               | Support Services                     |

| <b>Symbol</b> | <b>Name</b>                    | <b>Industry</b>                          |
|---------------|--------------------------------|--|
| JD.L          | JD Sports Fashion              | General Retailers                        |
| KGF.L         | Kingfisher                     | Retailers                                |
| LAND.L        | Land Securities                | Real Estate Investment Trusts            |
| LGEN.L        | Legal & General                | Life Insurance                           |
| LLOY.L        | Lloyds Banking                 | Banks                                    |
| LMP.L         | LondonMetric Property          | Real Estate Investment Trusts            |
| LSEG.L        | London Stock Exchange<br>Group | Financial Services                       |
| MNG.L         | M&G                            | Financial Services                       |
| MKS.L         | Marks and Spencer              | Food & Drug Retailing                    |
| MRO.L         | Melrose Industries             | Aerospace & Defence                      |
| MNDI.L        | Mondi                          | Containers & Packaging                   |
| NG.L          | National Grid                  | Multiline Utilities                      |
| NWG.L         | NatWest                        | Banks                                    |
| NXT.L         | NEXT                           | General Retailers                        |
| PERSON.L      | Pearson                        | Media                                    |
| PSH.L         | Pershing Square Hold-<br>ings  | Financial Services                       |
| PSN.L         | Persimmon                      | Household Goods & Home Con-<br>struction |
| PHNX.L        | Phoenix Group                  | Life Insurance                           |
| PCT.L         | Polar Capital Technol-<br>ogy  | Investment Trusts                        |
| PRU.L         | Prudential                     | Life Insurance                           |

| <b>Symbol</b> | <b>Name</b>          | <b>Industry</b>                                    |
|---------------|----------------------|--|
| RKT.L         | Reckitt Benckiser    | Household Goods & Home Construction                |
| REL.L         | RELX                 | Media  |
| RTO.L         | Rentokil Initial     | Support Services                                   |
| RMV.L         | Rightmove            | Media  |
| RIO.L         | Rio Tinto            | Mining   |
| RR.L          | Rolls-Royce Holdings | Aerospace & Defence                                |
| SGE.L         | The Sage Group       | Software & Computer Services                       |
| SBRY.L        | J Sainsbury          | Food & Drug Retailing                              |
| SDR.L         | Schroders            | Financial Services                                 |
| SMT.L         | Scottish Mortgage    | Collective Investments                             |
| SGRO.L        | SEGRO                | Real Estate Investment Trusts                      |
| SVT.L         | Severn Trent         | Multiline Utilities                                |
| SHEL.L        | Shell                | Oil & Gas Producers                                |
| SMIN.L        | Smiths Group         | Industrial Engineering                             |
| SN.L          | Smith & Nephew       | Health Care Equipment & Services                   |
| SPX.L         | Spirax Group         | Industrial Engineering                             |
| SSE.L         | SSE                  | Electrical Utilities & Independent Power Producers |
| STAN.L        | Standard Chartered   | Banks  |
| STJ.L         | St. James's Place    | Financial Services                                 |
| TW.L          | Taylor Wimpey        | Household Goods & Home Construction                |
| TSCO.L        | Tesco                | Food & Drug Retailing                              |
| ULVR.L        | Unilever             | Personal Goods                                     |

| Symbol | Name             | Industry                      |
|--------|------------------|-------------------------------|
| UU.L   | United Utilities | Multiline Utilities           |
| UTG.L  | Unite Group      | Real Estate Investment Trusts |
| VOD.L  | Vodafone Group   | Mobile Telecommunications     |
| WEIR.L | The Weir Group   | Industrial Goods and Services |
| WTB.L  | Whitbread        | Retail Hospitality            |
| WPP.L  | WPP              | Media                         |

## D.2 Commodities

The commodities market includes a variety of physical goods that are traded on exchanges. The following table lists a sample of 6 commodities:

Table D.4: List of 6 Commodities chosen for the portfolio.

| Symbol | Name        |
|--------|-------------|
| CL=F   | Crude Oil   |
| NG=F   | Natural Gas |
| GC=F   | Gold        |
| SI=F   | Silver      |
| ALI=F  | Aluminum    |
| HG=F   | Copper      |

## D.3 Currencies

The currencies market includes a variety of currency pairs that are traded on exchanges. The following table lists a sample of 10 currency pairs, selected for their trading volume.

