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Explainable Deep Reinforcement Learning for Portfolio Optimisation of Financial Assets

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Abstract

The dynamic and stochastic nature of financial markets together with the highly nonstationary and noisy financial time series data make the task of portfolio optimisation particularly challenging. However, their nature makes them particularly well-suited for Deep Reinforcement Learning (DRL) algorithms, which can learn a trading strategy directly from the environment. Nonetheless, there are still significant challenges preventing its widespread adoption in the financial industry, such as difficulty in finding the appropriate algorithm with a suitable reward function and lack of transparency and interpretability. This thesis proposes an explainable DRL model for portfolio optimisation with the ability to leverage historical data to learn the optimal trading strategy that balances return maximisation and risk minimisation. Five prominent DRL algorithms are implemented and their performance is evaluated in different scenarios, including the impact of a larger financial environment representation, portfolio size and asset composition. Once the algorithms are trained, post-hoc explainability techniques are applied to understand which market conditions lead to a particular portfolio allocation. Although the performance of the algorithms does not generally outperform all of the benchmarks, the results show that the agents are a powerful tool in portfolio management capable of learning from high-dimensional data and adapting to changing market conditions. The crucial contribution of this research lies in the explainability framework, particularly the use of SHapley Additive exPlanations (SHAP) to provide insights into the decisionmaking process over the testing period in conjunction with interpretation for specific trading days.

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Table of Contents

1	Intr	oducti	ion	1
	1.1	Objec	tives	3
	1.2	Repor	t Structure	4
2	Bac	kgrou	nd	6
	2.1	Portfo	lio Optimisation	6
		2.1.1	Modern Portfolio Theory	7
	2.2	Deep 2	Reinforcement Learning	9
		2.2.1	Reinforcement Learning	10
		2.2.2	Deep Reinforcement Learning Algorithms	16
	2.3	Expla	inable Artificial Intelligence	23
		2.3.1	Feature Importance	25
		2.3.2	Local Interpretable Model-agnostic Explanations	25
		2.3.3	Shapley Additive Explanations	27
	2.4	State	of the Art of Deep Learning and Explainability for Portfolio Opti-	
		misati	on	32
3	Met	thodol	ogy	36
	3.1	Proble	em Definition	36
	3.2	Marko	ov Decision Process Model	37

	3.3	Deep Reinforcement Learning Algorithms	40
		3.3.1 Hyper-parameter tuning	40
	3.4	Post-hoc Explainability	41
		3.4.1 Surrogate Model Explainability	42
		3.4.2 Direct Model Explainability	43
4	Res	ulte	45
-1			
	4.1	Dataset	45
	4.2	Experiment Design	47
	4.3	Evaluation	51
		4.3.1 Performance Metrics	51
		4.3.2 Benchmark Strategies	52
	4.4	Experiment: Algorithm Comparison	53
	4.5	Experiment: Environment Representation	57
	4.6	Experiment: Hyper-parameter Tuning	59
	4.7	Explainability Results	61
		4.7.1 Feature Importance Results	62
		4.7.2 Local Interpretable Model-agnostic Explanations Results	63
		4.7.3 Shapley Additive Explanations Results	64
5	Leg	al, Social, Ethical and Professional Issues	68
	5.1	Legal Issues	68
	5.2	Social Issues	69
	5.3	Ethical Issues	
			70
	5.4	Professional Issues	71
6	Con	nclusion	72
	6.1	Future Work	73

Re	efere	nces	75
\mathbf{A}	Alge	orithms	85
	A.1	Deep Reinforcement Learning Algorithms	85
	A.2	Explainability Algorithms	91
В	Stat	te Representation	92
	B.1	Technical Indicators	92
	B.2	Macroeconomic Indicators	97
\mathbf{C}	Нур	per-parameter tuning	99
D	Dat	asets	101
	D.1	Equities	101
		D.1.1 Dow Jones 30	101
		D.1.2 Euro Stoxx 50	103
		D.1.3 FTSE 100	107
	D.2	Commodities	112
	D.3	Currencies	112
\mathbf{E}	Defa	ault Hyper-parameter Selection	114
\mathbf{F}	Eva	luation Metrics	117
\mathbf{G}	Exp	eriment Results	120
	G.1	Experiment: Algorithm Comparison	120
	G.2	Experiment: Environment Representation	122
н	Exp	lainability Results	124
	H.1	Feature Importance	124

	H.2	Local Importance Model-Agnostic Explanation Results	126
Ι	Cod	le	128
	I.1	Configuration Module	131
	I.2	Data Download and Pre-processing Module	142
	I.3	Agents Module	152
	I.4	Environments Module	156
	I.5	Benchmarking Module	163
	I.6	Explainability Module	168
	I.7	Visualisation Module	180
	I.8	Optimisation Module	196
	10	Examples	200

List of Figures

2.1	Efficient Frontier in Risk-Return Space. [1]	9
2.2	Agent interaction with environment	11
2.3	Markov Decision Process with policy, transition, and reward functions $$	12
2.4	Taxonomy of Reinforcement Learning Algorithms [2]	17
2.5	Taxonomy of Explainable Artificial Intelligence Methods [3] $\dots \dots$	24
4.1	Evolution of the Cumulative Returns for the DowJones30 dataset with the OHLCV prices and indicators environment representation	55
4.2	Top features from the surrogate model according to feature importance	62
4.3	Mean feature importance per asset from the surrogate model	63
4.4	LIME explanations for the A2C algorithm at the first time step of the test dataset for the MSFT asset. The orange bars indicate features that contribute positively to the prediction, while the blue bars indicate features that contribute negatively	64
4.5	Beeswarm SHAP explanations for the A2C algorithm for the AAPL asset. The x-axis represents the SHAP values, whilst the y-axis represents the top features. The colour indicates the feature value, with magenta being high and blue being low	65
4.6	SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm	66
4.7	SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm	67

4.8	SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm at the first time step of the test dataset
E.1	Train-Validation-Test Split for the Hyper-parameter tuning on a sample of five assets from the Dow Jones Industrial Average index
E.2	Hyper-parameter tuning results for the A2C algorithm
H.1	Top features grouped by asset from the surrogate model according to feature importance
H.2	Mean feature importance per type of feature from the surrogate model 125
Н.3	LIME explanations for the A2C algorithm at the first time step of the test dataset for the AAPL asset
H.4	LIME explanations for the A2C algorithm at the first time step of the test dataset for the CSCO asset
H.5	LIME explanations for the A2C algorithm at the first time step of the test dataset for the HON asset
H.6	LIME explanations for the A2C algorithm at the first time step of the test dataset for the V asset

List of Tables

2.1	Comparison of Deep Reinforcement Learning Algorithms	23
4.1	Train-Validation-Test Split for each dataset	47
4.2	Default hyper-parameter configurations	48
4.2	Default hyper-parameter configurations	49
4.3	Summary of experiments conducted	50
4.4	Algorithm comparison results for the A2C implementation	54
4.5	Algorithm comparison results for the DowJones30 dataset. The colour correspond to the best performing configurations, with blue for the best performing DRL algorithm and green for the best benchmark	56
4.6	Environment representation experiment comparison according to the Sharpe ratio. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset	57
4.6	Environment representation experiment comparison according to the Sharpe ratio. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset	58
4.7	Hyper-parameter tuning experiment results for the DowJones30 dataset with simple environment representation	59
4.8	Hyper-parameter tuning experiment results for the DowJones30 dataset with indicators environment representation	60
C.1	Hyper-parameter tuning configurations for different RL algorithms, 1	100

D.1	Constituents of the Dow Jones Industrial Average index as of April 2025.	
	[4]	103
D.2	Constituents of the Euro Stoxx 50 index as of April 2025. [5]	107
D.3	Constituents of the FTSE100 index as of April 2025. [6]	112
D.4	6 Commodities Futures Contracts	112
D.5	10 Currency Pairs	113
E.1	Results of hyper-parameter tuning on the test dataset	116
G.1	Algorithm comparison results for the PPO implementation	121
G.2	Algorithm comparison results for the DDPG implementation	121
G.3	Algorithm comparison results for the TD3 implementation	121
G.4	Algorithm comparison results for the SAC implementation	122
G.5	Environment representation experiment comparison according to the cumulative return. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset	122
G.5	Environment representation experiment comparison according to the cumulative return. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities	
	dataset	123

List of Algorithms

1	Advantage Actor-Critic (A2C) Pseudo-code	86
2	Proximal Policy Optimisation (PPO) Pseudo-code	87
3	Deep Deterministic Policy Gradient (DDPG) Pseudo-code	88
4	Twin Delayed Deep Deterministic Policy Gradient (TD3) Pseudo-code	89
5	Soft Actor-Critic (SAC) Pseudo-code	90
6	Shapley Value Approximation	91

Nomenclature

Numbers and Arrays

a Scalar

a Vector

A Matrix

1 Matrix of 1's

\mathbf{Sets}

A Set

 \mathbb{R} Set of real numbers

[a,b] Real interval including a and b

(a, b) Real interval excluding a and b

[a, b) Real interval including a but excluding b

(a, b] Real interval excluding a but including b

 $\{0,1\}$ Set containing 0 and 1

 $\{0,1,...,n\}$ Set of all integers between 0 and n inclusive

Ø Empty set

 $\mathbb{A} \subset \mathbb{B}$ Set \mathbb{A} is a subset of set \mathbb{B}

 $\mathbb{A} \subseteq \mathbb{B}$ Set \mathbb{A} is a subset or equal to set \mathbb{B}

 $\mathbb{A} \cap \mathbb{B}$ Intersection of sets \mathbb{A} and \mathbb{B}

 $\mathbb{A} \cup \mathbb{B}$ Union of sets \mathbb{A} and \mathbb{B}

 $\mathbb{A} \setminus \mathbb{B}$ Set difference of sets \mathbb{A} and \mathbb{B}

Indexing

 a_i Element i of vector **a**, with indexing start at 1

 $A_{i,j}$ Element i, j of matrix **A**, with indexing start at 1

Algebra Operations

 \mathbf{A}^T Transpose of matrix \mathbf{A}

 \mathbf{A}^{-1} Inverse of matrix \mathbf{A}

Probability

P(x) Probability distribution over a random variable x

E[x] Expected value of random variable x

Var[x] Variance of random variable x

Cov[x, y] Covariance of random variables x and y

 μ Mean

 σ Standard deviation

 σ^2 Variance

 Σ Covariance matrix

 $\mathcal{N}(\mu, \sigma^2)$ Normal distribution with mean μ and variance σ^2

 $\mathcal{N}(0,1)$ Standard normal distribution

Functions

 $f: \mathbb{A} \to \mathbb{B}$ Function f with domain \mathbb{A} and range \mathbb{B}

f(x) Function f evaluated at x

 $f(x;\theta)$ Function f with parameters θ evaluated at x

f'(x) Derivative of function f

 $\int f(x) dx$ Integral of function f with respect to x

 $\min f(x)$ Minimum of function f

 $\min_{x} f(x)$ Minimum of function f with respect to x

 $\max f(x)$ Maximum of function f

 $\max_{x} f(x)$ Maximum of function f with respect to x

 $\log x$ Natural logarithm of x

x! Factorial of x

Markov Decision Process

t Time step

 \mathcal{S} State space

 S_t Observation of the state at time step t

 \mathcal{A} Action space

 a_t Action taken at time step t

R(s, a, s') Reward function

 r_t Reward received at time step t

T(s, a, s') Transition function

 γ Discount factor

 π Policy

G Long-term reward

 V^{π} State Value function for policy π

 Q^{π} State-Action Value function for policy π

 A^{π} Advantage function for policy π

Other Symbols

∀ For all

- \in Element of
- ∇ Gradient
- \sum Summation symbol

Glossary

- Advantage Actor-Critic Algorithm that uses both an actor (policy) and a critic (value function) to learn optimal policies by estimating the advantage of actions taken.
- **Algorithmic Trading** Use of computer algorithms to automate trading decisions and execute trades in financial markets.
- **Artificial Intelligence** Simulation of human intelligence processes by machines enabling them to perform tasks that typically require human intelligence, such as visual perception, speech recognition, decision-making, and language translation.
- **Bellman Equations** Set of equations that describe the relationship between the value of a state or action and the values of subsequent states or actions in dynamic programming and reinforcement learning.
- **Black Box** Term used to describe a system or model whose internal workings are not transparent or easily understood.
- **Deep Deterministic Policy Gradient** Algorithm that uses deep neural networks to learn policies for continuous action spaces, combining the benefits of deep learning and policy gradient methods.
- **Deep Learning** Subset of machine learning that uses neural networks with many layers to learn from large amounts of data, enabling the model to automatically learn complex patterns and representations.
- **Deep Neural Network** Type of artificial neural network with a succession of layers of non-linear transformations capable of learning a representation of the data with various levels of abstraction.

- **Deep Reinforcement Learning** Combination of deep learning and reinforcement learning, where deep neural networks are used to approximate the value function or policy in reinforcement learning tasks.
- Efficient Frontier Set of optimal portfolios that offer the highest expected return for a given level of risk, or the lowest risk for a given level of expected return, in the context of portfolio optimisation.
- **Entropy** Measure of uncertainty or randomness in a system, often used in the context of information theory and reinforcement learning to encourage exploration.
- **Explainable Artificial Intelligence** Methods and techniques in the application of artificial intelligence that make the results of the models understandable by humans, providing insights into how decisions are made.
- **Exploitation** Process of leveraging known information to make decisions or take actions that are expected to yield the highest reward.
- **Exploration** Process of investigating and experimenting with different actions or strategies to discover their effects and improve decision-making.
- **Feature Importance** Technique for determining the contribution of each feature in a machine learning model to its predictions, helping to identify which features are most influential.
- **Financial Markets** Marketplaces where people trade financial securities, commodities, and other fungible items of value at low transaction costs and at prices that reflect supply and demand.
- **Hyper-parameter** Parameter that is set before the learning process begins and control the learning process of a machine learning model, such as learning rate, batch size, and number of layers in a neural network.
- Local Interpretable Model-agnostic Explanations Technique for explaining the predictions of any machine learning model by approximating it with a locally interpretable model, allowing users to understand the model's behaviour in a specific instance.
- Machine Learning Subset of artificial intelligence that enables systems to learn from data and improve their performance over time without being explicitly programmed.

- Markov Decision Process Mathematical model for sequential-decision making where the outcomes are uncertain, characterised by states, actions, rewards and a transition function.
- Mean-Variance Optimisation Investment strategy that aims to construct a portfolio of assets that maximises expected return for a given level of risk, or minimises risk for a given level of expected return.
- Modern Portfolio Theory Investment theory that aims to construct a portfolio of assets that maximises expected return for a given level of risk, or minimises risk for a given level of expected return, through diversification.
- Partially Observable Markov Decision Process Extension of Markov Decision Process where the agent does not have access to the complete state information, requiring the use of belief states or observations to make decisions.
- **Portfolio Optimisation** Process of selecting the best distribution of assets in a portfolio to achieve specific investment goals, such as maximising returns or minimising risk, while considering constraints and preferences.
- **Proximal Policy Optimisation** Algorithm that optimises policies by ensuring that updates to the policy are not too large, maintaining a balance between exploration and exploitation.
- Python Interpreted, object-oriented, high-level programming language.
- **Reinforcement Learning** Subset of machine learning where an agent learns to make decisions by taking actions in an environment to maximise cumulative reward.
- **Reward Function** Function that defines the feedback signal received by an agent in reinforcement learning, guiding the agent's learning process by providing rewards or penalties based on its actions.
- **SHapley Additive exPlanations** Method for interpreting machine learning models by assigning each feature an importance value for a particular prediction, based on cooperative game theory.
- **Soft Actor-Critic** Algorithm that combines the benefits of off-policy learning and entropy regularisation, allowing for more exploration and better stability in learning policies for continuous action spaces.

- **Supervised Learning** Machine learning task where a model is trained on labelled data to learn a mapping from inputs to outputs.
- Twin Delayed Deep Deterministic Policy Gradient Extension of Deep Deterministic Policy Gradient that addresses the overestimation bias in value function estimation by using two critic networks and delaying policy updates.
- **Unsupervised Learning** Machine learning task where a model learns patterns or structures in unlabelled data without explicit supervision.

Acronyms

A2C Advantage Actor-Critic.

A3C Asynchronous Advantage Actor-Critic.

ADX Average Directional Index.

AI Artificial Intelligence.

AI Act Artificial Intelligence Act.

ATR Average True Range.

AUD Australian Dollar.

BCS British Computer Society.

BXY British Pound Currency Index.

CAD Canadian Dollar.

CCI Commodity Channel Index.

CHF Swiss Franc.

CNY Chinese Yuan.

DDPG Deep Deterministic Policy Gradient.

DJIA Dow Jones Industrial Average.

DL Deep Learning.

DNN Deep Neural Network.

DPG Deterministic Policy Gradient.

DQN Deep Q-Network.

DRL Deep Reinforcement Learning.

DW30 Dow Jones 30 Index.

DX Directional Movement Index.

DXY U.S. Dollar Index.

EMA Exponential Moving Average.

EU European Union.

EUR Euro.

Euro Stoxx 50 Euro Stoxx 50 Index.

EXY Euro Index.

FCA Financial Conduct Authority.

FTSE 100 Financial Times Stock Exchange 100 Index.

FVX 5-Year Treasury Yield.

GBP British Pound.

HKD Hong Kong Dollar.

HTML HyperText Markup Language.

IET The Institution of Engineering and Technology.

INR Indian Rupee.

IRX 3-Month Treasury Yield.

JPY Japanese Yen.

KRW South Korean Won.

LIME Local Interpretable Model-agnostic Explanations.

LLM Large Language Model.

LSTM Long Short-Term Memory.

MACD Moving Average Convergence Divergence.

MAPE Mean Absolute Percentage Error.

MDI Negative Directional Index.

MDP Markov Decision Process.

MiFID II Markets in Financial Instruments Directive II.

ML Machine Learning.

 \mathbf{MPT} Modern Portfolio Theory.

MSE Mean Squared Error.

MVO Mean-Variance Optimisation.

OHLCV Open, High, Low, Close, Volume.

PCA Principal Component Analysis.

PDI Positive Directional Index.

POMDP Partially Observable Markov Decision Process.

PPO Proximal Policy Optimisation.

RL Reinforcement Learning.

ROC Rate of Change.

RSI Relative Strength Index.

S&P 500 Standard and Poor's 500 Index.

SAAC Synchronous Advantage Actor Critic.

SAC Soft Actor-Critic.

SHAP SHapley Additive exPlanations.

 ${\bf SMA}$ Simple Moving Average.

 ${\bf TD3}\,$ Twin Delayed Deep Deterministic Policy Gradient.

 \mathbf{TNX} 10-Year Treasury Yield.

TRPO Trust Region Policy Optimisation.

U.S. United States.

 ${f UK}$ United Kingdom.

USD United States Dollar.

VaR Value at Risk.

VIX Volatility Index.

VXD Volatility DW30.

XAI Explainable Artificial Intelligence.

Chapter 1

Introduction

Financial markets are highly complex systems influenced by numerous factors, including financial and political events, social trends and technological advancements. Moreover, their evolving and stochastic nature requires using the most advance computational developments to model the financial environment. The tasks of financial time series prediction and portfolio optimisation are considerably intricate, due to the semi-strong form of market efficiency and the high level of noise. [7]

Algorithmic trading focuses on the application of analytical methods to automatically execute trading actions based on an algorithm without human intervention. Initially, the field mainly studied the usage of a computer program to follow a predefined strategy [8]. More recently, algorithmic trading involves environment perception by learning feature representation from highly non-stationary and noisy financial time series data, and decision-making by exploring the environment and simultaneously taking actions without supervision [9].

Machine Learning (ML) has an advantage for the task due to its ability to learn from historical data and make predictions about the future state of an environment. Research has explored the application of Deep Learning (DL) in future price prediction of financial assets [10, 11, 7, 12]. However, its main disadvantage is the inability to directly deal with trading, requiring an additional step to convert the predictions into actionable strategies. In contrast, Reinforcement Learning (RL) allows the algorithm to learn a trading strategy directly from the environment, without the need for a separate step [13, 14]. In this case, there are two main approaches: first, the algorithm can learn the amount of assets to buy, sell or hold at each time step [15], or second, the algorithm can learn the optimal portfolio allocation and automatically rebalance the portfolio weights at each time step [16].

Despite the potential of RL in portfolio optimisation, its widespread adoption in the financial industry remains limited. This is primarily due to following challenges [17]:

- 1. difficulty in finding the appropriate algorithm with a suitable reward function and hyper-parameters to ensure efficiency and performance,
- 2. challenge of testing the algorithm in a real-world environment, and
- 3. lack of transparency of ML models, often referred to as black boxes, making it increasingly complex to interpret the algorithm's decisions.

In recent years, the rise in popularity of Artificial Intelligence (AI) and its widespread use have led to concerns regarding its decisions due to its black box nature. The concept of explainability in AI, known as Explainable Artificial Intelligence (XAI), refers to a model's ability to provide details and reasons to make itself understandable [18]. The term was first coined in 2016 to describe the need for users to effectively understand, trust and manage artificial intelligence applications [19]. The need for explainability becomes particularly relevant within the financial domain, where the regulatory framework requires transparency and accountability in automated decision-making. Various relevant applications, including volatility models [20], credit risk assessment [21] and portfolio

construction [17], have explored the concept of explainability in financial applications.

Consequently, this thesis will focus on addressing the aforementioned challenges by exploring the application of Deep Reinforcement Learning (DRL) to portfolio optimisation and implementing explainability techniques.

1.1 Objectives

The objective of this thesis is to develop an explainable Deep Reinforcement Learning model for portfolio optimisation. A DRL model has the ability to leverage historical financial data to learn an investment strategy that efficiently allocates financial assets while maximising expected returns and minimising risk. Moreover, the incorporation of advanced explainability techniques enhances the interpretability and transparency of the model's decision-making. This project aims to bridge the gap between cutting-edge machine learning techniques and their practical application in finance by addressing the challenges of algorithm selection, simulation of real-world scenarios, and black box nature of ML models.

First, DRL models, such as Advantage Actor-Critic (A2C), Proximal Policy Optimisation (PPO), Deep Deterministic Policy Gradient (DDPG), Twin Delayed Deep Deterministic Policy Gradient (TD3) and Soft Actor-Critic (SAC), will be implemented to learn the optimal portfolio allocation from high-dimensional environment representations. The algorithms will be trained on historical financial data, including technical and macroeconomic indicators, with the goal of capturing the complex market dynamics. Each of the algorithms is better suited to a particular scenario, for instance, DDPG encourages maximum returns, while A2C reduces the variance and PPO is better at balancing exploration versus exploitation.

Second, post-hoc explainability techniques: Feature Importance, Local Interpretable

Model-agnostic Explanations (LIME) and SHapley Additive exPlanations (SHAP) will be applied to interpret the model's decisions. The goal of these is to understand which market conditions, represented by financial data, lead to the actions/decisions, encoded as portfolio weights.

Finally, the performance of the DRL models will be analysed in different scenarios, including the impact of a larger financial environment representation, portfolio size and asset composition. The results will be compared with traditional portfolio optimisation methods to evaluate the effectiveness of the proposed approach.

1.2 Report Structure

This report is organised into six chapters, each of which focuses on a concrete area related to the problem. Additional material, together with source code, is included in the appendices.

The current chapter, 1, presents the motivation and the objectives of this thesis. It gives an overview of the potential of DRL in portfolio optimisation and its main challenges, particularly the lack of transparency of ML models.

Chapter 2 provides an overview of the theoretical background of the project, including portfolio allocation and concepts. The problem of portfolio optimisation in the financial domain is outlined and the potential of DRL in this context is discussed. The chapter provides a comprehensive background explanation of the fundamentals of Deep Learning and Reinforcement Learning, including the main algorithms (A2C, PPO, DDPG, TD3, SAC). In addition, it gives an overview of the post-hoc explainability techniques: Feature Importance, Local Interpretable Model-agnostic Explanations (LIME) analysis and SHapley Additive exPlanations (SHAP) values, which will be used to interpret the model's decisions. Finally, it includes a comprehensive in-depth literature review on the

topics of ML applied to portfolio optimisation and relevant applications of explainability techniques.

The methodology, chapter 3, describes the techniques and methods used to tackle the problem and outlines the implementation of the proposed solution. The chapter provides a detailed explanation of the architecture and components of the proposed DRL model, including the state representation and reward function. Furthermore, given the trained algorithms, it describes the implementation of the post-hoc explainability techniques.

The results of the experiments are presented in chapter 4, which analyses and evaluates the results obtained from the proposed implementation, while critically discussing the findings. It provides a detailed comparison of the proposed DRL strategies with traditional portfolio optimisation methods. Furthermore, it consists of an in-depth analysis of the model's decisions using post-hoc explainability techniques, in particular, feature importance, LIME and SHAP.

Chapter 5 discusses the legal, social, ethical and professional implications within the context of the project. By addressing these issues, the project aims to ensure that the proposed solution adheres to industry standards, while considering the implications of the technology.

Finally, the report concludes with a summary of the main points of the work, the contributions made, the results achieved as well as potential applications and future work in chapter 6.

Chapter 2

Background

This chapter provides an overview of the problem of portfolio optimisation in the financial domain, followed by a comprehensive explanation of the fundamentals of Deep Learning (DL) and Reinforcement Learning (RL), including the relevant algorithms in the field of Deep Reinforcement Learning (DRL). In addition, it discusses the need for explainability in Machine Learning (ML) and the relevant post-hoc explainability techniques to achieve interpretable and transparent models. Finally, it presents the state of the art in portfolio optimisation using DRL and the recent advancements in explainability techniques in the field.

2.1 Portfolio Optimisation

Portfolio optimisation is the process of selecting optimal weights for a portfolio of assets in order to maximise expected returns for a given level of risk, or conversely, to minimise risk for a given level of expected returns [22]. In mathematical terms, the problem requires finding a solution to the specified objective function, which is typically a function of the expected returns and the risk associated with the portfolio [23]. The task becomes

further complicated if a time dimension is introduced, as the portfolio weights need to be adjusted over time to capture the changes in market conditions and asset prices [24].

2.1.1 Modern Portfolio Theory

There exist several traditional frameworks that formalise the problem of portfolio allocation. Markowitz's Modern Portfolio Theory (MPT) was proposed in 1952 [25] and it provides a mathematical framework where investors choose optimal portfolios based on risk and return, by either minimising the risk given a specified return or, maximising the return given a specified risk [26]. The theory extends the concept of diversification by suggesting that owning financial assets of different kinds is less risky than owning assets of the same kind, due to the correlations between assets.

The main assumptions in MPT are:

- investors are risk-averse, rational, and seek to maximise return for a given risk;
- returns are normally distributed;
- markets are frictionless, meaning there are no transaction costs; and
- assets are infinitely divisible.

Under these assumptions, portfolio risk and return can be modelled as an optimisation problem. Let $\mathbf{w} = (w_1, w_2, \dots, w_N)^T$ denote the portfolio weight vector, where each w_i indicates the proportion of capital allocated to asset i, subject to the budget constraint:

$$\sum_{i=1}^{N} w_i = 1 \quad \Leftrightarrow \quad \mathbf{w}^T \mathbf{1} = 1 \tag{2.1}$$

with $\mathbf{1} \in \mathbb{R}^N$ being a vector of ones, and subject to the non-negativity constraint,

meaning that short-selling is not allowed:

$$w_i \ge 0 \quad \forall i = 1, 2, \dots, N. \tag{2.2}$$

Let $\boldsymbol{\mu} = (R_1, R_2, \dots, R_N)^T$ represent the vector of expected returns, and $\Sigma \in \mathbb{R}^{N \times N}$ the covariance matrix of asset returns. The expected return of the portfolio is then given by:

$$R_p = \mathbf{w}^T \boldsymbol{\mu},\tag{2.3}$$

and the portfolio risk is quantified by the variance of returns:

$$\sigma_p^2 = \mathbf{w}^T \Sigma \mathbf{w}. \tag{2.4}$$

This formulation provides the foundation for solving the mean-variance optimisation problem, by either:

- minimising portfolio variance σ_p^2 subject to a target expected return R_p , or
- maximising expected return R_p subject to a risk constraint σ_p .

The Markowitz mean-variance optimisation problem can be expressed as:

$$\min_{\mathbf{w}} \quad \mathbf{w}^T \Sigma \mathbf{w}$$
subject to
$$\begin{cases}
\mathbf{w}^T \boldsymbol{\mu} = R_p \\
\mathbf{w}^T \mathbf{1} = 1 \\
\mathbf{w} \ge 0
\end{cases}$$
(2.5)

Solving for varying levels of target return leads to a set of optimal portfolios that form the efficient frontier. It is typically visualised in a risk-return space, where the x-axis

represents the risk (standard deviation) and the y-axis represents the expected return, as shown in Figure 2.1. Portfolios below the curve are sub-optimal, while those on the frontier represent the best achievable combinations of risk and return.

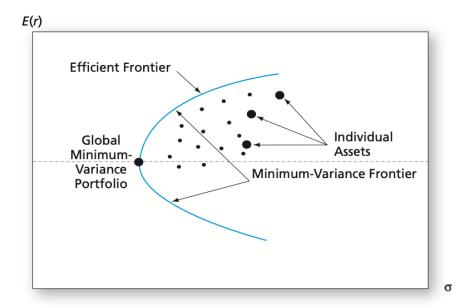


Figure 2.1: Efficient Frontier in Risk-Return Space. [1]

Despite the simplicity in the formulation of MPT, its assumptions do not reflect the behaviour of real markets. Modern financial markets are dynamic, non-stationary, and feature non-linear relationships, which have driven research into other approaches better suited to capture their complexities.

2.2 Deep Reinforcement Learning

Machine Learning is a branch of Artificial Intelligence (AI) that focuses on the use of data and algorithms to imitate the way humans learn by gradually improving their accuracy over time [27]. There are three main tasks in ML [28]:

• Supervised Learning: Task of training a classification or regression model from

labelled data, where the model learns to map inputs to outputs based on examples.

- Unsupervised Learning: Task of drawing inferences from datasets consisting of unlabelled data, where the model learns to identify patterns or structures in the data.
- Reinforcement Learning: Task of training an agent to sequentially make decisions by taking actions in an environment with the goal of maximising cumulative reward, using feedback from the environment to learn an optimal strategy.

Deep Learning is a set of methods and techniques to solve such ML tasks, specially in supervised and unsupervised learning tasks. DL focuses on the use of Deep Neural Networks (DNNs) [29], which are characterised by a succession of layers of non-linear transformations that allow the model to learn a representation of the data with various levels of abstraction.

Therefore, Deep Reinforcement Learning (DRL) combines Deep Learning (DL) and Reinforcement Learning (RL) to solve sequential decision-making problems with high-dimensionality in the environment representation. This approach has gained significant attention in recent years due to its success in various applications, including robotics [30] and game playing [31, 32].

2.2.1 Reinforcement Learning

As mentioned, RL is a type of ML that solves the problem of sequential decision-making through continuous interaction with an environment. The agent learns to take actions given a representation of the environment's state with the goal of optimising a predefined notion of reward. The agent learns by successively adjusting its policy based on its observations and interactions with the environment.

The RL problem can be formalised as a discrete-time stochastic control process where an agent interacts with the environment. At each time step t, the agent observes the state of the environment $s_t \in \mathcal{S}$, takes an action $a_t \in \mathcal{A}$ to obtain a reward $r_t \in \mathbb{R}$ and transition to a new state $s_{t+1} \in \mathcal{S}$, where \mathcal{S} is the state space and \mathcal{A} is the action space [28]. The agent's interaction with the environment is visually represented in Figure 2.2.

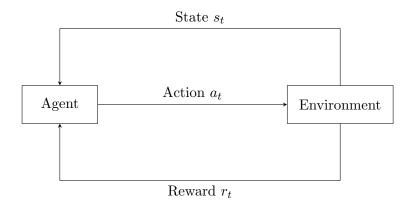


Figure 2.2: Agent interaction with environment

A discrete time stochastic control process can be formalised as a Markov Decision Process (MDP), if it fulfils the Markov Property.

Definition 2.2.1 (Markov Property). A discrete time stochastic control process satisfies the Markov Property if:

$$P(s_{t+1}|s_t, a_t) = P(s_{t+1}|s_t, a_t, s_{t-1}, a_{t-1}, \dots, s_0, a_0)$$
(2.6)

$$P(r_t|s_t, a_t) = P(r_t|s_t, a_t, s_{t-1}, a_{t-1}, \dots, s_0, a_0)$$
(2.7)

where $P(s_{t+1}|s_t, a_t)$ is the transition probability of moving to state s_{t+1} given the current state s_t and action a_t , and $P(r_t|s_t, a_t)$ is the reward function that defines the expected reward received at time t given the current state and action.

This implies that the state s_{t+1} at a future time step t+1 only depends on the current state s_t and action a_t . Similarly, the reward r_t only depends on the current state and

action and not on the history of previous states and actions. Consequently, a Markov Decision Process [33] is a discrete time stochastic control process defined as:

Definition 2.2.2 (Markov Decision Process). An MDP is a tuple $\mathcal{M} = (\mathcal{S}, \mathcal{A}, T, R, \gamma)$, where:

- S is the state space: $s_t \in S$,
- \mathcal{A} is the action space: $a_t \in \mathcal{A}$,
- $T: \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow [0,1]$ is the transition function,
- $R: \mathcal{S} \times \mathcal{A} \times \mathcal{S} \to \mathcal{R}$ is the reward function, where $\mathcal{R} \in [0, R_{max}]$ is the set of all possible rewards bounded by $R_{max} \in \mathbb{R}^+$, and
- $\gamma \in [0,1)$ is the discount factor.

At each time step, the probability of advancing to the next state s_{t+1} is given by the transition function $T(s_t, a_t, s_{t+1})$ and the reward r_t is given by the reward function $R(s_t, a_t, s_{t+1})$. This can be visualised in Figure 2.3.

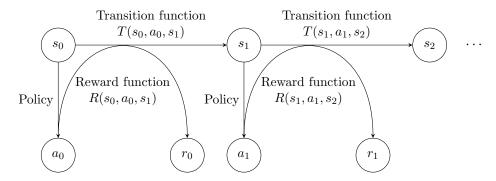


Figure 2.3: Markov Decision Process with policy, transition, and reward functions

The agent's objective is to learn a policy $\pi: \mathcal{S} \to \mathcal{A}$ that maps states to actions, in order to maximise the expected cumulative reward over time. Policies can be categorised as:

- deterministic: $\pi(s): \mathcal{S} \to \mathcal{A}$, at a given state s, the policy specifies the only available action to take, or
- stochastic: $\pi(s, a) : \mathcal{S} \times \mathcal{A} \to [0, 1]$, at a given state s, the policy specifies the probability of taking action a.

Markov Decision Process are based on the idea that the current state is fully representative of the environment. However, in most real world scenarios, the agent does not have access to the complete state. In such cases, a Partially Observable Markov Decision Process (POMDP) can be used to model the uncertainty in the agent's observations and actions.

The goal of the agent is to maximise the cumulative long-term reward G_t , which is defined as the sum of discounted rewards over time:

$$G_t = r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} + \dots = r_{t+1} + \gamma G_{t+1}$$
 (2.8)

where $\gamma \in [0, 1)$ is the discount factor and is used to balance the importance between immediate and future rewards. If the discount factor is set to 0, the agent is myopic and only maximises the immediate reward; whereas, as γ approaches 1, the agent becomes more far-sighted and places greater importance on future rewards.

The expected cumulative reward is defined as the state value function $V^{\pi}(s): \mathcal{S} \to \mathbb{R}$, which is the expected return when starting from state s and following policy π :

$$V^{\pi}(s) = \mathbb{E}_{\pi} \left[G_t | s_t = s \right] \tag{2.9}$$

where \mathbb{E}_{π} denotes the expectation over the policy π .

Similarly, the state-action value function $Q^{\pi}(s, a) : \mathcal{S} \times \mathcal{A} \to \mathbb{R}$ is defined as the expected

return when starting from state s, taking action a, and then following policy π :

$$Q^{\pi}(s,a) = \mathbb{E}_{\pi} [G_t | s_t = s, a_t = a]$$
(2.10)

The state value function $V^{\pi}(s)$ and the state-action value function $Q^{\pi}(s,a)$ are related as follows:

$$V^{\pi}(s) = \sum_{a \in A} \pi(a|s) Q^{\pi}(s, a) = \mathbb{E}_{\pi} \left[Q^{\pi}(s, a) \mid s_t = s \right]$$
 (2.11)

Moreover, the advantage function $A^{\pi}(s, a)$ combines both the state value function $V^{\pi}(s)$ and the state-action value function $Q^{\pi}(s, a)$, and is defined as:

$$A^{\pi}(s,a) = Q^{\pi}(s,a) - V^{\pi}(s) \tag{2.12}$$

A policy π is said to be optimal if the policy's value function is the optimal value function of the MDP, defined as:

$$V^*(s) = \max_{\pi'} V^{\pi'}(s), \forall s \in \mathcal{S}$$
(2.13)

$$Q^*(s,a) = \max_{\pi'} Q^{\pi'}(s,a), \forall s \in \mathcal{S}, a \in \mathcal{A}$$
(2.14)

The optimal policy π^* is:

$$\pi^*(s) = \arg\max_{a \in \mathcal{A}} Q^*(s, a) \tag{2.15}$$

As a result, the optimal policy is the greedy policy that performs the optimal actions at each time step as determined by the optimal value functions. This framework enables the agent to determine optimal actions that maximise long-term returns by evaluating immediate information, without requiring knowledge of the values of future states and actions.

The Bellman equations [34] provide a recursive relation between the value functions in terms of the future state/action values. There are four main Bellman equations, classified in two groups: the Bellman expectation equations and the Bellman optimality equations. The Bellman expectation equations are defined as follows:

$$V^{\pi}(s) = \sum_{a \in A} \pi (a \mid s) \sum_{s' \in S} T(s, a, s') \left[R(s, a, s') + \gamma V^{\pi}(s') \right]$$
 (2.16)

$$Q^{\pi}(s, a) = \sum_{s' \in \mathcal{S}} T\left(s, a, s'\right) \left[R\left(s, a, s'\right) + \gamma \sum_{a' \in \mathcal{A}} \pi\left(a' \mid s'\right) Q^{\pi}(s', a') \right]$$
(2.17)

and the Bellman optimality equations are defined as:

$$V^*(s) = \max_{a \in \mathcal{A}} \sum_{s' \in \mathcal{S}} T\left(s, a, s'\right) \left[R\left(s, a, s'\right) + \gamma V^*(s')\right]$$
(2.18)

$$Q^*(s,a) = \sum_{s' \in \mathcal{S}} T\left(s, a, s'\right) \left[R\left(s, a, s'\right) + \gamma \max_{a' \in \mathcal{A}} Q^*(s', a') \right]$$
(2.19)

Although explicitly solving the Bellman equations would lead to the optimal policy, it is often intractable due to the size of the state and action spaces. Therefore, in RL algorithms, the goal is to learn an approximation of the optimal value functions, which can be used to derive the optimal policy. Another problem that arises is that of balancing exploration and exploitation [35]. Theoretically, following the greedy action yields the optimal policy, but this is only true if all the action values are known. In practice, the agent at each time step and given state chooses either an action whose value is higher, thus exploiting its current knowledge, or picks an action at random, thus exploring the environment and gaining more information about the state-action space, leading to potentially discovering a better action than the greedy one.

2.2.2 Deep Reinforcement Learning Algorithms

A Reinforcement Learning (RL) agent includes one or more of the following components [28]:

- a representation of the value function that provides a prediction of the value of each state or state-action pair,
- a direct representation of the policy, and
- a model of the environment, consisting of estimates of transition and reward functions.

