



# Temporal Aggregation Using a Multidimensional Index

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## ABSTRACT

*We present a new method for computing temporal aggregation that uses a multidimensional index. The novelty of our method lies in mapping the start time and end time of a temporal tuple to a data point in a two-dimensional space, which is stored in a two-dimensional index, and in calculating the temporal aggregates through a temporal join between the data in the index and the base intervals (defined as the intervals delimited by the start times or end times of the tuples). To enhance the performance, this method calculates the aggregates by incrementally modifying the aggregates from that of the previous base interval without re-reading all tuples for the current base interval. We have compared our method with the SB-tree, which is the state-of-the-art method for temporal aggregation. The results show that our method is an order of magnitude more efficient than the SB-tree method in an environment with frequent updates, while comparable in a read-only environment as the number of aggregates calculated in a query increases.*

*Keywords:* multidimensional index; temporal aggregation

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## INTRODUCTION

Temporal aggregation is an operation for finding the aggregate value of an attribute over a certain period of time. Specifically, it finds the time intervals in which the aggregate value does not change, namely the constant intervals (Kline & Snodgrass, 1995), and performs the aggregation at each constant interval. Typically, there are two kinds of aggregate functions: cumulative

(e.g., COUNT, SUM, AVG) and selective (e.g., MIN, MAX).

There have been several temporal aggregation methods proposed to date. The early ones included the linked list method by Tuma (1992) and the aggregation tree method by Kline and Snodgrass (1995) and its variants (Gendrano, Huang, Rodrigue, Moon, & Snodgrass, 1999; Kim, Kang, & Kim, 1999; Moon, Lopez, & Immanuel,

2000; Ye & Keane, 1997). Although these methods do facilitate computing temporal aggregates, they require the data structures to reside in main memory. The data structures, however, are typically much larger than the available main memory because a temporal database retains all tuples from the past. Moreover, they require one data structure for each aggregate function.

Recently, Yang and Widom (2003) proposed a method using the SB-tree. This method is similar to the aggregation tree method, but uses a *disk-resident* data structure. (It, however, still requires one data structure for each aggregate function.) In this method, every time a new tuple is inserted or an existing tuple is updated or deleted, the temporal aggregates are updated *immediately* using the SB-tree. Then, queries are executed quickly by simply reading the precomputed aggregate values. However, the overhead of immediate updates is nontrivial, particularly because the update is done for each aggregate function through a separate SB-tree. Thus, this method is not suitable in an environment with frequent insertions, deletions, or updates (collectively called updates from now on) of tuples and relatively less frequent aggregation queries.

Many temporal database applications, however, are update intensive. Examples include financial applications handling stock market data and reservation systems for airlines, hotels, trains, and so forth. For these applications, there are very frequent updates and only a limited number of temporal aggregation queries. Thus, the ratio between updates and aggregation queries in these cases could be in the order of thousands.

In this article, we propose a new method that resolves the problems of the existing methods for update-intensive ap-

plications, while accomplishing reasonably efficient temporal aggregation. Like the SB-tree method, our method uses a disk-resident data structure that is applicable to a large temporal database. The novelty of the method lies in mapping the start time and the end time of a temporal tuple to a data point in a two-dimensional space and storing the data point through a multidimensional index. (In this regard, we call this method the *multidimensional index (MD-index) method* (Trujillo, Luján-Mora, & Song, 2004).) An update operation incurs only a small overhead of inserting a tuple through the index. For an aggregation query operation, aggregates are computed through a temporal join between the data in the index and the *base intervals* (to be defined in the Temporal Aggregation Using a Multidimensional Index section), constituting constant intervals. For efficiency's sake, this calculation is done by incrementally modifying the aggregate from that of the previous base interval without re-reading all tuples for the current base interval.

Compared with the SB-tree method, our method (1) incurs little overhead when updating tuples and, thus, is more efficient for update operations; and (2) uses only one index structure for *all* aggregate functions and, consequently, achieves increasingly comparable aggregation query performance (through incremental calculations) as the number of aggregates in the query increases.

In this article, “time” may be interpreted as any of the valid time, transaction time, and user-defined time, but we do not consider more than one of them at the same time. In other words, we do not consider bitemporal databases (Jensen et al., 1998). Moreover, the semantics of time is point-based atelic<sup>1</sup>. This means that a tuple value is true at any point within a given

time interval, not as a result of achieving a certain goal during the interval.

Experimental results show that our method is an order of magnitude more efficient than the SB-tree method for update operations, and the gap becomes wider as more aggregate functions (e.g., COUNT, SUM, AVG, MIN, MAX) are supported by the system. The results also show that multiaggregation query performance approaches that of the SB-tree method as the number of the aggregate functions increases, becoming comparable to that of the SB-tree, when the query specifies all five aggregate functions (i.e., COUNT, SUM, AVG, MIN, MAX).

Following the Introduction, we provide some background information, followed by a discussion of related work. The Temporal Aggregation Using a Multidimensional Index section elaborates on the proposed MD-index method. The Performance Evaluation section compares the performance between the MD-index

method and the SB-tree method, then we provide a conclusion for the article.

