Integrated Circuit Operational Amplifiers

Analog Integrated Circuit Design A video course under the NPTEL

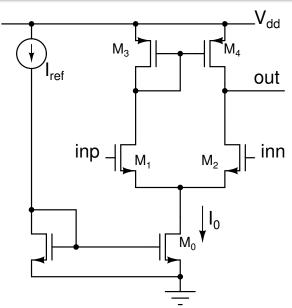
Nagendra Krishnapura

Department of Electrical Engineering Indian Institute of Technology, Madras Chennai, 600036, India

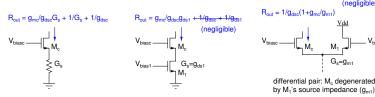
National Programme on Technology Enhanced Learning



Differential pair opamp



Cascode output resistance



 Output resistance looking into one side of the differential pair is $2/g_{ds1}$ ($g_{m1} = g_{mc}$ in the figure)

 $R_{out} = g_{mc}/g_{dec}g_{m1} + 1/g_{dec} + \frac{1}{g_{m1}}$

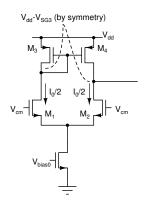
(negligible)

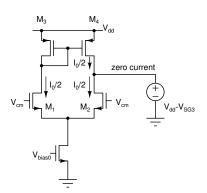
Opamp: dc small signal analysis

- Bias values in black
- Incremental values in red
- Impedances in blue

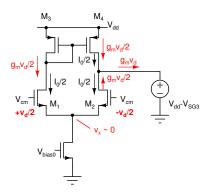
Total quantity = Bias + increment

Differential pair: Quiescent condition

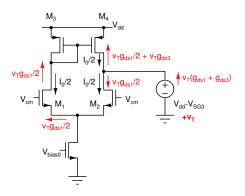




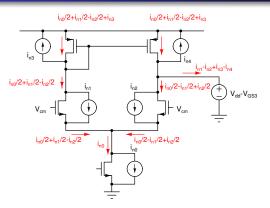
Differential pair: Transconductance



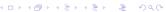
Differential pair: Output conductance



Differential pair: Noise



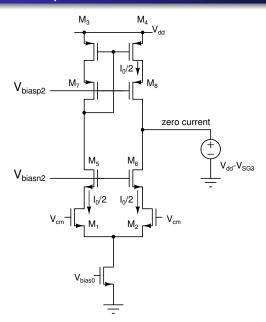
- Carry out small signal linear analysis with one noise source at a time
- Add up the results at the output (current in this case)
- Add up corresponding spectral densities
- Divide by gain squared to get input referred noise



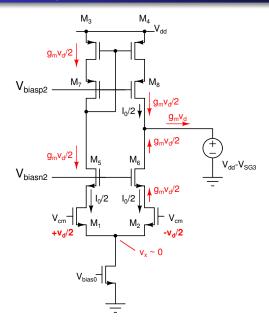
Differential pair opamp

G_m	g_{m1}			
G_{out}	$g_{d\mathrm{s}1}+g_{d\mathrm{s}3}$			
A_o	$g_{ extit{m1}}/(g_{ extit{ds1}}+g_{ extit{ds3}})$			
A_{cm}	$g_{ds0}/2g_{m3}$			
C_i	$C_{g m s1}/2$			
ω_{u}	g_{m1}/C_L			
p_k, z_k	$p_2 = -g_{m3}/(C_{db1} + C_{db3} + 2C_{gs3}); z_1 = 2p_2$			
S_{vi}	$16kT/3g_{m1}\left(1+g_{m3}/g_{m1} ight)$			
σ_{Vos}^{2}	$\sigma_{VT1}^2 + (g_{m3}/g_{m1})^2 \sigma_{VT3}^2$			
V_{cm}	$\geq V_{T1} + V_{DSAT1} + V_{DSAT0}$			
	$\leq \mathit{V_{dd}} - \mathit{V_{DSAT_3}} - \mathit{V_{T_3}} + \mathit{V_{T_1}}$			
V_{out}	$\geq V_{cm} - V_{T1}$			
	$\leq V_{dd} - V_{DSAT_3}$			
SR	$\pm I_0/C_L$			
I _{supply}	$I_0 + I_{ref}$			