Depending on the components, the main RL paradigms are:

- Model-free algorithms do not learn a representation of the environment, but focus
 on the value function, the policy or both. These algorithms can be further divided
 into:
 - Value-based algorithms learn an approximation of the value function, which is used to compute the state or state-action values. The policy is not learnt explicitly but can be derived from the value function. Examples include Deep Q-Network (DQN) [36] and C51 [37].
 - Policy-based algorithms learn a direct representation of the policy, which is
 used to select actions. Advantage Actor-Critic (A2C), Asynchronous Advantage Actor-Critic (A3C) [38] and Proximal Policy Optimisation (PPO) [39]
 are examples of policy-based algorithms.
 - Actor-Critic algorithms combine both value-based and policy-based approaches, where the actor learns the policy and the critic learns the value function. The critic provides feedback to the actor to improve the policy.

Some examples are Deep Deterministic Policy Gradient (DDPG) [40], Twin Delayed Deep Deterministic Policy Gradient (TD3) [41], and Soft Actor-Critic (SAC) [42].

• Model-based algorithms include a model of the environment, which can be used to simulate future states and rewards. For example, World Models [43] learns a model of the environment and AlphaZero [44] has a representation of the model.

The taxonomy of the RL algorithms is shown in Figure 2.4.

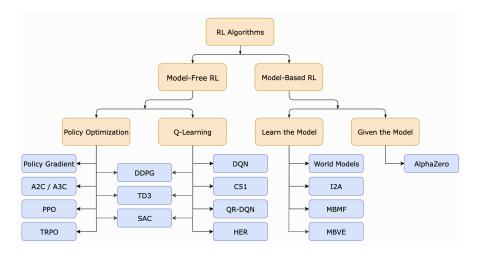


Figure 2.4: Taxonomy of Reinforcement Learning Algorithms [2]

The full potential of RL algorithms is achieved when leveraging the power of Deep Learning to solve dynamic stochastic control problems that have high-dimensionality in their representation of the state and action spaces. DRL algorithms use Deep Neural Networks to approximate the value functions, or use gradient ascent to find the optimal policy parameters. This thesis will focus on policy-based and actor-critic algorithms.

2.2.2.1 Advantage Actor-Critic (A2C)

The Advantage Actor-Critic (A2C) algorithm was developed by Mnih et al. (2016) in their paper on Asynchronous methods for deep reinforcement learning [38]. The main contribution is the usage of the advantage function to address the variance issues present in policy gradient methods. The A2C is the synchronous version of A3C, and is preferred due to its better performance in terms of training time and cost-effectiveness [45].

The algorithm consists of a dual-network architecture, where the actor network learns a stochastic policy $\pi(a_t \mid s_t; \theta)$ and the critic network learns the value function $V(s_t; \theta_v)$. The policy and the value function are updated after every t_{max} actions or when a terminal state is reached. The advantage function is estimated as follows:

$$A(s_{t}, a_{t}; \theta, \theta_{v}) = \sum_{i=0}^{k-1} \gamma^{i} r_{t+i} + \gamma^{k} V(s_{t+k}; \theta_{v}) - V(s_{t}; \theta_{v})$$
(2.20)

where k represents the n-step return and is upper-bounded by the maximum number of steps t_{max} , and γ is the discount factor. The algorithm's objective function is defined as:

$$J(\theta, \theta_v) = \mathbb{E}_{\pi} \left[\log \pi \left(a_t \mid s_t; \theta \right) A\left(s_t, a_t; \theta, \theta_v \right) \right]$$
 (2.21)

The pseudo-code for the algorithm for A2C is outlined in Appendix ??.

2.2.2.2 Proximal Policy Optimisation (PPO)

Proximal Policy Optimisation (PPO) is a policy gradient algorithm that was introduced by Schulman et al. (2017) in their paper on *Proximal Policy Optimization Algorithms* [39] with the objective of constraining policy updates. The algorithm balances sufficiently large updates in order to improve the policy, while avoiding excessively large changes that could hinder performance.

PPO improves the performance of Trust Region Policy Optimisation (TRPO) [46] by using a clipped surrogate objective function that ensures that the probability ratio r_t is bounded within a range of $[1 - \epsilon, 1 + \epsilon]$, where ϵ is a hyperparameter that controls the clipping range. The objective function is defined as:

$$L_t^{CLIP}(\theta) = \mathbb{E}_t \left[\min \left(r_t(\theta) \hat{A}_t, \operatorname{clip} \left(r_t(\theta), 1 - \epsilon, 1 + \epsilon \right) \hat{A}_t \right) \right], \tag{2.22}$$

where

$$r_t(\theta) = \frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_{old}}(a_t|s_t)}$$
(2.23)

is the probability ratio between the current policy π_{θ} and the old policy $\pi_{\theta_{old}}$

Another improvement with respect to TRPO is the use of simple first-order optimisation methods as opposed to the second-order methods used in TRPO. Consequently, PPO maintains the stability and reliability of other trust-region methods, while being easier to implement and more computationally efficient. The pseudo-code for the algorithm for PPO is outlined in Appendix ??.

2.2.2.3 Deep Deterministic Policy Gradient (DDPG)

Deep Deterministic Policy Gradient (DDPG) is an off-policy actor-critic algorithm that was introduced by Lillicrap et al. (2015) in their paper on *Continuous control with deep reinforcement learning* [40]. The algorithm arises to solve the challenges of applying Deep Q-Network [36] to continuous action spaces by applying Deterministic Policy Gradient (DPG), which enables the efficient computation of the policy gradient without the need to integrate over the action space.

The algorithm uses the following networks: the actor network $\mu(s_t; \theta_{\mu})$, which learns a deterministic policy, the critic network $Q(s_t, a_t; \theta_Q)$, which learns the state-action value function, and the actor's and critic's target networks. The actor network is updated

using DPG:

$$\nabla_{\theta_u} J \approx \mathbb{E}_{s_t \sim \mathcal{D}} \left[\nabla_a Q(s_t, a_t; \theta_Q) \nabla_{\theta_u} \mu(s_t; \theta_\mu) \right], \tag{2.24}$$

where \mathcal{D} is the replay buffer that stores the agent's experiences, θ_{μ} are the parameters of the actor network, and θ_{Q} are the parameters of the critic network, and the critic network is updated using the Bellman equations:

$$\nabla_{\theta_Q} J \approx \mathbb{E}_{s_t \sim \mathcal{D}} \left[\left(r_t + \gamma Q(s_{t+1}, \mu(s_{t+1}; \theta_{\mu}); \theta_Q') - Q(s_t, a_t; \theta_Q) \right) \nabla_{\theta_Q} Q(s_t, a_t; \theta_Q) \right],$$
(2.25)

where θ_Q' are the parameters of the target critic network.

From Deep Q-Network, the algorithm incorporates a replay buffer to store the agent's experiences, which allows the agent to learn from past experiences and improve its performance over time. Moreover, DDPG incorporates noise, typically Ornstein-Uhlenbeck noise [47], to the actions taken by the actor network to encourage exploration of the action space. The pseudo-code for the algorithm for DDPG is outlined in Appendix ??.

2.2.2.4 Twin Delayed Deep Deterministic Policy Gradient (TD3)

Twin Delayed Deep Deterministic Policy Gradient (TD3) is an extension of DDPG introduced by Fujimoto et al. (2018) in their paper on Addressing Function Approximation Error in Actor-Critic Methods [41]. The proposal addresses the hyper-parameter sensitivity and overestimation bias present in the critic network of DDPG. The main improvements are:

- Clipped Double Q-Learning: The algorithm employs two critic networks and uses their minimum value to compute the target value for the actor network, which reduces the overestimation bias.
- Delayed Policy Updates: The actor and critic networks updates are performed

at different frequencies. The critic networks are updated every time step, whereas the actor and target networks are updated less frequently. The main benefit is that it allows the critic to improve the accuracy of the value estimates before the actor updates its policy.

• Target Policy Smoothing: The algorithm adds noise to the target action during the critic updates to smooth the value function over similar actions, resulting in a lower impact of approximation errors and more robust policies.

The pseudo-code for the algorithm for TD3 is outlined in Appendix ??.

2.2.2.5 Soft Actor-Critic (SAC)

Soft Actor-Critic (SAC), despite being an off-policy actor-critic algorithm, represents a paradigm shift in RL. The algorithm was presented by Haarnoja et al. (2018) in their paper on Soft Actor-Critic: Off-Policy Maximum Entropy Deep Reinforcement Learning with a Stochastic Actor [42] and is based on the maximum entropy framework, which aims to maximise both the expected return and the entropy of the policy, encouraging the agent to succeed at the task while acting as randomly as possible.

The algorithm uses two critic networks to estimate the state-action value function, and a stochastic actor network that learns a policy that maximises the expected return while also maximising the entropy of the policy. The critic networks are updated using the Bellman equations, and the actor network is updated using the policy gradient method. The objective function for the actor network is defined as:

$$J(\theta) = \mathbb{E}_{s_t \sim \mathcal{D}} \left[\mathbb{E}_{a_t \sim \pi_\theta} \left[\alpha \log \pi_\theta(a_t | s_t) + Q(s_t, a_t; \theta_Q) \right] \right], \tag{2.26}$$

where α is a temperature parameter that controls the trade-off between exploration and exploitation, and \mathcal{D} is the replay buffer that stores the agent's experiences. The critic

networks are updated using the Bellman equations:

$$J(\theta_Q) = \mathbb{E}_{s_t \sim \mathcal{D}} \left[\left(r_t + \gamma \min_{i=1,2} Q(s_{t+1}, \mu_{\theta}(s_{t+1}) + \mathcal{N}(0, \sigma); \theta_{Q_i}) - Q(s_t, a_t; \theta_{Q_i}) \right)^2 \right],$$
(2.27)

where $\mathcal{N}(0,\sigma)$ is the noise added to the action to encourage exploration, and θ_{Q_i} are the parameters of the two critic networks. The temperature parameter α is learned automatically by maximising the entropy of the policy, which is defined as:

$$J(\alpha) = \mathbb{E}_{s_t \sim \mathcal{D}} \left[\alpha \log \pi_{\theta}(a_t | s_t) \right]. \tag{2.28}$$

This parameter is used to control the trade-off between the entropy and the reward terms, effectively controlling the stochasticity of the policy.

The pseudo-code for the algorithm for SAC is outlined in Appendix ??.

2.2.2.6 Algorithm comparison

The five algorithms presented above are among the most widely used in the field of DRL, each addressing specific challenges in policy estimation and value function approximation. A2C is an on-policy actor-critic method that reduces variance through advantage estimation, while PPO changed on-policy learning by introducing a clipped surrogate objective that ensures stable policy updates. Although DDPG pioneered continuous control through deterministic policies, TD3 addressed the overestimation bias of its predecessor via twin critics and delayed updates. SAC revolutionised the field of DRL by incorporating maximum entropy principles.

An overview of the algorithms and their key characteristics is summarised in Table 2.1.

Algorithm	Policy Type	On/Off Policy	Key Idea
A2C	Stochastic	On-Policy	Advantage Function Estimation
PPO	Stochastic	On-Policy	Clipped Policy Updates
DDPG	Deterministic	Off-Policy	Actor-Critic + Replay buffer
TD3	Deterministic	Off-Policy	Double critics + Delayed updates
SAC	Stochastic	Off-Policy	Max-entropy RL

Table 2.1: Comparison of Deep Reinforcement Learning Algorithms

2.3 Explainable Artificial Intelligence

Explainable Artificial Intelligence (XAI) refers to a set of processes, methods and techniques that enable human users to comprehend and trust the outcomes and decisions made by Artificial Intelligence (AI) systems. The goal is to make AI algorithms more transparent, interpretable, and accountable, allowing end-users to understand the outputs of the models. This is particularly important in Deep Learning (DL) where the models are often considered black boxes due to their complexity, non-linearity and high-dimensionality, making it difficult to understand how they arrive at their decisions. With explainable systems, the benefits are numerous ranging from informed decision making to increased user adoption and better governance [48].

Although there are many possible classifications of XAI methods, they can be broadly categorised into two main categories. First, transparent algorithms are inherently understandable and interpretable, such as linear regression, decision trees and rule-based systems. Second, post-hoc explanations are methods that require the usage of an additional algorithm to clarify the decisions made by a model. Examples include saliency maps [49] and interaction data [50].

Another classification relates to whether the explanation method depends on the type of model it is being applied to. On the one hand, model-agnostic methods can be applied to any model regardless of its internal architecture, effectively treating all types of models as black boxes. The analysis is conducted by understanding the input-output behaviour and how small perturbations to the input impact the output. Examples include Local Interpretable Model-agnostic Explanations (LIME) [51] and SHapley Additive ex-Planations (SHAP) [52]. On the other hand, model-specific methods are tailored to a particular architecture and leverage its components as part of the explanation process. In the case of neural networks, this can be achieved by analysing the learned features or by incorporating attention mechanisms [53]. The model-agnostic methods can be further sub-divided between global and local explanations. The goal of global explainability is to provide an understanding of the model's overall behaviour across an entire dataset, while local explainability focuses on explaining the individual predictions.

The taxonomy of the XAI methods is shown in Figure 2.5.

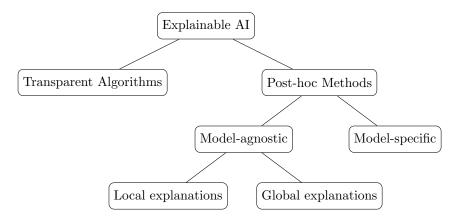


Figure 2.5: Taxonomy of Explainable Artificial Intelligence Methods [3]

2.3.1 Feature Importance

Feature Importance is a global model-specific method that quantifies the contribution of each feature to the model's predictions. In particular, permutation feature importance [54] measures the contribution of each feature by evaluating the model's performance on the original dataset and comparing it to the performance on a permuted version of the dataset, where a specific feature is randomly shuffled. The process allows to understand how much the model's relies on a particular feature for its prediction, by measuring the decrease in predictive power if the input feature's values vary.

An alternative method, well-suited for tree-based models, is impurity-based feature importance. Random forests split their features with the goal of reducing an impurity measure at each node, normally Gini impurity for classification tasks or Mean Squared Error (MSE) for regression. As such, a variable responsible for a split with a large decrease in impurity is considered important [55]. As a result, the impurity importance of a feature is the sum of all impurity reductions across all nodes and trees in the forest where the particular feature was used to split the data. While powerful, this method suffers from bias towards features with high cardinality and they do not necessarily reflect the ability of a feature to make useful predictions on the test set, given that importance is computed on the training set.

2.3.2 Local Interpretable Model-agnostic Explanations

Local Interpretable Model-agnostic Explanations (LIME) is a model-agnostic explanation method that interprets individual predictions of a Machine Learning model by analysing the model locally around the prediction of interest. The method, introduced by Ribeiro et al. (2016) in their paper on Why should I trust you? Explaining the predictions of any classifier [51], utilises the black box model to understand what happens to the outputs when the input data is slightly modified, then fits a simpler, interpretable model to the perturbed data to approximate the black box model's behaviour in that local region.

For a more rigorous definition, let $\mathcal{L}(f, g, \pi_x)$ be a measure of how unfaithful an explanation model g is in approximating the model $f : \mathbb{R}^d \to \mathbb{R}$ in the neighbourhood of the instance x defined as π_x . The goal is to find an interpretable model $g \in G$ that minimises the following objective function:

$$\xi(x) = \mathcal{L}(f, g, \pi_x) + \Omega(g) \tag{2.29}$$

where $\Omega(g)$ is a regularisation term that penalises the complexity of the explanation model g. This encourages interpretability, meaning a qualitative understanding of the relationship between inputs and outputs, and promotes local fidelity, ensuring the explanation accurately approximates the model's behaviour in that region.

The method works as follows:

- **Instance Selection**: Start with a specific prediction instance that requires explanation.
- **Perturbation**: Generate synthetic data points by perturbing the original instance.
- Model Querying: Obtain predictions from the black box model for these perturbed instances.
- Weighting: Assign weights to the synthetic data points based on their proximity to the original instance.
- Surrogate Training: Train a simple, interpretable model (typically linear regression) on the weighted synthetic dataset.

• Explanation: Use the surrogate model to explain the original prediction by interpreting its coefficients or structure.

Its main advantages are its ability to work across different types of data and models, due to its model-agnostic nature, and the fact that its explanations are human-friendly and include a fidelity measure that indicates how well the explanation approximates the black box model's local behaviour. Nonetheless, the method offers only local explanations, which may not generalise well to the entire dataset; it relies on the choice of neighbourhood; and the complexity of the surrogate model needs to be defined in advance and can compromise the interpretability of the explanation [3].

2.3.3 Shapley Additive Explanations

Another model-agnostic technique is SHapley Additive exPlanations (SHAP), which was introduced by Lundberg and Lee (2017) in their paper on *A unified approach to interpreting model predictions* [52]. The method is based on cooperative game theory and the concept of Shapley values [56].

The Shapley value arises in cooperative game theory to answer the question of how to fairly distribute the contribution of each player in a coalition. In this framework, a coalitional game is represented as a tuple (N, v), where $N = \{1, 2, ..., n\}$ is the set of players and $v: 2^N \to \mathbb{R}$ is the characteristic function that assigns a value v(S) to each possible coalition $S \subseteq N$, with the convention that $v(\emptyset) = 0$. The characteristic function v(S) represents the total value that coalition S can achieve through cooperation.

Mathematically, the Shapley value for a feature i is defined as:

$$\phi_i = \sum_{S \subseteq N \setminus \{i\}} \frac{|S|!(|N| - |S| - 1)!}{|N|!} \left[v_{S \cup \{i\}}(x_{S \cup \{i\}}) - v_S(x_S) \right]$$
 (2.30)

where $S \subseteq N$ is a subset of all features N, $v_{S \cup \{i\}}$ is marginal contribution of player i

to coalition S, and v_S is the value of coalition S without player i. This formula can be understood as computing the weighted average of marginal contributions of feature i across all possible coalitions.

The advantage of Shapley values is that it is the only attribution method that results in a fair payout. In particular, it satisfies the four fundamental properties that define a fair allocation:

• Efficiency: The sum of all Shapley values equals the value of the grand coalition:

$$\sum_{i \in N} \phi_i = v(N)$$

• **Symmetry:** The contributions of two players *i* and *j* should be equal if they make identical marginal contributions to all possible coalitions:

$$v(S \cup \{i\}) = v(S \cup \{j\}), \forall S \subseteq N \setminus \{i, j\} \implies \phi_i = \phi_j$$

• **Dummy:** If a player contributes nothing to any coalition they join, their Shapley value should be zero:

$$v(S \cup \{i\}) = v(S), \forall S \subseteq N \setminus \{i\} \implies \phi_i = 0$$

• Additivity: For two games (N, v_1) and (N, v_2) , the Shapley value of the combined game $(N, v_1 + v_2)$ equals the sum of individual Shapley values:

$$\phi_i(v_1 + v_2) = \phi_i(v_1) + \phi_i(v_2)$$

The algorithm for approximating Shapley values is outlined in Appendix 6. However, the method is computationally expensive, as it requires evaluating the model for all possible

coalitions of features.

The use of Shapley values in ML was not introduced until 2011, when Štrumbelj and Kononenko [57] proposed it as a method for explaining black-box regression models. However, it was popularised in 2017 by Lundberg and Lee [52], who introduced the SHAP framework. Although their proposal relies on the principles of Shapley values, their main contribution is to represent the Shapley value as an additive feature attribution method. The explanation is given as:

$$g(\mathbf{z}') = \phi_0 + \sum_{j=1}^{M} \phi_j z_j'$$
 (2.31)

where g is the explanation model, $\mathbf{z}' \in \{0,1\}^M$ is the coalition vector, M is the maximum coalition size, ϕ_0 is the bias term, and ϕ_j is the feature attribution for feature j.

2.3.3.1 KernelSHAP

The KernelSHAP algorithm builds on the SHAP framework by using a kernel-based approach to estimate Shapley values. It approximates the Shapley value by sampling different coalitions and using a weighted linear regression model to fit the contributions of each feature. The method relies on not all coalitions contributing equally to the final Shapley value and as such uses kernel weights to identify the most important coalitions. The main steps of the KernelSHAP algorithm are:

- Sample a set of coalitions from the feature space: $\mathbf{z}'_k \in \{0,1\}^M, k \in \{1,\ldots,K\}$, where K is the total number of samples.
- For each coalition \mathbf{z}'_k , compute the model's prediction by first converting \mathbf{z}'_k to the original feature space and then applying the model $\hat{f}: \hat{f}(h_{\mathbf{x}}(\mathbf{z}'_k))$.
- Compute the weight for each coalition with the SHAP kernel: $\pi_{\mathbf{x}}(\mathbf{z}')$
- Fit a weighted linear regression model to the sampled coalitions and their corre-

sponding predictions.

• Return Shapley values ϕ_k as the coefficients of the fitted model.

The sample coalitions are generated by randomly selecting subsets of the features, or equivalently, a vector of 0s and 1s indicating whether a feature is included in the coalition. The sampled coalitions represent the dataset for the regression model whose target is the prediction for a coalition. However, the sampled coalitions are not on the target feature space and, as such, it is necessary to implement another function $h_{\mathbf{x}}(\mathbf{z}') = \mathbf{z}$ that maps the sampled coalitions to the original feature space. In the case of tabular data, this is done by replacing the features that are not included in the coalition with their mean value or a random sample from its possible values. As a result, sampling from the marginal distribution ignores the dependence structure between features.

Although there are similarities between SHAP and LIME, their main difference lies in feature weighting in the regression model. The SHAP weighting assumes that small and large coalitions provide the most information about its isolated effects or its total effects, respectively. Whereas coalitions with half the features add little information about a specific feature's contributions. The proposed weighting function for KernelSHAP is:

$$\pi_{\mathbf{x}}(\mathbf{z}') = \frac{(M-1)}{\binom{M}{|\mathbf{z}'|}|\mathbf{z}'|(M-|\mathbf{z}'|)},$$
(2.32)

where M is the maximum coalition size and $|\mathbf{z}'|$ is the number of features in the coalition \mathbf{z}' .

In addition, since the coalitions with the smallest and the largest number of features are the most informative, the sampling process is biased towards coalitions of size 1 and M-1, resulting in 2M possible coalitions. Then, the remaining budget K-2M is used to sample coalitions of size 2 to M-2. This process continues until the sampled coalitions reach the desired number of samples.

Consequently, given the samples, the KernelSHAP algorithm fits a weighted linear regression model to estimate the Shapley values. The model is defined as:

$$g(\mathbf{z}') = \phi_0 + \sum_{j=1}^{M} \phi_j z_j'. \tag{2.33}$$

The goal is to minimise the following loss function:

$$\mathcal{L}(\hat{f}, g, \pi_{\mathbf{x}}) = \sum_{\mathbf{z}' \in \mathcal{Z}} \left[\hat{f} \left(h_{\mathbf{x}} \left(\mathbf{z}' \right) \right) - g(\mathbf{z}') \right]^{2} \pi_{\mathbf{x}}(\mathbf{z}'), \tag{2.34}$$

where \mathbf{Z} is the dataset of sampled coalitions.

2.3.3.2 TreeSHAP

A variant of their original proposal is TreeSHAP [58], designed specifically for tree-based models, such as decision trees, random forests or gradient-boosted trees. In this case, the method is model-specific and by leveraging the structure of the tree, it improves the computational efficiency by reducing computation time from exponential for KernelSHAP to polynomial.

The method works by exploiting the tree structure and the main steps of the algorithm are as follows:

- For each feature, traverse the tree and compute the contribution of the feature to the prediction at each node.
- For each node, compute the contribution of the feature to the prediction by considering the difference between the prediction at the node and the prediction at the parent node.
- For each feature, compute the Shapley value by averaging the contributions across

all nodes in the tree.

2.4 State of the Art of Deep Learning and Explainability for Portfolio Optimisation

The emergence of Machine Learning (ML) and its rise in popularity have led to a new research direction in various financial applications, due to its ability to learn complex patterns from high-dimensional data and adapt to changing market conditions. Particularly, the main approaches in the financial field include the use of Deep Learning and Reinforcement Learning (RL) for price trend prediction [59] and portfolio optimisation [60].

The topic of portfolio optimisation with multiple risky financial assets has been extensively studied and it still poses a challenging task due to the complex and stochastic nature of financial markets. Traditional approaches to portfolio optimisation, such as the Mean-Variance Optimisation (MVO) [25], have been widely used, but they often rely on assumptions that do not hold in practice, such as the normality of returns and the stability of the covariance matrix. As a result, these methods can lead to suboptimal portfolios and poor performance in real-world scenarios.

The use of Deep Learning architectures is particularly prominent in the context of price prediction, where deep neural networks are employed to learn complex patterns in historical price data. For instance, Long Short-Term Memory (LSTM) architectures are particularly well-suited for financial time series forecasting due to their ability to capture long-term dependencies and temporal patterns in the data. The performance of these architectures can lead to a Mean Absolute Percentage Error (MAPE) as low as 2.72%, as demonstrated by Chaudhary (2025) [61]. Shen et al. (2020) [7] also propose a LSTM architecture for short-term trend prediction. Despite its simple architecture, its main

contributions rely on the feature engineering process. The proposal incorporates feature extension, followed by recursive feature elimination and finally, performs Principal Component Analysis (PCA) to reduce the dimensionality of the input data for the LSTM model. The use of PCA improves the training efficiency of the architecture by 36.8% [7]. The use of ensemble methods is also prominent for price prediction, where techniques such as stacking, blending, boosting and bagging are employed to combine the predictions of multiple models. For example, Nti et al. (2020) [11] explore twenty-five different ensemble classifiers and regressors based on Decision Trees, Support Vector Machines and Neural Networks. Their research shows that although stacking and boosting ensemble algorithms provide better results in terms of accuracy, they are the most computationally expensive.

When it comes to portfolio optimisation, DRL algorithms are particularly better suited as they address the sequential decision making nature of portfolio management. Unlike traditional Supervised Learning approaches that require labelled data, DRL enables agents to learn optimal investment strategies through direct interaction with market environments. This paradigm allows for the dynamic adjustment of portfolio weights without the need for predefined rules, making it suitable to capture market non-linearities and adapt to changing conditions. There are numerous DRL algorithms, as outlined in Section 2.2.2, with each being particularly befitting to different aspects of the portfolio management process, namely, DDPG encourages maximum returns, while A2C reduces the variance.

Liu et al. (2018) [15] propose the use of DDPG for profitable stock trading, where the agent learns to buy, hold and sell stocks based on the historical price data with the goal of maximising the investment return. Their proposal outperforms the Dow Jones Industrial Average (DJIA) and the min-variance portfolio allocation strategies, achieving an annualised return of 25.86% and a Sharpe ratio of 1.79. Their work is further extended

by Liu (2020) [62] by proposing a Python library, FinRL, which provides a comprehensive framework for developing and evaluating DRL algorithms in the context of financial trading. Although the library provides implementation for numerous DRL algorithms including DQN, A2C and SAC, in this paper, they only evaluate the performance of TD3 and DDPG on the Dow Jones Industrial Average (DJIA) constituents for the tasks of multiple stock trading and portfolio allocation. Notwithstanding, an interesting aspect of their work is the incorporation of the turbulence index, that measures extreme asset price fluctuations, to control portfolio risk. Beyond traditional assets, optimal portfolio allocation has also been explored in the context of cryptocurrencies [63] and future contracts [64].

Despite the significant applications of DRL in portfolio optimisation, the field still faces significant challenges that prevent its widespread adoption. When it comes to market conditions, identifying the correct objective function that guarantees both efficiency and accuracy remains an open research question. Finally, one of the most significant concerns is the lack of transparency of ML models. If there is to be widespread use of these models in the financial field, great strides must be made in the area of explainability.

Barriedo et al. (2020) [18] provide a comprehensive overview of Explainable Artificial Intelligence (XAI) methods and their need in different fields. In 2024, the European Union has passed the Regulation 2024/1689, commonly known as the AI Act [65]. The goal is to ensure that the AI systems used in the European Union are safe, transparent and traceable. Given the regulatory requirements, it is crucial for financial institutions to adopt techniques that enhance the interpretability and traceability of ML models.

The application of XAI methods has gained traction in the financial domain, with notable use cases including stock market trend prediction [66] and auditing [67]. However, despite examples of XAI methods in finance, there is still a lack of research in DRL. An interesting study was conducted by González Cortés et al. (2024) [17], whose au-

thors address the black box behaviour of DRL models by proposing an intrinsically transparent algorithm. They use Advantage Actor-Critic (A2C) ¹ enhanced with an attention-layered LSTM to determine the importance of the input features. Although their results show an improvement in performance compared against two variants of the Markowitz model, their implementation does not scale well with the number of assets in the portfolio, as the attention mechanism is independent for each stock.

Another recent study by de-la-Rica-Escudero et al. (2025) [68] proposes post-hoc explainability methods to interpret the decisions of PPO agent optimised for portfolio management. They implement three model-agnostic explainability techniques: SHAP, LIME and feature importance analysis. Despite their proposal's ability to provide insights into the model's decision-making process, they do not use the model prediction function directly but instead implement a surrogate model to approximate the decision boundary of the PPO agent, effectively adding an additional layer to the model.

Given the lack of research in the area of explainability for DRL models that perform automated portfolio allocation and the current limitations of existing methods, this thesis proposes to provide a comprehensive study of DRL techniques tailored for portfolio optimisation in financial markets, by exploring the potential of five prominent algorithms (A2C, PPO, DDPG, TD3 and SAC) across various market conditions and asset classes. Moreover, due to the complex and hidden nature of those algorithms, their decision-making process will be explained using XAI methods. The objective is to bridge the gap between the performance of DRL and algorithmic transparency.

¹In the paper [17], they refer to A2C as Synchronous Advantage Actor Critic (SAAC)

Chapter 3

Methodology

This chapter covers the methodology and framework established to provide an explainable Deep Reinforcement Learning (DRL) model capable of optimising a portfolio of financial assets. The chapter is structured as follows: first, it describes the architecture and components of the proposed DRL model, including the state representation, reward function and training process. Second, it discusses the evaluation metrics and experimental setup used to assess the performance of the proposed solution. Finally, it outlines the implementation of the explainability techniques used to interpret the model's decisions.

3.1 Problem Definition

The problem of portfolio optimisation is the task of finding an optimal allocation of financial assets in a portfolio to maximise expected returns while minimising risk. Thus, it is necessary to decide how to rebalance the portfolio at each time step in a highly stochastic and complex financial market. This can be formulated using a Markov Decision Process (MDP) framework, where the agent interacts with the environment by deciding the optimal allocation based on the state of the environment at each time step

to maximise the expected cumulative reward over time. Deep Reinforcement Learning (DRL) gives the agent the ability to learn the optimal policy directly from the environment by taking actions and receiving rewards.

3.2 Markov Decision Process Model

Due to the dynamic, stochastic and interactive nature of financial markets, a Markov Decision Process is a suitable framework to model the problem. The main elements of the MDP model are defined as follows:

- State space S
- Action space A
- Reward function $R: \mathcal{S} \times \mathcal{A} \times \mathcal{S} \to \mathbb{R}$
- Transition function $T: \mathcal{S} \times \mathcal{A} \to \mathcal{S}$
- Discount factor $\gamma \in [0, 1)$

The state space S is a vector representation of the financial environment. For a portfolio of D assets, the features that describe the state include asset prices, technical indicators and macroeconomic indicators:

- Close price $\mathbf{p}_t \in \mathbb{R}^D$: Adjusted close prices of the assets at time t.
- Open price $\mathbf{o}_t \in \mathbb{R}^D$: Opening prices of the assets at time t.
- High price $\mathbf{h}_t \in \mathbb{R}^D$: Highest prices of the assets at time t.
- Low price $\mathbf{l}_t \in \mathbb{R}^D$: Lowest prices of the assets at time t.
- Volume $\mathbf{v}_t \in \mathbb{R}^D$: Trading volume of the assets at time t.

- Technical indicators $\mathbf{I}_t \in \mathbb{R}^{D \times I}$: For each of the D assets, a vector \mathbf{i}_t of I technical indicators, such as moving averages, relative strength index (RSI), and Bollinger Bands, calculated from the asset prices.
- Macroeconomic indicators $\mathbf{M}_t \in \mathbb{R}^{D \times M}$: For each of the D assets, a vector \mathbf{m}_t of M macroeconomic indicators, such as volatility index and interest rates, which provide additional context about the financial environment.
- Covariance matrix $\mathbf{C}_t \in \mathbb{R}^{D \times D}$: For each of the D assets, a vector of D values representing the covariance between the assets in the portfolio at time t.

The description of technical and macroeconomic indicators is provided in more detail in Appendix B.

The action space \mathcal{A} is the set of possible actions that the agent can take at each time step. For the portfolio optimisation problem, the actions correspond to portfolio weights and are defined as follows:

$$\mathbf{a}_t = \mathbf{w}_t : w_{t,d} \in [0,1] \quad \forall d \in \{1,\dots,D\},$$
 (3.1)

where \mathbf{w}_t is a vector of portfolio weights at time t, representing the allocation of the portfolio to each asset. The weights are constrained to be non-negative and sum to one:

$$\sum_{d=1}^{D} w_{t,d} = 1, \quad w_{t,d} \ge 0 \quad \forall d \in \{1, \dots, D\}.$$
(3.2)

Moreover, they are initialised to be equal for all assets, meaning that the agent starts with an equal allocation to each asset in the portfolio. The reason behind this is to avoid an initial bias and allow the agent to learn an allocation from the environment rather than favour any particular asset.

The transition function T describes how the state of the environment changes in response

to the action taken. It is defined as:

$$s_{t+1} = T(s_t, a_t),$$
 (3.3)

where s_{t+1} is the new state of the environment after taking action a_t in state s_t . The transition function is determined by the dynamics of the financial market, which are influenced by the asset prices, trading volume and other factors.

The reward function R models the direct reward of taking an action a_t in state s_t and transitioning to a new state s_{t+1} . It is defined as the change in the portfolio value from time t to time t+1:

$$R_{t+1} = R(s_t, a_t, s_{t+1}) = V_{t+1} - V_t, \tag{3.4}$$

where the value of the portfolio at time t is given by the dot product of the portfolio weights and the asset close prices:

$$V_t = \mathbf{w}_t \cdot \mathbf{p}_t. \tag{3.5}$$

Regardless of the choice of reward function, the goal of the agent is to learn a policy $\pi: \mathcal{S} \to \mathcal{A}$ that maximises the expected cumulative reward over time, which can be expressed as:

$$J(\pi) = \mathbb{E}\left[\sum_{t=0}^{T} \gamma^t R(s_t, a_t, s_{t+1})\right],\tag{3.6}$$

where T is the time horizon and γ is the discount factor that determines the importance of future rewards.

The environment is implemented in Python ¹ using the Gym library [69], which provides a standard interface for reinforcement learning environments. The environment is defined as a class that inherits from the gym. Env class and implements the required methods:

¹https://www.python.org/

reset, step and render.

3.3 Deep Reinforcement Learning Algorithms

The proposed solution is based on the DRL framework, which allows the agent to learn the optimal policy directly from the environment by taking actions and receiving rewards. The algorithms used are:

- Advantage Actor-Critic (A2C)
- Proximal Policy Optimisation (PPO)
- Deep Deterministic Policy Gradient (DDPG)
- Twin Delayed Deep Deterministic Policy Gradient (TD3)
- Soft Actor-Critic (SAC)

The implementation is done using the Stable Baselines3 library [70], which provides a set of state-of-the-art DRL algorithms with a consistent interface and easy-to-use API. The pseudo-code for each algorithm is provided in Appendix A.1.

3.3.1 Hyper-parameter tuning

Hyper-parameter tuning is a crucial step in the training process of DRL models, as the right choice of hyper-parameters can significantly impact the model's performance. In this thesis, hyper-parameter tuning refers to the process of optimising the training parameters of the DRL algorithms to maximise their performance in the task of portfolio optimisation. The hyper-parameters tuned include the learning rate, batch size, number of training steps, and other algorithm-specific parameters, which are summarised in Appendix C.

To implement hyper-parameter tuning in Python, the wandb [71] library is used, which provides a simple and efficient way to track experiments, visualise results, and manage hyper-parameter sweeps. A sweep is defined as a search for hyper-parameters that optimises a cost function, in our case, the Sharpe ratio [72]. Given that the models were implemented using the Stable Baselines3 library, the integration with wandb allows for seamless tracking of hyper-parameter configurations and their corresponding performance metrics [73].

As mentioned above, sweeps can optimise a cost function to avoid naively testing every possible combination. Using wandb, a Bayesian optimisation approach is taken [74], which uses a probabilistic model to estimate the performance of different hyper-parameter configurations and selects the next configuration to test based on the expected improvement over the current best configuration. This allows for a more efficient search of the hyper-parameter space and reduces the number of configurations that need to be tested. Another option to reduce the time taken to find the optimal hyper-parameters is to use early termination. This method will stop a poorly performing run before it has fully completed, saving computational resources.

3.4 Post-hoc Explainability

Given the goal of improving the explainability of the DRL models, this thesis adopts explainability techniques to interpret the model's decision-making process in a transparent manner. By using post-hoc methods, rather than modifying each model's architecture to enhance their transparency, the proposal is model-agnostic and can be applied to any DRL model. Consequently, it combines the ability to find the most suitable architecture while maintaining the interpretability.

The explainability techniques implemented are:

- Feature Importance
- Local Interpretable Model-agnostic Explanations (LIME)
- SHapley Additive exPlanations (SHAP)

Following the work from de-la-Rica-Escudero et al. (2025) [68], the implementation of these techniques follows two directions. First, as in their paper, a surrogate model maps the state space to the action space as a proxy for the model's decisions. The second direction is to use the LIME and SHAP techniques directly on the DRL model to interpret its decisions.

3.4.1 Surrogate Model Explainability

The surrogate model is trained to approximate the behaviour of the DRL model by learning the mapping from its inputs, the environment representation, to its outputs, the portfolio weights. In the paper [68], the authors do not explicitly acknowledge the use of a surrogate model, even though their code implementation does so. A potential reason behind not explaining the model's actions directly could be the code complexity in using SHAP with a DL model.

Given that the action space is continuous, the surrogate model is implemented using a RandomForestRegressor [75], which is a non-parametric model that can capture complex relationships between the inputs and outputs. The model is trained on the state-actions pairs of the test data, which is the object of the explanations. However, since the model has a number of hyper-parameters, it requires careful tuning to achieve optimal performance. Consequently, hyperparameter tuning was used find the optimal architecture using HalvingGridSearchCV [76], which is a method that iteratively narrows down the search space by evaluating a subset of hyper-parameters and discarding the less promising ones. The use of grid search rather than Bayesian Optimisation, as

was done for DRL hyper-parameter tuning 3.3.1, is to replicate the approach taken in [68]. Once the optimal hyper-parameters have been found and the surrogate model has been trained, its prediction function is used as a proxy to interpret the original model's decisions.

Firstly, feature importance is built-in for Random Forest Regressors, and can be easily accessed with the built-in property feature_importances_ [77]. This method provides the importance of each feature in the state representation by using a combination of the fraction of the samples a feature contributes to and the mean decrease in impurity.

Secondly, LIME and SHAP are applied to the surrogate model via the predict function to provide local explanations for individual predictions. Both of these techniques provide insights into the model's decisions by perturbing the input data and observing the changes in the output.

The LIME implementation is done using the LimeTabularExplainer [78], which is designed to work with tabular data and provides a way to explain individual predictions by approximating the model's behaviour locally with a linear model. Similarly, for SHAP, the framework provides a particular implementation for tree-based models, which is used to compute the SHAP values efficiently by exploiting the structure of the trees. Consequently, the TreeExplainer [79] is used to compute the SHAP values for the surrogate model.

3.4.2 Direct Model Explainability

Undoubtedly, a surrogate model adds an additional layer of complexity and may obscure the understanding of the original model's decisions. Therefore, the LIME and SHAP techniques are also applied directly to the prediction function of DRL model. This approach allows for a more direct interpretation of the model's decision-making process, without the need of a supplementary level. For LIME, the implementation is again done using LimeTabularExplainer, but the prediction function is now obtained from the relevant DRL algorithm. For SHAP, the KernelExplainer is used, which is a model-agnostic method that randomly samples feature coalitions to approximate SHAP values to reduce computation [80].