## BACKGROUND

### Temporal Aggregation

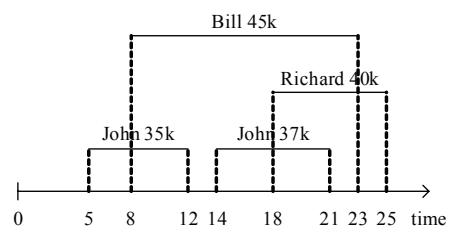
Each tuple in a temporal relation has an associated time interval (Kline & Snodgrass, 1995). Figure 1a shows an example of a temporal relation E\_SALARY, which stores the salary history of employees. The attribute *Time Interval* defines [*Start time*, *End time*) of tuples as shown Figure 1b<sup>2</sup>. Figure 2 shows the COUNT and MIN of *Salary* changing over time. Note that each aggregate function generates different constant intervals.

### MBR-MLGF

We use the multilevel grid file (MLGF) (Whang & Krishnamurthy, 1991) as the multidimensional index<sup>3</sup>. It is a multilevel extension of a grid file and is similar to the K-D-B-tree (Robinson, 1981)—a disk ver-

Figure 1. An example of a temporal relation

Name	Salary	Time Interval
Richard	40k	[18, 25)
John	37k	[14, 21)
John	35k	[5, 12)
Bill	45k	[8, 23)



a) Table E\_SALARY.

b) Time intervals of tuples in E\_SALARY.

sion of the K-D tree—but using hashing. Specifically, it is a dynamic hash file supporting multikey accesses to data through a multilevel directory tree structure.

An MLGF is made of a balanced tree consisting of a multilevel directory and data pages. Each directory level reflects the space partitioning, and each directory entry consists of a region vector and a pointer to either a data page or a lower-level directory page. A region vector in an  $n$ -dimensional MLGF consists of  $n$ -hash values that uniquely identify the region, including its position, shape, and size. The  $i$ -th hash value is the common prefix of the hash values for the  $i$ -th attribute of all records in the region. A region for a higher-level directory entry contains all regions in the subtree, rooted by the page and pointed by the entry.

Figure 3 illustrates a two-level MLGF with two keys,  $k_1$  and  $k_2$ . Figure 3a shows the directory structure, where the two levels are denoted by  $D_1$  and  $D_2$ . Figure 3b and

Figure 3c show the regions represented by  $D_1$  and  $D_2$ , respectively. Here, each region corresponds to a disk page. There are 11 entries in  $D_1$ , one for each of the 11 regions A through K, and four entries in  $D_2$ , one for each of the  $D_1$  regions a through d. For example, the region vector  $\langle 01, 1 \rangle$  of the directory entry in  $D_2$  represents the region c, in which the two key values are prefixed with 01 and 1, respectively. This region is in turn split into the regions F, G, and H by  $D_1$ , each identified with the directory entry with the region vector  $\langle 010, 10 \rangle$ ,  $\langle 011, 10 \rangle$ , or  $\langle 01, 11 \rangle$ . In the MBR-MLGF, each directory entry maintains information about the minimum bounding regions of objects (without additional storage overhead). For example, Figure 4 shows the region  $R_1$  in a rectangle and the objects in it as points. The vertical line at  $\min-t_s$  and horizontal line at  $\max-t_e$  reduces  $R_1$  to its MBR.

We particularly use the MBR-MLGF (minimum-bounding-region MLGF) (Song, Shang, Lee, Lee, & Kim, 1999),

Figure 2. Temporal aggregates COUNT and MIN on E\_SALARY.Salary

Constant Interval	COUNT
[5, 8)	1
[8, 12)	2
[12, 14)	1
[14, 18)	2
[18, 21)	3
[21, 23)	2
[23, 25)	1

Constant Interval	MIN
[5, 12)	35k
[12, 14)	45k
[14, 21)	37k
[21, 25)	40k

a) COUNT

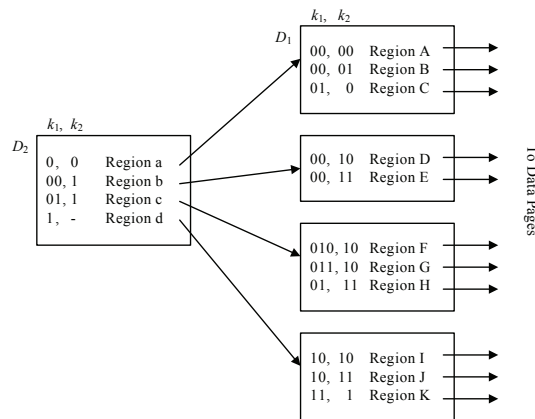
b) MIN

which is an extension of the MLGF targeted toward efficient spatiotemporal data accesses. In the MBR-MLGF, each directory entry maintains information about the minimum bounding regions of objects (without additional storage overhead). For example, Figure 4 shows the region  $R_1$  in a rectangle and the objects in it as points. The vertical line at  $\min-t_s$  and the horizontal line at  $\max-t_e$  reduces  $R_1$  to its MBR.