Note that the trading symbols all have United States Dollar (USD) as the quote currency.

Table D.5: List of 10 currency pairs chosen for the portfolio.

| Symbol   | Name                        |
|----------|-----------------------------|
| EURUSD=X | Euro (EUR)/USD              |
| GBPUSD=X | British Pound (GBP)/USD     |
| JPYUSD=X | Japanese Yen (JPY)/USD      |
| AUDUSD=X | Australian Dollar (AUD)/USD |
| CADUSD=X | Canadian Dollar (CAD)/USD   |
| CNYUSD=X | Chinese Yuan (CNY)/USD      |
| CHFUSD=X | Swiss Franc (CHF)/USD       |
| HKDUSD=X | Hong Kong Dollar (HKD)/USD  |
| KRWUSD=X | South Korean Won (KRW)/USD  |
| INRUSD=X | Indian Rupee (INR)/USD      |



## Appendix E

# Default Hyper-parameter Selection

The choice of hyper-parameters is crucial for the performance of DRL algorithms. However, it is computationally expensive to perform hyper-parameter tuning for all combinations of algorithms, datasets and environment representations. Therefore, the default hyper-parameters used in the experiments are outlined in Table C.2. These hyper-parameters were selected based on preliminary tests conducted on a small dataset of five tickers (AAPL, CSCO, HON, MSFT, V) sampled from the DJIA and only the open, close, high and low prices as the environment representation.

The hyper-parameters were tuned according to the specifications in Table C.1 and the results were used to inform the default settings, outlined in Table C.2. For each of the five DRL algorithms, the hyper-parameter search was performed using Bayesian optimisation using the `wandb` library and a maximum number of runs set to 20. The training set was data from January 2016 to December 2022, the validation set started in January 2023 and ended in December 2023, and the test set was between January 2024 and June 2025. The dataset split is visualised in Figure E.1.

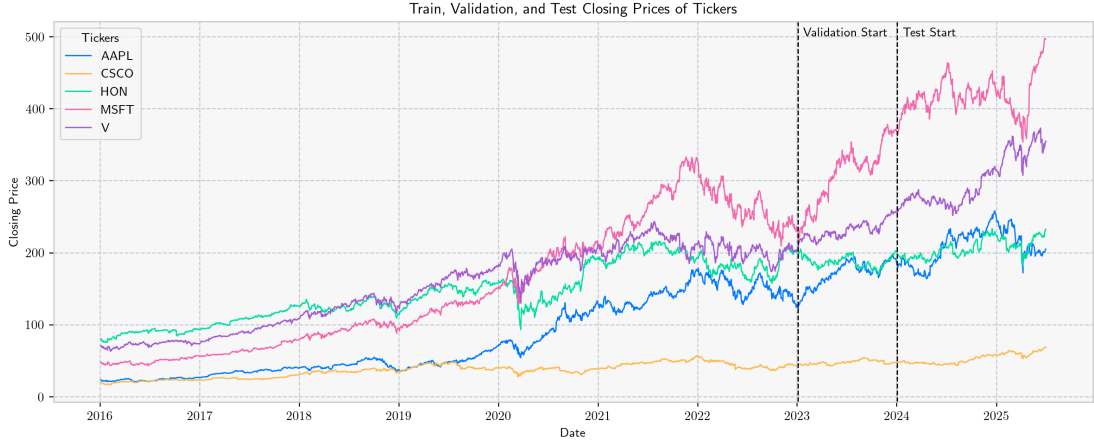


Figure E.1: Train-Validation-Test Split for the Hyper-parameter tuning on a sample of five assets from the Dow Jones Industrial Average index.