Chapter 4

Results

This chapter presents the results of conducting experiments under the methodology proposed in Chapter 3. The experiments were designed to evaluate the performance of the implemented DRL models for portfolio optimisation in changing environment representations and market conditions. Moreover, to analyse the interpretability of the model's decisions, a framework using post-hoc explainability techniques is explored.

4.1 Dataset

Given the general difficulty in finding the appropriate DRL algorithm with a suitable reward function for portfolio optimisation, the five implemented algorithms were tested on five different datasets. Each dataset consists of a different set of financial assets, ranging from three different asset classes. First, three datasets were constructed using the stock constituents of three renowned indexes:

- Dow Jones Industrial Average (DJIA) with 30 stocks,
- Euro Stoxx 50 Index (Euro Stoxx 50) with 50 stocks,

• Financial Times Stock Exchange 100 Index (FTSE 100) with 100 stocks.

The constituents of each of the indexes were retrieved in April 2025 and can be found in Appendix D.1. It is important to note that the datasets were chosen to illustrate different currencies, as this introduces another factor of changing market conditions.

Additionally, two datasets were constructed using commodities and currencies, respectively. The commodities dataset includes six different commodities, which are listed in Appendix D.2. These are a sample of the most traded commodities in the market and were chosen by their availability in the Yahoo! Finance API ¹. With regard to the currencies dataset, it includes ten different currency pairs, listed in Appendix D.3. These were selected based on their trading volume and liquidity, with all pairs quoted in United States Dollar (USD).

The datasets are constructed using daily data from January 2016 to July 2025 down-loaded using the Python yfinance library [81]. The dataset is partitioned into two disjoint sets: training and testing, with the training set containing data from January 2016 to December 2023, and the testing set starting on January 2024 until July 2025. The training set is used to train the DRL models, while the testing set is used to evaluate their performance. For hyper-parameter tuning, the training set is further split into a training and validation set, with the validation set corresponding to the period between January 2023 and December 2023. The validation set is used to evaluate the performance of the models for each hyper-parameter combination. The train-validation-test split is summarised in Table 4.1.

Dataset	Training Period	Validation Period	Testing Period
Dow Jones 30	Jan 2016 - Dec 2022	Jan 2023 - Dec 2023	Jan 2024 - Jul 2025
Euro Stoxx 50	Jan 2016 - Dec 2023	Not applicable	Jan 2024 - Jul 2025

¹https://uk.finance.yahoo.com

Dataset	Training Period	Validation Period	Testing Period
FTSE 100	Jan 2016 - Dec 2023	Not applicable	Jan 2024 - Jul 2025
Commodities	Jan 2016 - Dec 2022	Jan 2023 - Dec 2023	Jan 2024 - Jul 2025
Currencies	Jan 2016 - Dec 2022	Jan 2023 - Dec 2023	Jan 2024 - Jul 2025

Table 4.1: Train-Validation-Test Split for each dataset

4.2 Experiment Design

To address the challenge of finding a suitable algorithm for portfolio optimisation, the five implemented DRL algorithms were tested on the five datasets described in Section 4.1, with the goal of evaluating the performance of each algorithm in different scenarios and market conditions. Moreover, the environment representation will also be varied to assess the impact of more information on the model's performance. Four environment representations were considered, each with a different number of features:

- Simple dataset: Open, High, Low, Close, Volume (OHLCV) prices of the assets.
- Covariance dataset: To the simple dataset, the covariance matrix of the assets is added to explicitly model the relationships between the assets.
- Indicators dataset: Technical and macroeconomic indicators are added to the simple dataset.
- Complete dataset: The complete dataset includes the simple dataset, the covariance matrix and the technical and macroeconomic indicators.

The strength of DRL algorithms lies in their ability to learn from high-dimensional data, which is why the goal is to evaluate whether a more exhaustive environment

representation leads to better performance. However, with higher dimensionality comes a higher computational cost.

Finally, the performance of the algorithms is closely related to the choice of hyper-parameters. Ideally, the hyper-parameters should be tuned to find the optimal configuration for each algorithm and dataset combination. However, it was not feasible to perform tuning for all combinations of algorithms, datasets and environment representations. Consequently, the default hyper-parameters for all the experiments are outlined in Table 4.2. The hyper-parameters were chosen based on those from a testing run that was done on a small dataset of five tickers with indicators as environment representation. Those results can be seen in Appendix E.

Model	Hyperparameter	Values / Range
	Number of steps	40
A2C	Entropy coefficient	0.0003
	Learning rate	0.003
	Number of steps	512
PPO	Entropy coefficient	0.0005
PPO	Learning rate	0.0015
	Batch size	64
	Batch size	256
DDPG	Buffer size	200000
	Learning rate	0.005
	Batch size	128
TD3	Buffer size	500000
	Learning rate	0.001
	Batch size	64

Table 4.2: Default hyper-parameter configurations.

SAC

Model	Hyperparameter	Values / Range
	Buffer size	500000
	Learning rate	0.001
	Learning starts	2000
	Entropy coefficient	"auto_0.1"

Table 4.2: Default hyper-parameter configurations.

Overall, the experiments were designed to evaluate the performance of the implemented DRL algorithms in different scenarios, with the goal of finding the most suitable algorithm for portfolio optimisation. However, testing five algorithms on five distinct datasets with four possible environment representations would result in a total of twenty different experiments per algorithm. Additionally, optimising the parameters for each experiment further expands the experimental space and significantly increases the computational time required. Due to limited computational resources², the scope of experiments was adjusted as follows:

- Hyper-parameter tuning was performed only for the Dow Jones 30 dataset with simple and indicators environment representation, as it is the smallest equities dataset and requires less computational time.
- Since the covariance matrix, significantly increases the dimensionality of the environment representation, it was only included in the experiments with the Dow Jones 30, the currencies and the commodities datasets.

The final experimental design consists of 16 experiments, which are summarised in Table

²The university did not provide access to a computing cluster; therefore, all experiments were conducted on a personal computer.

4.3, where each row represents a unique combination of dataset, environment representation and whether hyper-parameter tuning is performed for this combination.

Dataset	Environment	Hyper-parameter
	Representation	Tuning
Dow Jones 30	Simple	Yes
Dow Jones 30	Covariance	No
Dow Jones 30	Indicators	Yes
Dow Jones 30	Complete	No
Euro Stoxx 50	Simple	No
Euro Stoxx 50	Indicators	No
FTSE 100	Simple	No
FTSE 100	Indicators	No
Commodities	Simple	No
Commodities	Covariance	No
Commodities	Indicators	No
Commodities	Complete	No
Currencies	Simple	No
Currencies	Covariance	No
Currencies	Indicators	No
Currencies	Complete	No

Table 4.3: Summary of experiments conducted.

4.3 Evaluation

As outlined in the previous section, the experiments are designed to evaluate the performance of the implemented DRL algorithms in different scenarios and market conditions. The evaluation will focus on key performance metrics, as well as benchmarking against traditional portfolio optimisation techniques.

4.3.1 Performance Metrics

The performance metrics are provided through the pyfolio library [82], which includes a perf_stats method to calculate various performance metrics of a strategy.

The main metrics for comparison are:

• The cumulative return is the total change in investment price over a period of time, representing the overall percentage gain or loss from the initial investment value.

The formula is given by:

$$Cumulative return = \frac{Final portfolio value - Initial portfolio value}{Initial portfolio value}.$$
 (4.1)

• The annualised return is the geometric average of the amount of money earned by an investment each year over a given period of time, providing a standardised measure of annual performance. It is calculated as follows:

Annualised Return =
$$\left(\frac{\text{Final portfolio value}}{\text{Initial portfolio value}}\right)^{\frac{1}{\text{Number of years}}} - 1.$$
 (4.2)

• The annualised volatility is the standard deviation of returns annualised to provide a measure of investment risk on a yearly basis and can be computed with the following formula:

Annualised Volatility = Standard Deviation of Returns
$$\times$$
 $\sqrt{\text{Yearly trading days}}$,
(4.3)

where the number of trading days per year is typically assumed to be 252.

• The Sharpe ratio is a measure of risk-adjusted performance that compares the excess return of an investment to a risk-free asset against its volatility. The ratio is given by:

Sharpe Ratio =
$$\frac{R_p - R_f}{\sigma_p}$$
, (4.4)

where R_p is the annualised return of the portfolio, R_f is the annualised risk-free rate, and σ_p is the annualised volatility of the portfolio.

 The max drawdown is the maximum percentage loss from a peak to a trough during a specified period, indicating the worst-case scenario for portfolio decline.
 Its formula is:

$$Max Drawdown = \frac{Peak Value - Trough Value}{Peak Value}.$$
 (4.5)

Other metrics available through the pyfolio library are outlined in Appendix F.

4.3.2 Benchmark Strategies

Aside from computing relevant performance metrics, the algorithms will be benchmarked against traditional portfolio optimisation methods. The benchmarks are designed to provide a baseline for comparison and to evaluate the performance of the DRL algorithms in relation to established methods. The following benchmark strategies were considered.

• Equal-weighted portfolio: A simple strategy that allocates an equal weight to each

asset in the portfolio.

- Mean-variance optimisation: A classic portfolio optimisation method that aims to maximise Sharpe ratio.
- Min-variance portfolio: Another classic portfolio optimisation method that seeks to minimise the portfolio's volatility.
- Momentum portfolio: A strategy that invests in assets with positive momentum,
 i.e. those that have performed well in the previous time step, and avoids those with negative momentum.

The implementation of the mean-variance and the min-variance portfolio allocation strategies has been done using the PyPortfolioOpt Python library [83], whereas the equal-weighted and momentum strategies have been implemented using custom code.

Finally, if the portfolio is made up of equities of a relevant index, the benchmark will also include the index itself, which serves as a reference point for the performance of the portfolio.

4.4 Experiment: Algorithm Comparison

In this section, the results of the experiment to identify the suitability of the implemented DRL algorithms for portfolio optimisation under different market conditions are presented. The algorithms are trained on data with a simple environment representation, which only includes the OHLCV prices of the assets, and evaluated on the five datasets. The table 4.4 summarises the results of the experiment for the A2C algorithm, where each row corresponds to a different dataset and each column to a different performance metric. The results for the other algorithms are presented in Appendix G.1.

Dataset	Cumulative	Annualised	Annualised volatility	Sharpe	Max
	return	return	volatility	ratio	drawdown
Dow Jones 30	0.2165	0.3387	0.1579	1.3203	-0.1649
Euro Stoxx 50	0.1467	0.2293	0.1549	0.9617	-0.1667
FTSE 100	0.1052	0.1623	0.1268	0.8520	-0.1409
Commodities	0.2353	0.3694	0.2041	1.1372	-0.1512
Currencies	-0.0011	-0.0017	0.0462	-0.0018	-0.0665

Table 4.4: Algorithm comparison results for the A2C implementation.

For the case of A2C, the algorithm demonstrates competitive performance particularly for the DowJones30 dataset, achieving a cumulative return of 21.65% and a Sharpe ratio of 1.32. Positive results are also obtained with the commodities dataset, which demonstrates the highest cumulative return of 23.53% and a Sharpe ratio of 1.14. Despite being of the same asset class, the EuroStoxx50 and the FTSE100 datasets show relatively lower performance, with cumulative returns of 14.67% and 10.52%, respectively. With regard to the currencies dataset, the performance of the algorithm is less impressive, with near-zero cumulative returns and Sharpe ratios, indicating that the algorithm struggles to learn a profitable strategy in this asset class.

Although similar observations can be made for the other algorithms, the performance varies significantly across different datasets. Regarding PPO, better performance is achieved in the commodities dataset, with a cumulative return of 25.31% and a Sharpe ratio of 1.26. which is slightly more than 0.1 higher than that of the A2C algorithm. DDPG performs the best in the DowJones30 dataset, achieving similar performance to that of A2C, with a 22.06% cumulative return and a Sharpe ratio of 1.38. However, TD3 surpasses all other algorithms for the DowJones30 dataset and the Commodities datasets, achieving 24.78% and 27.68% in cumulative return, respectively. Finally, SAC

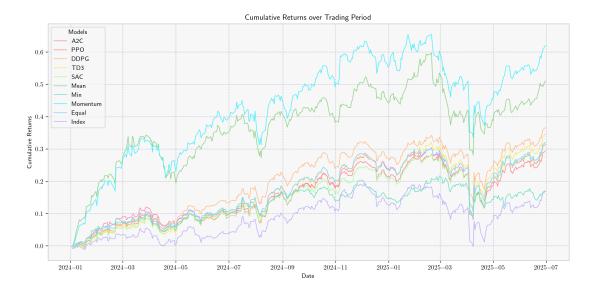


Figure 4.1: Evolution of the Cumulative Returns for the DowJones30 dataset with the OHLCV prices and indicators environment representation.

demonstrates a strong performance in the EuroStoxx50 dataset, with a cumulative return of 17.61% and a Sharpe ratio of 1.14, but it does not outperform the other algorithms in the DowJones30 and Commodities datasets. The algorithm that performs better in the FTSE100 dataset is DDPG, with a cumulative return of 13.36% and a Sharpe ratio of 1.08.

Taking the DowJones30 dataset with an environment representation made up of the OHLCV prices and the indicators, the performance of the algorithms can be benchmarked against traditional strategies and the DJIA Index. The evolution of the cumulative returns over the testing period is shown in Figure 4.1 and the corresponding performance metrics are summarised in Table 4.5.

Dataset	Cumulative	Annualised	Annualised	Sharpe	Max
	return	return	volatility	ratio	drawdown
A2C	0.2020	0.3139	0.1559	1.2575	-0.1716
PPO	0.1895	0.2937	0.1487	1.2407	-0.1556

Algorithm	Cumulative	Annualised	Annualised	Sharpe	Max
/ Bench-	return	return	volatility	ratio	drawdown
mark					
DDPG	0.2341	0.3663	0.1486	1.4896	-0.1546
TD3	0.2214	0.3456	0.1517	1.3938	-0.1609
SAC	0.2050	0.3189	0.1480	1.3340	-0.1538
Mean	0.3218	0.5114	0.1839	1.6096	-0.1983
Min	0.1123	0.1705	0.1157	0.9777	-0.1066
Momentum	0.3855	0.6204	0.1990	1.7388	-0.1929
Equal	0.2066	0.3205	0.1476	1.3461	-0.1541
Index	0.1110	0.1692	0.1532	0.7635	-0.1637

Table 4.5: Algorithm comparison results for the DowJones30 dataset. The colour correspond to the best performing configurations, with blue for the best performing DRL algorithm and green for the best benchmark.

The results show that all the algorithms outperform the performance of the index for all the considered metrics, as well as the min-variance portfolio. Out of all the DRL algorithms, DDPG achieves the highest cumulative return of 23.41% and a Sharpe ratio of 1.49, followed by TD3 with a cumulative return of 22.14% and a Sharpe ratio of 1.39, while PPO has the worst performance of the five with a cumulative return of 18.95% and a Sharpe ratio of 1.24. However, none of these outperform the mean-variance and momentum benchmark strategies, with the latter achieving a Sharpe ratio of 1.74 and a cumulative return of 38.55%, which is significantly higher than the performance of the DRL algorithms.

4.5 Experiment: Environment Representation

Another source of variability in the performance of the algorithms is the environment representation. In this section, the results of comparing the DRL algorithms on different environment representations are presented. For the experiment to be meaningful, it has been performed on the DowJones30 dataset, the currencies and the commodities datasets. This choice provides the ability to compare the performance of the algorithms across different asset classes, while also allowing for a more manageable computational cost. The table 4.6 compares the performance according to the Sharpe ratio and, in Appendix G.2, according to the cumulative return.

Algorithm	Dataset	Simple	Indicators	Covariance	Complete
	DowJones30	1.3203	1.2575	1.3615	1.3929
A2C	Commodities	1.1373	1.2881	1.0273	1.2079
	Currencies	-0.0018	-0.0571	-0.0674	-0.0053
	DowJones30	1.3410	1.2407	1.3524	1.1890
PPO	Commodities	1.2600	1.1256	1.1559	1.2015
	Currencies	0.0014	0.0699	0.0652	0.1399
	DowJones30	1.3826	1.4896	1.3562	1.3261
DDPG	Commodities	1.1745	0.9871	1.0731	1.1612
	Currencies	0.0528	0.0689	0.0200	0.0115
	DowJones30	1.4911	1.3938	1.1792	1.2084
TD3	Commodities	1.4537	0.9776	1.0462	1.2388
	Currencies	0.0807	-0.0088	-0.0086	-0.0436
	DowJones30	0.9769	1.3340	1.4670	1.3017
SAC	Commodities	1.3727	1.1973	1.1773	1.0500

Table 4.6: Environment representation experiment comparison according to the Sharpe ratio. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Comparadities dataset.

Algorithm	Dataset	Simple	Indicators	Covariance	Complete
	Currencies	0.0806	0.1771	-0.1441	0.2550

Table 4.6: Environment representation experiment comparison according to the Sharpe ratio. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset.

The results show that the performance of the algorithms varies significantly across different environment representations. For the DowJones30 dataset, the OHLCV prices representation achieves the highest Sharpe ratio of 1.49 for TD3, closely followed by the OHLCV prices with indicators. The OHLCV prices with covariance representation achieves 1.47 for SAC. For the complete feature set, only the A2C algorithm achieves a higher Sharpe ratio of 1.39 than the other algorithms.

For the commodities dataset, the results are completely different to those of the DowJones 30. The only coincidence is that TD3 achieves the highest Sharpe ratio and highest cumulative return in the simple feature set. Moreover, when looking at this dataset, explicitly adding the covariance to the environment representation does not lead to better performance in terms of Sharpe ratio and there is only one instance where the cumulative returns are highest, which would be for the DDPG algorithm with the complete feature set.

Finally, for the currencies dataset, the performance of the algorithms is significantly lower, going negative in some cases. A possible reason is the particular set of hyper-parameters used. In this experiment, algorithm configuration was not altered or tuned for each specific feature set.

4.6 Experiment: Hyper-parameter Tuning

As has been mentioned in the above experiments, the performance of the algorithms is substantially influenced by the choice of hyper-parameters. Ideally, a systematic approach should be employed to find the optimal hyper-parameters for each algorithm, dataset and environment representation combination. However, due to the computational cost of hyper-parameter tuning, it was only performed for the DowJones30 dataset with the OHLCV and indicators environment representations over five trials. The results for each of the algorithms with the default hyper-parameters versus the tuned hyper-parameters are compared in Table 4.7 and Table 4.8 for the two features sets: simple and with indicators, respectively.

Algorithm	Metric	Default parameters	Tuned parameters
4.90	Cumulative Return	0.3387	0.3491
A2C	Sharpe ratio	1.3203	1.4307
DDO	Cumulative Return	0.3174	0.2844
PPO	Sharpe ratio	1.3410	1.1939
DDDG	Cumulative Return	0.3454	0.27404
DDPG	Sharpe ratio	1.3826	1.2088
TD 9	Cumulative Return	0.3902	0.2974
TD3	Sharpe ratio	1.4911	1.2354
G A G	Cumulative Return	0.2243	0.3703
SAC	Sharpe ratio	0.9769	1.4521

Table 4.7: Hyper-parameter tuning experiment results for the DowJones30 dataset with simple environment representation.

Algorithm	Metric	Default parameters	Tuned parameters
And	Cumulative Return	0.3139	0.3573
A2 C	Sharpe ratio	1.2575	1.3994
DDO	Cumulative Return	0.2937	0.3134
PPO	Sharpe ratio	1.2407	1.3679
DDDG	Cumulative Return	0.3663	0.4086
DDPG	Sharpe ratio	1.4896	1.5597
TD 9	Cumulative Return	0.3456	0.2891
$ brack ext{TD3}$	Sharpe ratio	1.3938	1.2332
	Cumulative Return	0.3189	0.2646
SAC	Sharpe ratio	1.3340	1.1688

Table 4.8: Hyper-parameter tuning experiment results for the DowJones30 dataset with indicators environment representation.

By looking at the data presented in these tables, it is clear that finding the optimal configuration can have a significant impact on the performance of the algorithms. For instance, although the cumulative return for A2C in the simple feature set only improves by 1%, the Sharpe ratio increases from 1.32 to 1.43, meaning that the algorithm learns to better balance risk while maximising returns. Another example is the SAC algorithm, which achieves a better performance than that of the default configuration. However, for the PPO, DDPG and TD3 algorithms, there are no improvements and the default hyper-parameters perform better. Similarly, when looking at the indicators feature set, not all the algorithms show sign of improvements. These means that, for that particular algorithm, dataset and environment representation combination, the optimal

hyper-parameter configuration has not been found. Understandably, due to the limited computational resources, the hyper-parameter search was very limited to only five runs, which is not sufficient for a thorough search.

4.7 Explainability Results

A main objective of this thesis is to be able to interpret the decisions made by the DRL algorithms. The following explainability framework is designed to provide insights into the decision-making process of the algorithms and present the most relevant features that influence the portfolio allocation decision at each time step in a visual and human-readable manner. As described in Section 3.4, two approaches were employed: a surrogate model and direct explanations.

For the purposes of visualisation, the results are shown for a sample dataset of five tickers (AAPL, CSCO, HON, MSFT, V) from the DJIA and using only the open, close, high, and low prices as the environment representation. This choice is made because explanations are more easily visualised when the number of assets and features is small. However, the explainability framework itself is general and can be applied to any number of assets and any environment representation. In practice, to support larger portfolios and more complex feature sets, an interactive dashboard could be developed, allowing users to select the relevant assets in the portfolio for which explanations are required. Moreover, only the explanations of the A2C algorithm are presented, as it serves as a representative example of the framework's capabilities.

The surrogate model was implemented following the proposal by de-la-Rica-Escudero et al. (2025) [68]. Although their paper does not explicitly acknowledge the use of a surrogate model nor outline the reasons for its use, it can be inferred that using a simpler transparent algorithm as a proxy provides built-in feature importance, which is

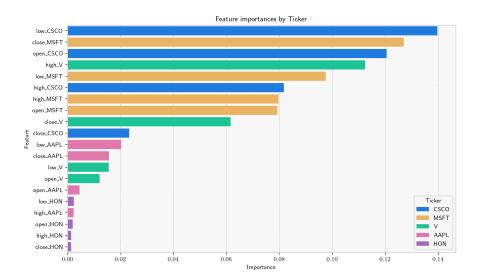


Figure 4.2: Top features from the surrogate model according to feature importance.

a global explainability method. However, there does not seem to be any clear value when using LIME and SHAP as they are both model-agnostic methods capable of providing explanations for any black-box model, given the prediction function of the algorithm.

4.7.1 Feature Importance Results

The feature importance results from the surrogate model are shown in Figure 4.2, where the top 20 features are ranked according to the importance measure. The ranking shows that the low price of CSCO and the close price of MSFT are the two most important features, followed by the open price of CSCO. At the bottom section of the ranking, HON and AAPL features have a lower importance.

This trend is further confirmed by looking at the mean importance of the features for each asset, as shown in Figure 4.3. This indicates that the agent heavily relied on the performance of MSFT and CSCO to guide its portfolio allocation decisions, while the other assets played a less significant role.

Another interesting result about the feature importance shown in Figure 4.2 is that the

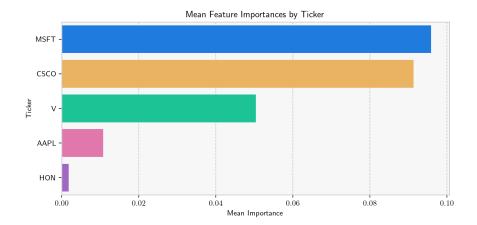


Figure 4.3: Mean feature importance per asset from the surrogate model.

different assets have a different OHLCV feature importance distribution, which suggests that the agent may have developed distinct strategies for each asset. Figure H.1 in the Appendix H.1 shows the top features grouped by asset, where it can be seen more clearly how each asset has a different most important feature. In the case of AAPL, HON and CSCO, the low price played a more critical role in informing the agent's decisions, showing how extreme price changes lead the agent to adjust the portfolio allocation. In contrast, for MSFT, the close price is the most important feature, which might imply the agent is more focused on the end of day activities of this asset. Finally, looking over all the assets, Figure H.2 in Appendix H.1 shows how features corresponding to low and high prices contributed to the agent's decisions. This again indicates that the agent is sensitive to price extremes of the assets.

4.7.2 Local Interpretable Model-agnostic Explanations Results

Moving on to the local explanations of LIME, the direct explanations for the A2C algorithm are provided. The benefit of LIME is its ability to provide explanations at a particular point in time. In this case, the local explanations are provided for the first time step of the test dataset, which corresponds to the 2nd of January 2024. In this

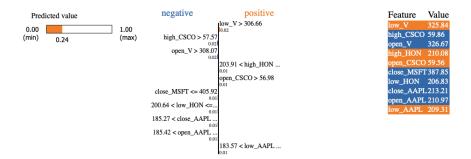


Figure 4.4: LIME explanations for the A2C algorithm at the first time step of the test dataset for the MSFT asset. The orange bars indicate features that contribute positively to the prediction, while the blue bars indicate features that contribute negatively.

section, Figure 4.4 illustrates the local explanations for the MSFT asset, whilst the other assets are found in Appendix H.2. This particular instance is affected by V's low price in the positive terms, meaning that it pushes the price higher, whilst the high price of CSCO and the open of V negatively affect the prediction by pushing it lower. Looking at these explanations over a number of days can help an investor decide whether there exist particular features that consistently contribute to the portfolio allocation decision.

4.7.3 Shapley Additive Explanations Results

Finally, the results of the SHAP analysis are presented. These provide a global view of the feature importance across all time steps and assets, as well as a local interpretation for individual predictions. As with the case of LIME, instead of using a surrogate model, the explanations are extracted from the A2C model directly. Since the predictions of the output are weight allocations across all portfolio assets, the SHAP values presented in this section correspond only to the AAPL asset, but the interpretations can be generalised to other assets and algorithms.

Looking at Figure 4.5, the x-axis represents the SHAP value, which measures the impact of a feature on the model's output; while the y-axis displays the top features. Each point



Figure 4.5: Beeswarm SHAP explanations for the A2C algorithm for the AAPL asset. The x-axis represents the SHAP values, whilst the y-axis represents the top features. The colour indicates the feature value, with magenta being high and blue being low.

in the beeswarm plot represents a single prediction, with the point's colour indicating whether its corresponding feature value is low, coloured in blue, or high, coloured in magenta. The beeswarm plot provides a visual representation of the distribution of SHAP values for each feature, allowing for an easy comparison of their importance. Surprisingly, the most important feature for the AAPL asset is the low price of the MSFT asset and, by visual inspection, the high values of the low price of MSFT push the AAPL allocation lower, while the low values of the low price of MSFT push the AAPL allocation higher. However, this is not quite significant as there is a cluster of data points around the zero, indicating that most frequently, the low price of MSFT does not have an impact on AAPL's allocation.

The shap Python library provides numerous visualisations to explain the prediction of a model. An interesting one is the force plot, shown in Figure 4.6, for the AAPL weight

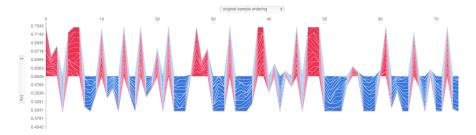


Figure 4.6: SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm.

allocation and the contribution of all features. The force plot visualises the impact of each feature on the model's weight allocation over the entire test dataset ordered by time. Positive values, visualised in magenta, show feature contributions that push the allocation higher, while negative values, in blue, push it lower. The baseline is the average weight allocation across all time steps.

The shap library provides the output in an interactive HyperText Markup Language (HTML) format that allows us to interact with the visualisation and gain deeper insights into the model's behaviour. From the beeswarm plot in Figure 4.5, the most important feature for the AAPL asset is the low price of MSFT. Using the force plot, it is possible to single out the effects of this particular feature over the test period, as shown in Figure 4.7, as well as its isolated effect in one specific prediction. Its impact is very well-defined as for approximately the first 30 samples, it has a positive contribution, increasing the AAPL allocation, while for the rest of the time steps, it has a negative contribution, decreasing the AAPL allocation.

Lundberg and Lee (2017) [52] showed that LIME is a subset of SHAP, it is possible to obtain local explanations using the shap library. Figure 4.8 shows the local explanation for the AAPL asset at the first time step of the test dataset, which corresponds to the 2nd of January 2024. Although the visualisation is different, the information it provides is similar to that of LIME. Shown horizontally, the features shown in magenta push the

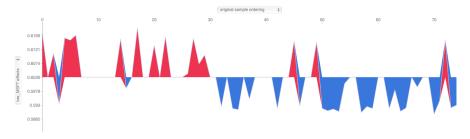


Figure 4.7: SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm.



Figure 4.8: SHAP force plot for the weight allocation of the AAPL asset for the A2C algorithm at the first time step of the test dataset.

allocation higher, while those in blue push it lower.

Chapter 5

Legal, Social, Ethical and

Professional Issues

The development and deployment of Deep Reinforcement Learning (DRL) algorithms to perform profitable portfolio allocation raises several legal, social, ethical and professional issues that must be considered. The incorporation of post-hoc explainable techniques to understand, interpret and clarify the decision-making process of these algorithms is a crucial step towards addressing these concerns. This chapter explores them in detail, referencing relevant regulatory frameworks and professional codes of conducts, and highlights potential mitigation strategies.

5.1 Legal Issues

When deploying Machine Learning (ML) algorithms in finance, the European Union (EU)'s Artificial Intelligence Act (AI Act) [65] classifies them as high-risk under Article 6 due to their potential impact on an individual's economic well-being. Consequently, high-risk systems must comply with Chapter 3 - Section 2, Articles 9-15, which include

the obligations for risk management, data governance, documentation, transparency and human supervision. In particular, Article 13 requires that high-risk AI systems's outputs are interpretable. The use of explainability techniques ensures that the decision-making process of the algorithm can be understood and justified, thus adhering to the legal requirements set forth by the AI Act.

In addition, algorithmic trading systems must adhere to the European Union directive on Markets in Financial Instruments Directive II (MiFID II) [84] and the United Kingdom (UK) Financial Conduct Authority (FCA) guidance on Algorithmic Trading Compliance in Wholesale Markets. These regulations require robust governance and oversight frameworks, risk controls and thorough testing infrastructure. In this project, back-testing has been carried out to assess the algorithm's performance under varying market conditions followed by explainability techniques to enable the auditability of the system.

5.2 Social Issues

Despite the growing exposure to Artificial Intelligence (AI) systems with the rise of Large Language Models (LLMs), there is still a significant lack of understanding and trust in these systems. Some of the reasons behind this mistrust include:

- the black box nature of models, making outputs hard to interpret,
- lack of human-like qualities in the models, and
- perceived limitations to adapt to new situations and learn from previous mistakes.

In the context of this work, the integration of explainability techniques addresses the black box behaviour of the implemented technology by offering clear, data-driven justifications. However, transparency must also be accessible. It is essential to provide a user-friendly interface to easily access the explanations and generate plain language descriptions for non-technical audiences.

5.3 Ethical Issues

The ethical implications of DRL in portfolio optimisation are multifaceted. The primary concern is the potential for these systems to make decisions that may not align with human values or ethical standards. For instance, if the algorithm prioritises profit maximisation without considering the social or environmental impact of its investment choices, it could lead to unethical outcomes, such as supporting companies with poor labour practices or those contributing to environmental degradation. To address this concern, the following practices can be put in place:

- 1. the end-user should have full control over the assets included in their portfolio, allowing them to exclude companies that do not meet their ethical standards; or
- 2. the environment's representation can be expanded to include ethical dimensions, like social impact or environmental sustainability metrics.

Regarding the environment representation, it was not possible to incorporate such data as it is not readily available nor in a standardised format. This is why, although there was an interest to broaden the environment representation to include other sources outside of the financial domain, it was not feasible to do so given the available resources.

A critical point in portfolio allocation is risk management. In this research, a performance metric that balances return maximisation and risk minimisation is used for hyper-parameter tuning, ensuring that the agent learns to avoid overly risky investments. Additionally, the inclusion of a risk-free asset enables a safe-guard mechanism. The agent can be implemented to allocate all the resources to cash when market volatility exceeds a pre-defined threshold and resume only when said volatility decreases.

Finally, potential biases in the training data or model structure could result in allocations favouring certain industries or assets classes. This thesis mitigates such biases by constructing a portfolio from diversified indices (Appendix D.1) and using explainability techniques to audit the decisions for systematic biases.

5.4 Professional Issues

This work has been conducted in accordance with the British Computer Society (BCS) Code of Conduct [85] and the The Institution of Engineering and Technology (IET) Rules of Conduct [86]. All the work in this report is original unless stated otherwise, and all external contributions are explicitly acknowledged, following the principles of the BCS Code of Conduct [85]. Moreover, all third-party libraries, datasets and code have been explicitly acknowledged and their use complies with the respective licences and guidelines.

Most importantly, the project has been conducted within my own area of expertise: computational finance, Reinforcement Learning, and Explainable Artificial Intelligence. If any aspects of the project were beyond these, proper academic sources have been consulted to ensure the integrity and quality of the work.

Chapter 6

Conclusion

This thesis has explored the application of Deep Reinforcement Learning (DRL) algorithms for optimal portfolio allocation in dynamic financial markets. The primary objective was to develop an explainable model-agnostic framework capable of enhancing the understanding of any DRL algorithm's predictions. Such a tool would provide insights into the decision-making process of these complex models and facilitate auditability.

Five state-of-the-art DRL algorithms were implemented and evaluated on a portfolio management task. To assess the behaviour of these algorithms in different market conditions, a comprehensive experimental setup was designed, involving various datasets and environment representations. The datasets ranged from equities to commodities and currencies, each presenting unique challenges and opportunities for the DRL algorithms. The results demonstrated that DRL algorithms can effectively learn and adapt to dynamic market conditions, achieving competitive performance compared to traditional portfolio management strategies. However, the challenge remains in finding the optimal hyper-parameters, uniquely suited to each algorithm and dataset combination, in order to be able to fully exploit their potential.

Regarding the explainability aspect, the framework developed in this thesis successfully enhances the interpretability, transparency and auditability of these black box models. The incorporation of feature importance through a surrogate model, Local Interpretable Model-agnostic Explanations (LIME) analysis and SHapley Additive ex-Planations (SHAP) values provides an exhaustive methodology for understanding both individual predictions and the overall decision-making process of the models over a test set. However, the results highlight the superiority of the SHAP technique, which is capable of providing global explanations and feature importance without the need for an additional layer, in conjunction with local explanations.

6.1 Future Work

Despite the comprehensive and exhaustive nature of this report, there are several areas through which future research could enhance this work. Indisputably, the main limitation of this thesis has been the lack of computation resources. Any future work should aim to fully explore the hyper-parameter space for each of the DRL algorithms, datasets and environment representations. In a similar vein, current research in price prediction has investigated the impact of a smaller feature representation by performing feature engineering techniques, such as feature selection and dimensionality reduction. Such measures might not only improve model performance and reduce over-fitting, but could also reduce computational requirements.

Moreover, even in the case of optimal hyper-parameter configuration, comparing the performance of the models to those of traditional methods left room for improvement. Exploring alternative reward functions, such as Sharpe ratio, incorporating additional constraints, such as transaction costs, or explicitly handling periods of high volatility could lead to more robust and effective trading strategies. Another possibility that led to reduced performance against the benchmarks was the exclusion of a risk-free asset in

the portfolio. Future work could include a risk-free asset in the portfolio, which would result in a more diversified and potentially less risky portfolio. In terms of real-world scenarios, portfolios tend to be composed of different asset classes. Although this thesis explored the performance of the algorithms in different classes, forthcoming research could investigate the performance of these algorithms in multi-asset class portfolios.

Lastly, for the explainability aspect, the current framework would benefit from a more user-friendly interface that allows users to provide their dataset and prediction function easily and interactively explore the model's explanations. Another direction is to add intrinsic interpretability methods directly within the DRL algorithms, such as attention-based mechanisms [17], reducing the need for post-hoc explanation techniques.