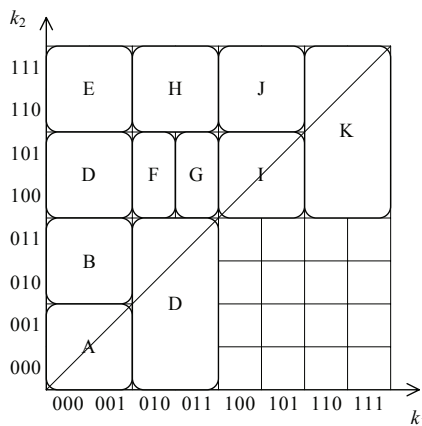
## RELATED WORK

The first proposal for computing temporal aggregates has been made by Tuma (1992). It was based on an extension to the nontemporal aggregate computation algorithm by Epstein (1979). The approach consists of two steps, each requiring one scan of the base table. The first step partitions the time line into constant intervals. The second step considers each tuple  $t$  in the

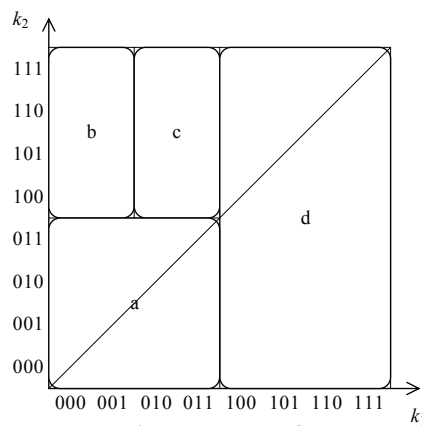
Figure 3. An example of an MLGF



a) A two-level directory structure



b) Regions in D1



c) Regions in D2

base table in turn, updating the aggregate values for all resultant tuples, covered by the tuple  $t$ 's valid interval. This method takes  $O(mn)$  time to compute temporal aggregates, where  $n$  is the size of the base table and  $m$  is the number of result tuples. This method builds a linked list which resides in main memory to represent constant intervals that are generated in the first step and used in the second step.

Kline and Snodgrass (1995) proposed the aggregation tree based on the binary segment-tree (Preparata & Shamos, 1985). This segment-tree feature allows efficient processing of tuples with long intervals. The tree structure, however, is unbalanced. In the worst case, it takes  $O(n^2)$  to compute a temporal aggregate from a table with  $n$  tuples. There has been balanced aggregation trees (Kim et al., 1999; Moon et al., 2000) proposed so that the worst-case run time is  $O(n \log m)$ , where  $m$  is the number of the constant interval. There have been parallel versions of the aggregation-trees (Ye & Keane, 1997; Gendrano et al., 1999), but

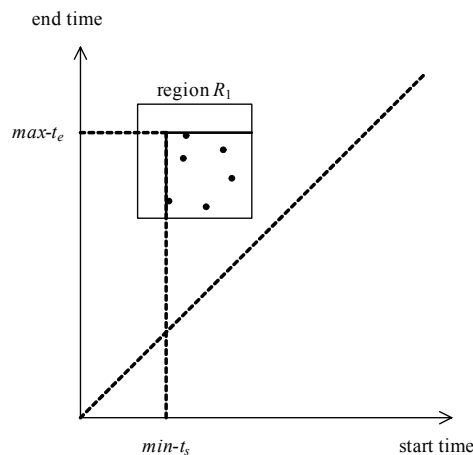
they all inherit the same limitations of the original (i.e., nonparallel) versions.

One major drawback of the methods described so far is that they use main-memory resident data structures. It limits the applicability of the methods to a temporal database that is often too large to fit in main memory.

Yang and Widom (2003) proposed the SB-tree based on the segment-tree (Preparata & Shamos, 1985) and the B-tree. Although similar to the aggregation tree in terms of storing a time interval and a value in each node, the SB-tree is different for storing multiple time intervals in each node. More importantly, the SB-tree is a disk-resident data structure.

Figure 5 shows an example SB-tree for COUNT. Each node of the SB-tree consists of key-value pairs. Each key is the start time of a constant interval. Note that the end time of one interval is the same as the start time of the next interval. Each value is the value for the constant interval. For example, in Figure 5a, the node B contains

Figure 4. Minimum bounding region in an MBR-MLGF



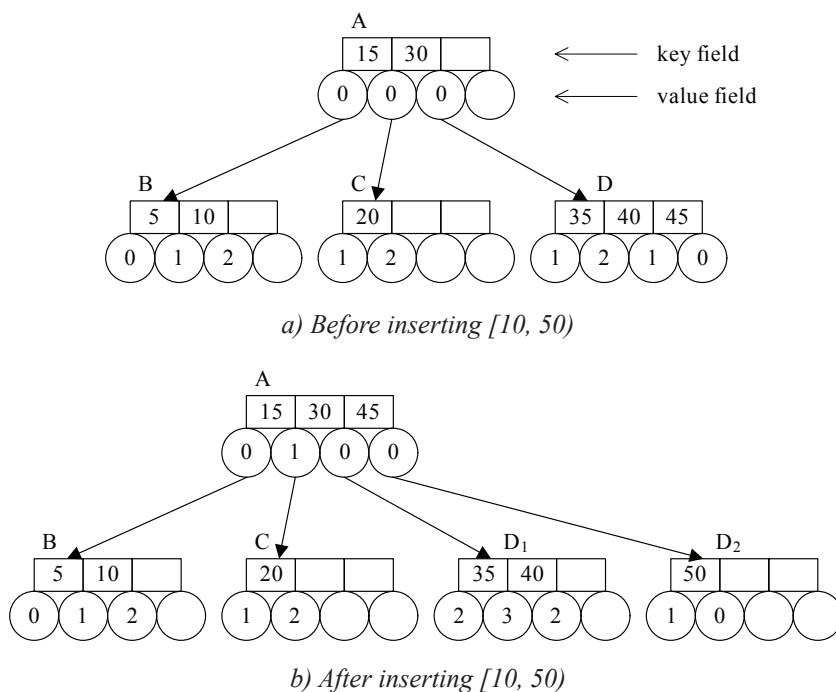
three constant intervals  $[0, 5)$ ,  $[5, 10)$  and  $[10, 15)$ , and the values of COUNT are 0 in  $[0, 5)$ , 1 in  $[5, 10)$  and 2 in  $[10, 15)$ .