The **wandb** library provides an interactive website to visualise the results of the hyper-parameters in terms of the metric chosen for the optimisation and, if applicable, any other metrics that were chosen to be reported. In this case, the optimisation metric was the Sharpe ratio, as it balances the trade-off between risk and return, and additionally, the cumulative return was also reported. Figure E.2 shows the reported results for the hyper-parameter tuning of the A2C algorithm. Within the figure, there are three charts where the left one shows the Sharpe ratio over all sweeps, the middle one shows the cumulative return, and the right one shows the hyper-parameters that were tuned and the resulting optimisation metric.



Figure E.2: Hyper-parameter tuning results for the A2C algorithm.

The hyper-parameter tuning process was repeated for the other four algorithms, resulting in the hyper-parameters shown in Table C.2. Since the search had been done in the validation dataset, the best-performing models were evaluated and benchmarked against the test dataset to assess their generalisation performance, whose results are presented in Table E.1.

Table E.1: Results of hyper-parameter tuning on the test dataset.

| <b>Dataset</b>  | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|-----------------|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>A2C</b>      | 0.2598                       | 0.1679                       | 0.1968                           | 0.8859                  | -0.2186                 |
| <b>PPO</b>      | 0.3375                       | 0.2158                       | 0.1697                           | 1.2364                  | -0.1630                 |
| <b>DDPG</b>     | 0.3494                       | 0.2231                       | 0.1763                           | 1.2300                  | -0.1684                 |
| <b>TD3</b>      | 0.3401                       | 0.2174                       | 0.1731                           | 1.2227                  | -0.1598                 |
| <b>SAC</b>      | 0.2659                       | 0.1717                       | 0.1762                           | 0.9866                  | -0.1825                 |
| <b>Mean</b>     | 0.1503                       | 0.0989                       | 0.1896                           | 0.5923                  | -0.1972                 |
| <b>Min</b>      | 0.3609                       | 0.2308                       | 0.1681                           | 1.3193                  | -0.1559                 |
| <b>Momentum</b> | 0.1635                       | 0.1074                       | 0.1868                           | 0.6396                  | -0.2025                 |
| <b>Equal</b>    | 0.3123                       | 0.2010                       | 0.1758                           | 1.1290                  | -0.1762                 |

## Appendix F

# Experiment Results

In this Appendix, the results of the experiments conducted to evaluate the performance of the implemented algorithms under changing conditions are presented. Only the tables that do not fit in the main Results chapter 4 are included here.

### F.1 Experiment: Algorithm Comparison

The following tables summarise the results of the algorithm comparison experiment conducted on the 5 datasets with OHLCV prices as the environment representation. The results for the A2C algorithm are presented in Table 4.1 in Section 4.4.1, whereas for the PPO, DDPG, TD3 and SAC algorithms, the results are presented in the following tables.

Table F.1: Algorithm comparison results for the PPO implementation.

| <b>Dataset</b>      | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|---------------------|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>Dow Jones 30</b> | 0.2035                       | 0.3174                       | 0.1461                           | 1.3410                  | -0.1503                 |

| <b>Dataset</b>       | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|----------------------|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>Euro Stoxx 50</b> | 0.1557                       | 0.2438                       | 0.1549                           | 1.0117                  | -0.1706                 |
| <b>FTSE 100</b>      | 0.1246                       | 0.1931                       | 0.1244                           | 1.0063                  | -0.1315                 |
| <b>Commodities</b>   | 0.2531                       | 0.3990                       | 0.1941                           | 1.2600                  | -0.1522                 |
| <b>Currencies</b>    | -0.0011                      | -0.0017                      | 0.0493                           | 0.0014                  | -0.0726                 |

Table F.2: Algorithm comparison results for the DDPG implementation.

| <b>Dataset</b>       | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|----------------------|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>Dow Jones 30</b>  | 0.2206                       | 0.3454                       | 0.1526                           | 1.3826                  | -0.1560                 |
| <b>Euro Stoxx 50</b> | 0.1292                       | 0.2011                       | 0.1556                           | 0.8592                  | -0.1774                 |
| <b>FTSE 100</b>      | 0.1336                       | 0.2076                       | 0.1229                           | 1.0822                  | -0.1248                 |
| <b>Commodities</b>   | 0.2168                       | 0.3391                       | 0.1811                           | 1.1745                  | -0.1237                 |
| <b>Currencies</b>    | 0.0014                       | 0.0021                       | 0.0559                           | 0.0528                  | -0.0802                 |