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Appendix A

Algorithms

A.1 Deep Reinforcement Learning Algorithms

Algorithm 1 Advantage Actor-Critic (A2C) Pseudo-code

```
Initialise:
    Global shared policy parameters \theta and value parameters \theta_v
    Number of parallel workers N
    Global step counter T \leftarrow 0
    Hyper-parameters: discount \gamma, max steps per update t_{\text{max}}, max total steps T_{\text{max}},
learning rates \alpha_{\pi}, \alpha_{v}
repeat
       Reset gradients: d\theta \leftarrow 0, d\theta_v \leftarrow 0
      Initialise empty batch storage for all workers
       for worker i = 1 to N do
             t_{\text{start}} \leftarrow t
             Get initial state s_t^{(i)} from worker i
             repeat
                    Select action a_t^{(i)} \sim \pi_{\theta}(\cdot|s_t^{(i)})
                   Execute a_t^{(i)}, observe reward r_t^{(i)} and next state s_{t+1}^{(i)}
                   Store (s_t^{(i)}, a_t^{(i)}, r_t^{(i)}) in worker i's trajectory
             \begin{aligned} & \iota \leftarrow \iota + 1 \\ & \textbf{until terminal } s_t^{(i)} \text{ or } t - t_{\text{start}} == t_{\text{max}} \\ & R^{(i)} = \begin{cases} 0 & \text{if terminal } s_t^{(i)} \\ V_{\theta_v}(s_t^{(i)}) & \text{otherwise} \end{cases}  
            for j \in \{t-1, \dots, t_{\text{start}}\} do
R^{(i)} \leftarrow r_j^{(i)} + \gamma R^{(i)}
                   Accumulate gradients w.r.t. \theta:
d\theta \leftarrow d\theta + \nabla_{\theta} \log \pi_{\theta}(a_{j}^{(i)}|s_{j}^{(i)})(R^{(i)} - V_{\theta_{v}}(s_{j}^{(i)}))
Accumulate gradients w.r.t. \theta_{v}:
                        d\theta_v \leftarrow d\theta_v + \nabla_{\theta_v} (R^{(i)} - V_{\theta_v}(s_i^{(i)}))^2
             end for
      end for
      // Synchronous update: wait for all workers to complete
      Average gradients: d\theta \leftarrow \frac{1}{N}d\theta, d\theta_v \leftarrow \frac{1}{N}d\theta_v
       Update \theta \leftarrow \theta + \alpha_{\pi} d\theta, \theta_v \leftarrow \theta_v - \alpha_v d\theta_v
       T \leftarrow T + N \times t_{\text{max}}
until T > T_{\text{max}}
```

Algorithm 2 Proximal Policy Optimisation (PPO) Pseudo-code

```
Initialise:
    Policy parameters \theta_0 and value function parameters \phi_0
    Global step counter T \leftarrow 0
    Hyper-parameters: discount \gamma, GAE parameter \lambda, clipping parameter \epsilon, learning
rates \alpha_{\pi}, \alpha_{v}, epochs per update K_{\text{epochs}}, minibatch size N_{\text{minibatch}}, loss coefficients
c_1, c_2
for k = 0, 1, 2, ... do
      Collect set of trajectories \mathcal{D}_k = \{\tau_i\} by running policy \pi_{\theta_k} in environment
      Store transitions: \{(s_t, a_t, r_t, s_{t+1}, done_t)\}
      for each trajectory \tau in \mathcal{D}_k do
             Compute value estimates: V_t = V_{\phi_k}(s_t)
            Compute TD residuals: \delta_t = r_t + \gamma V_{t+1} (1 - \text{done}_t) - V_t
Compute GAE advantages: \hat{A}_t = \sum_{l=0}^{\infty} (\gamma \lambda)^l \delta_{t+l}
             Compute returns: \hat{R}_t = \hat{A}_t + V_t
      end for
      for epoch e = 1 to K_{\text{epochs}} do
             Shuffle dataset \mathcal{D}_k
             for each minibatch \mathcal{B} in \mathcal{D}_k do
                  r_t(\theta) = \frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_k}(a_t|s_t)}
                   L^{\text{CLIP}}(\theta) = \frac{1}{|\mathcal{B}|} \sum_{t \in \mathcal{B}} \min \left( r_t(\theta) \hat{A}_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right)
                  L^{VF}(\phi) = \frac{1}{|\mathcal{B}|} \sum_{t \in \mathcal{B}} \left( V_{\phi}(s_t) - \hat{R}_t \right)^2
L(\theta, \phi) = L^{\text{CLIP}}(\theta) - c_1 L^{VF}(\phi) + c_2 S[\pi_{\theta}]
\theta \leftarrow \theta + \alpha_{\pi} \nabla_{\theta} L^{\text{CLIP}}(\theta)
                   \phi \leftarrow \phi - \alpha_v \nabla_{\phi} L^{VF}(\phi)
             end for
      end for
      Update policy: \theta_{k+1} = \theta
      Update value function: \phi_{k+1} = \phi
      T \leftarrow T + |\mathcal{D}_k|
end for
```

Algorithm 3 Deep Deterministic Policy Gradient (DDPG) Pseudo-code

```
Initialise:
    Critic network Q_{\theta^Q}(s, a) and actor \mu_{\theta^{\mu}}(s) with random weights \theta^Q, \theta^{\mu} Target networks: \theta^{Q'} \leftarrow \theta^Q, \theta^{\mu'} \leftarrow \theta^{\mu}
    Replay buffer \mathcal{B}
    Hyper-parameters: discount \gamma, soft update rate \tau, batch size N, exploration noise
process \mathcal{N}, learning rates \alpha_Q, \alpha_\mu, total episodes M, steps per episode T
for episode = 1 to M do
      Initialise random process \mathcal{N} for action exploration
      Receive initial state s_1
      for t = 1 to T do
            Select action a_t = \mu_{\theta^{\mu}}(s_t) + \mathcal{N}_t
            Execute a_t, observe reward r_t and next state s_{t+1}
            Store (s_t, a_t, r_t, s_{t+1}) in \mathcal{B}
            Sample mini-batch \{(s_i, a_i, r_i, s_{i+1})\}_{i=1}^N from \mathcal{B}
            Compute target: y_i = r_i + \gamma Q_{\theta^{Q'}}(s_{i+1}, \mu_{\theta^{\mu'}}(s_{i+1}))
Update critic by minimising: L(\theta^Q) = \frac{1}{N} \sum_i (y_i - Q_{\theta^Q}(s_i, a_i))^2
            Update actor by policy gradient:
                \nabla_{\theta^{\mu}} J \approx \frac{1}{N} \sum_{i} \nabla_{a} Q_{\theta^{Q}}(s_{i}, a)|_{a = \mu_{\theta^{\mu}}(s_{i})} \nabla_{\theta^{\mu}} \mu_{\theta^{\mu}}(s_{i})
            Update target networks: \theta^{Q'} \leftarrow \tau \theta^Q + (1 - \tau)\theta^{Q'}
                \theta^{\mu'} \leftarrow \tau \theta^{\mu} + (1 - \tau) \theta^{\mu'}
      end for
end for
```

Algorithm 4 Twin Delayed Deep Deterministic Policy Gradient (TD3) Pseudo-code

```
Initialise:
    Critic networks Q_{\theta_1}(s,a) and Q_{\theta_2}(s,a) with random weights \theta_1,\theta_2
    Actor policy \mu_{\phi}(s) with random weights \phi
   Target networks: \theta_1' \leftarrow \theta_1, \, \theta_2' \leftarrow \theta_2, \, \phi' \leftarrow \phi
    Replay buffer \mathcal{B}
    Hyper-parameters: discount \gamma, target policy noise \tilde{\sigma}, noise clip c, policy delay d,
exploration noise \sigma, update rate \tau, batch size N, total steps T
for t = 1 to T do
     Observe state s_t
     Sample action with exploration: a_t = \mu_{\phi}(s_t) + \epsilon, \epsilon \sim \mathcal{N}(0, \sigma)
     Execute a_t, observe reward r_t and next state s_{t+1}
     Store (s_t, a_t, r_t, s_{t+1}) in \mathcal{B}
     Sample mini-batch \{(s_i, a_i, r_i, s_{i+1})\}_{i=1}^N from \mathcal{B}
         Sample clipped noise: \tilde{\epsilon} \sim \text{clip}(\mathcal{N}(0, \tilde{\sigma}), -c, c)
         Compute target action: \tilde{a}_{i+1} = \mu_{\phi'}(s_{i+1}) + \tilde{\epsilon}
         Compute target Q-value: y_i = r_i + \gamma \min_{j=1,2} Q_{\theta'_i}(s_{i+1}, \tilde{a}_{i+1})
         Update each critic by minimising L(\theta_j) = \frac{1}{N} \sum_i (y_i - Q_{\theta_j}(s_i, a_i))^2
     if t \mod d = 0 then
           Update actor by policy gradient: \nabla_{\phi} J \approx \frac{1}{N} \sum_{i} \nabla_{a} Q_{\theta_{1}}(s_{i}, a) \mid_{a=\mu_{\phi}(s_{i})} \nabla_{\phi} \mu_{\phi}(s_{i})
           Update target networks:
              \theta'_{j} \leftarrow \tau \, \theta_{j} + (1 - \tau) \, \theta'_{j} \text{ for } j = 1, 2
\phi' \leftarrow \tau \, \phi + (1 - \tau) \, \phi'
     end if
end for
```

Algorithm 5 Soft Actor-Critic (SAC) Pseudo-code

```
Initialise:
    Actor network \pi_{\theta}(a|s) with parameters \theta
    Two critic networks Q_{\phi_1}(s, a) and Q_{\phi_2}(s, a) with parameters \phi_1, \phi_2
    Target critic networks: \phi_1' \leftarrow \phi_1, \, \phi_2' \leftarrow \phi_2
    Replay buffer \mathcal{D}
    Hyper-parameters: discount \gamma, temperature \alpha (fixed or learnable), target entropy
\mathcal{H} (if \alpha is learnable), batch size N, learning rates \lambda_Q, \lambda_\pi, \lambda_\alpha, soft update rate \tau
for each training step do
     Observe state s_t
     Sample action: a_t \sim \pi_{\theta}(\cdot|s_t)
     Execute a_t, observe reward r_t and next state s_{t+1}
     Store (s_t, a_t, r_t, s_{t+1}) in \mathcal{D}
     if time to update then
           Sample mini-batch \{(s_i, a_i, r_i, s_{i+1})\}_{i=1}^N from \mathcal{D}
           Update Critics:
           for j = 1, 2 do
                 Sample next actions: \tilde{a}_{i+1} \sim \pi_{\theta}(\cdot|s_{i+1})
                 Compute target Q-values:
                    y_i = r_i + \gamma \left( \min_{k=1,2} Q_{\phi'_k}(s_{i+1}, \tilde{a}_{i+1}) - \alpha \log \pi_{\theta}(\tilde{a}_{i+1}|s_{i+1}) \right)
                 Update critic: \phi_j \leftarrow \phi_j - \lambda_Q \nabla_{\phi_i} \frac{1}{N} \sum_i (Q_{\phi_i}(s_i, a_i) - y_i)^2
           end for
           Update Actor:
           Sample actions with reparametrisation: \tilde{a}_i = f_{\theta}(\epsilon_i; s_i) where \epsilon_i \sim \mathcal{N}(0, I)
           Compute policy loss:
               J(\theta) = \frac{1}{N} \sum_{i} \left[ \alpha \log \pi_{\theta}(\tilde{a}_{i}|s_{i}) - \min_{j=1,2} Q_{\phi_{j}}(s_{i}, \tilde{a}_{i}) \right]
           Update actor: \theta \leftarrow \theta - \lambda_{\pi} \nabla_{\theta} J(\theta)
           if \alpha is learnable then
                 Update Temperature:
                 J(\alpha) = \frac{1}{N} \sum_{i} \alpha \left( \log \pi_{\theta}(\tilde{a}_{i}|s_{i}) + \mathcal{H} \right) Update temperature: \alpha \leftarrow \alpha - \lambda_{\alpha} \nabla_{\alpha} J(\alpha)
           end if
           Update Target Networks:
           \phi'_j \leftarrow \tau \phi_j + (1 - \tau) \phi'_j \text{ for } j = 1, 2
     end if
end for
```

Explainability Algorithms A.2

Algorithm 6 Shapley Value Approximation

Require: Number of iterations M, instance of interest \mathbf{x} , feature index j, data matrix \mathbf{X} , model f

Ensure: Estimated Shapley value $\phi_j(\mathbf{x})$

for m=1 to M do

Draw a random instance ${\bf z}$ from data matrix ${\bf X}$

Choose a random permutation \mathbf{o} of the feature indices

Order **x** according to **o**:
$$\mathbf{x_o} = (x_{(1)}, \dots, x_{(j)}, \dots, x_{(p)})$$

Order **z** according to **o**: $\mathbf{z_o} = (z_{(1)}, \dots, z_{(j)}, \dots, z_{(p)})$

Construct two new instances:

$$\begin{aligned} \mathbf{x}_{+j} &= \left(x_{(1)}, \dots, x_{(j-1)}, x_{(j)}, z_{(j+1)}, \dots, z_{(p)}\right) \\ \mathbf{x}_{-j} &= \left(x_{(1)}, \dots, x_{(j-1)}, z_{(j)}, z_{(j+1)}, \dots, z_{(p)}\right) \\ \text{Compute marginal contribution:} \end{aligned}$$

$$\phi_j^{(m)} = \hat{f}(\mathbf{x}_{+j}) - \hat{f}(\mathbf{x}_{-j})$$

end for

Compute average Shapley value:

$$\phi_j(\mathbf{x}) = \frac{1}{M} \sum_{m=1}^{M} \phi_j^{(m)}$$

Appendix B

State Representation

B.1 Technical Indicators

The following technical indicators are used to represent the state of the financial environment. They are calculated based on the historical price data of the assets in the portfolio.

• Simple Moving Average (SMA): Lagging indicator that smooths the price over a period of time. It is the unweighted mean of the previous k data points and is computed following:

$$SMA_t^k = \frac{1}{k} \sum_{i=t-k+1}^t p_i, \tag{B.1}$$

where t is the current time step, k is the look-back period and p_i is the close price at time i. In this thesis, the SMA is calculated for 5, 10 and 20 days.

• Exponential Moving Average (EMA): Weighted moving average that gives more importance to recent prices with the goal of making it more responsive to new

information. It is calculated using the formula:

$$EMA_{t}^{k} = \begin{cases} p_{t} & \text{if } t = 0\\ \frac{2}{k+1}p_{t} + \left(1 - \frac{2}{k+1}\right)EMA_{t-1}^{k} & \text{if } t > 0 \end{cases}$$
(B.2)

where k is the look-back period, p_t is the close price at time t and $\frac{2}{k+1}$ is the smoothing factor. In this thesis, the EMA is calculated for 5 and 10 days.

• Moving Average Convergence Divergence (MACD): Momentum indicator that shows the relationship between two moving average of an asset's price. The formula is:

$$MACD_t = EMA_t^{k_1} - EMA_t^{k_2}, (B.3)$$

where k_1 and k_2 are the look-back periods for the short-term (12 periods) and long-term (26 periods) EMAs, respectively, and p_t is the close price at time t.

Relative Strength Index (RSI): Momentum indicator that measures the magnitude
of recent changes to identify overbought or oversold conditions in the market. It is
computed using smoothed moving averages for the upward change in closing price
p_t, defined as u_t = max{p_t - p_{t-1}, 0}:

$$SMMA_{t}^{k}(u_{t}) = \frac{1}{k}u_{t} + \left(1 - \frac{1}{k}\right)SMMA_{t-1}^{k}(u_{t-1})$$
(B.4)

and for the downward change, defined as $d_t = \max\{p_{t-1} - p_t, 0\}$:

$$SMMA_t^k(d_t) = \frac{1}{k}d_t + \left(1 - \frac{1}{k}\right)SMMA_{t-1}^k(d_{t-1}).$$
 (B.5)

Then, the Relative Strength Index (RSI) is given by:

$$RSI_t = 100 - \frac{100}{1 + RS_t},\tag{B.6}$$

where the relative strength RS_t is defined as:

$$RS_t = \frac{SMMA_t^k(u_t)}{SMMA_t^k(d_t)}.$$
(B.7)

• Commodity Channel Index (CCI): Momentum indicator that measures the deviation of the price from its historical average price over a period of time. It is calculated as:

$$CCI_t^k = \frac{TP_t^k - MA_t^k}{0.015 \cdot MD_t},$$
(B.8)

where k is the number of periods (14 days), the typical price TP_t is:

$$TP_t = \sum_{i=t-k+1}^t \frac{p_i + h_i + l_i}{3},$$
(B.9)

with p_t , h_t and l_t being the close, high and low prices at time step t, respectively, and the moving average MA_t^k is:

$$MA_t^k = \frac{1}{k} \sum_{i=t-k+1}^t TP_i$$
 (B.10)

and the mean deviation MD_t is:

$$MD_t = \frac{1}{k} \sum_{i=t-k+1}^{t} \left| TP_i - MA_i^k \right|.$$
(B.11)

 Bollinger Bands: Volatility indicator that defines the trend-line for high and low prices based on the deviation of the asset from the moving average. The upper bands is calculated as:

$$BOLLUB_t^k = MA_t^k + m \cdot SD_t^k,$$
 (B.12)

where k is the number of periods (20 days), m is the number of standard deviations

away from the moving average (2 standard deviations) and SD_t^k is the standard deviation of the typical price over the same period. Similarly, the lower band is calculated as:

$$BOLLDB_t^k = MA_t^k - m \cdot SD_t^k.$$
(B.13)

• Average True Range (ATR): Volatility indicator that measures the average range of price movement over a period of time, usually 14 days. It is calculated as:

$$ATR_t^k = \frac{1}{k} \sum_{i=t-k+1}^t TR_i,$$
(B.14)

where the true range TR_i is defined as:

$$TR_i = \max\{h_i - l_i, |h_i - p_{i-1}|, |l_i - p_{i-1}|\},$$
 (B.15)

where h_i and l_i are the high and low prices of the asset at time i, respectively, and p_{i-1} is the close price of the asset at time i-1. The true range finds the maximum of the following three:

- most recent period high minus most recent period low,
- absolute value of the most recent period high minus the previous close, and
- absolute value of the most recent period low minus the previous close.
- Average Directional Index (ADX): Trend indicator used to measure the strength of a trend by quantifying the price movement. It is calculated as:

$$ADX_t^k = \frac{1}{k} \sum_{i=t-k+1}^t DX_i,$$
 (B.16)

where the Directional Movement Index (DX) is defined as:

$$DX_t = \frac{100 \cdot |PDI_t - MDI_t|}{PDI_t + MDI_t}$$
(B.17)

with the Positive Directional Index (PDI) and Negative Directional Index (MDI) calculated as

$$PDI_{t} = \frac{100 \cdot SMMA_{t}^{k}(DM^{+})}{ATR_{t}^{k}}$$
(B.18)

and

$$MDI_t = \frac{100 \cdot SMMA_t^k(DM^-)}{ATR_t^k},$$
(B.19)

where DM⁺ and DM⁻ are the positive and negative directional movements, respectively, calculated as:

$$DM^{+} = \max(0, h_{t} - h_{t-1})$$
(B.20)

and

$$DM^{-} = \max(0, l_{t-1} - l_t), \qquad (B.21)$$

where h_t and l_t are the high and low prices of the asset at time t, respectively.

• Rate of Change (ROC): Momentum indicator that measures the percentage change in price between the current price p_t and the price p_{t-k} periods ago. It is given by the formula:

$$ROC_t^k = \frac{p_t - p_{t-k}}{p_{t-k}} \cdot 100.$$
 (B.22)

In this thesis, the ROC is calculated for k = 10 days.

B.2 Macroeconomic Indicators

The following macroeconomic indicators are used to represent the state of the financial environment. They provide additional context about the market conditions and are calculated based on external data sources.

- Volatility Index (VIX) measures the market's expectation of future volatility based on options prices. This is only available for US markets.
 - VIX is calculated using the implied volatility of Standard and Poor's 500
 Index (S&P 500) options.
 - VXD is calculated using the implied volatility of Dow Jones 30 Index (DW30) options.
- Currency index captures the impact from the monetary market on the stock market.
 - U.S. Dollar Index (DXY): United States (U.S.) dollar's value relative to a basket of foreign currencies.
 - Euro Index (EXY): Euro's value relative to a basket of foreign currencies.
 - British Pound Currency Index (BXY): British pound's value relative to a basket of foreign currencies.
- Interest rates reflect the cost of borrowing money and the return on savings. This is only available for US markets.
 - 3-Month Treasury Yield (IRX): Reflects the return on investment for a 3-month government bond.
 - 5-Year Treasury Yield (FVX): Reflects the return on investment for a 5-year government bond.

 10-Year Treasury Yield (TNX): Reflects the return on investment for a 10-year government bond.

Appendix C

Hyper-parameter tuning

For the five implemented Deep Reinforcement Learning algorithms, the following table summarises the hyper-parameters that were tuned during the training process.

Model	Hyperparameter	Values / Range
	Number of steps	{5, 10, 20, 30, 40}
A2C	Entropy coefficient	Uniform[1×10^{-8} , 1×10^{-3}]
	Learning rate	Uniform[1×10^{-5} , 1×10^{-2}]
	Number of steps	{128, 256, 512, 1024, 2048}
PPO	Entropy coefficient	Uniform[1×10^{-8} , 1×10^{-3}]
PPO	Learning rate	Uniform[1×10^{-5} , 1×10^{-2}]
	Batch size	{32, 64, 128, 256, 512}
	Batch size	{64, 128, 256}
DDPG	Buffer size	{50000, 100000, 200000, 500000}
	Learning rate	Uniform[1×10^{-5} , 1×10^{-2}]
	Batch size	{64, 100, 128, 256}
TD3	Buffer size	{500000, 1000000, 2000000}

Model	Hyperparameter	Values / Range
	Learning rate	Uniform[1×10^{-5} , 1×10^{-2}]
	Batch size	{32, 64, 128}
	Buffer size	{100000, 500000, 1000000, 2000000}
SAC	Learning rate	Uniform[1×10^{-5} , 1×10^{-2}]
	Learning starts	{500, 1000, 2000, 5000}
	Entropy coefficient	{"auto", "auto_0.1", "auto_0.01"}

Table C.1: Hyper-parameter tuning configurations for different RL algorithms.

Appendix D

Datasets

D.1 Equities

D.1.1 Dow Jones 30

The Dow Jones Industrial Average (DJIA) is a stock market index with 30 companies listed on United States (U.S.) stock exchanges. The trading symbol is $\hat{D}JI$ and as of April 2025, its constituents are:

Symbol	Name	Sector	Industry
AXP	American Ex-	Financial Services	Credit Services
	press		
AMGN	Amgen	Healthcare	Drug Manufacturers -
			General
AAPL	Apple	Technology	Consumer Electronics
AMZN	Amazon	Consumer Cyclical	Internet Retail
BA	Boeing	Industrials	Aerospace & Defense

Symbol	Name	Sector	Industry
CAT	Caterpillar	Industrials	Farm & Heavy Con-
			struction Machinery
CRM	Salesforce	Technology	Software - Application
CSCO	Cisco	Technology	Communication Equip-
			ment
CVX	Chevron	Energy	Oil & Gas Integrated
DIS	Walt Disney	Communication Ser-	Entertainment
		vices	
GS	Goldman Sachs	Financial Services	Capital Markets
HD	Home Depot	Consumer Cyclical	Home Improvement Re-
			tail
HON	Honeywell	Industrials	Conglomerates
IBM	IBM	Technology	Information Technology
			Services
JNJ	Johnson & John-	Healthcare	Drug Manufacturers -
	son		General
JPM	JP Morgan Chase	Financial Services	Banks - Diversified
КО	Coca-Cola	Consumer Defensive	Beverages - Non-
			Alcoholic
MCD	McDonald's	Consumer Cyclical	Restaurants
MMM	3M	Industrials	Conglomerates
MRK	Merck	Healthcare	Drug Manufacturers -
			General
MSFT	Microsoft	Technology	Software - Infrastruc-
			ture

Symbol	Name	Sector	Industry
NKE	Nike	Consumer Cyclical	Footwear & Accessories
NVDA	NVIDIA	Technology	Semiconductors
PG	Procter & Gam-	Consumer Defensive	Household & Personal
	ble		Products
SHW	Sherwin-Williams	Basic Materials	Specialty Chemicals
TRV	Travelers	Financial Services	Insurance - Property &
			Casualty
UNH	UnitedHealth	Healthcare	Healthcare Plans
V	Visa	Financial Services	Credit Services
VZ	Verizon	Communication Ser-	Telecom Services
		vices	
WMT	Walmart	Consumer Defensive	Discount Stores

Table D.1: Constituents of the Dow Jones Industrial Average index as of April 2025. [4]

D.1.2 Euro Stoxx 50

The Euro Stoxx 50 Index (Euro Stoxx 50) is a stock market index that represents 50 of the largest companies in the Eurozone. The trading symbol is \$TOXX50E and as of April 2025, its constituents are:

Symbol	Name	Sector	Industry
ADS.DE	adidas	Consumer Cyclical	Footwear & Accessories
ADYEN.AS	Adyen	Technology	Software - Infrastruc-
			ture

Symbol	Name	Sector	Industry
AD.AS	Koninklijke	Consumer Defensive	Grocery Stores
	Ahold Delhaize		
AI.PA	L'Air Liquide	Basic Materials	Specialty Chemicals
AIR.PA	Airbus	Industrials	Aerospace & Defense
ALV.DE	Allianz	Financial Services	Insurance - Diversified
ABI.BR	Anheuser-Busch	Consumer Defensive	Beverages - Brewers
	InBev		
ASML.AS	ASML Holding	Technology	Semiconductor Equip-
			ment & Materials
CS.PA	AXA	Financial Services	Insurance - Diversified
BAS.DE	BASF	Basic Materials	Chemicals
BAYN.DE	Bayer	Healthcare	Drug Manufacturers -
			General
BBVA.MC	BBVA	Financial Services	Banks - Diversified
SAN.MC	Banco Santander	Financial Services	Banks - Diversified
BMW.DE	BMW	Consumer Cyclical	Auto Manufacturers
BNP.PA	BNP Paribas	Financial Services	Banks - Regional
BN.PA	Danone	Consumer Defensive	Packaged Foods
DB1.DE	Deutsche Börse	Financial Services	Financial Data & Stock
			Exchanges
DHL.DE	Deutsche Post	Industrials	Integrated Freight &
			Logistics
DTE.DE	Deutsche	Communication Ser-	Telecom Services
	Telekom	vices	
ENEL.MI	Enel	Utilities	Utilities - Diversified

Symbol	Name	Sector	Industry
ENI.MI	Eni	Energy	Oil & Gas Integrated
EL.PA	EssilorLuxottica	Healthcare	Medical Instruments & Supplies
RACE.MI	Ferrari	Consumer Cyclical	Auto Manufacturers
FLTR.L	Flutter Enter- tainment	Consumer Cyclical	Gambling
RMS.PA	Hermès Interna- tional	Consumer Cyclical	Luxury Goods
IBE.MC	Iberdrola	Utilities	Utilities - Diversified
ITX.MC	Industria de Diseño Textil	Consumer Cyclical	Apparel Retail
IFX.DE	Infineon Technologies	Technology	Semiconductors
INGA.AS	ING Groep	Financial Services	Banks - Diversified
ISP.MI	Intesa Sanpaolo	Financial Services	Banks - Regional
KER.PA	Kering	Consumer Cyclical	Luxury Goods
OR.PA	L'Oréal	Consumer Defensive	Household & Personal Products
MC.PA	LVMH Moët Hennessy - Louis Vuitton	Consumer Cyclical	Luxury Goods
MBG.DE	Mercedes-Benz Group AG	Consumer Cyclical	Auto Manufacturers

Symbol	Name	Sector	Industry
MUV2.DE	Münchener	Financial Services	Insurance - Reinsurance
	Rückversicherungs-		
	Gesellschaft		
NOKIA.HE	Nokia	Technology	Communication Equipment
NDA-	Nordea Bank	Financial Services	Banks - Regional
FI.HE			
RI.PA	Pernod Ricard	Consumer Defensive	Beverages - Wineries &
			Distilleries
PRX.AS	Prosus	Communication Ser-	Internet Content & In-
		vices	formation
SAF.PA	Safran	Industrials	Aerospace & Defense
SGO.PA	Compagnie de	Industrials	Building Products &
	Saint-Gobain		Equipment
SAN.PA	Sanofi	Healthcare	Drug Manufacturers -
			General
SAP.DE	SAP	Technology	Software - Application
SU.PA	Schneider Electric	Industrials	Specialty Industrial
			Machinery
SIE.DE	Siemens	Industrials	Specialty Industrial
			Machinery
STLAM.MI	Stellantis	Consumer Cyclical	Auto Manufacturers
TTE.PA	TotalEnergies	Energy	Oil & Gas Integrated
DG.PA	Vinci	Industrials	Engineering & Construction

Symbol	Name	Sector	Industry
UCG.MI	UniCredit	Financial Services	Banks - Regional
VOW.DE	Volkswagen	Consumer Cyclical	Auto Manufacturers

Table D.2: Constituents of the Euro Stoxx 50 index as of April 2025. [5]

D.1.3 FTSE 100

The Financial Times Stock Exchange 100 Index (FTSE 100) is a stock market index that represents 100 of the largest companies listed on the London Stock Exchange. The trading symbol is FTSE and as of April 2025, its constituents are:

Symbol	Name	Industry
III.L	3i Group	Financial Services
ADM.L	Admiral Group	Insurance
AAF.L	Airtel Africa	Telecommunications Services
ALW.L	Alliance Witan	Investment Trusts
AAL.L	Anglo American	Mining
ANTO.L	Antofagasta	Mining
AHT.L	Ashtead Group	Support Services
ABF.L	Associated British	Food & Tobacco
	Foods	
AZN.L	AstraZeneca	Pharmaceuticals & Biotechnology
AUTO.L	Auto Trader Group	Media
AV.L	Aviva	Life Insurance
BAB.L	Babcock International	Aerospace & Defence
	Group	

Symbol	Name	Industry
BA.L	BAE Systems	Aerospace & Defence
BARC.L	Barclays	Banks
BTRW.L	Barratt Redrow	Household Goods & Home Con-
		struction
BEZ.L	Beazley	Insurance
BKG.L	The Berkeley Group	Household Goods & Home Con-
	Holdings	struction
BP.L	BP	Oil & Gas Producers
BATS.L	British American To-	Tobacco
	bacco	
BT-A.L	BT Group	Telecommunications Services
BNZL.L	Bunzl	Support Services
CNA.L	Centrica	Multiline Utilities
CCEP.L	Coca-Cola Europacific	Beverages
	Partners	
CCH.L	Coca-Cola HBC	Beverages
CPG.L	Compass Group	Support Services
CTEC.L	ConvaTec Group	Health Care Equipment & Services
CRDA.L	Croda International	Chemicals
DCC.L	DCC	Support Services
DGE.L	Diageo	Beverages
DPLM.L	Diploma	Industrial Support Services
EDV.L	Endeavour Mining	Precious Metals and Mining
ENT.L	Entain	Travel & Leisure
EZJ.L	easyJet	Travel & Leisure

Symbol	Name	Industry	
EXPN.L	Experian	Support Services	
FCIT.L	F&C Investment Trust	Collective Investments	
FRES.L	Fresnillo	Mining	
GAW.L	Games Workshop	Leisure Goods	
	Group		
GLEN.L	Glencore	Mining	
GSK.L	GSK	Pharmaceuticals & Biotechnology	
HLN.L	Haleon	Pharmaceuticals & Biotechnology	
HLMA.L	Halma	Electronic Equipment & Parts	
HIK.L	Hikma Pharmaceuticals	Pharmaceuticals & Biotechnology	
HSX.L	Hiscox	Non-life insurance	
HWDN.L	Howden Joinery Group	Homebuilding & Construction Sup-	
		plies	
HSBA.L	HSBC Holdings	Banks	
IHG.L	InterContinental Hotels	Travel & Leisure	
	Group		
IMI.L	IMI	Industrial Engineering	
IMB.L	Imperial Brands	Tobacco	
INF.L	Informa	Media	
ICG.L	ICG	Financial Services	
IAG.L	International Consoli-	Travel & Leisure	
	dated Airlines Group		
ITRK.L	Intertek Group	Support Services	
JD.L	JD Sports Fashion	General Retailers	
KGF.L	Kingfisher	Retailers	

Symbol	Name	Industry		
LAND.L	Land Securities	Real Estate Investment Trusts		
LGEN.L	Legal & General	Life Insurance		
LLOY.L	Lloyds Banking	Banks		
LMP.L	LondonMetric Property	Real Estate Investment Trusts		
LSEG.L	London Stock Exchange	Financial Services		
	Group			
MNG.L	M&G	Financial Services		
MKS.L	Marks and Spencer	Food & Drug Retailing		
MRO.L	Melrose Industries	Aerospace & Defence		
MNDI.L	Mondi	Containers & Packaging		
NG.L	National Grid	Multiline Utilities		
NWG.L	NatWest	Banks		
NXT.L	NEXT	General Retailers		
PSON.L	Pearson	Media		
PSH.L	Pershing Square Hold-	Financial Services		
	ings			
PSN.L	Persimmon	Household Goods & Home Con-		
		struction		
PHNX.L	Phoenix Group	Life Insurance		
PCT.L	Polar Capital Technol-	Investment Trusts		
	ogy			
PRU.L	Prudential	Life Insurance		
RKT.L	Reckitt Benckiser	Household Goods & Home Con-		
		struction		
REL.L	RELX	Media		

Symbol	Name	Industry	
RTO.L	Rentokil Initial	Support Services	
RMV.L	Rightmove	Media	
RIO.L	Rio Tinto	Mining	
RR.L	Rolls-Royce Holdings	Aerospace & Defence	
SGE.L	The Sage Group	Software & Computer Services	
SBRY.L	J Sainsbury	Food & Drug Retailing	
SDR.L	Schroders	Financial Services	
SMT.L	Scottish Mortgage	Collective Investments	
SGRO.L	SEGRO	Real Estate Investment Trusts	
SVT.L	Severn Trent	Multiline Utilities	
SHEL.L	Shell	Oil & Gas Producers	
SMIN.L	Smiths Group	Industrial Engineering	
SN.L	Smith & Nephew	Health Care Equipment & Services	
SPX.L	Spirax Group	Industrial Engineering	
SSE.L	SSE	Electrical Utilities & Independent	
		Power Producers	
STAN.L	Standard Chartered	Banks	
STJ.L	St. James's Place	Financial Services	
TW.L	Taylor Wimpey	Household Goods & Home Con-	
		struction	
TSCO.L	Tesco	Food & Drug Retailing	
ULVR.L	Unilever	Personal Goods	
UU.L	United Utilities	Multiline Utilities	
UTG.L	Unite Group	Real Estate Investment Trusts	
VOD.L	Vodafone Group	Mobile Telecommunications	

Symbol	Name	Industry	
WEIR.L	The Weir Group	Industrial Goods and Services	
WTB.L	Whitbread	Retail Hospitality	
WPP.L	WPP	Media	

Table D.3: Constituents of the FTSE100 index as of April 2025. [6]

D.2 Commodities

The commodities market includes a variety of physical goods that are traded on exchanges. The following table lists a sample of 6 commodities:

Symbol	Name	
CL=F	Crude Oil	
NG=F	Natural Gas	
GC=F	Gold	
SI=F	Silver	
ALI=F	Aluminum	
HG=F	Copper	

Table D.4: 6 Commodities Futures Contracts

D.3 Currencies

The currencies market includes a variety of currency pairs that are traded on exchanges. The following table lists a sample of 10 currency pairs, selected for their trading volume. Note that the trading symbols all have United States Dollar (USD) as the quote currency.

Symbol	Name		
EURUSD=X	Euro (EUR)/USD		
GBPUSD=X	British Pound (GBP)/USD		
JPYUSD=X	Japanese Yen (JPY)/USD		
AUDUSD=X	Australian Dollar (AUD)/USD		
CADUSD=X	Canadian Dollar (CAD)/USD		
CNYUSD=X	Chinese Yuan (CNY)/USD		
CHFUSD=X	Swiss Franc (CHF)/USD		
HKDUSD=X	Hong Kong Dollar (HKD)/USD		
KRWUSD=X	South Korean Won (KRW)/USD		
INRUSD=X	Indian Rupee (INR)/USD		

Table D.5: 10 Currency Pairs

Appendix E

Default Hyper-parameter

Selection

The choice of hyper-parameters is crucial for the performance of DRL algorithms. However, it is computationally expensive to perform hyper-parameter tuning for all combinations of algorithms, datasets and environment representations. Therefore, the default hyper-parameters used in the experiments are outlined in Table 4.2. These hyper-parameters were selected based on preliminary tests conducted on a small dataset of five tickers (AAPL, CSCO, HON, MSFT, V) sampled from the DJIA and only the open, close, high and low prices as the environment representation.

The hyper-parameters were tuned according to the specifications in Table C.1 and the results were used to inform the default settings, outlined in Table 4.2. For each of the five DRL algorithms, the hyper-parameter search was performed using Bayesian optimisation using the wandb library and a maximum number of runs set to 20. The training set was data from January 2016 to December 2022, the validation set started in January 2023 and ended in December 2023, and the test set was between January 2024 and June 2025. The dataset split is visualised in Figure E.1.

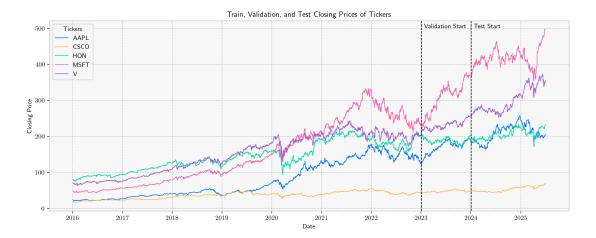


Figure E.1: Train-Validation-Test Split for the Hyper-parameter tuning on a sample of five assets from the Dow Jones Industrial Average index.

The wandb library provides an interactive website to visualise the results of the hyperparameters in terms of the metric chosen for the optimisation and, if applicable, any other metrics that were chosen to be reported. In this case, the optimisation metric was the Sharpe ratio, as it balances the trade-off between risk and return, and additionally, the cumulative return was also reported. Figure E.2 shows the reported results for the hyper-parameter tuning of the A2C algorithm. Within the figure, there are three charts where the left one shows the Sharpe ratio over all sweeps, the middle one shows the cumulative return, and the right one shows the hyper-parameters that were tuned and the resulting optimisation metric.



Figure E.2: Hyper-parameter tuning results for the A2C algorithm.

The hyper-parameter tuning process was repeated for the other four algorithms, resulting in the hyper-parameters shown in Table 4.2. Since the search had been done in the validation dataset, the best-performing models were evaluated and benchmarked against the test dataset to assess their generalisation performance, whose results are presented in Table E.1.

Dataset	Cumulative	Annualised	Annualised	Sharpe	Max
	return	return	volatility	ratio	drawdown
A2C	0.2598	0.1679	0.1968	0.8859	-0.2186
PPO	0.3375	0.2158	0.1697	1.2364	-0.1630
DDPG	0.3494	0.2231	0.1763	1.2300	-0.1684
TD3	0.3401	0.2174	0.1731	1.2227	-0.1598
SAC	0.2659	0.1717	0.1762	0.9866	-0.1825
Mean	0.1503	0.0989	0.1896	0.5923	-0.1972
Min	0.3609	0.2308	0.1681	1.3193	-0.1559
Momentum	0.1635	0.1074	0.1868	0.6396	-0.2025
Equal	0.3123	0.2010	0.1758	1.1290	-0.1762

Table E.1: Results of hyper-parameter tuning on the test dataset.

Appendix F

Evaluation Metrics

The following list outlines additional evaluation metrics that can be used to assess the performance of trading strategies.

• Calmar ratio: A risk-adjusted performance measure that compares the average annual compounded rate of return to the maximum drawdown, providing insight into how much return an investor receives for each unit of risk taken.

$$Calmar Ratio = \frac{Average Annualised Return}{Max Drawdown}$$
 (F.1)

• Stability: A measure that determines the R-square of a linear fit to the cumulative log returns, to indicate how well returns follow a linear trend over time.

Stability =
$$R^2 = 1 - \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$
 (F.2)

where y_i is the observed cumulative log return, \hat{y}_i is the predicted cumulative log return from the linear fit, \bar{y} is the mean of the observed cumulative log returns and n is the number of observations.

• Omega ratio: A probability-weighted ratio that compares the gains versus losses relative to a threshold return target, either set to zero or the risk-free rate. It is a proxy for the likelihood of achieving returns above a certain threshold compared to the likelihood of experiencing losses below that threshold.

Omega Ratio =
$$\Omega(\theta) = \frac{\int_{\theta}^{\infty} (1 - F(r)) dr}{\int_{-\infty}^{\theta} F(r) dr}$$
 (F.3)

where θ is the threshold return and F(r) is the cumulative distribution function of returns.

• Sortino ratio: A modification of the Sharpe ratio that only considers downside risk, measuring the risk-adjusted return of an investment by comparing the excess return to the downside deviation.

Sortino Ratio =
$$\frac{R_p - R_f}{\sigma_d}$$
 (F.4)

where R_p is the annualised return of the portfolio, R_f is the annualised risk-free rate, and σ_d is the downside deviation of the portfolio returns, i.e. the standard deviation of only the negative returns.

• Skewness: A measure of the asymmetry of the return distribution, indicating whether returns have a tendency toward positive or negative extremes.

Skewness =
$$\frac{\sum_{i=1}^{n} (R_i - \mu)^3}{(n-1) \cdot \sigma^3}$$
 (F.5)

where R_i is the return of the portfolio at time i, μ is the mean return, σ is the standard deviation of returns, and n is the number of observations.

• Kurtosis: A measure of the "tailedness" of the return distribution, indicating the

frequency of extreme values compared to a normal distribution.

$$Kurtosis = \frac{\sum_{i=1}^{n} (R_i - \mu)^4}{(n-1) \cdot \sigma^4}$$
 (F.6)

where R_i is the return of the portfolio at time i, μ is the mean return, σ is the standard deviation of returns, and n is the number of observations.

• Tail ratio: A measure of the relative magnitude of extreme positive returns compared to extreme negative returns, calculated as the ratio between the right (95th percentile) and the left (5th percentile) tails of the distribution of returns.

$$Tail Ratio = \frac{Right Tail (95th Percentile)}{Left Tail (5th Percentile)}$$
(F.7)

• Daily Value at Risk (VaR): A measure of the potential loss that could occur in a portfolio over a single day at a specified confidence level, typically 95%. The computation is done using the variance-covariance calculation:

Daily VaR =
$$(R_p - z \cdot \sigma_p) \times V_p$$
 (F.8)

where R_p is the expected daily return, z is the z-score of the desired level of confidence, σ_p is the daily standard deviation of portfolio returns, and V_p is the value of the portfolio.

Appendix G

Experiment Results

In this Appendix, the results of the experiments conducted to evaluate the performance of the implemented algorithms under changing conditions are presented. Only the tables that do not fit in the main Results chapter 4 are included here.

G.1 Experiment: Algorithm Comparison

The following tables summarise the results of the algorithm comparison experiment conducted on the 5 datasets with OHLCV prices as the environment representation. The results for the A2C algorithm are presented in Table 4.4 in Section 4.4, whereas for the PPO, DDPG, TD3 and SAC algorithms, the results are presented in the following tables.

Dataset	Cumulative Annualised		Annualised	Sharpe	Max
	return	return	volatility	ratio	drawdown
Dow Jones 30	0.2035	0.3174	0.1461	1.3410	-0.1503
Euro Stoxx 50	0.1557	0.2438	0.1549	1.0117	-0.1706

Dataset	Cumulative	Annualised Annualis		Sharpe	Max
	return	return	volatility	ratio	drawdown
FTSE 100	0.1246	0.1931	0.1244	1.0063	-0.1315
Commodities	0.2531	0.3990	0.1941	1.2600	-0.1522
Currencies	-0.0011	-0.0017	0.0493	0.0014	-0.0726

Table G.1: Algorithm comparison results for the PPO implementation.