A key insertion of SB-tree is handled as in the B-tree, and a value-update is done to a node at the highest possible level. For example, let us assume we insert a tuple with the time interval  $[10, 50)$  and, as a result, two keys 10 and 50 are inserted into the SB-tree shown in Figure 5a. Since the key 10 already exists, only 50 is inserted. This insertion causes the node D to overflow. Then, (as in the B-tree) the node D is split into the nodes  $D_1$  and  $D_2$  as shown in Figure 5b, and the keys are redistributed to the two new nodes while the center value 45 is moved to the parent. Besides, 1 is added to the values in all nodes whose keys lie within the interval  $[10, 50)$ . Note in Figure

5b that 1 is added to the second value in the parent node A instead of the first and the second values in the node C, since the entire interval  $[15, 30)$  is included in the interval  $[10, 50)$ . Figure 6 shows how the SB-tree is constructed as the tuples in Figure 1a are inserted.

All the methods described in this section share a common disadvantage and advantage. The disadvantage is that they require one data structure for each aggregate function. The advantage is that, when an aggregation query is issued, they have only to retrieve the up-to-date aggregate values in the data structures immediately (with an exception of the linked list method (Tuma, 1992)). As mentioned in the Introduction, our MD-index method has the opposite disadvantage and advantage. That is, it

Figure 5. An example of the SB-tree for COUNT



requires only one data structure for all aggregate functions, and computes the aggregate values at query time.

## TEMPORAL AGGREGATION USING A MULTI-DIMENSIONAL INDEX

As mentioned in the Introduction, we represent temporal tuples as points in a two-dimensional (2-D) space defined by the start time and end time of the tuples. This

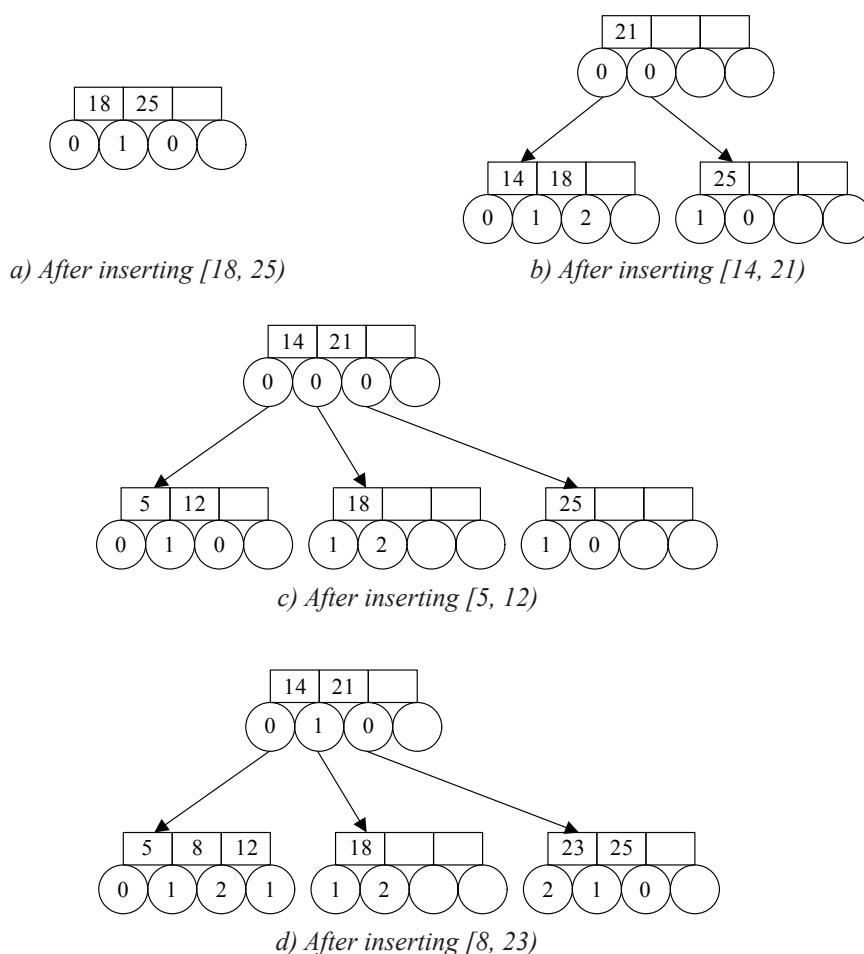
mapping enables the proposed MD-index method. Based on this concept, we define the temporal join window and present the aggregation algorithms.

### Temporal Join Windows

We first define the base interval as follows.

*Definition 1* (base intervals): Given temporal tuples, their base intervals are the

Figure 6. An example of the SB-tree construction





time intervals delimited by the start times or end times of all tuples.

For a given aggregate function, if we merge all adjacent base intervals with the same aggregate values, then the merged intervals compose one constant interval (Kline & Snodgrass, 1995) for the aggregate function. Base intervals are maintained by storing the start time and end time of each tuple in a separate B+-tree.