Table F.3: Algorithm comparison results for the TD3 implementation.

| <b>Dataset</b>       | <b>Cumulative<br/>return</b> | <b>Annualised<br/>return</b> | <b>Annualised<br/>volatility</b> | <b>Sharpe<br/>ratio</b> | <b>Max<br/>drawdown</b> |
|----------------------|------------------------------|------------------------------|----------------------------------|-------------------------|-------------------------|
| <b>Dow Jones 30</b>  | 0.2478                       | 0.3902                       | 0.1567                           | 1.4911                  | -0.1567                 |
| <b>Euro Stoxx 50</b> | 0.1547                       | 0.2423                       | 0.1487                           | 1.0420                  | -0.1645                 |
| <b>FTSE 100</b>      | 0.1325                       | 0.2058                       | 0.1231                           | 1.0729                  | -0.1263                 |
| <b>Commodities</b>   | 0.2768                       | 0.4386                       | 0.1792                           | 1.4537                  | -0.1224                 |
| <b>Currencies</b>    | 0.0026                       | 0.0038                       | 0.0438                           | 0.0807                  | -0.0639                 |

Table F.4: Algorithm comparison results for the SAC implementation.

| Dataset              | Cumulative<br>return | Annualised<br>return | Annualised<br>volatility | Sharpe<br>ratio | Max<br>drawdown |
|----------------------|----------------------|----------------------|--------------------------|-----------------|-----------------|
| <b>Dow Jones 30</b>  | 0.1457               | 0.2243               | 0.1508                   | 0.9769          | -0.1750         |
| <b>Euro Stoxx 50</b> | 0.1761               | 0.2771               | 0.1520                   | 1.1437          | -0.1718         |
| <b>FTSE 100</b>      | 0.1319               | 0.2048               | 0.1279                   | 1.0326          | -0.1404         |
| <b>Commodities</b>   | 0.0027               | 0.0041               | 0.0480                   | 0.0806          | -0.0704         |
| <b>Currencies</b>    | 0.2563               | 0.4044               | 0.1778                   | 1.3727          | -0.1356         |

## F.2 Experiment: Environment Representation

The table F.5 summarises the performance, according to the cumulative return, of the five algorithms in the four possible different environment representations: OHLCV prices, OHLCV prices with indicators, OHLCV prices with covariance, and OHLCV prices with indicators and covariance. The results are presented for three datasets: DowJones30, Commodities, and Currencies.

Table F.5: Environment representation experiment comparison according to the cumulative return. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset.

| Algorithm  | Dataset     | Simple  | Indicators | Covariance | Complete |
|------------|-------------|---------|------------|------------|----------|
| <b>A2C</b> | DowJones30  | 0.3387  | 0.3139     | 0.3464     | 0.3239   |
|            | Commodities | 0.3695  | 0.4133     | 0.3883     | 0.4098   |
|            | Currencies  | -0.0017 | -0.0071    | -0.0069    | -0.0023  |
| <b>PPO</b> | DowJones30  | 0.3174  | 0.2937     | 0.3221     | 0.2713   |
|            | Commodities | 0.3990  | 0.3565     | 0.3689     | 0.3751   |