Dataset	Cumulative	umulative Annualised Annualised		Sharpe	Max
	return	return	volatility	ratio	drawdown
Dow Jones 30	0.2206	0.3454	0.1526	1.3826	-0.1560
Euro Stoxx 50	0.1292	0.2011	0.1556	0.8592	-0.1774
FTSE 100	0.1336	0.2076	0.1229	1.0822	-0.1248
Commodities	0.2168	0.3391	0.1811	1.1745	-0.1237
Currencies	0.0014	0.0021	0.0559	0.0528	-0.0802

Table G.2: Algorithm comparison results for the DDPG implementation.

Dataset	Cumulative return	Annualised return	Annualised volatility	Sharpe ratio	Max drawdown
Dow Jones 30	0.2478	0.3902	0.1567	1.4911	-0.1567
Euro Stoxx 50	0.1547	0.2423	0.1487	1.0420	-0.1645
FTSE 100	0.1325	0.2058	0.1231	1.0729	-0.1263
Commodities	0.2768	0.4386	0.1792	1.4537	-0.1224
Currencies	0.0026	0.0038	0.0438	0.0807	-0.0639

Table G.3: Algorithm comparison results for the TD3 implementation.

Dataset	Cumulative	Annualised Annualised		Sharpe	Max
	return	return	volatility	ratio	drawdown
Dow Jones 30	0.1457	0.2243	0.1508	0.9769	-0.1750
Euro Stoxx 50	0.1761	0.2771	0.1520	1.1437	-0.1718
FTSE 100	0.1319	0.2048	0.1279	1.0326	-0.1404
Commodities	0.0027	0.0041	0.0480	0.0806	-0.0704
Currencies	0.2563	0.4044	0.1778	1.3727	-0.1356

Table G.4: Algorithm comparison results for the SAC implementation.

G.2 Experiment: Environment Representation

The table G.5 summarises the performance, according to the cumulative return, of the five algorithms in the four possible different environment representations: OHLCV prices, OHLCV prices with indicators, OHLCV prices with covariance, and OHLCV prices with indicators and covariance. The results are presented for three datasets: DowJones30, Commodities, and Currencies.

Algorithm	Dataset	Simple	Indicators	Covariance	Complete
A2C	DowJones30	0.3387	0.3139	0.3464	0.3239
	Commodities	0.3695	0.4133	0.3883	0.4098
	Currencies	-0.0017	-0.0071	-0.0069	-0.0023
PPO	DowJones30	0.3174	0.2937	0.3221	0.2713
	Commodities	0.3990	0.3565	0.3689	0.3751
	Currencies	-0.0017	0.0033	0.0029	0.0083

Table G.5: Environment representation experiment comparison according to the cumulative return. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset.

Algorithm	Dataset	Simple	Indicators	Covariance	Complete
DDPG	DowJones30	0.3454	0.3663	0.3128	0.3301
	Commodities	0.3391	0.3339	0.3616	0.4211
	Currencies	0.0021	0.0032	-0.0002	-0.0006
TD3	DowJones30	0.3902	0.3456	0.2571	0.2787
	Commodities	0.4386	0.3632	0.3292	0.4312
	Currencies	0.0038	-0.0022	-0.0023	-0.005
SAC	DowJones30	0.2243	0.3189	0.3774	0.3162
	Commodities	0.4044	0.3371	0.3958	0.3025
	Currencies	0.0041	0.0114	-0.0117	0.0179

Table G.5: Environment representation experiment comparison according to the cumulative return. The colour correspond to the best performing per row, with blue for the DowJones30 dataset and green for the Commodities dataset.

Appendix H

Explainability Results

H.1 Feature Importance

Figure H.1 shows the top features grouped by asset according to the feature importance of the surrogate model.

Figure H.2 shows the mean feature importance for each type of feature, i.e. open, close, high and low prices, over the assets.

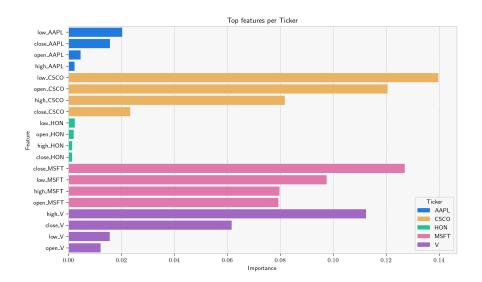


Figure H.1: Top features grouped by asset from the surrogate model according to feature importance.

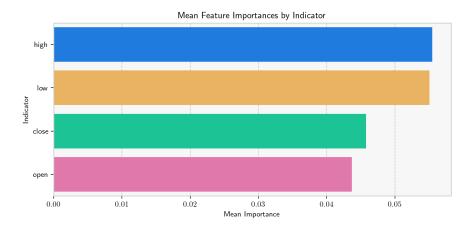


Figure H.2: Mean feature importance per type of feature from the surrogate model.

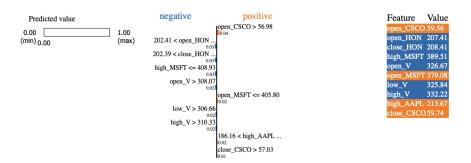


Figure H.3: LIME explanations for the A2C algorithm at the first time step of the test dataset for the AAPL asset.

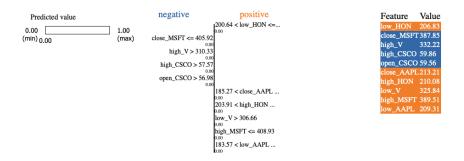


Figure H.4: LIME explanations for the A2C algorithm at the first time step of the test dataset for the CSCO asset.

H.2 Local Importance Model-Agnostic Explanation Results

With the LIME analysis, the explanations for the A2C algorithm are provided. Since these are local observations, the following figures provide the explanation for the first time step on the test dataset of the assets not included in the main text. Values coloured in orange represent features that contribute positively to the prediction, while blue values indicate features that contribute negatively.



Figure H.5: LIME explanations for the A2C algorithm at the first time step of the test dataset for the HON asset.

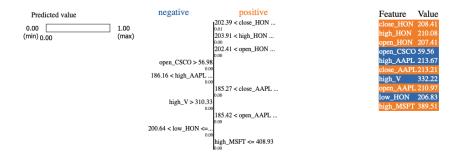


Figure H.6: LIME explanations for the A2C algorithm at the first time step of the test dataset for the V asset.

Appendix I

Code

The following section illustrates the code implementation of the project. It includes the main components of the codebase such as data download and pre-processing, model training and evaluation, benchmarking and explainability techniques.

The code is structured in a modular way, where each module corresponds to a specific functionality. The main components are:

- Configuration: This module manages the configuration settings that define the list of assets, the training-test periods, and other hyper-parameters.
- Data Download and Pre-processing: This module handles the downloading of datasets, cleaning, and pre-processing steps necessary for training the models.
- Agents: This module contains the implementation of the DRL agents capable of interacting with the environment, learning from it, and making decisions based on the observations received.
- Environments: This module defines the various environments in which the agents operate, including the state and action spaces, as well as the reward functions.

- Benchmarking: This module contains the implementation of the benchmarking strategies as well as the evaluation metrics used to assess the performance of the agents.
- Explainability: This module implements the explainability techniques used to interpret the agents' decisions and understand their behaviour.
- Visualiser: This module provides visualisations tools for the data, agents' performance, benchmarking comparisons and explainability results.
- **Optimisation**: This module contains the integration with hyper-parameter tuning libraries to find optimal configurations and track the experiments.

The modules are implemented as Python packages, each containing the necessary code and resources for its specific functionality. Additionally, the project contains a folder titled examples, where the main Jupyter notebooks to perform each of the separate tasks of this project are implemented. The directory structure is organised as follows:

```
xdl-portfolio/
|
+-- agents/
| +-- __init__.py
| +-- drl_agent.py
| +-- tb_callback.py
|
+-- config/
| +-- __init__.py
| +-- config.py
| +-- config_indicators.py
| +-- config_tickers.py
```

```
+-- config_models.py
+-- environments/
| +-- __init__.py
  +-- env_portfolio_optimisation.py
+-- examples/
| +-- findownloader.ipynb
| +-- finpreprocessor.ipynb
+-- portfolio_optimisation.ipynb
| +-- backtesting.ipynb
 +-- hyperparameter_tuning.ipynb
  +-- explainability.ipynb
+-- explainability/
| +-- __init__.py
+-- explainability.py
+-- feature_importance.py
+-- lime_explainability.py
  +-- shap_explainability.py
+-- optimisation/
| +-- __init__.py
| +-- wandb_opt.py
+-- pbenchmark/
| +-- __init__.py
```

```
+-- portfolio_benchmark.py
|
+-- preprocessor/
| +-- __init__.py
| +-- findata_downloader.py
| +-- findata_preprocessor.py
|
+-- visualisation/
| +-- __init__.py
| +-- benchmark_visualiser.py
| +-- findata_visualiser.py
| +-- model_visualiser.py
| +-- shap_visualiser.py
| +-- style.mplstyle
+-- README.md
+-- requirements.txt
```

The code is available as a GitHub repository at XDL-Portfolio.

I.1 Configuration Module

Listing 1: config.py

```
from config import config_indicators, config_tickers

START_DATE = "2016-01-01"

END_DATE = "2025-07-01"

DATA_DIR = "data"

PLOT_DIR = "figures"

RESULTS_DIR = "results"

MODELS_DIR = "models"

LOGS_DIR = "logs"
```

```
INITIAL_AMOUNT = 100000 # Initial capital for the portfolio
12
13
    TEST_NAME = "test"
14
    DOW_3O_NAME = "dow30"
15
    EURO_STOXX_50_NAME = "eurostoxx50"
16
    FTSE_100_NAME = "ftse100"
17
    SP_500_NAME = "sp500"
18
    FX_NAME = "currencies"
19
    COMMODITY_NAME = "futures"
20
21
   DOW_30_INDEX = "^DJI"
22
   EURO_STOXX_50_INDEX = "^STOXX50E"
23
   FTSE_100_INDEX = "^FTSE"
   SP_500_INDEX = "^GSPC"
25
26
   EXCHANGE_NYSE = "XNYS" # New York Stock Exchange
27
28
    EXCHANGE_LSE = "XLON" # London Stock Exchange
   EXCHANGE_DAX = "XFRA" # Frankfurt Stock Exchange
29
30
   TRAIN_START_DATE = START_DATE
31
   TRAIN_END_DATE = "2022-12-31"
32
   VAL_START_DATE = "2023-01-01"
33
   VAL_END_DATE = "2023-12-31"
   TEST_START_DATE = "2024-01-01"
    TEST_END_DATE = END_DATE
36
37
    # Configuration for indicators
38
    USE_TECHNICAL_INDICATORS = True
39
    USE_MACROECONOMIC_INDICATORS = True
    # Configuration for covariance features
41
    USE_COVARIANCE_FEATURES = False
42
43
    # Environment representation columns
44
45
    ENVIRONMENT_COLUMNS = [
46
        "open",
        "high",
47
        "low",
48
        "close"
49
50
        "volume",
51
    ]
52
    if USE_TECHNICAL_INDICATORS:
53
        ENVIRONMENT_COLUMNS += list(config_indicators.TECHNICAL_INDICATORS.keys())
54
55
    if USE_MACROECONOMIC_INDICATORS:
56
        MACROECONOMIC_INDICATORS = (
57
            \verb|config_indicators.MACROECONOMIC_INDICATORS_DEFAULT| \\
58
59
60
        # Remove non-letter characters from string
61
        ENVIRONMENT_COLUMNS += list(
62
63
            map(
                lambda x: "".join(
64
65
                     for ch in x.split(".", 1)[0].lower()
66
```

```
if ch.isalnum() or ch == "_"
67
                 ),
                 list(MACROECONOMIC_INDICATORS.keys()),
69
             )
70
71
72
     if USE_COVARIANCE_FEATURES:
73
         ENVIRONMENT_COLUMNS += ["covariance"]
74
75
     # Tickers configurations
76
    TICKERS = config_tickers.TEST_TICKERS
77
    INDEX = None
78
    TICKERS_NAME = TEST_NAME
    EXCHANGE = EXCHANGE_NYSE
80
81
     # Set dataset name based on the configuration
82
83
         USE_TECHNICAL_INDICATORS
84
         and USE_MACROECONOMIC_INDICATORS
85
         and USE_COVARIANCE_FEATURES
86
    ):
87
         DATASET_NAME = "dataset-indicators-covariance"
88
     elif USE_TECHNICAL_INDICATORS and USE_MACROECONOMIC_INDICATORS:
89
         DATASET_NAME = "dataset-indicators"
90
     elif USE_COVARIANCE_FEATURES:
91
         DATASET_NAME = "dataset-covariance"
92
     else:
93
         DATASET_NAME = "simple-dataset"
94
95
     WANDB_ENTITY = "xdl-team"
96
     WANDB_PROJECT = "xdl-portfolio"
97
98
     SWEEP_CONFIG = {
99
100
         "method": "bayes",
         "metric": {"name": "sharpe_ratio", "goal": "maximize"},
101
         "early_terminate": {
102
             "type": "hyperband",
103
             "s": 2,
104
             "eta": 2,
105
             "max_iter": 10,
         },
107
    }
108
```

Listing 2: config_tickers.py

```
TEST_TICKERS = [

"AAPL",

"CSCO",

"MSFT",

"HON",

"V",

"J
```

```
8
    DOW_30_TICKERS = [
         "AXP",
10
         "AMGN",
11
         "AAPL",
12
         "AMZN",
13
         "BA",
14
         "CAT",
15
         "CRM",
16
         "CSCO",
17
         "CVX",
18
         "DIS",
19
         "GS",
"HD",
20
21
         "HON",
22
23
         "IBM",
24
         "JNJ",
         "JPM",
25
         "KO",
26
         "MCD",
27
         "MMM",
28
         "MRK",
29
30
         "MSFT",
         "NKE",
31
         "NVDA",
32
         "PG",
33
         "SHW",
34
         "TRV",
35
         "UNH",
36
         "V",
37
         "VZ",
38
         "WMT",
39
40
    ]
41
    EURO_STOXX_50_TICKERS = [
42
         "ADS.DE",
43
         "ADYEN.AS",
44
         "AD.AS",
45
         "AI.PA",
46
         "AIR.PA",
47
         "ALV.DE",
48
         "ABI.BR",
49
         "ASML.AS",
50
         "CS.PA",
51
52
         "BAS.DE",
         "BAYN.DE",
53
         "BBVA.MC",
54
         "SAN.MC",
55
         "BMW.DE",
56
57
         "BNP.PA",
         "BN.PA",
58
         "DB1.DE",
59
         "DHL.DE",
60
         "DTE.DE",
61
         "ENEL.MI",
62
```

```
"ENI.MI",
 63
          "EL.PA",
 64
          "RACE.MI",
 65
          "FLTR.L",
 66
          "RMS.PA",
 67
          "IBE.MC",
 68
          "ITX.MC",
 69
          "IFX.DE",
 70
          "INGA.AS",
 71
          "ISP.MI",
 72
          "KER.PA",
 73
          "OR.PA",
 74
          "MC.PA",
 75
          "MBG.DE",
 76
          "MUV2.DE",
 77
 78
          "NOKIA.HE",
 79
          "NDA-FI.HE",
          "RI.PA",
 80
          "PRX.AS",
 81
          "SAF.PA",
 82
          "SGO.PA",
 83
          "SAN.PA",
 84
          "SAP.DE",
 85
          "SU.PA",
 86
          "SIE.DE",
 87
          "STLAM.MI",
 88
          "TTE.PA",
 89
 90
          "DG.PA",
          "UCG.MI",
 91
          "VOW.DE",
 92
     ]
 93
 94
 95
     FTSE_100_TICKERS = [
 96
          "III.L",
          "ADM.L",
 97
          "AAF.L",
 98
          "ALW.L",
 99
          "AAL.L",
100
          "ANTO.L",
101
          "AHT.L",
102
          "ABF.L",
103
          "AZN.L",
104
          "AUTO.L",
105
          "AV.L",
106
          "BAB.L",
107
          "BA.L",
108
          "BARC.L",
109
          "BTRW.L",
110
          "BEZ.L",
111
          "BKG.L",
112
          "BP.L",
113
          "BATS.L",
114
          "BT-A.L",
115
          "BNZL.L",
116
          "CNA.L",
117
```

```
"CCEP.L",
118
          "CCH.L",
119
          "CPG.L",
120
          "CTEC.L",
121
          "CRDA.L",
122
          "DCC.L",
123
          "DGE.L",
124
          "DPLM.L",
125
          "EDV.L",
126
          "ENT.L",
127
          "EZJ.L",
128
          "EXPN.L",
129
          "FCIT.L",
130
          "FRES.L",
131
          "GAW.L",
132
          "GLEN.L",
133
134
          "GSK.L",
          "HLN.L",
135
          "HLMA.L",
136
          "HIK.L",
137
          "HSX.L",
138
          "HWDN.L",
139
          "HSBA.L",
140
          "IHG.L",
141
          "IMI.L",
142
          "IMB.L",
143
          "INF.L",
144
145
          "ICG.L",
          "IAG.L",
146
          "ITRK.L",
147
          "JD.L",
148
          "KGF.L",
149
          "LAND.L",
150
          "LGEN.L",
151
          "LLOY.L",
152
          "LMP.L",
153
          "LSEG.L",
154
          "MNG.L",
155
156
          "MKS.L",
          "MRO.L",
157
          "MNDI.L",
158
          "NG.L",
159
          "NWG.L",
160
          "NXT.L",
161
          "PSON.L",
162
          "PSH.L",
163
          "PSN.L",
164
          "PHNX.L",
165
          "PCT.L",
166
          "PRU.L",
167
          "RKT.L",
168
          "REL.L",
169
          "RTO.L",
170
          "RMV.L",
171
          "RIO.L",
172
```

```
173
          "RR.L",
          "SGE.L",
174
          "SBRY.L",
175
          "SDR.L",
176
          "SMT.L",
177
          "SGRO.L",
178
          "SVT.L",
179
          "SHEL.L",
180
          "SMIN.L",
181
          "SN.L",
182
          "SPX.L",
183
          "SSE.L",
184
          "STAN.L",
185
          "STJ.L",
186
          "TW.L",
187
          "TSCO.L",
188
189
          "ULVR.L",
          "UU.L",
190
          "UTG.L",
191
          "VOD.L",
192
          "WEIR.L",
193
          "WTB.L",
194
195
          "WPP.L",
196
     ]
197
     FX_TICKERS = [
198
          "EURUSD=X",
199
          "GBPUSD=X",
200
201
          "JPYUSD=X",
          "AUDUSD=X",
202
          "CADUSD=X",
203
          "CNYUSD=X",
204
205
          "CHFUSD=X",
206
          "HKDUSD=X",
          "KRWUSD=X",
207
          "INRUSD=X",
208
     ]
209
210
     COMMODITY_TICKERS = [
211
          "CL=F", # Crude oil
212
          "NG=F", # Natural gas
213
          "GC=F", # Gold
214
          "SI=F", # Silver
215
          "ALI=F", # Aluminum
216
217
          "HG=F", # Copper
218
     ]
```

Listing 3: config_indicators.py

```
# List of technical indicators

TECHNICAL_INDICATORS = {

"close_5_sma": "Simple Moving Average over 5 days (1 week)",
```

```
"close_10_sma": "Simple Moving Average over 10 days (2 weeks)",
4
        "close_20_sma": "Simple Moving Average over 20 days (1 month)",
        "close_5_ema": "Exponential Moving Average over 5 days (1 week)",
6
        "close_10_ema": "Exponential Moving Average over 10 days (2 weeks)",
7
        "macd": "Moving Average Convergence Divergence",
8
        "rsi": "Relative Strength Index over 14 days",
9
        "cci": "Commodity Channel Index",
10
        "boll_ub": "Bollinger Bands Upper Band",
11
        "boll_lb": "Bollinger Bands Lower Band",
12
        "atr": "Average True Range",
13
        "adx": "Average Directional Index",
14
        "close_10_roc": "Rate of Change over 10 days (2 weeks)",
15
   }
16
17
    # List of macroeconomic indicators
18
    MACROECONOMIC_INDICATORS_DEFAULT = {
19
20
        "^VIX": "Volatility Index (VIX)".
        "DX-Y.NYB": "US Dollar Index (DXY)",
21
        "^IRX": "3-Month Treasury Yield (IRX)",
22
        "^FVX": "5-Year Treasury Yield (FVX)",
23
        "^TNX": "10-Year Treasury Yield (TNX)",
24
   }
25
26
27
    MACROECONOMIC_INDICATORS_DW30 = {
        "^VXD": "Volatility Index (VXD)",
28
        "DX-Y.NYB": "US Dollar Index (DXY)",
29
        "^IRX": "3-Month Treasury Yield (IRX)",
30
        "^FVX": "5-Year Treasury Yield (FVX)"
31
        "^TNX": "10-Year Treasury Yield (TNX)",
32
33
34
    MACROECONOMIC_INDICATORS_EUROSTOXX50 = {
35
        "^XDE": "Euro Currency Index (EXY)",
36
37
38
   MACROECONOMIC_INDICATORS_FTSE100 = {
39
        "^XDB": "British Pound Currency Index (BXY)",
40
41
```

Listing 4: config_models.py

```
# Stable Baselines DRL Models
    from stable_baselines3 import A2C, DDPG, PPO, SAC, TD3
2
3
    MODELS = {
4
        "a2c": A2C,
5
        "ppo": PPO,
6
        "ddpg": DDPG
7
        "td3": TD3,
        "sac": SAC,
9
    }
10
```

```
# Training parameters for stock trading task
12
    MODEL_KWARGS_STOCK = {
        "a2c": {
14
             "n_steps": 40,
15
             "ent_coef": 0.0003,
16
             "learning_rate": 0.003,
17
18
         "ppo": {
19
             "n_steps": 512,
20
             "ent_coef": 0.0005,
21
             "learning_rate": 0.0015,
22
             "batch_size": 64,
23
24
        "ddpg": {
25
             "batch_size": 256,
26
             "buffer_size": 200000,
27
28
             "learning_rate": 0.005,
29
        "td3": {
30
             "batch_size": 128,
31
             "buffer_size": 500000,
32
             "learning_rate": 0.001,
33
        },
34
        "sac": {
35
             "batch_size": 64,
36
             "buffer_size": 500000,
37
             "learning_rate": 0.001,
38
             "learning_starts": 2000,
39
             "ent_coef": "auto_0.1",
40
        },
41
    }
42
43
    # Training parameters for portfolio optimisation task
44
45
    MODEL_KWARGS_PORTFOLIO = {
        "a2c": {
46
             "n_steps": 10,
47
             "ent_coef": 0.005,
48
             "learning_rate": 0.0004,
49
50
        },
         "ppo": {
51
             "n_steps": 2048,
52
             "ent_coef": 0.005,
53
             "learning_rate": 0.001,
54
             "batch_size": 128,
55
56
         "ddpg": {
57
             "batch_size": 128,
58
             "buffer_size": 50000,
59
             "learning_rate": 0.001,
60
        },
61
         "td3": {
62
             "batch_size": 100,
63
             "buffer_size": 1000000,
64
             "learning_rate": 0.001,
65
        },
66
```

```
"sac": {
67
              "batch_size": 128,
              "buffer_size": 1000000,
69
              "learning_rate": 0.0003,
70
              "learning_starts": 100,
71
              "ent_coef": "auto_0.1",
72
73
     }
74
75
     # Training visualisation config
76
     train_visualisation_config = {
77
         "a2c": {
78
              "x": "time/iterations",
79
              "y": [
80
                  "train/reward",
81
                  "train/policy_loss",
82
                  "train/entropy_loss",
83
                  "train/value_loss",
84
             ],
85
              "title": [
86
                  "Iterations vs Reward",
87
                  "Iterations vs Policy Loss",
88
                  "Iterations vs Entropy loss",
89
90
                  "Iterations vs Value loss",
             ],
91
         },
92
          "ppo": {
93
              "x": "time/iterations",
94
              "y": [
95
                  "train/reward",
96
                  "train/policy_gradient_loss",
97
                  "train/entropy_loss",
98
                  "train/value_loss",
99
100
              "title": [
101
                  "Iterations vs Reward",
102
                  "Iterations vs Policy Gradient Loss",
103
                  "Iterations vs Entropy loss",
104
105
                  "Iterations vs Value loss",
             ],
106
107
          "ddpg": {
108
              "x": "time/episodes",
109
              "y": [
110
                  "train/reward",
111
                  "train/actor_loss",
112
                  "train/critic_loss",
113
             ],
114
              "title": [
115
                  "Episodes vs Reward",
116
                  "Episodes vs Actor Loss",
117
                  "Episodes vs Critic Loss",
118
             ],
119
         },
120
         "td3": {
121
```

```
"x": "time/episodes",
122
              "y": [
123
                  "train/reward",
124
                  "train/actor_loss",
125
                  "train/critic_loss",
126
127
              ],
              "title": [
128
                  "Episodes vs Reward",
129
                  "Episodes vs Actor Loss",
130
                  "Episodes vs Critic Loss",
131
              ],
132
         },
133
         "sac": {
134
              "x": "time/episodes",
135
              "y": [
136
                  "train/reward",
137
138
                  "train/actor_loss",
                  "train/critic_loss",
139
                  "train/ent_coef_loss",
140
              ],
141
              "title": [
142
                  "Episodes vs Reward",
143
                  "Episodes vs Actor Loss",
144
                  "Episodes vs Critic Loss",
145
                  "Episodes vs Entropy Coefficient Loss",
146
              ],
147
         },
148
     }
149
150
     \# Model hyperparameter sweep configuration
151
     MODEL_SWEEP_CONFIG = {
152
         "a2c": {
153
              "n_steps": {"values": [5, 10, 20, 30, 40]},
154
155
              "ent_coef": {
                  "distribution": "uniform",
156
                  "min": 1e-8,
157
                  "max": 1e-3,
158
              },
159
160
              "learning_rate": {
                  "distribution": "uniform",
161
                  "min": 1e-5,
162
                  "max": 1e-2,
163
              },
164
         },
165
         "ppo": {
166
              "n_steps": {"values": [128, 256, 512, 1024, 2048]},
167
              "ent_coef": {
168
                  "distribution": "uniform",
169
                  "min": 1e-8,
170
                  "max": 1e-3,
171
172
              "learning_rate": {
173
                  "distribution": "uniform",
174
                  "min": 1e-5,
175
                  "max": 1e-2,
176
```

```
177
              "batch_size": {"values": [32, 64, 128, 256, 512]},
178
179
         "ddpg": {
180
              "batch_size": {"values": [64, 128, 256]},
181
              "buffer_size": {"values": [50000, 100000, 200000, 500000]},
182
              "learning_rate": {
183
                  "distribution": "uniform",
                  "min": 1e-5,
185
                  "max": 1e-2,
186
             },
187
         },
188
         "td3": {
              "batch_size": {"values": [64, 100, 128, 256]},
190
              "buffer_size": {"values": [500000, 1000000, 2000000]},
191
              "learning_rate": {
192
                  "distribution": "uniform",
193
                  "min": 1e-5,
                  "max": 1e-2,
195
             },
196
         },
197
         "sac": {
198
              "batch_size": {"values": [32, 64, 128]},
199
              "buffer_size": {"values": [100000, 500000, 1000000, 2000000]},
200
              "learning_rate": {
201
                  "distribution": "uniform",
202
                  "min": 1e-5,
203
                  "max": 1e-2,
204
205
              "learning_starts": {"values": [500, 1000, 2000, 5000]},
206
              "ent_coef": {"values": ["auto", "auto_0.1", "auto_0.01"]},
207
208
         },
     }
209
```

I.2 Data Download and Pre-processing Module

Listing 5: findata_downloader.py

```
from typing import List
1
    import pandas as pd
3
    import yfinance as yf
4
6
    class FinancialDataDownloader:
7
8
        def __init__(self, start_date: str, end_date: str) -> None:
9
10
            Initialise the FinancialDataDownloader with a date range.
11
            :param start_date: Start date for data download in 'YYYY-MM-DD' format.
12
            :param end_date: End date for data download in 'YYYY-MM-DD' format.
13
```

```
14
            self.start_date = start_date
            self.end_date = end_date
16
            self.data = None
17
18
        def download_data(self, tickers: List[str]) -> pd.DataFrame:
19
20
21
             Download financial data for the specified tickers within the date range.
             :param tickers: List of stock tickers to download data for.
22
             :return: DataFrame containing the downloaded financial data.
23
             :raises Exception: If an error occurs during data download.
24
             :raises ValueError: If no data is returned from the download.
25
            if self.data is not None:
27
                print("Data already downloaded. Returning existing data.")
28
                 return self.data
29
30
31
            try:
                 data = yf.download(
32
                     tickers,
33
                     start=self.start_date,
34
                     end=self.end_date,
35
                     group_by="Ticker",
36
37
                     auto_adjust=True,
38
                     progress=False,
                )
39
             except Exception as e:
40
                raise Exception(f"An error occurred while downloading data: {e}")
41
42
43
             if data is None:
                raise ValueError(
44
                     "No data returned from the download. Please check the tickers and date
45
                     \hookrightarrow range."
                 )
46
47
             \# Flatten the MultiIndex columns
48
49
            data = (
                data.stack(level=0, future_stack=True)
50
                 .rename_axis(["Date", "Ticker"])
51
52
                 .reset_index(level=1)
            )
53
54
             # Reset index to have a clean DataFrame
55
            data.reset_index(inplace=True)
56
57
             # Rename index columns
            data.columns.rename("", inplace=True)
59
60
             # Convert column names to lowercase
61
             data.columns = [col.lower() for col in data.columns]
62
63
             # Rename ticker column to 'tic'
            data.rename(columns={"ticker": "tic"}, inplace=True)
65
66
```

```
self.data = data
67
              print(
                  f"Data downloaded for {len(tickers)} tickers from {self.start_date} to
69
                     {self.end_date}."
              )
70
              return data
71
72
         def save_data(self, directory: str, filename: str) -> None:
73
74
              Save the downloaded data to a CSV file.
75
              :param directory: Directory where the CSV file will be saved.
76
              :param filename: Name of the CSV file (without extension).
77
              :raises ValueError: If there is no data to save.
78
79
              if self.data is None or self.data.empty:
80
                  raise ValueError("No data to save. Please download data first.")
81
82
83
              file_path = f"{directory}/{filename}.csv"
              self.data.to_csv(file_path, index=False)
             print(f"Data saved to {file_path}")
85
86
         def load_data(self, directory: str, filename: str) -> pd.DataFrame:
87
              11 11 11
88
              Load financial data from a CSV file.
89
              : param\ directory:\ Directory\ where\ the\ \textit{CSV}\ file\ is\ located.
90
91
              :param filename: Name of the CSV file (without extension).
              : return \colon \textit{DataFrame containing the loaded financial data}.
92
              : raises \ \textit{FileNotFoundError}: \ \textit{If the specified file does not exist}.
93
              :raises Exception: If an error occurs while loading the data.
94
95
              file_path = f"{directory}/{filename}.csv"
96
97
             try:
98
                  data = pd.read_csv(file_path)
99
100
101
                  # Convert date columns to datetime format if they exist
                  data["date"] = pd.to_datetime(data["date"])
102
103
                  # Sort the data by date, tic
104
                  data.sort_values(by=["date", "tic"], inplace=True)
105
106
                  # Reset index after sorting
                  data.reset_index(drop=True, inplace=True)
107
108
                  print(f"Data loaded from {file_path}")
109
                  self.data = data
110
111
112
                  return data
113
              except FileNotFoundError:
114
                  raise FileNotFoundError(f"No data file found at {file_path}")
115
116
              except Exception as e:
117
                  raise Exception(f"An error occurred while loading data: {e}")
118
```

Listing 6: findata_preprocessor.py

```
import itertools
1
    from datetime import datetime
2
    from typing import List, Optional
3
    import exchange_calendars as ecals
5
6
    import pandas as pd
    from stockstats import StockDataFrame
    from preprocessor.findata_downloader import FinancialDataDownloader
9
10
11
    class FinancialDataPreprocessor:
12
13
        def __init__(self, start_date: str, end_date: str) -> None:
14
             Initialses the FinancialDataPreprocessor with a date range.
15
             :param start_date: Start date for the data processing in 'YYYY-MM-DD' format.
16
             :param end_date: End date for the data processing in 'YYYY-MM-DD' format.
17
             HHHH
18
             self.start_date = start_date
19
             self.end_date = end_date
20
21
        def preprocess(
22
23
             self,
24
             data: pd.DataFrame,
25
             exchange: str,
             use_tech_indicators: bool = False,
26
27
             tech_indicators: Optional[List[str]] = None,
28
             use_macro_indicators: bool = False,
             macro_indicators: Optional[List[str]] = None,
30
             use_covariance: bool = False,
            lookback_period: int = 252,
31
        ) -> pd.DataFrame:
32
33
34
             Preprocess financial data by cleaning it and adding additional features.
35
             :param data: DataFrame containing financial data with columns ['date', 'tic',
             → 'open', 'high', 'low', 'close', 'volume'].
             :param exchange: The stock exchange for which the data is being processed (e.g.,
36
             \hookrightarrow 'NYSE', 'LSE').
             : param\ use\_tech\_indicators:\ Whether\ to\ add\ technical\ indicators\ (Default\ is
37
             \hookrightarrow False).
             :param tech_indicators: List of technical indicators to add.
38
             :param use_macro_indicators: Whether to add macroeconomic indicators (Default is
             \hookrightarrow False).
             : param\ macro\_indicators:\ List\ of\ macroeconomic\ indicators\ to\ add.
40
             :param use_covariance: Whether to add covariance features (Default is False).
41
             :param lookback_period: The lookback period for calculating covariance features
42
             \hookrightarrow (Default is 252).
             :return: Processed DataFrame with additional features.
43
44
             df = data.copy()
45
46
            df = self.__clean_data(df, exchange)
47
```

```
48
            # Add day of the week column
49
            df["day"] = df["date"].dt.dayofweek
50
51
            if use_tech_indicators and tech_indicators:
52
                 df = self.__add_technical_indicators(df, tech_indicators)
53
            if use_macro_indicators and macro_indicators:
55
                 df = self.__add_macroeconomic_indicators(df, macro_indicators)
56
57
            if use_covariance:
58
                 df = self.__add_covariance_features(df, lookback_period)
59
            df = self.__rename_columns(df)
61
62
            return df
63
64
65
        def __clean_data(self, data: pd.DataFrame, exchange: str) -> pd.DataFrame:
66
            Clean the financial data by ensuring all trading days are represented
67
            and filling missing values appropriately.
68
            :param data: DataFrame containing financial data with columns ['date', 'tic',
69
             → 'open', 'high', 'low', 'close', 'volume'].
            :param exchange: The stock exchange for which the data is being processed (e.g.,
70
            \hookrightarrow 'NYSE', 'LSE').
71
            :return: Cleaned DataFrame with all trading days represented and missing values
            \hookrightarrow filled.
72
            trading_days = self.__get_trading_dates(exchange)
73
            tickers = data["tic"].unique()
74
75
            # Create a DataFrame with all combinations of trading dates and tickers
76
            index = list(itertools.product(trading_days, tickers))
77
            df = pd.DataFrame(index, columns=["date", "tic"]).merge(
78
                 data, on=["date", "tic"], how="left"
79
80
81
            df = df.sort_values(by=["tic", "date"])
82
83
            # Fill missing values with forward fill method and then backward fill
84
85
            df["open"] = df.groupby("tic")["open"].ffill().bfill()
            df["close"] = df.groupby("tic")["close"].ffill().bfill()
86
            df["high"] = df.groupby("tic")["high"].ffill().bfill()
87
            df["low"] = df.groupby("tic")["low"].ffill().bfill()
88
89
            # Fill missing volumes with 0 to indicate no trading activity
90
            df["volume"] = df["volume"].fillna(0)
92
            return df
93
94
        def __get_trading_dates(self, exchange: str) -> List[datetime]:
95
96
97
            Get trading dates for a given exchange within a specified date range.
            :param exchange: The stock exchange for which the trading dates are needed
98
             \hookrightarrow (e.g., 'NYSE', 'LSE').
```

```
:return: List of trading dates as datetime objects.
99
100
101
             dates = (
                  ecals.get_calendar(exchange)
102
                  .sessions_in_range(start=self.start_date, end=self.end_date)
103
                  .to_list()
104
105
106
             # Convert to datetime objects
107
             return [d.to_pydatetime() for d in dates]
108
109
         def __add_technical_indicators(
110
             self, data: pd.DataFrame, indicators: List[str]
111
         ) -> pd.DataFrame:
112
113
             Add technical indicators to the DataFrame based on the specified indicators.
114
             :param data: DataFrame containing financial data with columns ['date', 'tic',
115
              → 'open', 'high', 'low', 'close', 'volume'].
             :param indicators: List of technical indicators to add (e.g., ['macd', 'rsi',
              \hookrightarrow 'cci']).
             :return: DataFrame with additional technical indicators.
117
             :raises Exception: If there is an error processing a specific indicator for a
118
              \hookrightarrow ticker.
119
             # Convert the dataframe to StockDataFrame
120
121
             stock_df = StockDataFrame.retype(data.copy())
             tickers = data["tic"].unique()
122
123
             # Iterate over the indicators
124
             for indicator in indicators:
125
                  indicator_df = pd.DataFrame()
126
127
                  # Iterate over each ticker
128
                  for ticker in tickers:
129
130
                      # Extract the indicator data for the ticker
131
132
                      try:
                          ind_df = stock_df[stock_df["tic"] == ticker][indicator]
133
                          ind_df = pd.DataFrame(ind_df)
134
                          ind_df["tic"] = ticker
135
136
                          ind_df["date"] = data[data["tic"] == ticker]["date"].values
137
                          indicator_df = pd.concat(
138
                               [indicator_df, ind_df], ignore_index=True
139
140
                      except Exception as e:
141
142
                              f"Error processing indicator '{indicator}' for ticker
143
                               → '{ticker}': {e}"
144
145
                  data = data.merge(indicator_df, on=["tic", "date"], how="left")
146
147
             data.fillna(0, inplace=True) # Fill NaN values with 0
148
```

```
149
             return data
150
151
         def __add_macroeconomic_indicators(
152
             self, data: pd.DataFrame, indicators: List[str]
153
         ) -> pd.DataFrame:
154
155
              Add macroeconomic indicators to the DataFrame based on the specified indicators.
156
              : param\ data:\ Data Frame\ containing\ financial\ data\ with\ columns\ ['date',\ 'tic',
157
              → 'open', 'high', 'low', 'close', 'volume'].
              :param indicators: List of macroeconomic indicators to add (e.q., ['^VIX']).
158
              :return: DataFrame with additional macroeconomic indicators.
159
160
161
             for indicator in indicators:
162
                  findownloader = FinancialDataDownloader(
163
                      self.start_date, self.end_date
164
165
166
                  ind_df = findownloader.download_data([indicator])
                  indicator_df = ind_df[["date", "close"]].rename(
167
                      columns={"close": indicator}
168
169
170
                  data = data.merge(indicator_df, on=["date"])
171
172
173
             return data
174
         def __add_covariance_features(
175
              self, data: pd.DataFrame, lookback_period: int = 252
176
177
         ) -> pd.DataFrame:
178
              Add covariance features to the DataFrame.
179
              :param data: DataFrame containing financial data.
180
              :param lookback_period: The lookback period for calculating covariance features.
181
182
              :return: DataFrame with additional covariance features.
183
              covariance_df = pd.DataFrame()
184
185
             dates = data.date.unique()
186
187
              tics = data.tic.unique()
188
              for i in range(len(dates)):
189
                  # If the date is smaller than the lookback period,
190
                  # do not calculate the covariance and set it to O
191
                  if i < lookback_period:</pre>
192
                      cov_df = pd.DataFrame(
193
194
                          {
                               "date": dates[i],
195
                               "tic": tics,
196
                               "covariance": [
197
                                   [0] * len(tics) for _ in range(len(tics))
198
                               ],
                          }
200
                      )
201
```

```
# Calculate the covariance features for the current lookback period
202
203
                  else:
                      # Get the start and end dates for the lookback period
204
                      start_date = dates[i - lookback_period]
205
                      end_date = dates[i]
206
207
                      # Retrieve the relevant data for the lookback period
208
                      window = data[
209
                          (data.date >= start_date) & (data.date < end_date)</pre>
210
211
                      # Pivot the table to get the price data for the lookback period
212
                      price_lookback = window.pivot_table(
213
                          index="date", columns="tic", values="close"
214
                      )
215
216
                      # Compute the covariance matrix
217
218
                      cov_matrix = price_lookback.cov()
219
                      cov_df = pd.DataFrame(
220
                          {
                              "date": dates[i],
221
                              "tic": tics,
222
                              "covariance": cov_matrix.values.tolist(),
223
                          }
224
                      )
225
226
                  # Append to the covariance dataframe
227
                 covariance_df = pd.concat(
228
                      [covariance_df, cov_df], ignore_index=True
229
                 )
230
231
             # Merge the data on date and tic
232
             data = data.merge(covariance_df, on=["date", "tic"])
233
234
235
             return data
236
         def __rename_columns(self, data: pd.DataFrame) -> pd.DataFrame:
237
238
             Rename columns to a consistent format to work with FinRL library.
239
240
             :param data: DataFrame containing financial data with columns ['date', 'tic',
              → 'open', 'high', 'low', 'close', 'volume'].
^{241}
             :return: DataFrame with renamed columns.
242
243
             # Convert column names
244
             # 1. Split by dot and take the first part
245
             # 2. Convert to lowercase
247
             # 3. Remove non-alphanumeric characters
             data.columns = (
248
                 data.columns.str.split(".")
249
                  .str[0]
250
                  .str.lower()
                  .str.replace(r"[^a-z0-9_]", "", regex=True)
252
             )
253
254
```

```
255
              return data
256
         def __set_index(self, data: pd.DataFrame) -> pd.DataFrame:
257
258
              Set the index of the DataFrame to a number from 0 to the number of distinct
259
              → dates in the dataset.
              This is useful for ensuring that the index is consistent with the FinRL
260
              → library's expectations.
              :param data: DataFrame containing financial data.
261
              : return: \ \textit{DataFrame with the index set to a number from 0 to the number of} \\
262
              \,\hookrightarrow\,\, \textit{distinct dates}.
              11 11 11
263
264
              data.sort_values(by=["date", "tic"], inplace=True)
265
266
              # Set the index to a number from 0 to number of distinct dates in the dataset
267
              data.set_index(data["date"].astype("category").cat.codes, inplace=True)
268
269
270
              return data
271
         def split_train_test(
272
              self, data: pd.DataFrame, test_start_date: pd.Timestamp | str
273
         ) -> tuple[pd.DataFrame, pd.DataFrame]:
274
275
              Split the data into training and testing sets based on the given test start
276
              \hookrightarrow date.
277
              : param\ data \colon \textit{DataFrame}\ containing\ financial\ data.
              :param\ test\_start\_date\colon \textit{The start date for the testing set. Data\ after\ this\ date}
278
              → will be used for testing.
              :return: A tuple containing the training DataFrame and the testing DataFrame.
279
280
281
              # Ensure test start date is part of the DataFrame
282
              test_start_date = pd.to_datetime(test_start_date)
283
              if "date" not in data.columns:
284
                  raise ValueError("Data must contain a 'date' column for splitting.")
285
              if (
286
                  test_start_date < data["date"].min()</pre>
287
                  or test_start_date > data["date"].max()
288
              ):
289
290
                  raise ValueError(
291
                      f"The test start date is outside of the 'date' column values."
292
                  )
293
              # Split the data into training and testing sets
294
              train_data = data[data["date"] < test_start_date].copy()</pre>
295
              test_data = data[data["date"] >= test_start_date].copy()
296
297
298
              train_data = self.__set_index(train_data)
              test_data = self.__set_index(test_data)
299
300
              return train_data, test_data
301
303
         def save_train_test_data(
```

```
304
              self,
              train_data: pd.DataFrame,
305
306
              test_data: pd.DataFrame,
              directory: str,
307
              filename: str.
308
         ) -> None:
309
              11 11 11
310
              Save the training and testing data to CSV files.
311
              :param train_data: DataFrame containing training data.
312
              :param test_data: DataFrame containing testing data.
313
              :param directory: Directory where the CSV files will be saved.
314
              :param filename: Base filename for the CSV files (without extension).
315
316
              train_file_path = f"{directory}/{filename}_train.csv"
317
              test_file_path = f"{directory}/{filename}_trade.csv"
318
319
320
              train_data.to_csv(train_file_path, index=False)
321
              test_data.to_csv(test_file_path, index=False)
322
              print(f"Train data saved to {train_file_path}")
323
              print(f"Test data saved to {test_file_path}")
324
325
         def __load_file(self, filepath: str) -> pd.DataFrame:
326
327
              Load a CSV file into a DataFrame.
328
              :param filepath: Path to the CSV file.
329
              : return \colon \mathit{DataFrame} \ \mathit{containing} \ \mathit{the} \ \mathit{data} \ \mathit{from} \ \mathit{the} \ \mathit{CSV} \ \mathit{file}.
330
              :raises FileNotFoundError: If the file does not exist.
331
              :raises ValueError: If the 'tic' column is missing from the data.
332
333
334
              try:
335
                  data = pd.read_csv(filepath)
                  # Convert date columns to datetime format if they exist
336
337
                  if "date" in data.columns:
338
                       data["date"] = pd.to_datetime(data["date"])
339
                  # Ensure the 'tic' column exists
340
                  if "tic" not in data.columns:
341
342
                       raise ValueError("The 'tic' column is missing from the data.")
343
344
                  # Set the index
                  data = self.__set_index(data)
345
346
                  return data
347
348
349
              except FileNotFoundError:
                  raise FileNotFoundError(f"No file found at {filepath}")
350
351
         def load_train_test_data(
352
              self, directory: str, filename: str
353
         ) -> tuple[pd.DataFrame, pd.DataFrame]:
354
355
              Load the training and testing data from CSV files.
356
              :param directory: Directory where the CSV files are located.
357
              :param filename: Base filename for the CSV files (without extension).
358
```