As the time interval of a tuple can be mapped to a 2-D point, so can the base interval be. Tuples thus mapped to 2-D points can be stored and retrieved through a 2-D index. Figure 7a shows the time intervals of four tuples and six base intervals of COUNT, and Figure 7b shows the 2-D points mapped from these intervals.

**Definition 2** (temporal join window of a base interval): In a 2-D space representing all possible temporal tuples,

we define the temporal join window (TJW) of a base interval  $B_i$  ( $TJW(B_i)$ ) as the 2-D region containing all tuples whose time intervals overlap  $B_i$ . That is, given  $B_i \equiv [s_i, e_i]$ ,

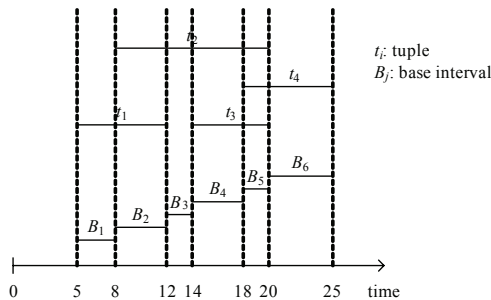
$$TJW(B_i) = \{ \langle t_s, t_e \rangle \mid t_s \leq s_i \text{ and } t_e \geq e_i \}$$

For example, in Figure 7b,  $TJW(B_4)$  contains the tuples  $t_2$  and  $t_3$ , and the tuple  $t_2$  belongs to  $TJW(B_2)$ ,  $TJW(B_3)$ ,  $TJW(B_4)$ , and  $TJW(B_5)$ . Note that the tuples' points are located only at the grid points formed by the TJWs because, by definition, there cannot be the start time or end time of any tuple within a base interval.

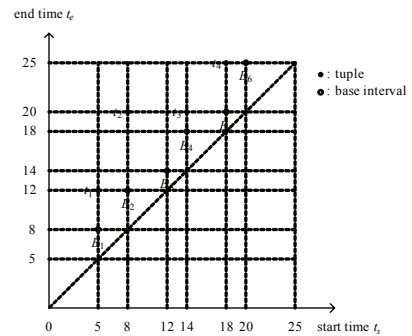
### Temporal Aggregation Algorithms

Temporal aggregate for each base interval,  $B_i$ , is obtained by aggregating tuples overlapping  $B_i$ , that is, tuples in  $TJW(B_i)$ . As we can see from Figure 8, aggregating tuples in the order of  $B_{i-1}, B_i, B_{i+1}$  allows

Figure 7. Tuples and base intervals



a) Intervals in the 1-D time



b) Points in the 2-D space

reusing tuples from the previous TJW. We now present the algorithms for computing aggregates in the order of base intervals. (It may well be done in the reverse order.)

The algorithm differs between cumulative aggregation and selective aggregation. Let us first consider the cumulative one using COUNT as an example. (SUM is obtained in the same way as COUNT, and AVG is obtained as SUM divided by COUNT.) In Figure 8, COUNT of tuples in  $TJW(B_i)$  is obtained from the COUNT of tuples in  $TJW(B_{i-1})$  by adding the COUNT of tuples in the region C+E and subtracting the COUNT of tuples in A.

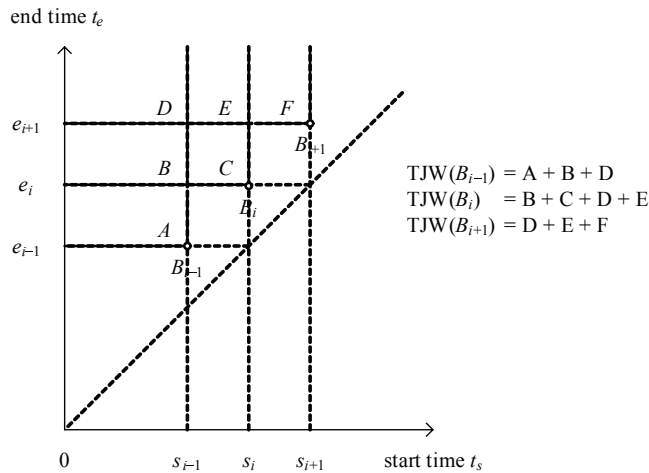
Because tuples' points are located only at the grid points formed by the TJWs, all tuples in the region A have the end time  $e_{i-1}$  and all tuples in the region C have the start time  $s_i$ . Let  $N_s(s_i)$  be the number of tuples with the start time  $s_i$  and  $N_e(e_{i-1})$  be the number of tuples with the end time  $e_{i-1}$ . Then,  $COUNT(B_i)$ , the value of COUNT in the base interval  $B_i$ , is obtained as

$$\begin{aligned} COUNT(B_i) &= \\ COUNT(B_{i-1}) - N_e(e_{i-1}) + N_s(s_i) \end{aligned} \quad (1)$$

Now, let us consider the selective aggregation with MIN as an example. MAX is symmetric to MIN and, therefore, is obtained in the same way as MIN. When calculating MIN in  $B_i$  after  $B_{i-1}$ , there are two cases depending on the MIN of the tuples in A. In case the MIN in  $B_{i-1}$  is different from the MIN in A, the tuple with the minimum value must be in B+D and, therefore, the MIN in  $B_i$  is the smaller of MIN in B+D (= MIN in  $B_{i-1}$ ) and that in C+E. In case the MIN in  $B_{i-1}$  and the MIN in A are the same, the tuple with the minimum value must be in A and, therefore, the MIN in  $B_i$  is the smaller between the MIN of tuples in A and that in C+E.

