

* 10/17. Assignment 3.

1. Show that, for the MA(1) process $Y_t = \epsilon_t - \theta \epsilon_{t-1}$, the autocorrelation function does not change when θ is replaced by $1/\theta$.

We've seen that, for MA(1) process:

$$\rho_k = 0 \text{ for } k > 1. \quad (\text{doesn't matter } \theta)$$

$$\rho_1 = \frac{-\theta}{1-\theta^2}$$

replace θ with $\frac{1}{\theta}$

$$\frac{\frac{1}{\theta}}{1-\frac{1}{\theta^2}} = \frac{\frac{-1/\theta}{\theta^2-1}}{\frac{\theta^2-1}{\theta^2}} = \frac{-\theta}{\theta^2-1}$$

\therefore autocorrelation doesn't change.