I.3 Agents Module

Listing 7: drl_agent.py

```
from typing import Literal, Optional, Tuple
1
    import pandas as pd
4
   from stable_baselines3.common.base_class import BaseAlgorithm
   from stable_baselines3.common.logger import configure
5
    from stable_baselines3.common.vec_env import DummyVecEnv
6
    from wandb.integration.sb3 import WandbCallback
    from wandb.sdk.wandb_run import Run
10
    from agents.tb_callback import TensorboardCallback
    from config import config_models
11
12
13
    class DRLAgent:
14
        def __init__(self, run: Optional[Run] = None):
15
16
            Initialises the DRL agent.
17
18
19
            self.run = run
20
        def get_model(
21
            self.
22
            model_name: str,
23
            environment: DummyVecEnv,
            use_case: Literal["stock-trading", "portfolio-optimisation"],
25
26
            directory: Optional[str] = None,
            model_kwargs: Optional[dict] = None,
27
            policy: str = "MlpPolicy",
28
            policy_kwargs: Optional[dict] = None,
29
30
            seed: Optional[int] = None,
            verbose: int = 1,
31
        ) -> BaseAlgorithm:
32
            HHHH
33
            Returns a DRL model based on the specified model name and parameters.
34
            :param model_name: The name of the DRL model to create.
            :param environment: The environment in which the model will be trained.
36
            :param use_case: The use case for the model (e.g., stock trading, portfolio
37
            \hookrightarrow optimization).
            :param directory: The directory where the tensorboard logs will be saved.
38
```

```
:param model_kwarqs: Additional keyword arguments for the model.
39
            :param policy: The policy to use for the model.
40
            : param\ policy\_kwargs\colon \textit{Additional}\ keyword\ arguments\ for\ the\ policy.
41
            :param seed: Random seed for reproducibility.
42
            :param verbose: Verbosity level for the model.
43
            :return: An instance of the specified DRL model.
44
            :raises ValueError: If the model name is not supported.
45
46
47
            if model_name not in config_models.MODELS:
48
                raise ValueError(
49
                    f"Model {model_name} is not supported. Choose from
50
                     )
51
52
            if model_kwargs is None:
53
                if use_case == "stock-trading":
54
55
                    model_kwargs = config_models.MODEL_KWARGS_STOCK[model_name]
                elif use_case == "portfolio-optimisation":
                    model_kwargs = config_models.MODEL_KWARGS_PORTFOLIO[model_name]
57
58
            if verbose:
59
                print(f"Model arguments: {model_kwargs}")
60
61
62
            if not self.run:
63
                if not directory:
                    raise ValueError(
64
                         "Directory must be specified if run is not provided."
65
66
67
                tensorboard_log = f"{directory}/{model_name}"
68
69
                logger = configure(tensorboard_log, ["csv", "tensorboard"])
70
71
72
                model = config_models.MODELS[model_name](
73
                    policy=policy,
74
                    env=environment,
                    verbose=verbose,
75
                     tensorboard_log=tensorboard_log,
76
77
                     seed=seed,
78
                    policy_kwargs=policy_kwargs,
79
                     **model_kwargs,
                )
80
81
                model.set_logger(logger)
82
83
84
            else:
                model = config_models.MODELS[model_name](
85
                    policy=policy,
86
                    env=environment,
87
                    verbose=verbose,
88
                     seed=seed,
                    policy_kwargs=policy_kwargs,
90
                    **model_kwargs,
91
```

```
)
92
93
             return model
94
95
         def train(
96
             self,
97
             model: BaseAlgorithm,
98
             tb_log_name: str,
99
             log_interval: int = 20,
100
             total_timesteps: int = 100000,
101
             callback: TensorboardCallback | WandbCallback = TensorboardCallback(),
102
         ) -> BaseAlgorithm:
103
              Trains the DRL model with the specified parameters.
105
              :param model: The DRL model to train.
106
              :param tb_log_name: The name for the tensorboard log.
107
              :param log_interval: The interval for logging training progress.
108
              :param total_timesteps: The total number of timesteps for training.
109
              :param callback: Callback function for additional logging or actions during
110
              \hookrightarrow training.
              :return: The trained DRL model.
111
              11 11 11
112
113
             model = model.learn(
114
115
                 total_timesteps=total_timesteps,
116
                  log_interval=log_interval,
                  tb_log_name=tb_log_name,
117
                  callback=callback,
118
              )
119
120
             return model
121
122
         def predict(
123
124
             self,
125
             model: BaseAlgorithm,
126
              environment,
             deterministic: bool = True,
127
         ) -> Tuple[pd.DataFrame, pd.DataFrame]:
128
129
130
              Makes a prediction given the provided model and environment.
131
              :param model: The trained DRL model.
              :param environment: The environment in which to run the prediction.
132
              :param deterministic: Whether to use deterministic actions.
133
              :return: The account memory and actions memory after the prediction.
134
135
              test_env, test_obs = environment.get_sb_env()
136
137
              account_memory = []
              actions_memory = []
138
139
              test_env.reset()
140
             max_steps = environment.df.index.nunique()
141
142
              for i in range(max_steps):
143
                  action, _ = model.predict(test_obs, deterministic=deterministic)
144
```

```
145
                 # Last step: Save account and actions memory
146
                 if i == max\_steps - 1:
147
                      account_memory = test_env.env_method(
148
                          method_name="save_asset_memory"
149
150
                      actions_memory = test_env.env_method(
151
152
                          method_name="save_action_memory"
153
154
                 test_obs, _, dones, _ = test_env.step(action)
155
156
                  # If the environment is done, break the loop
157
                 if dones[0]:
158
                     break
159
160
161
             return account_memory[0], actions_memory[0]
162
         def save_model(
163
             self,
164
             model: BaseAlgorithm,
165
             model_name: str,
166
             directory: str,
167
168
             11 11 11
169
             Saves the trained model to a specified directory.
170
             :param model: The trained DRL model.
171
             :param model_name: The name of the model.
172
             :param directory: The directory where the model will be saved.
173
174
             model_path = f"{directory}/{model_name}"
175
176
             model.save(model_path)
             print(f"Model saved to {model_path}")
177
178
         def load_model(
179
180
             self,
             model_name: str,
181
             directory: str,
182
183
         ) -> BaseAlgorithm:
184
             Loads a trained model from a specified directory.
185
             : param\ model\_name :\ The\ name\ of\ the\ model\ to\ load.
186
             :param directory: The directory where the model is saved.
187
             :return: The loaded DRL model.
188
             :raises ValueError: If the model name is not supported.
189
190
191
             if model_name not in config_models.MODELS:
192
                 raise ValueError(
193
                      f"Model {model_name} is not supported. Choose from
194
                      195
196
             model_path = f"{directory}/{model_name}"
197
```

```
198          model = config_models.MODELS[model_name].load(model_path)
199
200          print(f"Model successfully loaded from {model_path}")
201
202          return model
```

Listing 8: tb_callback.py

```
from stable_baselines3.common.callbacks import BaseCallback
2
3
    class TensorboardCallback(BaseCallback):
4
5
        Custom callback for plotting additional values in tensorboard
6
7
        def __init__(self, verbose: int = 0):
9
            super().__init__(verbose)
10
11
        def _on_step(self) -> bool:
12
            try:
13
                self.logger.record(
14
                     key="train/reward", value=self.locals["rewards"][0]
15
16
            except KeyError:
17
18
                self.logger.record(
                     key="train/reward", value=self.locals["reward"][0]
19
                )
20
            except Exception as e:
21
                print(f"Error recording reward: {e}")
22
            return True
```

I.4 Environments Module

Listing 9: env_portfolio_optimisation.py

```
from datetime import datetime
1
   from typing import Dict, List, Literal, Optional, Tuple
3
4
    import gymnasium as gym
   import numpy as np
5
   import pandas as pd
6
   from gymnasium import spaces
   from gymnasium.utils import seeding
   from stable_baselines3.common.vec_env import DummyVecEnv
9
   from stable_baselines3.common.vec_env.base_vec_env import VecEnvObs
10
11
   from config import config
12
   from pbenchmark.portfolio_benchmark import PortfolioBenchmark
```

```
14
    class PortfolioOptimisationEnv(gym.Env):
16
        def __init__(
17
             self,
18
             data: pd.DataFrame,
19
             stock_dimension: int,
20
21
             initial_amount: float,
            reward_scaling: float,
22
            state_space: int,
23
24
            action_space: int,
             state_columns: List[str],
25
            normalisation_strategy: Literal["sum", "softmax"],
27
            verbose: int = 10,
             day: int = 0,
28
             seed: Optional[int] = None,
29
        ):
30
31
             Initialise the portfolio optimisation environment.
32
             :param data: DataFrame containing stock data.
33
             :param stock_dimension: Number of stocks in the environment.
34
             :param initial_amount: Initial cash available for portfolio allocation.
35
             :param reward_scaling: Scaling factor for the reward.
36
37
             : param\ state\_space:\ Dimension\ of\ the\ state\ space.
38
             :param action_space: Dimension of the action space.
             :param\ state\_columns:\ List\ of\ columns\ in\ the\ data frame\ to\ represent\ the\ state
39
             \hookrightarrow space.
             :param normalisation_strategy: Strategy (softmax, sum) to normalise the actions
40
             \hookrightarrow to sum to 1.
             :param verbose: Verbosity level for logging.
41
             :param day: Current day in the trading data.
42
             :param seed: Random seed for reproducibility.
43
44
             self.df = data
45
             self.day = day
46
47
             self.data = self.df.loc[self.day, :]
48
             self.stock_dimension = stock_dimension
             self.initial_amount = initial_amount
49
             self.reward_scaling = reward_scaling
50
51
             self.state_space = state_space
52
             self.action_space = spaces.Box(low=0, high=1, shape=(action_space,))
53
             self.observation_space = spaces.Box(
                 low=-np.inf,
54
                 high=np.inf,
55
                 shape=(
56
                     self.state_space
57
                     + (
58
59
                          self.stock_dimension - 1
                          if "covariance" in state_columns
60
                          else 0
61
62
                     self.stock_dimension,
63
                 ),
64
            )
65
```

```
self.state_columns = state_columns
66
             self.terminal = False
67
68
             self.verbose = verbose
             self.normalisation_strategy = normalisation_strategy
69
70
             # Initialise state
71
             self.state = self.__get_state()
72
73
             self.portfolio_value = self.initial_amount
             self.weights = [1 / self.stock_dimension] * self.stock_dimension
74
75
             # Initialise reward
76
             self.reward = 0.0
77
             # Initialise counter variables
79
             self.episode = 0
80
81
             # Initialise memory variables
82
             self.asset_memory = [self.initial_amount]
             self.rewards_memory = [self.reward]
84
             self.return_memory = [0]
85
             self.actions_memory = [self.weights]
86
             self.date_memory = [self.__get_date()]
87
88
             # Initialise the benchmark
             self.benchmark = PortfolioBenchmark()
90
91
             # Set the random seed for reproducibility
92
             self._seed(seed)
93
94
         def __get_state(self) -> List:
95
96
             Get the current state representation from the data.
97
             :return: Current state as a list of values for each column in state_columns.
98
99
             if "covariance" in self.state_columns:
100
101
                 covariance = np.array(
                     self.data["covariance"]
102
                      .apply(lambda x: np.array(eval(x))) # type: ignore
103
104
                      .values.tolist()
                 )
105
106
                 return np.append(
                      covariance,
107
                      Γ
108
                          self.data[col].values.tolist()
109
                          for col in self.state_columns
110
                          if col != "covariance"
111
112
                     ],
                      axis=0.
113
                 ).tolist()
114
             else:
115
                 return [
116
                      self.data[col].values.tolist() for col in self.state_columns
117
118
119
         def __get_date(self) -> datetime:
120
```

```
11 11 11
121
             Get the current date from the data.
122
123
             :return: Current date.
124
125
             return self.data.date.unique()[0]
126
127
         def step(self, action: np.ndarray) -> Tuple[List, float, bool, bool, Dict]:
128
129
             Execute one time step within the environment.
130
             :param action: List of actions to take for each stock.
131
             :return: Tuple containing the next state, reward, done flag, truncated flag, and
132
             \hookrightarrow additional info.
133
             self.terminal = self.day >= len(self.df.index.unique()) - 1
134
135
             if self.terminal:
136
137
                 df_return = self.save_asset_memory()
                 # Print information if verbose
139
                 if self.verbose and self.episode % self.verbose == 0:
140
                     print("======="")
141
                     print(f"day: {self.day}, episode: {self.episode}")
142
                     print(f"begin_total_asset:{self.asset_memory[0]:.2f}")
143
144
                     print(f"end_total_asset:{self.portfolio_value:.2f}")
145
                     sharpe = self.benchmark.compute_sharpe_ratio(df_return)
                     print(f"sharpe_ratio: {sharpe:.2f}")
146
                     print("======="")
147
148
             else:
149
                 # Normalise actions
150
                 weights = self.__normalise_actions(
151
                     action, self.normalisation_strategy # type: ignore
152
153
154
                 self.actions_memory.append(weights.tolist())
155
                 # Retrieve previous day's prices
156
                 prev_prices = np.array(self.data.close.values)
157
158
                 # Update the state with the new actions
159
160
                 self.day += 1
                 self.data = self.df.loc[self.day, :]
161
                 self.state = self.__get_state()
162
163
                 # Retrieve current day's prices
164
                 curr_prices = np.array(self.data.close.values)
165
166
                 # Compute the portfolio returns
167
                 portfolio_return = np.dot(
168
                     ((curr_prices / prev_prices) - 1), weights
169
170
171
                 # Update portfolio value
172
                 new_portfolio_value = self.portfolio_value * (1 + portfolio_return)
173
```

```
174
                  # Update the reward: Change in portfolio value
175
                  self.reward = new_portfolio_value - self.portfolio_value
176
                  self.portfolio_value = new_portfolio_value
177
                  self.rewards_memory.append(self.reward)
178
                  self.reward *= self.reward_scaling
179
180
                  # Update the memory
181
                  self.return_memory.append(portfolio_return)
182
                  self.date_memory.append(self.__get_date())
183
                  self.asset_memory.append(new_portfolio_value)
184
185
              # The fourth element in the tuple is always False for this environment
              # Corresponds to whether the environment is truncated or not
187
             return self.state, self.reward, self.terminal, False, {}
188
189
         def reset(
190
191
              self,
192
              seed=None,
193
              options=None,
194
         ) -> Tuple[List, Dict]:
195
              11 11 11
196
             Resets the environment and returns a new state representation.
197
198
              :param seed: Random seed for reproducibility.
              : param\ options:\ {\it Options}\ for\ resetting\ the\ environment.
199
              :return: Tuple containing the initial state and an empty dictionary for
200
              \hookrightarrow additional info.
              11 11 11
201
              self.day = 0
202
              self.data = self.df.loc[self.day, :]
203
              self.state = self.__get_state()
204
              self.portfolio_value = self.initial_amount
205
206
207
              self.terminal = False
208
              self.weights = [1 / self.stock_dimension] * self.stock_dimension
209
              self.asset_memory = [self.initial_amount]
210
              self.return_memory = [0]
211
212
              self.rewards_memory = [0.0]
              self.actions_memory = [self.weights]
213
              self.date_memory = [self.__get_date()]
214
215
              self.episode += 1
216
217
             return self.state, {}
218
219
         def render(self, mode: str = "human", close=False) -> List:
220
221
              Render the current state of the environment.
222
              :param mode: The rendering mode (default is "human").
              :param close: Whether to close the rendering window (not used in this
              \rightarrow environment).
              :return: Current state.
225
```

```
226
227
             return self.state
228
         def __normalise_actions(
229
             self,
230
231
             actions: np.ndarray,
             strategy: Literal["sum", "softmax"],
232
         ) -> np.ndarray:
233
234
             Apply normalisation to the actions.
235
             :param actions: Actions to be normalised.
236
             :param strategy: Normalisation strategy to use.
237
238
             :return: Normalised actions.
239
             if strategy == "sum":
240
                 total_sum = np.sum(actions)
241
242
                 if total_sum != 0:
243
                      return actions / total_sum
244
                 else:
                      # Explicitly handle zero-sum case by returning uniform distribution
245
                      return np.ones_like(actions) / len(actions)
246
             else:
247
                  exp_actions = np.exp(actions)
248
249
                 return exp_actions / np.sum(exp_actions)
250
         def save_asset_memory(self) -> pd.DataFrame:
251
252
             Returns a DataFrame containing the asset memory.
253
             :return: DataFrame with asset memory.
255
             df_asset = pd.DataFrame(
256
                 {"date": self.date_memory, "account_value": self.asset_memory}
257
258
259
             # Add daily return
260
             df_asset["daily_return"] = (
261
                 df_asset["account_value"].pct_change().fillna(0)
262
263
264
             # Add cumulative return
             df_asset["cumulative_return"] = (
266
                 1 + df_asset["daily_return"]
267
             ).cumprod() - 1
268
269
             return df_asset
270
271
         def save_action_memory(self) -> pd.DataFrame:
272
273
             Returns a DataFrame containing the action memory.
274
             :return: DataFrame with actions memory.
275
276
             df_actions = pd.DataFrame(
277
                 self.actions_memory,
278
                 columns=self.data.tic.values,
279
             )
280
```

```
df_actions["date"] = self.date_memory
281
282
             return df_actions
283
284
         def _seed(self, seed: Optional[int] = None) -> List[int]:
285
              H = H
286
             Set the random seed for the environment.
287
             :param seed: Random seed for reproducibility.
288
             :return: List containing the seed used.
289
290
             self.np_random, seed = seeding.np_random(seed)
291
             return [seed]
292
293
         def get_sb_env(self) -> Tuple[DummyVecEnv, VecEnvObs]:
294
295
             Get the stable-baselines environment.
296
297
             :return: Stable-baselines environment and observation space.
298
             e = DummyVecEnv([lambda: self])
299
             obs = e.reset()
300
             return e, obs
301
302
303
     class PortfolioOptimisationEnvWrapper:
304
         def __init__(
305
             self,
306
             train_data: pd.DataFrame,
307
             trade_data: pd.DataFrame,
308
             state_columns: List[str] = ["close"],
             initial_amount: float = config.INITIAL_AMOUNT,
310
             reward_scaling: float = 1e-1,
311
             normalisation_strategy: Literal["sum", "softmax"] = "softmax",
312
             verbose: int = 10,
313
314
         ):
315
316
             Initialises the trading environment.
             :param train_data: DataFrame containing training data.
317
              :param trade_data: DataFrame containing trading data.
318
319
              :param state_columns: List of columns to represent the state space.
              :param initial_amount: Initial cash available for trading.
321
              :param reward_scaling: Scaling factor for the reward.
             :param normalisation_strategy: Strategy (softmax, sum) to normalise the actions
322
             \rightarrow to sum to 1.
             :param verbose: Verbosity level for logging.
323
324
             self.stock_dim = train_data.tic.nunique()
325
326
             self.state_space = len(state_columns)
             self.train_data = train_data
327
             self.trade_data = trade_data
328
329
             self.env_args = {
                  "initial_amount": initial_amount,
331
                  "state_space": self.state_space,
332
                 "stock_dimension": self.stock_dim,
333
```

```
"action_space": self.stock_dim,
334
335
                 "reward_scaling": reward_scaling,
                 "state_columns": state_columns,
336
                 "normalisation_strategy": normalisation_strategy,
337
                 "verbose": verbose,
338
339
340
            if verbose:
341
                print(
342
                    f"Environment successfully created with \n\tStock dimension:
343
                     344
345
346
        def get_train_env(self) -> DummyVecEnv:
347
             Creates and returns the training environment.
348
             :return: Training environment instance.
349
350
             self.train_env = PortfolioOptimisationEnv(
                data=self.train_data, **self.env_args
352
353
            return self.train_env.get_sb_env()[0]
354
355
        def get_trade_env(
356
357
            self,
        ) -> Tuple[PortfolioOptimisationEnv, Tuple[DummyVecEnv, VecEnvObs]]:
358
359
             Creates and returns the trading environment.
360
             :return: Trading environment instance and its stable-baselines environment.
361
362
363
             self.trade_env = PortfolioOptimisationEnv(
                data=self.trade_data, **self.env_args
364
365
366
            return self.trade_env, self.trade_env.get_sb_env()
```

I.5 Benchmarking Module

Listing 10: portfolio_benchmark.py

```
from typing import Dict, Literal

import pandas as pd
from pyfolio import timeseries
from pypfopt import EfficientFrontier, expected_returns, risk_models

from config import config
from preprocessor.findata_downloader import FinancialDataDownloader

class PortfolioBenchmark:
def __init__(self) -> None:
```

```
11 11 11
13
            Initialise the PortfolioBenchmark class.
15
            pass
16
17
        def convert_daily_return(
18
            self,
19
20
            df_account: pd.DataFrame,
        ) -> pd.Series:
21
22
            df_returns = df_account.copy()
23
24
            df_returns["date"] = pd.to_datetime(df_returns["date"])
25
            df_returns.set_index("date", drop=True, inplace=True)
26
            df_returns.index = df_returns.index.tz_localize("UTC") # type: ignore
27
            return pd.Series(
28
                 df_returns["daily_return"].values, index=df_returns.index
29
30
31
        def set_data(
32
            self.
33
            train_data: pd.DataFrame,
34
            trade_data: pd.DataFrame,
35
            lookback: int = 252,
        ) -> None:
37
            11 11 11
38
            Combine the training and testing data into a single DataFrame and
39
            filter the data for the specified time period.
40
             :param train_data: DataFrame containing training data.
41
42
            :param trade_data: DataFrame containing trading data.
            :param lookback: Lookback period in days for the test start date.
43
44
            data = pd.concat([train_data, trade_data], ignore_index=True)
45
46
47
            # Find the test start date or the next available trading date
48
            test_start = pd.to_datetime(config.TEST_START_DATE)
            if test_start not in data["date"].values:
49
                print("Test start date is not a trading date in the dataset.")
50
                 next_date = test_start
51
52
                 for lookahead in range(1, 6):
53
                     next_date = test_start + pd.Timedelta(days=lookahead)
                     if next_date in data["date"].values:
54
                         print(
55
                             f"Using next available trading date: {next_date.date()}"
56
57
                         test_start = next_date
58
59
                         break
60
                 else:
                     raise ValueError(
61
                         "No available trading date found after the test start date."
62
63
64
            data.set_index(data["date"].astype("category").cat.codes, inplace=True)
65
66
            # Filter data for the test period plus lookback window
67
```

```
start_idx = (
68
                  data[data["date"] == test_start].index.unique().values[0] - lookback
70
             end_idx = data.index.max()
71
72
             self.data = data.loc[start_idx:end_idx, :]
73
             self.lookback = lookback
75
         def optimise_portfolio(
76
             self.
77
             strategy: Literal["mean", "min", "momentum", "equal"],
78
             initial_amount: int = config.INITIAL_AMOUNT,
79
         ) -> pd.DataFrame:
81
             Optimises the portfolio depending on the specified strategy:
82
               'mean': Mean-variance optimisation
83
             - 'min': Minimum variance optimisation
84
85
             - 'momentum': Momentum-based strategy
             - 'equal': Equal weight strategy
86
             :param strategy: Type of optimisation
87
             :param initial_amount: Initial capital for the portfolio, default is 100000.
88
             : return: \ \textit{DataFrame with date, account\_value, and daily\_return columns.}
89
             # Pivot data: date as index, tics as columns
92
             price_df = self.data.pivot(
                 index="date", columns="tic", values="close"
93
             ).sort_index()
94
95
             # Calculate daily returns
96
             returns_df = price_df.pct_change().dropna()
97
98
             # Initialise memory
99
             weights_record = {}
100
             portfolio_returns = [0.0]
101
102
             portfolio_values = [initial_amount]
103
             portfolio_value = initial_amount
104
             dates = returns_df.index
105
106
107
             for i in range(self.lookback + 1, len(returns_df)):
108
                 current_date = dates[i]
109
                 window_prices = price_df.iloc[i - self.lookback : i + 1]
110
111
                 if strategy == "momentum":
112
113
                      weights = self.__momentum_strategy(window_prices)
                 elif strategy == "equal":
114
                      weights = self.__equal_weight_strategy(
115
                          price_df.columns.tolist()
116
117
                 elif strategy == "mean":
118
                      weights = self.__mean_variance_strategy(window_prices)
119
                 elif strategy == "min":
120
                      weights = self.__min_variance_strategy(window_prices)
121
                 else:
122
```

```
raise ValueError(
123
                          "Invalid strategy. Choose from 'mean', 'min', 'momentum', or
124
                          → 'equal'."
                      )
125
126
                  weights_record[current_date] = weights
127
128
                  # Calculate daily return of the portfolio
129
                  daily_return = sum(
130
                      weights.get(tic, 0) * returns_df.iloc[i][tic]
131
                      for tic in price_df.columns
132
133
                  portfolio_returns.append(daily_return)
134
135
                  # Calculate daily portfolio value
136
                  portfolio_value *= 1 + daily_return
137
                  portfolio_values.append(portfolio_value)
138
139
140
              # Convert to pandas DataFrame with date column, account_value and daily_return
              \hookrightarrow columns
             portfolio = pd.DataFrame(
141
                  {
142
                      "date": dates[self.lookback :],
143
                      "account_value": portfolio_values,
144
                      "daily_return": portfolio_returns,
145
                  }
146
             )
147
148
             return portfolio
149
150
151
         def __momentum_strategy(
             self, prices: pd.DataFrame, lookback: int = 252
152
         ) -> Dict:
153
154
              Implements a simple momentum strategy.
155
              :param prices: DataFrame of prices.
156
157
              :return: Dictionary of weights based on momentum.
158
159
160
             returns = prices.pct_change(lookback).iloc[-1]
161
              # Clipping negative returns to zero
162
             returns = returns.clip(lower=0)
163
164
              # If all returns are zero, return equal weights
165
              if returns.sum() == 0:
166
167
                 return {tic: 1 / len(prices.columns) for tic in prices.columns}
168
              \# Normalise weights to sum to 1
              weights = returns / returns.sum()
169
             return weights.to_dict()
170
171
         def __equal_weight_strategy(self, ticker_list: list) -> Dict:
172
173
              Implements an equal weight strategy.
174
```

```
:param ticker_list: List of asset tickers.
175
             :return: Dictionary of equal weights for each asset.
176
177
             num_assets = len(ticker_list)
178
             return {tic: 1 / num_assets for tic in ticker_list}
179
180
         def __mean_variance_strategy(self, prices: pd.DataFrame) -> Dict:
181
182
             Implements a mean-variance optimisation strategy.
183
             :param prices: DataFrame of prices.
184
             :return: Dictionary of weights based on mean-variance optimisation.
185
186
             mu = expected_returns.mean_historical_return(prices)
             S = risk_models.sample_cov(prices)
188
189
             ef = EfficientFrontier(mu, S)
190
             _ = ef.max_sharpe()
191
192
             return ef.clean_weights()
193
         def __min_variance_strategy(self, prices: pd.DataFrame) -> Dict:
194
195
             Implements a minimum variance optimisation strategy.
196
             :param prices: DataFrame of prices.
197
             : return: \ \textit{Dictionary of weights based on minimum variance optimisation}.
198
199
200
             mu = expected_returns.mean_historical_return(prices)
             S = risk_models.sample_cov(prices)
201
202
             ef = EfficientFrontier(mu, S)
203
204
             _ = ef.min_volatility()
             return ef.clean_weights()
205
206
         def get_index_performance(
207
208
             self, start_date: str, end_date: str, index_ticker: str
209
         ):
210
             findownloader = FinancialDataDownloader(start_date, end_date)
             index_df = findownloader.download_data([index_ticker])
211
             index_df = index_df[["date", "close"]].copy()
212
213
214
             # Compute daily returns
             index_df["daily_return"] = index_df["close"].pct_change().fillna(0)
215
216
             # Compute the cumulative returns
217
             index_df["cumulative_return"] = (
218
                 1 + index_df["daily_return"]
219
220
             ).cumprod() - 1
221
             # Compute the account value
222
             index_df["account_value"] = (
223
                 1 + index_df["daily_return"]
224
             ).cumprod() * config.INITIAL_AMOUNT
225
             # Set the model name and drop price column
226
             index_df["model"] = "Index"
227
             index_df.drop(columns=["close"], inplace=True)
228
229
```

```
return index_df
230
231
         def compute_perf_stats(self, df_account: pd.DataFrame) -> pd.Series:
232
233
             Computes performance statistics for the portfolio using PyFolio.
234
             :param df_account: DataFrame containing account values with 'date',
235
              'account_value', and 'daily_return' columns.
237
             :return: Series containing performance statistics.
238
             pf_returns = self.convert_daily_return(df_account)
239
             perf_stats_alg = timeseries.perf_stats(
240
                 returns=pf_returns,
241
                 factor_returns=pf_returns,
242
243
                 positions=None,
                 transactions=None,
244
                 turnover_denom="AGB",
245
246
247
             return perf_stats_alg
248
         def compute_sharpe_ratio(self, df_account: pd.DataFrame) -> float:
249
250
             Computes the Sharpe ratio for the portfolio.
251
             :param df_account: DataFrame containing account values with 'date',
252
                  'account\_value', \ and \ 'daily\_return' \ columns.
253
254
             :return: The Sharpe ratio as a float.
255
             perf_stats = self.compute_perf_stats(df_account)
256
             return perf_stats.get("Sharpe ratio", 0)
257
258
         def compute_cum_returns(self, df_account: pd.DataFrame) -> float:
259
260
             Computes the cumulative returns for the portfolio.
261
             :param df_account: DataFrame containing account values with 'date',
262
263
                  'account_value', and 'daily_return' columns.
264
             :return: The cumulative returns as a float.
265
             perf_stats = self.compute_perf_stats(df_account)
266
             return perf_stats.get("Cumulative returns", 0)
267
```

I.6 Explainability Module

Listing 11: explainability.py

```
from sklearn.model_selection import HalvingGridSearchCV # type: iqnore
8
    from sklearn.model_selection import train_test_split
10
11
    class Explainer:
12
        11 11 11
13
        Base class for explainers in the portfolio optimization environment.
14
        This class provides methods to build state and action spaces, split data,
15
        and build a proxy explanation model.
16
        11 11 11
17
18
        def __init__(self):
19
            self.state_space = None
20
            self.action_space = None
21
22
        def build_state_space(
23
            self, data: pd.DataFrame, columns: list
24
25
        ) -> pd.DataFrame:
26
            Build the state space dataframe from a given DataFrame.
27
            :param data: DataFrame containing trade data with 'date' and 'tic' columns.
28
            :param columns: List of columns to include in the state space.
29
            :return: DataFrame representing the state space columns.
30
31
32
            # Filter the trade data to include only the relevant columns
            pivot_df = data.pivot(index="date", columns="tic", values=columns)
33
            # Flatten the multi-index columns
34
            pivot_df.columns = [
35
                "_".join(col).strip() for col in pivot_df.columns.values
36
37
38
            state_space = pivot_df.reset_index()
39
40
41
            # Drop the 'date' column
            state_space.drop(columns=["date"], inplace=True)
42
43
            return state_space
44
45
46
        def build_action_space(self, data: pd.DataFrame) -> pd.DataFrame:
47
            Build the action space dataframe from a given DataFrame.
48
            :param data: DataFrame containing trade data with 'date' and 'tic' columns.
49
            :return: DataFrame representing the action space columns.
50
51
            # Filter the trade data to include only the relevant columns
52
            action_space = data.drop(columns=["date"])
53
54
55
            return action_space
56
        def split_data(
57
            self,
59
            state_space: pd.DataFrame,
            action_space: pd.DataFrame,
60
            test_size: float = 0.2,
61
        ) -> Tuple[pd.DataFrame, pd.DataFrame, pd.DataFrame]:
62
```

```
63
              Split the state and action space data into training and testing sets.
65
              :param state_space: DataFrame representing the state space.
              : param\ action\_space:\ DataFrame\ representing\ the\ action\ space.
66
              :param test_size: Proportion of the dataset to include in the test split.
67
              :return: Tuple containing training and testing sets for state and action spaces.
68
69
70
             X_train, X_test, y_train, y_test = train_test_split(
                  state_space, action_space, test_size=test_size, shuffle=False
71
72
73
             return X_train, X_test, y_train, y_test
74
         def build_proxy_explanation_model(
75
76
             self.
             X_train: pd.DataFrame,
77
             y_train: pd.DataFrame,
78
79
             find_best_params: bool = True,
80
         ) -> RandomForestRegressor:
81
              Build and train a RandomForestRegressor model to explain the actions
82
              taken by the agent based on the state space.
83
              :param X_train: DataFrame containing the training state space data.
84
              :param y_train: DataFrame containing the training action space data.
85
              : param\ find\_best\_params \colon \textit{Whether to perform hyperparameter tuning}.
87
              : return: \ \textit{The trained RandomForestRegressor model}.
88
89
              if find_best_params:
90
91
92
                  param_grid = {
                      "n_estimators": [100, 200, 300],
93
                      "max_depth": [10, 20, 30],
94
                      "min_samples_split": [2, 5, 10],
95
                      "min_samples_leaf": [1, 2, 4],
96
                  }
97
98
                  grid_search = HalvingGridSearchCV(
99
                      estimator=RandomForestRegressor(),
100
101
                      param_grid=param_grid,
102
                      cv=3,
103
                  ).fit(X_train, y_train)
                  print("Best parameters found: ", grid_search.best_params_)
104
                  print(f"Best score: {grid_search.best_score_:.4f}")
105
106
                  best_model = grid_search.best_estimator_
107
             else:
108
109
                  best_model = RandomForestRegressor(
                      n_estimators=200,
110
                      max_depth=10,
111
                      min_samples_split=5,
112
                      min_samples_leaf=4,
113
114
                  best_model.fit(X_train, y_train)
115
116
```