Let  $M_s(s_i)$  be the minimum value of the tuples with the start time  $s_i$  and  $M_e(e_{i-1})$  be the minimum value of the tuples with the end time  $e_{i-1}$ . Then,  $MIN(B_i)$ , the value of MIN

Figure 8. TJWs of three consecutive base intervals



in the base interval  $B_i$ , is obtained as

$$\begin{aligned} \text{MIN}(B_i) = & \\ & \begin{cases} \text{LESSER}(\text{MIN}(B_{i-1}), M_s(s_i)), & \text{if } \text{MIN}(B_{i-1}) \neq M_e(e_{i-1}) \\ \text{LESSER}(M_e(e_{i-1}), M_s(s_i)), & \text{otherwise} \end{cases} \end{aligned} \quad (2)$$

where the function LESSER returns the smaller of the two arguments.

Figure 9 outlines the algorithms for calculating COUNT and MIN based on Equations (1) and (2) given a series of base intervals. The aggregate for the first base interval is computed in line 1 of each

algorithm. Then, the aggregates for the rest of the base intervals are calculated incrementally in lines 2-15 and 2-17, respectively. It outputs one aggregate value per constant interval, resulting from merging adjacent base intervals in lines 7-11 lines 9-13, respectively.

## PERFORMANCE EVALUATION

We have conducted experiments to compare the performance with that of the SB-tree method. We describe the experimental setup and present the results in this section.

Figure 9. COUNT and MIN aggregation algorithms

### Algorithm Aggregate\_COUNT

Input: A series of base intervals  $B_i = [s_i, e_i]$ ,  $i=1,2,\dots,n$

Ouput: COUNT aggregate values for each constant interval C

begin

```

1:  prev_count := the number of tuples with the start time  $\leq s_1$  and the end time  $\geq e_1$ ;
2:   $s := B_1$ 's start time  $s_1$ ;
3:   $N_e :=$  the number of tuples with the end time  $= e_1$ ;
4:  for  $i := 2$  to  $n$  {
5:     $N_s :=$  the number of tuples with the start time  $= s_i$ ;
6:    count := prev_count -  $N_e$  +  $N_s$ ;
    /* if (count == prev_count) then merge the base intervals to a constant interval */
    /* else output the result: */
7:    if count != prev_count {
8:      output  $\langle [s, e_{i-1}), \text{prev\_count} \rangle$ ;
9:       $s := B_i$ 's start time  $s_i$ ;
10:   }
11:    $e := B_i$ 's end time  $e_i$ ;
12:    $N_e :=$  the number of tuples with the end time  $= e_i$ ;
13:   prev_count := count;
14: }
15: output  $\langle [s, e_n), \text{count} \rangle$ ;
end;
```

a) Aggregate\_COUNT

## Experiment Setup

We use two synthetic datasets (DS1, DS2) generated in a manner similar to the data used by Kline and Snodgrass (1995) and Moon et al. (2000). There are four temporal relations. Each tuple has four attributes: name (4 bytes), salary (4 bytes), start time (4 bytes), and end time (4 bytes). The relation sizes are 1, 4, 16, and 64 Mbytes, each of which contains 65,536, 262,144, 1,048,576, and 4,194,304 tuples.

The tuples in DS1 are uniformly distributed with respect to time. Their start time is selected randomly between 1 and the following time range (inclusive): 1 million for the 1 Mbyte relation, 4 million for the 4 Mbyte relation, and so forth. (Note that we use an integer for the time stamp.)

The end time is selected randomly between the start time + 1 and the start time + 30% of the time range. The tuples in DS2 are normally distributed, thus skewed, with respect to time. The mean and the standard deviation are 1/4 and 1/8 of the time range for the start time, and 3/4 and 1/8 of the time range for the end time.

After inserting tuples in a 1 Mbyte relation, for example, the size of the MD-index is 3.2 Mbytes, and the size of SB-tree is 2.4 Mbytes for SUM, 2.3 Mbytes for COUNT, 2.4 Mbytes for AVG, 0.8 Mbytes for MIN, and 0.8 Mbytes for MAX. The size of the SB-tree varies significantly between cumulative and selective aggregate functions. Considering a 16 Mbyte relation as another example, the SUM SB-tree is

Figure 9. continued

### Algorithm Aggregate\_MIN

Input: A series of base intervals  $B_i = [s_i, e_i], i=1,2,\dots,n$

Output: MIN aggregate values for  $B_i, i=1,2,\dots,n$

begin

```

1: prev_min := the minimum value of the tuples with the start time  $\leq s_1$  and the end time  $\geq e_1$ ;
2:  $s := B_1$ 's start time  $s_1$ ;
3:  $M_e :=$  the minimum value of the tuples with the end time  $e_1$ ;
4: for  $i := 2$  to  $n$  {
5:    $M_s :=$  the minimum value of the tuples with the start time  $s_i$ ;
6:   if (prev_min  $\neq M_e$ )
7:     then min := lesser(prev_min,  $M_s$ );
8:   else min := lesser( $M_e$ ,  $M_s$ );
9:   /* if (min == prev_min) then merge the base intervals to a constant interval */
10:  /* else output the result: */
11:  if min  $\neq$  prev_min {
12:    output  $\langle [s, e_{i-1}], \text{prev\_min} \rangle$ ;
13:     $s := B_i$ 's start time  $s_i$ ;
14:  }
15:   $e := B_i$ 's end time  $e_i$ ;
16:   $M_e :=$  the minimum value of the tuples with the end time  $e_i$ ;
17:  prev_min := min;
18: }
19: output  $\langle [s, e_n], \text{min} \rangle$ ;
20: end;
```

b) Aggregate\_MIN.

approximately 11 Mbytes, while the MIN SB-tree is only 12 Kbytes. This is because MIN typically generates a smaller number of constant intervals (see Figure 3).