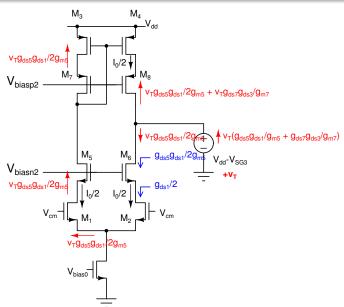
Telescopic cascode: Quiescent condition



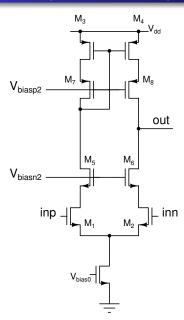
Telescopic cascode: Transconductance



Telescopic cascode: Output conductance



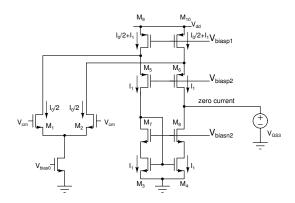
Telescopic cascode opamp



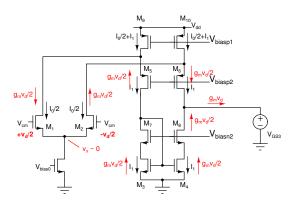
Telescopic cascode opamp

G_m	g_{m1}					
G_{out}	$g_{d m s1}g_{d m s5}/g_{m m 5}+g_{d m s3}g_{d m s7}/g_{m m 7}$					
A_o	$g_{ extit{m1}}/(g_{ extit{ds1}}g_{ extit{ds5}}/g_{ extit{m5}}+g_{ extit{ds3}}g_{ extit{ds7}}/g_{ extit{m7}})$					
A_{cm}	$g_{ds0}/2g_{m3}$					
C_i	$C_{gs1}/2$					
$\omega_{\it u}$	g_{m1}/C_L					
p_k, z_k	$ ho_{2} = -g_{m3}/(C_{db1} + C_{db3} + 2C_{gs3})$					
	$ ho_3=-g_{m5}/C_{p5}$					
	$ ho_4=-g_{m7}/C_{ ho7}$					
	$p_{2,4}$ appear for one half and cause mirrror zeros					
S_{vi}	$16kT/3g_{m1}\left(1+g_{m3}/g_{m1} ight)$					
$\frac{\sigma_{Vos}^2}{V}$	$\sigma_{VT1}^2 + (g_{m3}/g_{m1})^2 \sigma_{VT3}^2$					
V _{out}	$\geq V_{biasn1} - V_{T5}$					
	$\leq V_{biasp1} + V_{T7}$					
SR	$\pm I_0/C_L$					
I _{supply}	$I_0 + I_{ref}$					

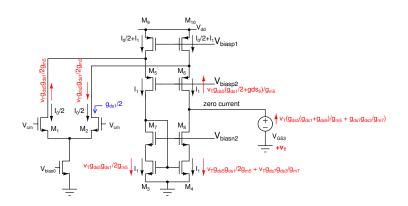
Folded cascode: Quiescent condition



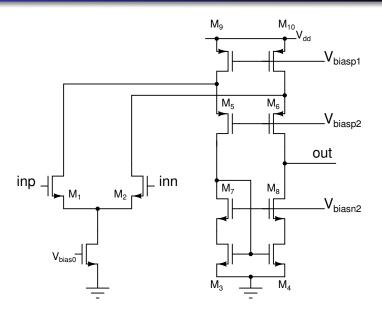
Folded cascode: Transconductance



Folded cascode: Output conductance



Folded cascode opamp



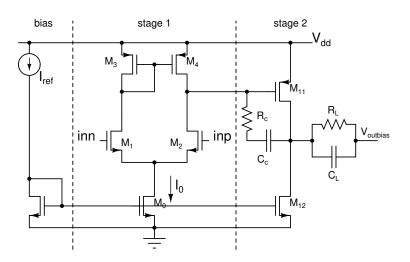
Folded cascode opamp

G_m	<i>9</i> _m 1				
G_{out}	$(g_{d extsf{s}1}+g_{d extsf{s}9})g_{d extsf{s}5}/g_{m extsf{b}}+g_{d extsf{s}3}g_{d extsf{s}7}/g_{m extsf{m}7}$				
A_o	$g_{ extit{m1}}/((g_{ extit{ds1}}+g_{ extit{ds9}})g_{ extit{ds5}}/g_{ extit{m5}}+g_{ extit{ds3}}g_{ extit{ds7}}/g_{ extit{m7}})$				
A_{cm}	$g_{ds0}/2g_{m3}$				
C_i	$C_{gs1}/2$				
ω_{u}	$g_{m1}/\mathit{C_L}$				
p_k, z_k	$ ho_{2}=-g_{m3}/(C_{db1}+C_{db3}+2C_{gs3})$				
	$p_3=-g_{m5}/C_{p5}$				
	$ ho_4=-g_{m7}/C_{p7}$				
	$p_{2,4}$ appear for one half and cause mirrror zeros				
S_{vi}	$16kT/3g_{m1}\left(1+g_{m3}/g_{m1}+g_{m9}/g_{m1} ight)$				
$\frac{\sigma_{Vos}^2}{V}$	$\sigma_{VT1}^2 + (g_{m3}/g_{m1})^2 \sigma_{VT3}^2 + (g_{m9}/g_{m1})^2 \sigma_{VT9}^2$				
V _{out}	$\geq V_{\it biasn1} - V_{\it T5}$				
	$\leq V_{biasp1} + V_{T7}$				
SR	$\pm \min\{\mathit{I}_{0},\mathit{I}_{1}\}/\mathit{C}_{\mathit{L}}$				
I _{supply}	$I_0 + I_1 + I_{ref}$				