Listing 12: feature_importance.py

```
from typing import List, Literal
2
    import matplotlib.pyplot as plt
3
    import pandas as pd
4
    import seaborn as sns
   from sklearn.ensemble import RandomForestRegressor
8
    class FeatureImportance:
9
        def __init__(
10
            self,
11
            model: RandomForestRegressor,
12
            columns: List[str],
13
            directory: str,
14
            model_name: str,
15
        ):
16
17
            Initialize\ the\ Feature Importance\ class.
18
            :param model: Trained Random Forest model.
19
             :param columns: List of feature names.
20
21
             :param directory: Directory where plots will be saved.
22
            :param model_name: Name of the DRL model to which the feature importances belong
23
            self.model = model
24
            self.columns = columns
25
            self.directory = directory
26
27
            self.model_name = model_name
28
        def get_feature_importances(self) -> pd.DataFrame:
29
30
            Calculate feature importances from the trained model.
31
             :return: DataFrame containing feature names and their importances.
32
33
            importances = self.model.feature_importances_
34
            feature_importances = pd.DataFrame(
35
                {
36
                     "feature": self.columns,
37
                     "importance": importances,
                }
39
            ).sort_values(by="importance", ascending=False)
40
41
            feature_importances.reset_index(drop=True, inplace=True)
42
            feature_importances["ticker"] = feature_importances["feature"].apply(
43
                lambda x: x.split("_")[-1] if "_" in x else ""
44
45
            feature_importances["indicator"] = (
46
                feature_importances["feature"]
47
```

```
.apply(lambda x: x.split("_")[:-1] if "_" in x else x)
48
                  .apply(lambda x: "_".join(x) if len(x) > 1 else x[0])
49
             )
50
             self.feature_importances = feature_importances
51
52
             return feature_importances
53
54
         def plot_feature_importances(
55
56
             self,
             max_features: int = 20,
57
         ) -> None:
58
             11 11 11
59
             Plot the feature importances
60
             :param max_features: Maximum number of features to display. Defaults to 20.
61
             :return: None
62
63
             plt.figure(figsize=(10, 6))
64
65
             sns.barplot(
                 data=self.feature_importances[:max_features],
66
                 y="feature",
67
                 x="importance",
68
                  orient="h",
69
             )
70
71
             plt.title("Feature importances")
             plt.xlabel("Importance")
72
             plt.ylabel("Feature")
73
             plt.tight_layout()
74
75
             plt.savefig(
                  f"{self.directory}/{self.model_name}_feature_importance.png"
76
77
             plt.show()
78
79
         def plot_feature_importances_by_ticker(
80
81
82
             max_features: int = 20,
83
         ) -> None:
84
             Plot the feature importances by ticker.
85
86
             :return: None
87
             plt.figure(figsize=(10, 6))
88
             sns.barplot(
89
                 data=self.feature_importances[:max_features],
90
                 y="feature",
91
                 x="importance",
92
93
                 orient="h",
                 hue="ticker",
94
             )
95
             plt.title("Feature importances by Ticker")
96
             plt.xlabel("Importance")
97
             plt.ylabel("Feature")
98
             plt.legend(title="Ticker")
99
             plt.tight_layout()
100
             plt.savefig(
101
                  f"{self.directory}/{self.model_name}_feature_importance_by_ticker.png"
102
```

```
103
             plt.show()
104
105
         def add_comparison(
106
              self.
107
             statistic: Literal["mean", "median", "q1", "q3"] = "mean",
108
         ) -> pd.DataFrame:
109
110
              Add a column to the feature importances DataFrame indicating whether
111
              the importance is above or below the provided statistical function.
112
              :param statistic: Statistical function to compare against (e.g., mean, median,
113
              \rightarrow q1, q3).
              :return: Updated DataFrame with a new column indicating comparison.
114
115
             if statistic == "mean":
116
                 threshold = self.feature_importances["importance"].mean()
117
              elif statistic == "median":
118
119
                 threshold = self.feature_importances["importance"].median()
120
              elif statistic == "q1":
                 threshold = self.feature_importances["importance"].quantile(0.25)
121
              elif statistic == "q3":
122
                 threshold = self.feature_importances["importance"].quantile(0.75)
123
              else:
124
                  raise ValueError(
125
126
                      "Invalid statistic. Use 'mean', 'median', 'q1', or 'q3'."
127
128
              self.feature_importances[statistic] = self.feature_importances[
129
                  "importance"
130
             ].apply(
131
132
                 lambda x: (
                      f"Above {statistic}" if x > threshold else f"Below {statistic}"
133
                  )
134
135
              )
136
137
             return self.feature_importances
138
         def plot_feature_importance_comparison(
139
              self,
140
             max_features: int = 20,
141
             statistic: Literal["mean", "median", "q1", "q3"] = "mean",
142
         ) -> None:
143
              11 11 11
144
             Plot the feature importances with comparison to a statistical threshold.
145
              :param max_features: Maximum number of features to display. Defaults to 20.
146
              :param statistic: Statistical function to compare against (e.g., mean, median,
147
              \hookrightarrow q1, q3).
148
              :return: None
149
              feature_importances = self.add_comparison(statistic)
150
151
             plt.figure(figsize=(10, 6))
152
153
              sns.barplot(
                  data=feature_importances[:max_features],
154
```

```
y="feature",
155
                  x="importance",
156
                  orient="h",
157
                  hue=statistic,
158
159
             plt.title(f"Feature importances with {statistic} comparison")
160
             plt.xlabel("Importance")
161
             plt.ylabel("Feature")
162
             plt.legend(title="")
163
             plt.tight_layout()
164
             plt.savefig(
165
                  f"{self.directory}/{self.model_name}_feature_importance_{statistic}_compari_
166
              )
167
             plt.show()
168
169
         def plot_feature_importance_by_indicator(
170
171
172
             max_features: int = 20,
         ) -> None:
173
             11 11 11
174
             Plot the feature importances by indicator.
175
              :param max_features: Maximum number of features to display. Defaults to 20.
176
              :return: None
177
178
179
             plt.figure(figsize=(10, 6))
              sns.barplot(
180
                  data=self.feature_importances[:max_features],
181
182
                  x="importance",
183
                  orient="h",
184
                  hue="indicator",
185
             )
186
187
             plt.title("Feature importances by Indicator")
188
             plt.xlabel("Importance")
189
             plt.ylabel("Feature")
             plt.legend(title="Indicator")
190
             plt.tight_layout()
191
             plt.savefig(
192
193
                  f"{self.directory}/{self.model_name}_feature_importance_by_indicator.png"
194
             plt.show()
195
196
         def plot_top_features_per_ticker(
197
             self,
198
             top_features: int = 5,
199
200
         ) -> None:
              11 11 11
201
              Plot the top features per ticker.
202
              :param directory: Directory where the plot will be saved.
203
              :param filename: Base filename for the saved plot.
204
              :param top_features: Number of top features to display per ticker. Defaults to 5
              :return: None
206
              11 11 11
207
```

```
208
              # Group by ticker and get the top features by importance
209
              grouped_features = (
210
                  self.feature_importances.groupby("ticker")[
211
                      ["ticker", "feature", "importance"]
212
213
                  .apply(lambda x: x.nlargest(top_features, "importance"))
214
215
                  .reset_index(drop=True)
             )
216
217
             plt.figure(figsize=(10, 6))
218
              sns.barplot(
219
220
                  data=grouped_features,
221
                  x="importance",
                  y="feature",
222
                  hue="ticker",
223
224
             plt.title("Top features per Ticker")
225
             plt.xlabel("Importance")
226
             plt.ylabel("Feature")
227
             plt.legend(title="Ticker")
228
             plt.tight_layout()
229
             plt.savefig(
230
231
                  f"{self.directory}/{self.model_name}_top_features_per_ticker.png"
              )
232
             plt.show()
233
234
         def plot_top_features_per_indicator(
235
              top_features: int = 5,
237
         ) -> None:
238
              11 11 11
239
             Plot the top features per indicator.
240
241
              :param top_features: Number of top features to display per indicator. Defaults
              \hookrightarrow to 5
242
              :return: None
243
244
              # Select the top indicators based on their total importance
245
246
              top_indicators = (
                  self.feature_importances.groupby("indicator")["importance"]
247
248
                  .sum()
                  .nlargest(top_features)
249
                  .index
250
              )
251
252
253
              # Filter the feature importances to include only the top indicators
             filtered_features = self.feature_importances[
254
                  self.feature_importances["indicator"].isin(top_indicators)
255
             ].copy()
256
              # Sort values by indicator column given the order of top_indicators
258
             filtered_features["indicator"] = pd.Categorical(
259
                  filtered_features["indicator"],
260
```

```
categories=top_indicators,
261
262
                  ordered=True,
             )
263
264
              # Sort the filtered features by indicator and importance
265
             filtered_features = filtered_features.sort_values(
266
                  by=["indicator", "importance"], ascending=[True, False]
267
268
269
             plt.figure(figsize=(10, 6))
270
             sns.barplot(
271
                  data=filtered_features,
272
273
                  x="importance",
                  y="feature",
274
                  hue="indicator",
275
276
277
             plt.title("Top features per Indicator")
278
             plt.xlabel("Importance")
             plt.ylabel("Feature")
279
             plt.legend(title="Indicator")
280
             plt.tight_layout()
281
             plt.savefig(
282
                  f"{self.directory}/{self.model_name}_top_features_per_indicator.png"
283
284
              )
             plt.show()
285
286
         def plot_mean_importance_by_ticker(
287
288
              self,
         ) -> None:
289
290
             Plot the mean feature importances by ticker.
291
292
              :return: None
              11 11 11
293
294
             mean_importances = (
                  self.feature_importances.groupby("ticker")["importance"]
295
296
                  .mean()
                  .reset_index()
297
                  .sort_values(by="importance", ascending=False)
298
299
             plt.figure(figsize=(8, 4))
301
              sns.barplot(
302
                  data=mean_importances,
303
                  x="importance",
304
                  y="ticker",
305
306
                  orient="h"
                  hue="ticker",
307
              )
308
             plt.title("Mean Feature Importances by Ticker")
309
             plt.xlabel("Mean Importance")
310
             plt.ylabel("Ticker")
311
             plt.tight_layout()
312
             plt.savefig(
313
                  f"{self.directory}/{self.model_name}_mean_importance_by_ticker.png"
314
315
```

```
plt.show()
316
317
         def plot_mean_importance_by_indicator(
318
             self.
319
         ) -> None:
320
              11 11 11
321
322
             Plot the mean feature importances by indicator.
323
              :return: None
324
             mean_importances = (
325
                  self.feature_importances.groupby("indicator")["importance"]
326
                  .mean()
327
328
                  .reset_index()
                  .sort_values(by="importance", ascending=False)
329
             )
330
331
             plt.figure(figsize=(8, 4))
332
333
              sns.barplot(
                  data=mean_importances,
334
                  x="importance",
335
                  y="indicator",
336
                  orient="h",
337
                  hue="indicator",
338
339
              )
             plt.title("Mean Feature Importances by Indicator")
340
             plt.xlabel("Mean Importance")
341
             plt.ylabel("Indicator")
342
             plt.tight_layout()
343
             plt.savefig(
344
                  f"{self.directory}/{self.model_name}_mean_importance_by_indicator.png"
345
346
347
             plt.show()
```

Listing 13: lime_explainability.py

```
from typing import Callable, List
1
    import pandas as pd
3
    from lime.lime_tabular import LimeTabularExplainer
4
6
    class LimeExplainer:
7
        def __init__(self, directory: str, model_name: str) -> None:
9
            Initialize the LimeExplainer with a directory to save explanation plots.
10
            :param directory: Directory where plots will be saved.
11
            :param model_name: Name of the DRL model to which the feature importances belong
12
13
            self.directory = directory
14
            self.model_name = model_name
15
16
```

```
def build_lime_explainer(
17
             self,
             X_train: pd.DataFrame,
19
        ) -> LimeTabularExplainer:
20
21
             Build a LIME explainer for the given training data.
22
             :param X_train: DataFrame containing the training data.
23
             : return: \ \mathit{LIME} \ explainer \ object.
24
25
             explainer = LimeTabularExplainer(
26
                 X_train.values, mode="regression", feature_names=X_train.columns
27
28
             self.explainer = explainer
29
             return explainer
30
31
        def explain_instance(
32
33
             self,
34
             instance: pd.Series,
35
             predict_fn: Callable,
        ) -> List:
36
             11 11 11
37
             Explain a single instance using the LIME explainer.
38
             Output the explanation in a notebook and return it as a list.
39
             :param instance: Series representing the instance to explain.
41
             : param\ predict\_fn\colon Function\ to\ predict\ actions\ based\ on\ states.
             : return: \ List \ containing \ the \ explanation.
42
43
             explanation = self.explainer.explain_instance(
44
                 instance.values, predict_fn
45
46
             explanation.show_in_notebook(show_table=True, show_all=False)
47
             return explanation.as_list()
48
49
        def explain_portfolio(
50
51
             self,
52
             instance: pd.Series,
             columns: List[str],
53
             predict_fn: Callable,
54
55
             filename: str,
        ) -> None:
57
             Explain the portfolio using the LIME explainer and save the explanations as HTML
58
             \hookrightarrow \quad \textit{files}.
             :param explainer: LIME explainer object.
59
             :param instance: Series representing the instance to explain.
60
             :param columns: List of asset names to explain.
62
             : param\ predict\_fn:\ Function\ to\ predict\ actions\ based\ on\ states.
             : param\ filename:\ Base\ filename\ for\ the\ HTML\ files.
63
64
             # Explain each output separately
65
             for index, column in enumerate(columns):
66
                 print(f"Explaining output for asset: {column}")
67
68
                 # Define a predict function for the specific asset
69
```

```
def predict(x):
70
71
                     return predict_fn(x)[:, index]
72
                 \# Explain the instance for the specific output
73
                 exp = self.explainer.explain_instance(
74
                     instance.values, predict, num_features=10
75
76
77
                 # Save the explanation as HTML
78
                html = exp.as_html()
79
                 with open(
80
                     f"{self.directory}/{self.model_name}_{filename}_lime_single_obs_{column}
81
                     "w",
82
                 ) as f:
83
                     f.write(html)
84
85
86
                 exp.show_in_notebook(show_table=True)
```

Listing 14: shap_explainability.py

```
from typing import Callable
1
2
    import numpy as np
3
    import pandas as pd
4
5
    import shap
    from sklearn.ensemble import RandomForestRegressor
8
    class ShapExplainer:
9
        def __init__(self):
10
            Initialize the SHAP explainer for the portfolio optimization environment.
12
13
            pass
14
15
        def build_proxy_explainer(
16
            self, model: RandomForestRegressor
17
        ) -> shap.TreeExplainer:
18
19
            Build a proxy SHAP explainer for the given model and training data.
20
            :param model: The trained RandomForestRegressor model.
21
22
            :param X_train: DataFrame containing the training data.
            :return: SHAP explainer object.
23
24
            explainer = shap.TreeExplainer(model)
25
            return explainer
26
27
        def build_kernel_explainer(
28
            self, predict_fn: Callable, X_train: pd.DataFrame
29
        ) -> shap.KernelExplainer:
30
            11 11 11
31
```

```
Build a Kernel SHAP explainer for the given prediction function and training
32
             \hookrightarrow data.
             :param predict_fn: Function to predict actions based on states.
33
             :param X_train: DataFrame containing the training data.
34
             :return: SHAP KernelExplainer object.
35
36
             explainer = shap.KernelExplainer(predict_fn, X_train)
37
            return explainer
38
39
        def compute_shap_values(
40
            self, explainer: shap.Explainer, X_test: pd.DataFrame
41
        ) -> shap.Explanation:
42
43
             Compute SHAP values for the test data using the given explainer.
44
             :param explainer: SHAP explainer object.
45
             :param X_test: DataFrame containing the test data.
46
             :return: SHAP explanation object containing the SHAP values.
47
48
49
             shap_values = explainer(X_test)
50
            return shap_values
51
        def compute_shap_interaction_values(
52
            self, explainer: shap.Explainer, X_test: pd.DataFrame
53
        ) -> np.ndarray:
54
55
             Compute SHAP interaction values for the test data using the given explainer.
56
             :param explainer: SHAP explainer object.
57
             :param X_test: DataFrame containing the test data.
58
             :return: SHAP explanation object containing the SHAP interaction values.
59
60
             shap_interaction_values = explainer.shap_interaction_values(X_test) # type:
61
             \hookrightarrow ignore
            return shap_interaction_values
62
```

I.7 Visualisation Module

Listing 15: __init__.py

```
import os

import os

import matplotlib.pyplot as plt

# Use custom matplotlib style

style = os.path.dirname(os.path.abspath(__file__)) + "/style.mplstyle"

plt.style.use(style)
```

Listing 16: benchmark_visualiser.py

import matplotlib.pyplot as plt

```
import pandas as pd
2
    import seaborn as sns
4
5
    class BenchmarkVisualiser:
6
        def __init__(
7
            self,
8
9
            directory: str,
10
11
            Initializes the BenchmarkVisualiser with a directory to save plots.
12
            :param directory: Directory where the plots will be saved.
13
            self.directory = directory
15
16
        def compare_account_value(
17
            self,
18
19
            data: pd.DataFrame,
20
        ) -> None:
21
            Visualises the account value over time for different models.
22
            :param data: DataFrame containing account values with 'date', 'model', and
23
            \hookrightarrow 'account_value' columns.
25
            plt.figure(figsize=(12, 6))
            sns.lineplot(data=data, x="date", y="account_value", hue="model")
26
            plt.title("Portfolio Value over Trading Period")
27
            plt.xlabel("Date")
28
            plt.ylabel("Account Value")
29
            plt.legend(title="Models")
30
31
            plt.tight_layout()
            plt.savefig(f"{self.directory}/account_value.png")
32
            plt.show()
33
34
35
        def compare_daily_returns(self, data: pd.DataFrame) -> None:
36
            Visualises the daily returns over time for different models.
37
            :param data: DataFrame containing returns with 'date', 'model', and
38
            \hookrightarrow 'daily_return' columns.
39
40
            plt.figure(figsize=(12, 6))
            sns.lineplot(data=data, x="date", y="daily_return", hue="model")
41
            plt.title("Daily Returns over Trading Period")
42
            plt.xlabel("Date")
43
            plt.ylabel("Daily Returns")
44
            plt.legend(title="Models")
45
46
            plt.tight_layout()
            plt.savefig(f"{self.directory}/daily_returns.png")
47
48
            plt.show()
49
        def compare_cum_returns(self, data: pd.DataFrame) -> None:
50
51
            Visualises the cumulative returns over time for different models.
52
            :param data: DataFrame containing returns with 'date', 'model', and
53
```

```
54
            plt.figure(figsize=(12, 6))
            sns.lineplot(data=data, x="date", y="cumulative_return", hue="model")
56
            plt.title("Cumulative Returns over Trading Period")
57
            plt.xlabel("Date")
58
            plt.ylabel("Cumulative Returns")
59
            plt.legend(title="Models")
60
61
            plt.tight_layout()
            plt.savefig(f"{self.directory}/cumulative_returns.png")
62
            plt.show()
63
```

Listing 17: findata_visualiser.py

```
from typing import Optional
1
    import matplotlib.pyplot as plt
3
    import pandas as pd
4
    import seaborn as sns
5
    class FinancialDataVisualiser:
        def __init__(self, directory: str) -> None:
9
10
             Initialise the FinancialDataVisualiser.
11
12
13
            self.directory = directory
14
        def plot_close_prices(
15
            self, data: pd.DataFrame, filename: Optional[str] = "close_prices"
16
        ) -> None:
17
             11 11 11
18
19
             Plot closing prices of tickers in the data.
             :param data: DataFrame containing financial data with 'date', 'tic', and 'close'
20
             \hookrightarrow columns.
             11 11 11
21
             # Sample the first 10 tickers if there are more than 10 unique tickers
22
             if data["tic"].nunique() > 10:
23
                 sample_tickers = data["tic"].unique()[:10]
24
                 data = data[data["tic"].isin(sample_tickers)].copy()
25
26
             # Sort the data by 'tic' to ensure consistent plotting
27
             data.sort_values(by="tic", inplace=True)
28
29
            plt.figure(figsize=(12, 5))
30
             sns.lineplot(data=data, x="date", y="close", hue="tic")
31
            plt.title("Closing Prices of Tickers")
32
            plt.xlabel("Date")
33
            plt.ylabel("Closing Price")
34
            plt.legend(title="Tickers")
35
            plt.tight_layout()
36
            plt.savefig(f"{self.directory}/{filename}.png")
37
            plt.show()
38
```

```
39
        def plot_technical_indicators(
40
41
             self,
             data: pd.DataFrame,
42
             indicators: dict[str, str],
43
        ) -> None:
44
             Plot technical indicators for each ticker in the data.
46
             : param\ data:\ Data Frame\ containing\ financial\ data\ with\ 'date',\ 'tic',\ and
47
             \hookrightarrow technical indicators.
             :param indicators: Dictionary mapping technical indicator names to their
48
             \hookrightarrow descriptions.
49
             # Sample the first 10 tickers if there are more than 10 unique tickers
51
             if data["tic"].nunique() > 10:
52
                 sample_tickers = data["tic"].unique()[:10]
53
                 data = data[data["tic"].isin(sample_tickers)].copy()
54
             # Sort the data by 'tic' to ensure consistent plotting
56
             data.sort_values(by="tic", inplace=True)
57
58
             # Sample the first 5 indicators if there are more than 5 unique indicators
59
             ind_size = n if (n := len(indicators)) < 5 else 5</pre>
60
61
62
             if ind_size == 1:
                 plt.figure(figsize=(12, 5))
63
                 indicator, name = list(indicators.items())[0]
64
                 if indicator in data.columns:
65
                     sns.lineplot(data=data, x="date", y=indicator, hue="tic")
66
67
                     plt.title(name)
                     plt.xlabel("Date")
68
                     plt.ylabel(indicator)
69
                     plt.legend(title="Tickers")
70
71
                     plt.savefig(f"{self.directory}/technical_indicators.png")
                     plt.show()
72
73
                 else:
                     print(f"Technical indicator '{indicator}' not found in data.")
74
             else:
75
                 _, ax = plt.subplots(
76
77
                     ind_size, 1, figsize=(12, 5 * ind_size), sharex=True
78
                 )
79
                 # Iterate over indicators to ind_size
80
                 for i, (indicator, name) in enumerate(
81
                     list(indicators.items())[:ind_size]
82
83
                 ):
84
                     if indicator in data.columns:
85
                         sns.lineplot(
                              data=data, x="date", y=indicator, hue="tic", ax=ax[i]
86
87
                         ax[i].set_title(name)
                         ax[i].set_xlabel("Date")
89
                         ax[i].set_ylabel(indicator)
90
```

```
ax[i].tick_params(labelbottom=True)
91
                           ax[i].legend(title="Tickers")
93
                      else:
                          print(
94
                               f"Technical indicator '{indicator}' not found in data."
95
96
97
                  plt.tight_layout()
98
                  plt.savefig(f"{self.directory}/technical_indicators.png")
aa
                  plt.show()
100
101
         def plot_macroeconomic_indicators(
102
              self,
103
              data: pd.DataFrame,
104
              indicators: dict[str, str],
105
         ) -> None:
106
              11 11 11
107
             Plot macroeconomic indicators.
              : param\ data:\ Data Frame\ containing\ financial\ data\ with\ 'date'\ and\ macroeconomic
109
              \hookrightarrow indicators.
              : param\ indicators:\ Dictionary\ mapping\ macroeconomic\ indicator\ names\ to\ their
110
              \hookrightarrow descriptions.
111
112
              # Sample the first 10 tickers if there are more than 10 unique tickers
113
              if data["tic"].nunique() > 10:
114
                  sample_tickers = data["tic"].unique()[:10]
115
                  data = data[data["tic"].isin(sample_tickers)].copy()
116
117
              # Sort the data by 'tic' to ensure consistent plotting
118
              data.sort_values(by="tic", inplace=True)
119
120
              # Sample the first 5 indicators if there are more than 5 unique indicators
121
              ind_size = n if (n := len(indicators)) < 5 else 5</pre>
122
123
124
              if ind_size == 1:
125
                  plt.figure(figsize=(12, 5))
                  indicator, name = list(indicators.items())[0]
126
                  # Convert indicator to alphanumeric
127
128
                  indicator = "".join(
                      for ch in indicator.split(".", 1)[0].lower()
130
                      if ch.isalnum() or ch == "_"
131
132
                  if indicator in data.columns:
133
                       # Take the date and the indicator column
134
135
                      ind_df = data[["date", indicator]]
136
                      # Remove duplicate dates
                      ind_df = ind_df.drop_duplicates(subset="date")
137
                      sns.lineplot(data=ind_df, x="date", y=indicator)
138
                      plt.title(name)
139
                      plt.xlabel("Date")
141
                      plt.ylabel(indicator)
                      plt.savefig(f"{self.directory}/macroeconomic_indicators.png")
142
```

```
plt.show()
143
144
                  else:
145
                      print(
                          f"Macroeconomic indicator '{indicator}' not found in data."
146
147
             else:
148
                  _, ax = plt.subplots(
149
                      ind_size, 1, figsize=(12, 5 * ind_size), sharex=True
150
151
152
                  colors = sns.color_palette().as_hex()[
153
                      :ind_size
154
                  ] # Use distinct colors
156
                  # Iterate over indicators to ind_size
157
                  for i, (indicator, name) in enumerate(
158
                      list(indicators.items())[:ind_size]
159
160
                      # Convert indicator to alphanumeric
161
                      indicator = "".join(
162
                          ch
163
                          for ch in indicator.split(".", 1)[0].lower()
164
                          if ch.isalnum() or ch == "_"
165
                      )
166
                      if indicator in data.columns:
167
                          # Take the date and the indicator column
168
                          ind_df = data[["date", indicator]]
169
                          # Remove duplicate dates
170
                          ind_df = ind_df.drop_duplicates(subset="date")
171
172
                          sns.lineplot(
                              data=ind_df,
173
174
                              x="date",
                              y=indicator,
175
176
                               ax=ax[i],
                               color=colors[i],
177
                          )
178
                          ax[i].set_title(name)
179
                          ax[i].set_xlabel("Date")
180
181
                          ax[i].set_ylabel(indicator)
182
                          ax[i].tick_params(labelbottom=True)
183
                      else:
                          print(
184
                               f"Macroeconomic indicator '{indicator}' not found in data."
185
186
187
188
                  plt.tight_layout()
                  plt.savefig(f"{self.directory}/macroeconomic_indicators.png")
189
                  plt.show()
190
191
         def plot_train_test_close_prices(
192
193
              train_data: pd.DataFrame,
194
             test_data: pd.DataFrame,
195
         ) -> None:
196
              11 11 11
197
```

```
Plot closing prices for train and test datasets.
198
             :param train_data: DataFrame containing training data with 'date', 'tic', and
199
             :param test_data: DataFrame containing testing data with 'date', 'tic', and
200
             :param directory: Directory where the plot will be saved.
201
             :param filename: Name of the file to save the plot (without extension).
202
204
             # Sample the first 10 tickers if there are more than 10 unique tickers
205
             if train_data["tic"].nunique() > 10:
206
                sample_tickers = train_data["tic"].unique()[:10]
207
                train_data = train_data[
208
                    train_data["tic"].isin(sample_tickers)
209
210
                1.copv()
                test_data = test_data[test_data["tic"].isin(sample_tickers)].copy()
211
212
213
             # Sort the data by 'tic' to ensure consistent plotting
214
             train_data.sort_values(by="tic", inplace=True)
             test_data.sort_values(by="tic", inplace=True)
215
216
             _, ax = plt.subplots(2, 1, figsize=(12, 10), sharex=True, sharey=True)
217
218
             sns.lineplot(data=train_data, x="date", y="close", hue="tic", ax=ax[0])
219
             ax[0].set_title("Train data set")
220
221
             ax[0].set_xlabel("Date")
222
             ax[0].set_ylabel("Closing Price")
             ax[0].tick_params(labelbottom=True)
223
             ax[0].legend(title="Tickers")
224
             sns.lineplot(data=test_data, x="date", y="close", hue="tic", ax=ax[1])
226
             ax[1].set_title("Test data set")
227
             ax[1].set_xlabel("Date")
228
             ax[1].set_ylabel("Closing Price")
229
230
             ax[1].legend(title="Tickers")
231
232
            plt.suptitle("Train and Test Closing Prices of Tickers")
            plt.tight_layout()
233
            plt.savefig(f"{self.directory}/train_test_close_prices.png")
234
235
            plt.show()
237
        def plot_train_val_test_close_prices(
238
            self.
            train_data: pd.DataFrame,
239
            val_data: pd.DataFrame,
240
241
            test_data: pd.DataFrame,
        ) -> None:
^{242}
             11 11 1
243
            Plot closing prices for train, validation, and test datasets.
244
             :param train_data: DataFrame containing training data with 'date', 'tic', and
245
             :param val_data: DataFrame containing validation data with 'date', 'tic', and
246
             :param test_data: DataFrame containing testing data with 'date', 'tic', and
247
```

```
11 11 11
248
249
             # Concatenate dataframes
250
             data = pd.concat([train_data, val_data, test_data])
251
252
             if data.tic.nunique() > 10:
253
                  sample_tickers = data["tic"].unique()[:10]
                  data = data[data["tic"].isin(sample_tickers)].copy()
255
256
             # Sort the data by 'tic' to ensure consistent plotting
257
             data.sort_values(by="tic", inplace=True)
258
259
             plt.figure(figsize=(12, 5))
260
             sns.lineplot(data=data, x="date", y="close", hue="tic")
261
262
             # Add vertical lines to indicate the split points
263
264
             plt.axvline(
                  x=val_data["date"].min(),
265
                  color="black",
266
                  linestyle="--",
267
             )
268
             plt.axvline(x=test_data["date"].min(), color="black", linestyle="--")
269
270
271
             # Add labels for the split points
272
             plt.text(
                 val_data["date"].min() + pd.Timedelta(days=20),
273
                  data["close"].max(),
274
                  "Validation Start",
275
                  horizontalalignment="left",
276
                 verticalalignment="bottom",
277
                  color="black",
278
279
             )
             plt.text(
280
281
                  test_data["date"].min() + pd.Timedelta(days=20),
282
                  data["close"].max(),
283
                  "Test Start",
                 horizontalalignment="left",
284
                  verticalalignment="bottom",
285
286
                  color="black",
             )
288
             plt.title("Train, Validation, and Test Closing Prices of Tickers")
289
             plt.xlabel("Date")
290
             plt.ylabel("Closing Price")
291
             plt.legend(title="Tickers")
292
293
             plt.tight_layout()
             plt.savefig(f"{self.directory}/train_val_test_close_prices.png")
294
             plt.show()
295
```

Listing 18: model_visualiser.py

```
1 from typing import List
```

```
import matplotlib.pyplot as plt
3
    import pandas as pd
    import seaborn as sns
6
7
    class ModelVisualiser:
8
        def __init__(
9
10
            self,
            directory: str,
11
        ):
12
13
            Initializes the ModelVisualiser with a directory to save plots.
14
            :param directory: Directory where the plots will be saved.
16
            self.directory = directory
17
18
        def evaluate_training(
19
20
            self,
21
            model_name: str,
            x: str,
22
            y: List[str],
23
            title: List[str],
24
            logs_dir: str,
26
        ) -> None:
27
            Visualises the training progress of an agent by plotting specified variables
28
            \hookrightarrow against a common
            x-axis variable.
29
            :param model_name: Name of the model being evaluated (e.g., 'a2c').
30
31
             :param x: The name of the x-axis variable (e.g., 'step').
            :param y: List of variable names to be plotted on the y-axis.
32
            :param title: List of titles for each subplot corresponding to the y variables.
33
            :param logs_dir: Directory where the training logs are stored.
34
35
36
37
            num_variables = len(y)
38
            _, ax = plt.subplots(
                num_variables, 1, figsize=(12, 5 * num_variables), sharex=True
39
40
41
            data = pd.read_csv(f"{logs_dir}/{model_name}/progress.csv")
42
43
            colors = sns.color_palette("husl", num_variables)
44
45
            # Iterate over the variables to plot
46
            for i, variable in enumerate(y):
47
48
                if variable in data.columns:
49
                     sns.lineplot(
                         data=data, x=x, y=variable, ax=ax[i], color=colors[i]
50
51
                     ax[i].set_title(title[i])
52
                     ax[i].set_xlabel(x.split("/")[-1].capitalize())
53
                     ax[i].set_ylabel(
54
                         " ".join(variable.split("/")[-1].split("_")).capitalize()
55
```

```
56
                      ax[i].tick_params(labelbottom=True)
57
58
             plt.suptitle(f"Training Progress of {model_name.upper()} Agent", y=1)
59
             plt.tight_layout()
60
             plt.savefig(f"{self.directory}/{model_name}_train_evaluation.png")
61
             plt.show()
62
63
         def evaluate_testing(
64
             self.
65
             model_name: str,
66
             account_data: pd.DataFrame,
67
             actions_data: pd.DataFrame,
68
         ) -> None:
69
70
             Visualises the testing results of an agent by plotting account value and actions
71
             \rightarrow over time.
72
              :param model_name: Name of the model being evaluated (e.g., 'a2c').
73
              :param account_data: DataFrame containing account values with a 'date' column.
             : param\ actions\_data\colon \textit{DataFrame}\ containing\ actions\ with\ a\ 'date'\ column.
74
75
76
             _, ax = plt.subplots(2, 1, figsize=(12, 10), sharex=True)
77
78
79
             # Plot account value
80
             sns.lineplot(
                  data=account_data,
81
                  x="date",
82
                  y="account_value",
83
                  ax=ax[0],
84
             )
85
             ax[0].set_title("Account Value Over Time")
86
             ax[0].set_xlabel("Date")
87
             ax[0].set_ylabel("Account Value")
88
89
             ax[0].tick_params(labelbottom=True)
90
91
             # Format the actions_data
             if "date" in actions_data.columns:
92
                  actions_data = actions_data.reset_index(drop=True).melt(
93
94
                      id_vars="date", var_name="tic", value_name="action"
95
96
             else:
                  actions_data = actions_data.reset_index().melt(
97
                      id_vars="date", var_name="tic", value_name="action"
98
                  )
99
             actions_data.sort_values(by=["date", "tic"]).reset_index(
100
101
                  drop=True, inplace=True
             )
102
103
             # Sample the first 10 tickers if there are more than 10 unique tickers
104
             if actions_data["tic"].nunique() > 10:
105
                  sample_tickers = actions_data["tic"].unique()[:10]
                  actions_data = actions_data[
107
                      actions_data["tic"].isin(sample_tickers)
108
```

```
]
109
110
              # Plot actions
111
             sns.lineplot(
112
                  data=actions_data,
113
                  x="date",
114
                  y="action"
115
                  hue="tic",
116
                  ax=ax[1],
117
              )
118
             ax[1].set_title("Actions Over Time")
119
              ax[1].set_xlabel("Date")
120
121
              ax[1].set_ylabel("Actions")
              ax[1].legend(title="Ticker")
122
123
             plt.suptitle(f"Testing Results of {model_name.upper()} Agent", y=1)
124
125
             plt.tight_layout()
             plt.savefig(f"{self.directory}/{model_name}_test_evaluation.png")
126
127
             plt.show()
```

Listing 19: shap_visualiser.py

```
from typing import Optional
1
2
    import matplotlib.pyplot as plt
3
    import numpy as np
    import pandas as pd
    import shap
    shap.initjs()
8
10
    class ShapVisualiser:
11
         def __init__(
12
              self,
13
              shap_values: shap.Explanation,
14
              action_space: pd.DataFrame,
15
             X_test: pd.DataFrame,
16
             directory: str,
17
             filename: str,
18
             model_name: str,
19
             shap_interaction_values: Optional[np.ndarray] = None,
20
         ) -> None:
^{21}
22
              Initializes the SHAP visualiser with SHAP values and action space.
23
              :param shap_values: SHAP explanation object containing the SHAP values.
24
              :param action_space: DataFrame containing the action space columns.
25
26
              :param\ \textit{X\_test}:\ \textit{DataFrame}\ \ \textit{containing}\ \ \textit{the test state}\ \ \textit{space}\ \ \textit{data}.
27
              :param directory: Directory where plots will be saved.
              : param\ filename:\ Base\ filename\ for\ the\ saved\ plots.
28
              :param model_name: Name of the DRL model to which the feature importances belong
29
              \hookrightarrow to.
```

```
:param shap_interaction_values: SHAP interaction values for the features.
30
31
32
             self.shap_values = shap_values
             self.action_space = action_space
33
             self.X_test = X_test
34
             self.directory = directory
35
             self.filename = filename
36
37
             self.model_name = model_name
             self.shap_interaction_values = shap_interaction_values
38
39
        def beeswarm_plot(
40
            self,
41
            index: int,
42
        ) -> None:
43
             11 11 1
44
             Create a beeswarm plot for the SHAP values.
45
             :param index: Index of the asset in the action space to plot.
46
47
             :return: None
             n n n
48
             ax = shap.plots.beeswarm(
49
                 self.shap_values[..., index],
50
                 show=False,
51
                 max_display=10,
52
                 group_remaining_features=False,
             )
54
             asset = self.action_space.columns[index]
55
             ax.set_title(f"SHAP Beeswarm Plot for {asset}")
56
57
            plt.savefig(
                 f"{self.directory}/{self.model_name}_{self.filename}_shap_beeswarm_{asset}.
58
                 \hookrightarrow png"
             )
59
            plt.show()
60
61
62
        def force_plot(
63
             self,
64
             index: int,
        ) -> None:
65
             11 11 11
66
             Create a force plot for the SHAP values.
67
68
             :param index: Index of the asset in the action space to plot.
69
             :return: None
70
             force_plot = shap.plots.force(
71
                 self.shap_values[..., index],
72
                 feature_names=self.X_test.columns,
73
                 link="logit",
74
75
             )
76
             shap.save_html(
77
                 f"{self.directory}/{self.model_name}_{self.filename}_shap_force_{self.actio_1
78

    n_space.columns[index]}.html",
                 force_plot,
79
             )
80
81
```

```
def force_plot_single_obs(
82
83
             self,
             index: int,
84
             obs: int,
85
         ) -> None:
86
             11 11 11
87
             Create a force plot for a single observation.
88
             :param index: Index of the asset in the action space to plot.
89
             :param obs: Index of the observation to plot in time.
90
             :return: None
91
92
             shap.plots.force(
93
                 self.shap_values[obs, ..., index],
                 feature_names=self.X_test.columns,
95
                 link="logit",
96
                 matplotlib=True,
97
                 show=False,
98
99
             asset = self.action_space.columns[index]
100
101
             plt.title(
102
                 f"SHAP Force Plot for {asset} for observation {obs}",
103
                 fontsize=16,
104
105
                 y=1.5,
             )
106
107
             # Format value labels to two decimal places
108
             for text in plt.gca().texts:
109
                 value = text.get_text()
110
                  \# If value contains = sign, format the number
111
                 if "=" in value:
112
                     parts = value.split("=")
113
                      if len(parts) == 2:
114
115
                              number = float(parts[1])
116
117
                              text.set_text(f"{parts[0]}= {number:.3f}")
                          except ValueError:
118
119
                              pass
120
121
             plt.savefig(
                 f"{self.directory}/{self.model_name}_{self.filename}_shap_force_single_obs_ |
122
                  )
123
             plt.show()
124
125
         def force_plot_assets(
126
127
             self,
             obs: int,
128
         ) -> None:
129
             11 11 11
130
             Create force plots for each asset in the portfolio.
131
             :param obs: Index of the observation to plot in time.
132
133
             for index, _ in enumerate(self.action_space.columns):
134
```

```
self.force_plot_single_obs(index, obs)
135
136
         def waterfall_plot_single_obs(
137
             self,
138
             index: int,
139
             obs: int,
140
         ) -> None:
141
142
              Create a waterfall plot for the SHAP values.
143
              :param index: Index of the asset in the action space to plot.
144
              :param obs: Index of the observation to plot in time.
145
146
              shap.plots.waterfall(
147
                  self.shap_values[obs, ..., index], show=False, max_display=10
148
149
150
             asset = self.action_space.columns[index]
151
152
             plt.title(f"SHAP Waterfall Plot for {asset}")
153
             plt.savefig(
154
                 f"{self.directory}/{self.model_name}_{self.filename}_shap_waterfall_{asset}|
155
                      .png"
             )
156
             plt.show()
157
158
         def heatmap(
159
             self,
160
             index: int,
161
         ) -> None:
162
163
              Create a heatmap for the SHAP values.
164
              :param index: Index of the asset in the action space to plot.
165
              :return: None
166
167
168
              shap.plots.heatmap(
                  {\tt self.shap\_values[..., index], max\_display=10, show=False}
169
170
             asset = self.action_space.columns[index]
171
             plt.title(f"SHAP Heatmap for {asset}")
172
173
             plt.savefig(
                  f"{self.directory}/{self.model_name}_{self.filename}_shap_heatmap_{asset}.p
174

→ ng"

             )
175
             plt.show()
176
177
         def interaction_plot(
178
179
             self,
180
             index: int,
         ) -> None:
181
             11 11 11
182
              Create a summary plot for the SHAP interaction values.
183
              :param index: Index of the asset in the action space to plot.
185
             if self.shap_interaction_values is None:
186
```

```
raise ValueError("SHAP interaction values are not provided.")
187
188
189
             shap.summary_plot(
                 self.shap_interaction_values[..., index], self.X_test, show=False
190
191
192
             asset = self.action_space.columns[index]
193
194
             plt.suptitle(
                 f"SHAP Interaction Values for {asset}",
195
                 y=1.1.
196
197
                 fontsize=14,
198
             plt.savefig(
                 f"{self.directory}/{self.model_name}_{self.filename}_shap_interaction_{asse_|
200
                  → t}.png"
201
             plt.show()
202
```