We measure the update performance by inserting new tuples amounting to 0.1% of the existing tuples into the datasets DS1 and DS2. The ratio of 0.1% is sufficient for our purpose because, evidently, the performance gap between the MD-index method and the SB-tree method would increase as more tuples are inserted. The maintenance cost of base intervals in the B+-tree is also

included in the update cost. The tuples have been inserted in a batch but without any optimization taking advantage of the batch processing, so the result would not differ much from that of inserting tuples in increments.

The performance metrics are the elapsed time and the number of disk page accesses. The elapsed time is the total execution time measured in a single-user environment. We consider only the five standard aggregate functions (i.e., SUM, COUNT, AVG, MIN, MAX). In order to avoid noise,

Figure 10. Update performance with respect to relation size using DS1

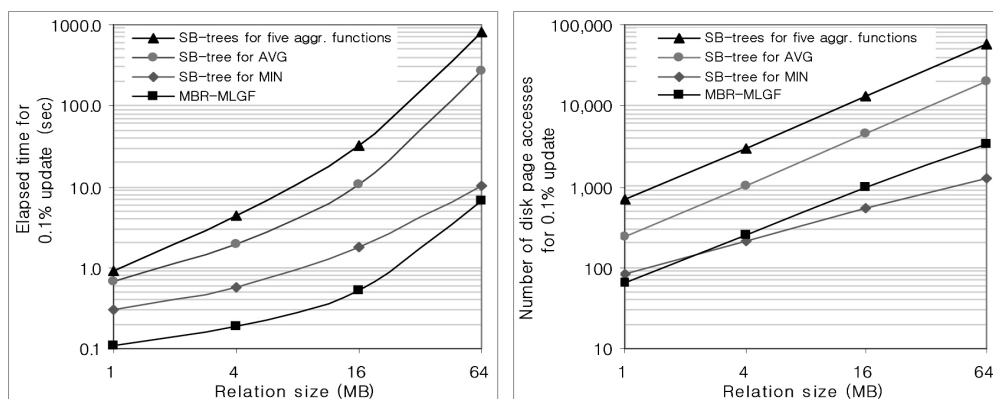
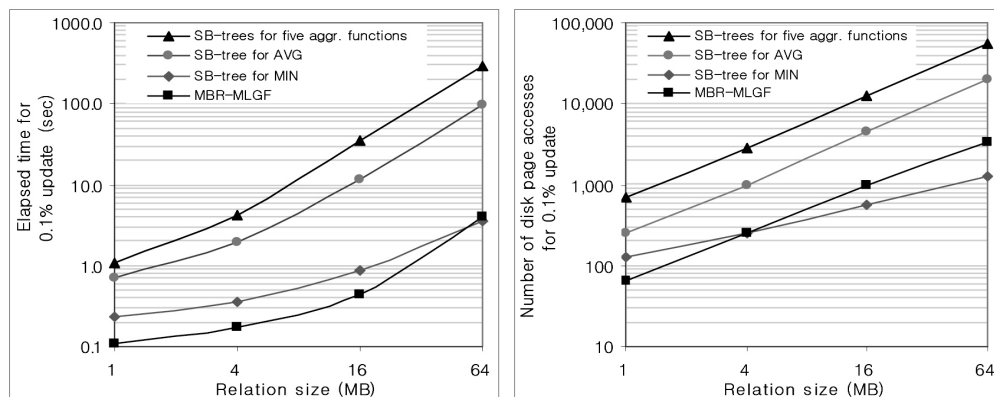


Figure 11. Update performance with respect to relation size using DS2



we execute each function more than three times and calculate an average.

The system is configured in Linux server with 1.0 Gbyte RAM and ATA-4 IDE hard disk drive, and it uses direct I/O to eliminate the unpredictable effect of operating system buffering. The page size is 4 Kbytes for both disk pages and buffer pages.

## Experiment Results

Experimental performance results of update operations and aggregation query

operations are presented in this subsection.