| Algorithm   | Dataset     | Simple  | Indicators | Covariance | Complete |
|-------------|-------------|---------|------------|------------|----------|
|             | Currencies  | -0.0017 | 0.0033     | 0.0029     | 0.0083   |
| <b>DDPG</b> | DowJones30  | 0.3454  | 0.3663     | 0.3128     | 0.3301   |
|             | Commodities | 0.3391  | 0.3339     | 0.3616     | 0.4211   |
|             | Currencies  | 0.0021  | 0.0032     | -0.0002    | -0.0006  |
| <b>TD3</b>  | DowJones30  | 0.3902  | 0.3456     | 0.2571     | 0.2787   |
|             | Commodities | 0.4386  | 0.3632     | 0.3292     | 0.4312   |
|             | Currencies  | 0.0038  | -0.0022    | -0.0023    | -0.005   |
| <b>SAC</b>  | DowJones30  | 0.2243  | 0.3189     | 0.3774     | 0.3162   |
|             | Commodities | 0.4044  | 0.3371     | 0.3958     | 0.3025   |
|             | Currencies  | 0.0041  | 0.0114     | -0.0117    | 0.0179   |

## Appendix G

# Explainability Results

### G.1 Feature Importance

Figure G.1 shows the top features grouped by asset according to the feature importance of the surrogate model.

Figure G.2 shows the mean feature importance for each type of feature, i.e. open, close, high and low prices, over the assets.



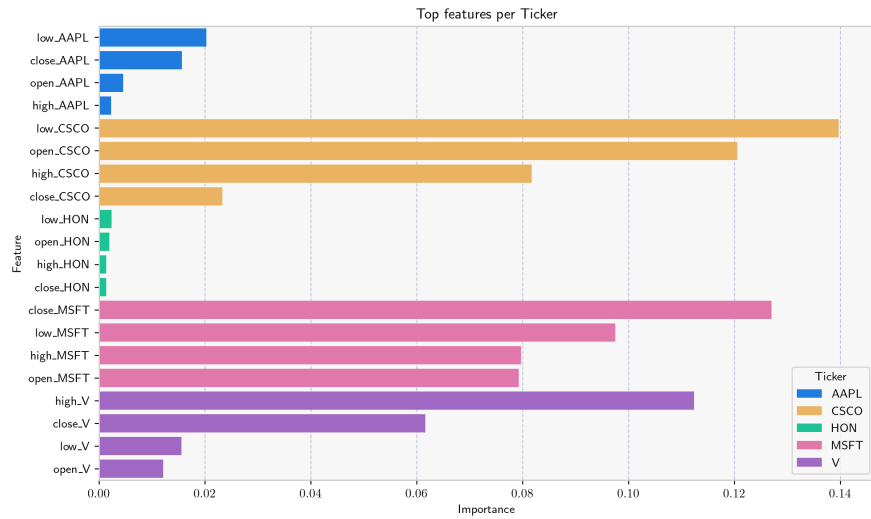


Figure G.1: Top features grouped by asset from the surrogate model according to feature importance.

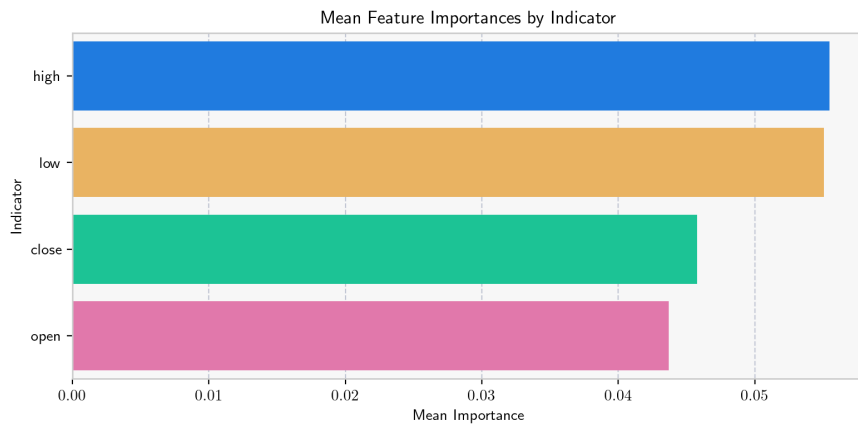


Figure G.2: Mean feature importance per type of feature from the surrogate model.