Listing 20: style.mplstyle

```
#### MATPLOTLIBRC FORMAT
2
  3
  ## * LINES
4
  5
  {\it \#\# See https://matplotlib.org/stable/api/artist\_api.html\#module-matplotlib.lines}
  ## for more information on line properties.
  lines.linewidth: 1.0
                      # line width in points
 lines.linestyle: -
                      # solid line
9
10
  11
 ## * FONT
  13
  ## The font properties used by `text.Text`.
14
15
16
17
  font.family: sans-serif
  font.style:
          normal
18
 font variant: normal
19
 font.weight: normal
20
 font.stretch: normal
21
 font.size:
23
24
  25
  ## * TEXT
26
  27
  ## The text properties used by `text.Text`.
28
  text.parse_math: True # Use mathtext if there is an even number of unescaped
30
                # dollar signs.
31
32
```

```
33
  ## * LaTeX
35
  36
  text.usetex: True # use latex for all text handling.
37
38
  ## ***************************
40
  ## * AXES
41
  42
  ## Following are default face and edge colors, default tick sizes,
43
44 ## default font sizes for tick labels, and so on. See
45 ## https://matplotlib.org/stable/api/axes_api.html#module-matplotlib.axes
46 axes.facecolor: 0.97, 0.97, 0.97 # axes background color
47 axes.edgecolor: 0.8, 0.8, 0.8
                          # axes edge color
  axes.linewidth: 1.0 # edge line width
48
49
  axes.grid:
                True
                      # display grid or not
                    # which axis the grid should apply to
  axes.grid.axis:
               both
  axes.titlelocation: center # alignment of the title: {left, right, center}
                      # draw axis gridlines and ticks:
  axes.axisbelow: True
52
                         - below patches (True)
53
                          - above patches but below lines ('line')
54
                      #
                          - above all (False)
56
57
  axes.spines.left: True # display axis spines
58
  axes.spines.bottom: True
59
60
  axes.spines.top:
  axes.spines.right: True
61
62
  axes.prop_cycle: cycler('color', ['ff85b6','ff8a91','ffbe88','fcea66','aaff99','8fd388']
63
  → ,'6de1c4','4aefff','84d1ff','bdb2ff'])
64
65
66
  67
  ## * GR.TDS
68
  ## ***************************
69
  grid.color: (0.76, 0.78, 0.83) # grid color
70
                 # solid
71
  grid.linestyle: --
  grid.linewidth: 0.8
72
                     # in points
  grid.alpha: 1.0
                     # transparency, between 0.0 and 1.0
73
74
75
  76
  ## * LEGEND
  78
79
  legend.loc:
                 best.
                 True
                       # if True, draw the legend on a background patch
  legend.frameon:
80
                       # if True, use a rounded box for the
  legend.fancybox:
                 True
81
                        # legend background, else a rectangle
             False
                       # if True, give background a shadow effect
  legend.shadow:
83
84
  85
```

```
## * FIGURE
86
   figure.titlesize: x-large # size of the figure title (``Figure.suptitle()``)
88
    \begin{tabular}{lll} figure.title weight: normal & {\it \# weight of the figure title} \\ \end{tabular} 
89
   figure.labelsize: large # size of the figure label (``Figure.sup[x/y]label()``)
figure.labelweight: normal # weight of the figure label
figure.dpi: 200 # figure dots per inch
figure.facecolor: white # figure face color
90
91
93
                             # figure edge color
    figure.edgecolor: white
94
    figure.frameon: True # enable figure frame
95
96
    ## Figure layout
97
    figure.autolayout: True # When True, automatically adjust subplot
                            # parameters to make the plot fit the figure
99
                            # using `tight_layout`
100
101
102
    103
    ## * HISTOGRAM PLOTS
104
    105
   hist.bins: 10 # The default number of histogram bins or 'auto'.
106
107
108
   ## ******************************
   ## * SAVING FIGURES
110
   111
   ## The default savefig parameters can be different from the display parameters
112
   savefig.facecolor: 'white' # figure face color when saving savefig.transparent: False # whether figures are saved with a transparent
113
    \hookrightarrow background by default
```

I.8 Optimisation Module

Listing 21: wandb_opt.py

```
from typing import Tuple
1
3
   import pandas as pd
   import wandb
4
   from wandb.integration.sb3 import WandbCallback
5
    from agents.drl_agent import DRLAgent
7
   from config import config_models
   from environments.env_portfolio_optimisation import (
9
        PortfolioOptimisationEnvWrapper,
10
11
   from pbenchmark.portfolio_benchmark import PortfolioBenchmark
12
13
   wandb.login()
14
15
16
```

```
class WandbOptimisation:
17
        def __init__(
            self,
19
            entity: str,
20
            project: str,
21
            train_data: pd.DataFrame,
22
23
             val_data: pd.DataFrame,
24
             test_data: pd.DataFrame,
             state_columns: list,
25
        ):
26
27
             Initialize the WandbOptimisation class.
28
             :param entity: The entity name for Weights & Biases.
             :param project: The project name for Weights & Biases.
30
             :param train_data: The training data.
31
             :param val_data: The validation data.
32
33
             :param test_data: The test data.
             :param state_columns: The columns that represent the environment.
35
             self.entity = entity
36
            self.project = project
37
            self.train_data = train_data
38
             self.val_data = val_data
39
            self.test_data = test_data
            self.state_columns = state_columns
41
42
             # Initialise wandb API
43
             self.api = wandb.Api()
44
45
             # Initialise portfolio benchmark
46
             self.portfolio_benchmark = PortfolioBenchmark()
47
48
        def wandb_train(
49
             self,
50
51
            model_name: str,
52
        ):
53
             \textit{Train a model using Weights \& Biases.}
54
55
             :param model_name: The name of the model to train.
56
             :param train_data: The training data.
             : param\ val\_data \colon\ The\ validation\ data.
57
             : param\ state\_columns:\ The\ columns\ that\ represent\ the\ environment.
58
59
             with wandb.init(settings={"quiet": "True"}) as run:
60
                 environment = PortfolioOptimisationEnvWrapper(
61
62
                     train_data=self.train_data,
63
                     trade_data=self.val_data,
                     state_columns=self.state_columns,
64
                     verbose=0,
65
                 )
66
67
68
                 env_train = environment.get_train_env()
                 gym_env, _ = environment.get_trade_env()
69
70
                 agent = DRLAgent(run)
71
```

```
72
73
                  configuration = wandb.config.as_dict()
74
                  model = agent.get_model(
75
                      model_name,
76
                      model_kwargs=configuration,
77
                       environment=env_train,
78
79
                      directory=None,
                      use_case="portfolio-optimisation",
80
                      verbose=0,
81
                  )
82
83
                  trained_model = agent.train(
85
                      model.
                      tb_log_name=model_name,
86
                       callback=WandbCallback(),
87
88
89
                  df_account, _ = agent.predict(trained_model, gym_env)
90
91
                  metrics = {
92
                       "sharpe_ratio": self.portfolio_benchmark.compute_sharpe_ratio(
93
                           df_account
94
                      ),
                       "cumulative_return": self.portfolio_benchmark.compute_cum_returns(
96
                           {\tt df\_account}
97
                      ),
98
                  }
99
100
                  wandb.log(metrics)
101
102
         def sweep(
103
             self,
104
105
              sweep_config: dict,
106
             model_name: str,
107
             number_trials: int = 5,
         ) -> str:
108
             11 11 11
109
110
              Start a sweep for hyperparameter optimization.
111
              :param sweep_config: The sweep configuration.
              :param\ model\_name\colon \ The\ name\ of\ the\ model\ to\ optimize.
112
              :param number_trials: The number of trials to run.
113
              :return: The sweep ID.
114
              11 11 11
115
              configuration = sweep_config
116
              configuration["parameters"] = config_models.MODEL_SWEEP_CONFIG[
117
118
                  model_name
              ]
119
120
              sweep_id = wandb.sweep(configuration, project=self.project)
121
122
              wandb.agent(
123
                  sweep_id,
                  lambda model_name=model_name: self.wandb_train(model_name),
124
                  count=number_trials,
125
              )
126
```

```
127
128
             return sweep_id
129
         def get_best_sweep_run(
130
              self, sweep_id: str, model_name: str
131
         ) -> Tuple[str, dict]:
132
              Get the best sweep run for a given model.
134
              :param sweep_id: The ID of the sweep.
135
              :param model_name: The name of the model.
136
              :return: The best run ID and configuration.
137
138
              sweep = self.api.sweep(f"{self.entity}/{self.project}/{sweep_id}")
139
             runs = sweep.runs
140
141
             best_run = max(
142
143
                  runs,
                  key=lambda run: run.summary.get("sharpe_ratio", 0),
144
145
             best_run_config = best_run.config
146
147
             best_config = dict()
148
             print("Best run configuration:")
149
              for key in config_models.MODEL_SWEEP_CONFIG[model_name]:
150
151
                  best_config[key] = best_run_config.get(key, 0)
                  if type(best_config[key]) is float:
152
                      print(f"\t{key}: {best_config[key]:.6f}")
153
154
                      print(f"\t{key}: {best_config[key]}")
155
156
             print("Best run metrics:")
157
             for key in [
158
                  "sharpe_ratio",
159
160
                  "cumulative_return",
161
             1:
162
                  print(f"\t{key}: {best_run.summary.get(key, 0):.4f}")
163
             return best_run.id, best_config
164
165
166
         def test_best_run(
167
             self,
             model_name: str,
168
             configuration: dict,
169
              train_val_data: pd.DataFrame,
170
              logs_directory: str,
171
172
             models_directory: str,
         ) -> Tuple[pd.DataFrame, pd.DataFrame]:
173
              11 11 11
174
              Test the best run configuration for a given model.
175
              :param model_name: The name of the model.
176
              : param\ configuration\colon \textit{The configuration of the model}.
177
              :param train_val_data: The training and validation data.
178
              :param logs_directory: The directory to save logs.
179
              :param models_directory: The directory to save models.
180
              :return: The account and actions DataFrames.
181
```

```
182
              environment = PortfolioOptimisationEnvWrapper(
183
184
                  train_data=train_val_data,
                  trade_data=self.test_data,
185
                  state_columns=self.state_columns,
186
187
188
              env_train = environment.get_train_env()
              gym_env, _ = environment.get_trade_env()
190
191
              agent = DRLAgent()
192
193
             model = agent.get_model(
194
195
                  model_name,
                  model_kwargs=configuration,
196
                  environment=env_train,
197
                  directory=logs_directory,
198
                  use_case="portfolio-optimisation",
              )
200
201
             print(f"Training model: {model_name.upper()}")
202
             trained_model = agent.train(
203
                  model,
204
205
                  tb_log_name=model_name,
             )
206
207
             print(f"Saving model: {model_name.upper()}")
208
              agent.save_model(
209
                  model=model,
210
211
                  model_name=model_name,
                  directory=models_directory,
212
213
214
215
             print(f"Evaluating model: {model_name.upper()}")
216
             df_account, df_actions = agent.predict(
217
                  model=trained_model,
                  environment=gym_env,
218
219
220
             return df_account, df_actions
```

I.9 Examples

The examples are originally a set of Jupyter Notebooks. However, for visualisation purposes in this report, they have been converted to Python scripts.

findownloader.ipynb demonstrates how to download the data for the tickers specified in the config/config.py file.

Listing 22: findownloader.py

```
# Financial Data Downloader example
1
3
    import os
    import sys
4
   REPO_ROOT = "/Users/ingridperez/Documents/GitHub Repositories/xdl-portfolio"
6
    sys.path.append(REPO_ROOT)
   from config import config
9
   from preprocessor.findata_downloader import FinancialDataDownloader
10
   from visualiser.findata_visualiser import FinancialDataVisualiser
11
12
13
   data_dir = f"{REPO_ROOT}/{config.DATA_DIR}/{config.DATASET_NAME}"
14
   plot_dir = (
        f"{REPO_ROOT}/{config.PLOT_DIR}/{config.TICKERS_NAME}/{config.DATASET_NAME}"
15
16
17
   if not os.path.exists(data_dir):
18
19
        os.makedirs(data_dir)
20
   if not os.path.exists(plot_dir):
21
        os.makedirs(plot_dir)
22
23
    findownloader = FinancialDataDownloader(
24
25
        start_date=config.START_DATE,
        end_date=config.END_DATE,
26
27
28
   data = findownloader.download_data(tickers=config.TICKERS)
29
30
   findownloader.save_data(
31
        directory=data_dir,
32
        filename=config.TICKERS_NAME,
33
34
35
   finvisualiser = FinancialDataVisualiser(directory=plot_dir)
36
   finvisualiser.plot_close_prices(data=data)
37
```

finpreprocessor.ipynb demonstrates how to preprocess the data downloaded in the previous step. This includes calculating technical indicators, macroeconomic indicators, and other features.

Listing 23: finpreprocessor.py

```
# Financial Data Preprocessing
import os
```

```
import sys
4
    REPO_ROOT = "/Users/ingridperez/Documents/GitHub Repositories/xdl-portfolio"
6
    sys.path.append(REPO_ROOT)
7
    from config import config, config_indicators
9
    from preprocessor.findata_downloader import FinancialDataDownloader
    from preprocessor.findata_preprocessor import FinancialDataPreprocessor
11
    from visualiser.findata_visualiser import FinancialDataVisualiser
12
13
    data_dir = f"{REPO_ROOT}/{config.DATA_DIR}/{config.DATASET_NAME}"
14
15
    plot_dir = (
        f"{REPO_ROOT}/{config.PLOT_DIR}/{config.TICKERS_NAME}/{config.DATASET_NAME}"
17
18
    if not os.path.exists(plot_dir):
19
        os.makedirs(plot_dir)
20
21
    findownloader = FinancialDataDownloader(
22
        start_date=config.START_DATE,
23
        end_date=config.END_DATE,
24
    )
25
    data = findownloader.load_data(
26
27
        directory=data_dir,
        filename=config.TICKERS_NAME,
28
    )
29
30
    finpreprocessor = FinancialDataPreprocessor(
31
        start_date=config.START_DATE,
32
33
        end_date=config.END_DATE,
34
    data = finpreprocessor.preprocess(
35
        data=data,
36
37
        exchange=config.EXCHANGE,
        use_tech_indicators=config.USE_TECHNICAL_INDICATORS,
38
        {\tt tech\_indicators=list(config\_indicators.TECHNICAL\_INDICATORS.keys())}\ ,
39
        {\tt use\_macro\_indicators=config.USE\_MACROECONOMIC\_INDICATORS,}
40
        macro_indicators=(
41
42
            list(config.MACROECONOMIC_INDICATORS.keys())
43
            if config.USE_MACROECONOMIC_INDICATORS
44
            else []
        ),
45
        use_covariance=config.USE_COVARIANCE_FEATURES,
46
    )
47
48
49
    finvisualiser = FinancialDataVisualiser(directory=plot_dir)
50
    finvisualiser.plot_close_prices(
        data=data,
51
        filename="processed_close_prices",
52
53
    if config.USE_TECHNICAL_INDICATORS:
55
        finvisualiser.plot_technical_indicators(
56
            data=data,
57
            indicators=config_indicators.TECHNICAL_INDICATORS,
58
```

```
)
59
    if config.USE_MACROECONOMIC_INDICATORS:
61
        finvisualiser.plot_macroeconomic_indicators(
62
            data=data,
63
             indicators=config.MACROECONOMIC_INDICATORS,
64
65
    train_data, test_data = finpreprocessor.split_train_test(
67
        data=data.
68
        test_start_date=config.TEST_START_DATE,
69
    )
70
71
    finvisualiser.plot_train_test_close_prices(
72
        train_data=train_data,
73
        test_data=test_data,
74
75
76
77
    finpreprocessor.save_train_test_data(
        train_data=train_data,
78
        test_data=test_data,
79
        directory=data_dir,
80
        filename=config.TICKERS_NAME,
81
    )
```

portfolio_optimisation.ipynb demonstrates how to use the portfolio optimisation environment and train agents to optimise a portfolio of stocks using reinforcement learning.

Listing 24: portfolio_optimisation.py

```
# Portfolio Optimisation Example
1
2
    import os
3
   import sys
4
   REPO_ROOT = "/Users/ingridperez/Documents/GitHub Repositories/xdl-portfolio"
6
    sys.path.append(REPO_ROOT)
7
   from agents.drl_agent import DRLAgent
9
    from config import config, config_models
10
11
    from environments.env_portfolio_optimisation import (
        PortfolioOptimisationEnvWrapper,
12
13
    from preprocessor.findata_preprocessor import FinancialDataPreprocessor
14
    from visualiser.model_visualiser import ModelVisualiser
15
    USE_CASE = "portfolio-optimisation"
17
18
   data_dir = f"{REPO_ROOT}/{config.DATA_DIR}/{config.DATASET_NAME}"
19
   plot_dir = f"{REPO_ROOT}/{config.PLOT_DIR}/{config.TICKERS_NAME}/{config.DATASET_NAME}/ |
20
```

```
models_dir = f"{REPO_ROOT}/{config.MODELS_DIR}/{USE_CASE}/{config.TICKERS_NAME}/{config.
           → .DATASET_NAME}"
          logs\_dir = f"\{REPO\_ROOT\}/\{config.LOGS\_DIR\}/\{USE\_CASE\}/\{config.TICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME\}/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/\{config.DAT\_ICKERS\_NAME]/

→ ASET_NAME

"

23
          if not os.path.exists(plot_dir):
24
                     os.makedirs(plot_dir)
25
26
          if not os.path.exists(models_dir):
27
                     os.makedirs(models_dir)
28
29
          if not os.path.exists(logs_dir):
30
                     os.makedirs(logs_dir)
31
         TRAIN = True
33
34
          finpreprocessor = FinancialDataPreprocessor(
35
                     start_date=config.START_DATE,
36
37
                     end_date=config.END_DATE,
         )
38
          train_data, trade_data = finpreprocessor.load_train_test_data(
39
                     directory=data_dir,
40
                     filename=config.TICKERS_NAME,
41
          )
42
43
          environment = PortfolioOptimisationEnvWrapper(
44
                     train_data=train_data,
45
                     trade_data=trade_data,
46
                     state_columns=config.ENVIRONMENT_COLUMNS,
47
48
49
         model_visualiser = ModelVisualiser(directory=plot_dir)
50
51
          for model_name in config_models.MODELS.keys():
52
53
                     env_train = environment.get_train_env()
54
55
                     gym_env, _ = environment.get_trade_env()
56
                     agent = DRLAgent()
57
58
59
                     model = agent.get_model(
60
                               model_name=model_name,
                               environment=env_train,
61
                               directory=logs_dir,
62
                               use_case=USE_CASE,
63
                     )
64
65
                     if TRAIN:
66
                               print(f"Training model: {model_name.upper()}")
67
                               trained_model = agent.train(
68
                                         model=model,
69
70
                                         tb_log_name=model_name,
71
                               print(f"Saving model: {model_name.upper()}")
72
```

```
agent.save_model(
73
                 model=model,
74
                 model_name=model_name,
75
                  directory=models_dir,
76
77
78
              visualisation_config = config_models.train_visualisation_config[
79
80
                  model_name
81
82
             model_visualiser.evaluate_training(
83
                 model_name=model_name,
84
                  x=visualisation\_config["x"],
                 y=visualisation_config["y"],
86
                 title=visualisation_config["title"],
87
                 logs_dir=logs_dir,
88
89
91
         else:
             print(f"Loading model: {model_name.upper()}")
92
             trained_model = agent.load_model(
93
                 model_name=model_name,
94
                  directory=models_dir,
95
              )
97
         print(f"Evaluating model: {model_name.upper()}")
98
         df_account, df_actions = agent.predict(
99
             model=trained_model,
100
              environment=gym_env,
101
102
103
         model_visualiser.evaluate_testing(
104
             model_name=model_name,
105
106
              account_data=df_account,
107
             actions_data=df_actions,
108
         )
```

backtesting.ipynb demonstrates how to run the benchmark strategies and compare the performance of the trained agents against these benchmarks according to the evaluation metrics.

Listing 25: backtesting.py

```
# Backtesting and benchmarking of the trading strategies
import os
import sys

REPO_ROOT = "/Users/ingridperez/Documents/GitHub Repositories/xdl-portfolio"
sys.path.append(REPO_ROOT)
```

```
import pandas as pd
8
   from agents.drl_agent import DRLAgent
10
   from config import config, config_models
11
    from environments.env_portfolio_optimisation import (
12
        PortfolioOptimisationEnvWrapper,
13
14
    from environments.env_stock_trading import StockTradingEnvWrapper
15
   from pbenchmark.portfolio_benchmark import PortfolioBenchmark
16
    from preprocessor.findata_preprocessor import FinancialDataPreprocessor
17
   from visualiser.benchmark_visualiser import BenchmarkVisualiser
18
19
   USE_CASE = "portfolio-optimisation"
20
21
   data_dir = f"{REPO_ROOT}/{config.DATA_DIR}/{config.DATASET_NAME}"
22
   plot_dir = f"{REPO_ROOT}/{config.PLOT_DIR}/{config.TICKERS_NAME}/{config.DATASET_NAME}/ |
23
    24
   models_dir = f"{REPO_ROOT}/{config.MODELS_DIR}/{USE_CASE}/{config.TICKERS_NAME}/{config.
    → .DATASET_NAME}"
25
   results_dir = (
        f"{REPO_ROOT}/{config.RESULTS_DIR}/{USE_CASE}/{config.DATASET_NAME}"
26
27
28
   if not os.path.exists(plot_dir):
29
        os.makedirs(plot_dir)
30
31
   if not os.path.exists(results_dir):
32
        os.makedirs(results_dir)
33
34
    finpreprocessor = FinancialDataPreprocessor(
35
        start_date=config.START_DATE,
36
        end_date=config.END_DATE,
37
38
    train_data, trade_data = finpreprocessor.load_train_test_data(
39
        directory=data_dir,
40
        filename=config.TICKERS_NAME,
41
42
    )
43
    if USE_CASE == "stock-trading":
44
45
        environment = StockTradingEnvWrapper(
^{46}
            train_data=train_data,
47
            trade_data=trade_data,
            \verb|state_columns=config.ENVIRONMENT_COLUMNS||,
48
49
    elif USE_CASE == "portfolio-optimisation":
50
        environment = PortfolioOptimisationEnvWrapper(
51
            train_data=train_data,
52
53
            trade_data=trade_data,
            state_columns=config.ENVIRONMENT_COLUMNS,
54
55
56
    benchmark = PortfolioBenchmark()
57
   df_account = pd.DataFrame()
59
```

```
perf_stats = dict()
60
61
     for model_name in config_models.MODELS.keys():
62
63
         env_train = environment.get_train_env()
64
         gym_env, _ = environment.get_trade_env()
65
66
         agent = DRLAgent()
67
68
         print(f"Loading model: {model_name.upper()}")
69
         trained_model = agent.load_model(
70
             model_name=model_name,
71
             directory=models_dir,
72
73
74
         print(f"Evaluating model: {model_name.upper()}")
75
         df_account_alg, _ = agent.predict(
76
77
             model=trained_model,
78
             environment=gym_env,
79
80
         df_account_alg["model"] = model_name.upper()
81
82
         df_account = pd.concat([df_account, df_account_alg], ignore_index=True)
83
84
         perf_stats_alg = benchmark.compute_perf_stats(df_account=df_account_alg)
85
86
         perf_stats[model_name.upper()] = perf_stats_alg
87
88
89
     benchmark.set_data(
         train_data=train_data,
90
         trade_data=trade_data,
91
     )
92
93
     for strategy in ["mean", "min", "momentum", "equal"]:
94
         print(f"Optimising portfolio with strategy: {strategy}")
95
96
         try:
             df_account_strat = benchmark.optimise_portfolio(
97
98
                 strategy=strategy, # type: ignore
99
100
             \# Add cumulative returns to the account dataframe
101
             df_account_strat["cumulative_return"] = (
102
                 1 + df_account_strat["daily_return"]
103
             ).cumprod() - 1
104
105
             df_account_strat["model"] = strategy.capitalize()
106
             df_account = pd.concat([df_account, df_account_strat], ignore_index=True) #
107
             \hookrightarrow type: ignore
108
             perf_stats_alg = benchmark.compute_perf_stats(
109
                  df_account=df_account_strat
111
             perf_stats[strategy.capitalize()] = perf_stats_alg
112
```

```
113
         except Exception as e:
             print(
114
                 f"Error occurred while optimising portfolio with strategy {strategy}: {e}"
115
116
117
     if config.INDEX is not None:
118
         df_account_strat = benchmark.get_index_performance(
119
120
             config.TEST_START_DATE, config.TEST_END_DATE, config.INDEX
121
122
         df_account = pd.concat([df_account, df_account_strat], ignore_index=True) # type:
123
         \hookrightarrow ignore
124
         perf_stats_alg = benchmark.compute_perf_stats(df_account=df_account_strat)
125
         perf_stats["Index"] = perf_stats_alg
126
127
     perf_stats = pd.DataFrame(perf_stats)
128
129
     perf_stats.to_csv(
         f"{results_dir}/{config.TICKERS_NAME}_performance_stats.csv",
131
         index=True,
     )
132
133
     benchmark_visualiser = BenchmarkVisualiser(directory=plot_dir)
134
135
136
     benchmark_visualiser.compare_account_value(data=df_account)
137
     benchmark_visualiser.compare_cum_returns(data=df_account)
138
```

hyperparameter_tuning.ipynb demonstrates how to use Weights and Biases to perform hyper-parameter tuning by running a sweep, whose configuration is in config.py and config_models.py.

Listing 26: hyperparameter_tuning.py

```
# Hyper-parameter tuning
1
2
   import os
3
    import sys
4
   REPO_ROOT = "/Users/ingridperez/Documents/GitHub Repositories/xdl-portfolio"
6
    sys.path.append(REPO_ROOT)
7
   from config import config
9
   from optimisation.wandb_opt import WandbOptimisation
10
   from pbenchmark.portfolio_benchmark import PortfolioBenchmark
11
  from preprocessor.findata_preprocessor import FinancialDataPreprocessor
   from visualiser.findata_visualiser import FinancialDataVisualiser
   from visualiser.model_visualiser import ModelVisualiser
14
15
    USE_CASE = "portfolio-optimisation"
```

```
17
    data_dir = f"{REPO_ROOT}/{config.DATA_DIR}/{config.DATASET_NAME}"
19
    plot_dir = (
        f"{REPO_ROOT}/{config.PLOT_DIR}/{config.TICKERS_NAME}/{config.DATASET_NAME}"
20
21
   models_dir = f"{REPO_ROOT}/{config.MODELS_DIR}/{USE_CASE}/{config.TICKERS_NAME}/{config}
22
    → .DATASET_NAME}"
23
    results_dir = (
        f"{REPO_ROOT}/{config.RESULTS_DIR}/{USE_CASE}/{config.DATASET_NAME}"
24
25
    logs_dir = f"{REPO_ROOT}/{config.LOGS_DIR}/{USE_CASE}/{config.TICKERS_NAME}/{config.DAT_
26
    → ASET_NAME}"
27
    if not os.path.exists(plot_dir):
        os.makedirs(plot_dir)
29
30
    if not os.path.exists(results_dir):
31
        os.makedirs(results_dir)
32
33
    finpreprocessor = FinancialDataPreprocessor(
34
        start_date=config.START_DATE,
35
        end_date=config.END_DATE,
36
   )
37
    train_val_data, trade_data = finpreprocessor.load_train_test_data(
38
        directory=data_dir,
39
        filename=config.TICKERS_NAME,
40
    )
41
42
    # Split the training data into training and validation sets
43
    train_data, val_data = finpreprocessor.split_train_test(
44
45
        data=train_val_data,
        test_start_date=config.VAL_START_DATE,
46
47
48
   visualiser = FinancialDataVisualiser(directory=plot_dir)
49
    visualiser.plot_train_val_test_close_prices(
51
        train_data=train_data,
        val_data=val_data,
52
        test_data=trade_data,
53
54
   )
55
    wandb_opt = WandbOptimisation(
56
        entity=config.WANDB_ENTITY,
57
        project=config.WANDB_PROJECT,
58
        train_data=train_data,
59
        val_data=val_data,
60
61
        test_data=trade_data,
62
        state_columns=config.ENVIRONMENT_COLUMNS,
   )
63
64
    model_visualiser = ModelVisualiser(directory=plot_dir)
65
    benchmark = PortfolioBenchmark()
67
   sweep_ids = {}
68
```

```
best_runs = {}
69
70
     perf_stats = {}
71
72
     def perform_model_sweep(model_name: str):
73
74
75
         # Start sweep
         sweep_id = wandb_opt.sweep(
76
              {\tt sweep\_config=config.SWEEP\_CONFIG},
77
             model_name=model_name,
78
79
         sweep_ids[model_name] = sweep_id
80
         # Retrieve best run
82
         run_id, configuration = wandb_opt.get_best_sweep_run(
83
              sweep_id=sweep_id, model_name=model_name
84
85
86
         best_runs[model_name] = (run_id, configuration)
87
88
         # Test the best hyperparameters on the test_set
89
         df_account, df_actions = wandb_opt.test_best_run(
90
             model_name=model_name,
91
92
              configuration=configuration,
93
             train_val_data=train_val_data,
             logs_directory=logs_dir,
94
             models_directory=models_dir,
95
96
         model_visualiser.evaluate_testing(
98
             model_name=model_name,
99
100
              account_data=df_account,
              actions_data=df_actions,
101
102
103
         {\it \# Compute performance statistics}
104
         perf_stats_alg = benchmark.compute_perf_stats(df_account=df_account)
105
         perf_stats[model_name] = perf_stats_alg
106
107
108
     # A2C
109
    model_name = "a2c"
110
    perform_model_sweep(model_name)
111
112
     # PPO
113
    model_name = "ppo"
114
115
     perform_model_sweep(model_name)
116
117
     model_name = "ddpg"
118
119
     perform_model_sweep(model_name)
120
121
    model_name = "td3"
122
    perform_model_sweep(model_name)
123
```

```
124
125 # SAC
126 model_name = "sac"
127 perform_model_sweep(model_name)
```

explainability.ipynb demonstrates how to use the explainability tools (feature importance, LIME and SHAP) to understand the decision-making process of a single model.

Listing 27: explainability.py

```
# Explainability
1
    import os
3
4
    import sys
5
    REPO_ROOT = "/Users/ingridperez/Documents/GitHub Repositories/xdl-portfolio"
6
    sys.path.append(REPO_ROOT)
7
    import numpy as np
9
    import torch
10
11
   from agents.drl_agent import DRLAgent
12
   from config import config
13
   from environments.env_portfolio_optimisation import (
14
        PortfolioOptimisationEnvWrapper,
15
16
   from environments.env_stock_trading import StockTradingEnvWrapper
17
    from explainability.explainability import Explainer
18
19
    from explainability.feature_importance import FeatureImportance
    from explainability.lime_explainability import LimeExplainer
    from explainability.shap_explainability import ShapExplainer
21
    from preprocessor.findata_preprocessor import FinancialDataPreprocessor
22
    from visualiser.shap_visualiser import ShapVisualiser
23
    USE_CASE = "portfolio-optimisation"
25
26
    data_dir = f"{REPO_ROOT}/{config.DATA_DIR}/{config.DATASET_NAME}"
27
   plot_dir = f"{REPO_ROOT}/{config.PLOT_DIR}/{config.TICKERS_NAME}/{config.DATASET_NAME}/ |
28

→ {USE_CASE}"

    models_dir = f"{REPO_ROOT}/{config.MODELS_DIR}/{USE_CASE}/{config.TICKERS_NAME}/{config}
    → .DATASET_NAME}"
    logs_dir = f"{REPO_ROOT}/{config.LOGS_DIR}/{USE_CASE}/{config.TICKERS_NAME}/{config.DAT | 
30

→ ASET_NAME

"

31
    if not os.path.exists(plot_dir):
32
        os.makedirs(plot_dir)
33
34
    finpreprocessor = FinancialDataPreprocessor(
35
        start_date=config.START_DATE,
36
        end_date=config.END_DATE,
37
38
```

```
train_data, trade_data = finpreprocessor.load_train_test_data(
39
40
        directory=data_dir,
        filename=config.TICKERS_NAME,
41
    )
42
43
    if USE_CASE == "stock-trading":
44
        environment = StockTradingEnvWrapper(
45
46
            train_data=train_data,
            trade_data=trade_data,
47
            \verb|state_columns=config.ENVIRONMENT_COLUMNS||,
48
49
    elif USE_CASE == "portfolio-optimisation":
50
        environment = PortfolioOptimisationEnvWrapper(
51
            train_data=train_data,
52
            trade_data=trade_data,
53
            state_columns=config.ENVIRONMENT_COLUMNS,
54
55
    # Load the results of a DRL agent
57
    model_name = "a2c"
58
59
    env_train = environment.get_train_env()
60
    gym_env, _ = environment.get_trade_env()
61
62
    agent = DRLAgent()
63
64
    model = agent.get_model(
65
        model_name=model_name,
66
        environment=env_train,
67
68
        directory=logs_dir,
        use_case=USE_CASE,
69
    )
70
71
72
    print(f"Loading model: {model_name.upper()}")
    trained_model = agent.load_model(
74
        model_name=model_name,
        directory=models_dir,
75
76
77
78
    policy = trained_model.policy
79
    print(f"Evaluating model: {model_name.upper()}")
80
    df_account, _ = agent.predict(
81
        model=trained_model,
82
        environment=gym_env,
83
84
    )
85
    print(f"Evaluating model: {model_name.upper()}")
86
    df_account, df_actions = agent.predict(trained_model, gym_env)
87
88
89
    # Set up the explainer
    explainability = Explainer()
90
91
    state_space = explainability.build_state_space(
92
        data=trade_data,
93
```

```
columns=config.ENVIRONMENT_COLUMNS,
94
     )
95
96
     action_space = explainability.build_action_space(data=df_actions)
97
98
     X_train, X_test, y_train, y_test = explainability.split_data(
99
         state_space=state_space,
100
101
         action_space=action_space,
     )
102
103
     ## Build Random Forest model to be used for Proxy explanations
104
    rf_model = explainability.build_proxy_explanation_model(
105
         X_train=X_train,
106
107
         y_train=y_train,
         {\tt find\_best\_params=False,}
108
    )
109
110
111
     ## Prediction function for the policy
112
     def predict(states: list) -> np.ndarray:
113
114
         Predict the action for a given state using the policy.
115
116
117
         with torch.no_grad():
             states_tensor = torch.tensor(states, dtype=torch.float32)
118
119
             action, _ = policy.predict(
                 states_tensor.reshape(
120
                      -1, environment.state_space, environment.stock_dim
121
                 ).numpy()
122
             )
123
             return action
124
125
126
127
     # Feature Importance
128
129
     ## Proxy Feature Importance
    feature_imp = FeatureImportance(
130
         model=rf_model,
131
132
         columns=X_train.columns.to_list(),
133
         directory=plot_dir,
134
         model_name=model_name,
     )
135
     feature_importances = feature_imp.get_feature_importances()
136
137
     feature_imp.plot_feature_importances()
138
139
140
     feature_imp.plot_feature_importances_by_ticker()
141
     feature_imp.plot_feature_importance_comparison(statistic="mean")
142
143
144
     feature_imp.plot_feature_importance_by_indicator()
145
     feature_imp.plot_top_features_per_ticker()
146
147
     feature_imp.plot_top_features_per_indicator()
148
```

```
149
     feature_imp.plot_mean_importance_by_ticker()
150
151
     feature_imp.plot_mean_importance_by_indicator()
152
153
154
     lime_explainer = LimeExplainer(directory=plot_dir, model_name=model_name)
155
156
     explainer = lime_explainer.build_lime_explainer(X_train=X_train)
157
     ## Proxy LIME
158
     lime_explainer.explain_portfolio(
159
         instance=X_test.iloc[0],
160
         columns=action_space.columns.values.tolist(),
161
         predict_fn=rf_model.predict,
162
         filename="proxy",
163
     )
164
165
     ## DRL Lime
166
167
     lime_explainer.explain_portfolio(
168
         instance=X_test.iloc[0],
169
         columns=action_space.columns.values.tolist(),
170
         predict_fn=predict,
171
172
         filename="direct",
173
     )
174
175
     shap_explainer = ShapExplainer()
176
177
     ## Proxy SHAP
178
     explainer = shap_explainer.build_proxy_explainer(model=rf_model)
179
180
     shap_values = shap_explainer.compute_shap_values(
181
182
         explainer=explainer,
183
         X_{\text{test}} = X_{\text{test}},
184
     )
185
     shap_interaction_values = shap_explainer.compute_shap_interaction_values(
186
187
         explainer=explainer,
188
         X_{\text{test}} = X_{\text{test}},
     )
189
190
     shap_visualiser = ShapVisualiser(
191
         shap_values=shap_values,
192
         action_space=action_space,
193
194
         X_test=X_test,
         \verb|shap_interaction_values=| \verb|shap_interaction_values|, \\
195
         directory=plot_dir,
196
         filename="proxy",
197
         model_name=model_name,
198
     )
199
200
     index = 0
201
     shap_visualiser.beeswarm_plot(index=index)
202
203
```

```
shap_visualiser.force_plot(index=index)
204
205
206
     shap_visualiser.force_plot_single_obs(
207
          index=index,
208
          obs=obs,
209
210
     )
211
     shap_visualiser.waterfall_plot_single_obs(
212
          index=index,
213
          obs=obs,
214
215
     )
216
     shap_visualiser.heatmap(
217
          index=index,
218
219
220
     shap_visualiser.interaction_plot(
221
222
          index=index,
223
224
     ## Kernel SHAP
225
     explainer = shap_explainer.build_kernel_explainer(
226
227
         predict_fn=predict,
          X_train=X_train,
228
     )
229
230
     shap_values = shap_explainer.compute_shap_values(
231
232
          explainer=explainer,
          X_{\text{test}} = X_{\text{test}},
233
     )
234
235
     shap_visualiser = ShapVisualiser(
236
237
          shap_values=shap_values,
238
          action_space=action_space,
239
          X_{\text{test}} = X_{\text{test}},
          shap_interaction_values=shap_interaction_values,
240
          directory=plot_dir,
241
242
          filename="direct",
243
          model_name=model_name,
     )
244
245
     index = 0
246
     shap_visualiser.beeswarm_plot(index=index)
247
248
249
     shap_visualiser.force_plot(index=index)
250
     obs = 0
251
     shap_visualiser.force_plot_single_obs(
252
          index=index,
253
254
          obs=obs,
     )
255
256
     shap_visualiser.force_plot_assets(obs=obs)
257
258
```

```
shap_visualiser.waterfall_plot_single_obs(
index=index,
obs=obs,
)

shap_visualiser.heatmap(index=index)
```