### Update Performance

Figures 10 and 11 compare the update performances of our MD-index method and the SB-tree method, using the dataset DS1 and the dataset DS2, respectively. Each figure shows two cases for the SB-tree method: the five aggregate functions together and each aggregate function separately. In the latter case, we show the results for only AVG and MIN because the results for

Figure 12. Temporal aggregation query performance with respect to relation size using DS1

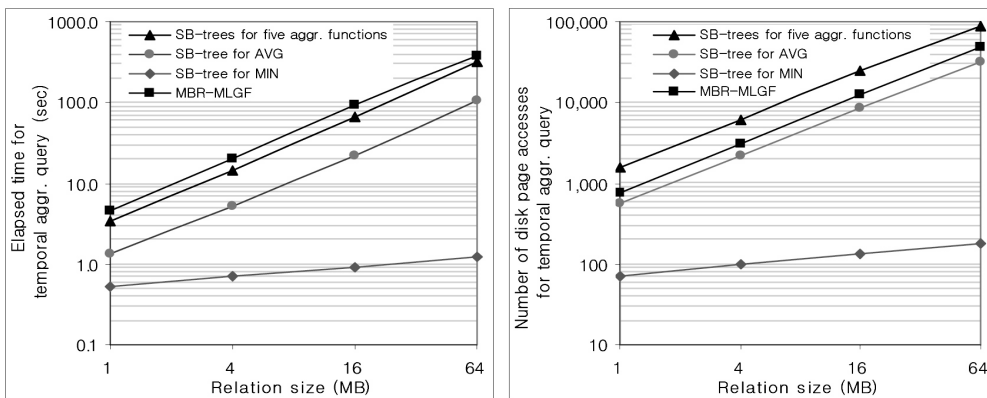
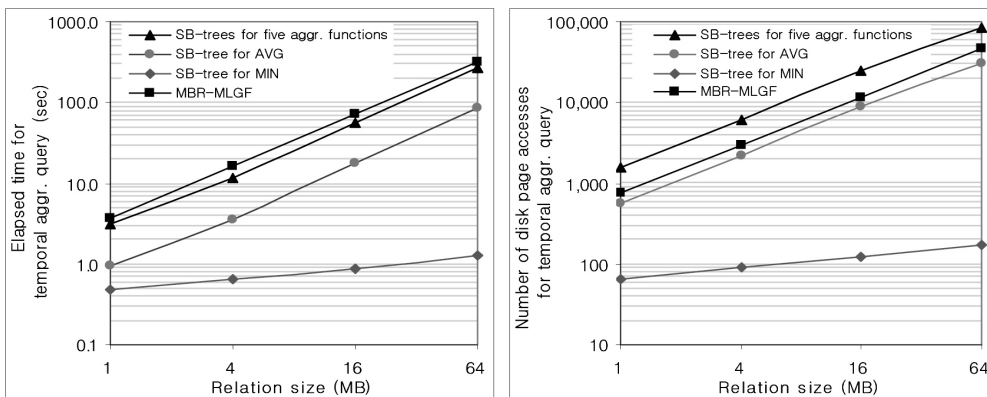


Figure 13. Temporal aggregation query performance with respect to relation size using DS2



SUM and COUNT are very close to that for AVG, and the result for MAX is very close to that for MIN.

As mentioned in the Introduction, the SB-tree method requires one SB-tree for each aggregate function, whereas our method uses one MD-index for all. Therefore, each update operation incurs updating five SB-trees in the SB-tree method, whereas it incurs updating one MBR-MLGF in the MD-index method. Figures 10 and 11 show that the MD-index method performs far better (by one to two orders of magnitude) than the SB-tree method when all the five aggregate functions are considered.

The two figures also show that the update performance of the SB-tree method is much better for MIN than AVG. While the AVG performance is much poorer than that of the MD-index method by an order of magnitude, the MIN performance is comparable. Moreover, the update costs of MIN SB-tree increases slower than those of the other three. The reason is the size of the MIN SB-tree, which is much smaller than the AVG SB-tree or the MD-index.

#### *Aggregation Query Performance*

Figures 12 and 13 compare the aggregation query performance of our MD-index method and the SB-tree method using the dataset DS1 and dataset DS2, respectively. Here, each figure also shows two cases for the SB-tree method: the five aggregate functions together and each aggregate function separately.

The two figures show that the aggregation query performance of the MD-index method is worse than that of the SB-tree method for a single aggregate function. This is as expected. We also see that the gap is larger for the MIN aggregate function due to the smaller size of the MIN SB-tree. Oftentimes, multiple aggregate functions

appear in the same aggregation query for periodic statistics reports, for example. This multiaggregation case brings a performance advantage to the MD-index method because it calculates all aggregates while accessing the index tree only once, regardless of the number of the aggregate functions. Indeed, the two figures show that the performance of the MD-index method is comparable to (and, in some cases, better than) that of the SB-tree method when all the five aggregate functions are considered together.

### **CONCLUSION**

We have presented a new temporal aggregation method called the MD-index method. It stores temporal tuples as 2-D points through a 2-D index; and it computes the aggregates by identifying the TJW of each base interval and joining the tuples in the window with the interval. The aggregates for base intervals are calculated by incrementally modifying the aggregates from the previous base intervals without re-reading all tuples in the TJW of the current base interval. Adjacent base intervals with the same aggregate value are subsequently merged into a constant interval. We have compared our method with the SB-tree method. The results show that our method is at least an order of magnitude faster than the SB-tree method for updates, while increasingly comparable for multiaggregation queries as the number of aggregate functions in the query increases. These results indicate that the MD-index method is preferable in an environment with frequent updates or multiaggregation queries.

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## ENDNOTES

<sup>1</sup> An atelic fact is characterized by being true at any point during a certain time interval, whereas a telic fact is characterized by being true as a result of completing a goal during an interval (Terenziani & Snodgrass, 2004).

<sup>2</sup> We represent the time as an integer for convenience without loss of generality.

<sup>3</sup> Nevertheless, any multidimensional point access method (Gaede & Gunther, 1998) can be used for this purpose.

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