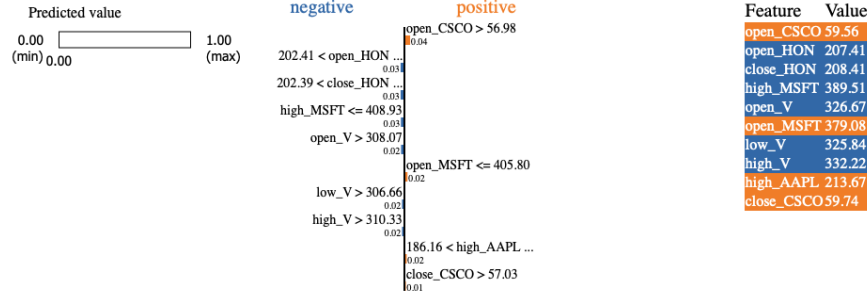


Figure G.3: LIME explanations for the A2C algorithm for a specific observation in the test dataset for the AAPL asset.

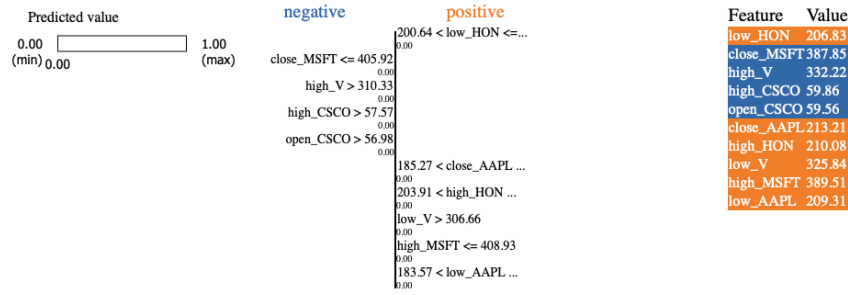


Figure G.4: LIME explanations for the A2C algorithm for a specific observation in the test dataset for the CSCO asset.

## G.2 Local Importance Model-Agnostic Explanation Results

With the LIME analysis, the explanations for the A2C algorithm are provided. Since these are local observations, the following figures provide the explanation for the first time step on the test dataset of the assets not included in the main text. Values coloured in orange represent features that contribute positively to the prediction, while blue values indicate features that contribute negatively.

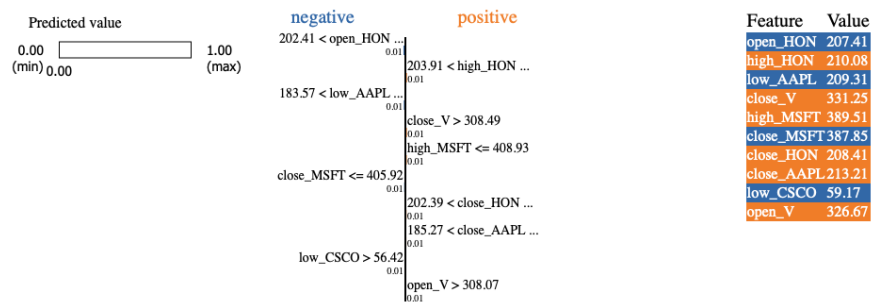


Figure G.5: LIME explanations for the A2C algorithm for a specific observation in the test dataset for the HON asset.

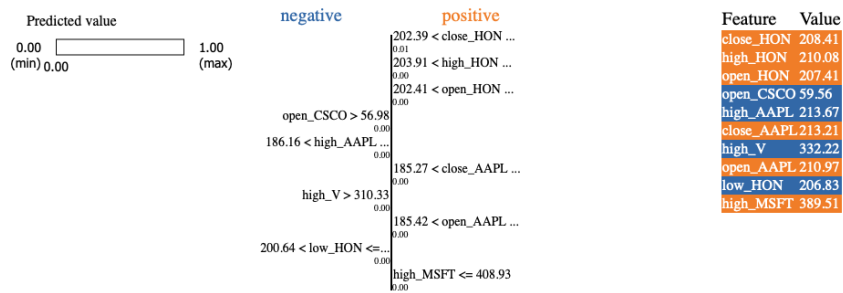


Figure G.6: LIME explanations for the A2C algorithm for a specific observation in the test dataset for the V asset.