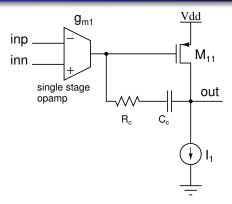
Body effect

- All nMOS bulk terminals to ground
- All pMOS bulk terminals to V_{dd}
- A_{cm} has an additional factor $g_{m1}/(g_{m1}+g_{mb1})$
- $g_{m5} + g_{mb5}$ instead of g_{m5} in cascode opamp results
- $g_{m7} + g_{mb7}$ instead of g_{m7} in cascode opamp results

Two stage opamp



Two stage opamp



- First stage can be Differential pair, Telescopic cascode, or Folded cascode; Ideal g_{m1} assumed in the analysis
- Second stage: Common source amplifier
- Frequency response is the product of frequency responses of the first stage g_m and a common source amplifier driven from a current source

Common source amplifier: Frequency response

$$\begin{array}{lcl} \frac{V_o(s)}{V_d(s)} & = & \left(\frac{g_{m_1}g_{m_{11}}}{G_1G_L}\right)\frac{sC_c(R_c-1/g_{m_{11}})+1}{a_3s^3+a_2s^2+a_1s+1} \\ a_3 & = & \frac{R_cC_1C_LC_c}{G_1G_L} \\ a_2 & = & \frac{C_1C_c+C_cC_L+C_LC_1+R_cC_c(G_1C_L+C_1G_L)}{G_1G_L} \\ a_1 & = & \frac{C_c(g_{m_{11}}+G_1+G_L+G_1G_LR_c)+C_1G_L+G_1C_L}{G_1G_L} \end{array}$$

- G₁: Total conductive load at the input
- G_L: Total conductive load at the output
- C₁: Total capacitive load at the input
- C_L: Total capacitive load at the output



Common source amplifier: Poles and zeros

$$\begin{array}{lll}
 & \rho_{1} & \approx & -\frac{G_{1}}{C_{c}(\frac{g_{m_{11}}}{G_{L}}+1+\frac{G_{1}}{G_{L}}+G_{1}R_{c})+C_{1}(1+\frac{G_{1}}{G_{L}})} \\
 & \rho_{2} & \approx & -\frac{g_{m_{11}}\frac{C_{c}}{C_{1}+C_{c}}+G_{L}+G_{1}\frac{C_{c}+C_{L}}{C_{1}+C_{c}}+G_{1}G_{L}R_{c}\frac{C_{c}}{C_{1}+C_{c}}} \\
 & \frac{C_{1}C_{c}}{C_{1}+C_{c}}+C_{L}+\frac{R_{c}C_{c}(G_{1}C_{L}+G_{L}C_{1})}{C_{c}+C_{L}} \\
 & \rho_{3} & \approx & -\left(\frac{1}{R_{c}}\left(\frac{1}{C_{L}}+\frac{1}{C_{c}}+\frac{1}{C_{1}}\right)+\frac{G_{1}}{C_{1}}+\frac{G_{L}}{C_{L}}\right) \\
 & z_{1} & = & \frac{1}{(1/g_{m_{11}}-R_{c})C_{c}}
 \end{array}$$

Unity gain frequency

$$\omega_{u} \approx \frac{g_{m_{1}}}{C_{c}\left(1+\frac{G_{L}}{g_{m_{11}}}+\frac{G_{1}}{g_{m_{11}}}+\frac{G_{1}G_{L}R_{c}}{g_{m_{11}}}\right)+C_{1}\left(\frac{G_{L}}{g_{m_{11}}}+\frac{G_{1}}{g_{m_{11}}}\right)}$$

Common source amplifier: Frequency response

- Pole splitting using compensation capacitor C_c
 - p₁ moves to a lower frequency
 - p_2 moves to a higher frequency (For large C_c , $p_2 = g_{m_{11}}/C_L$)
- Zero cancelling resistor R_c moves z_1 towards the left half s plane and results in a third pole p_3
 - z_1 can be moved to ∞ with $R_c = 1/g_{m_{11}}$
 - z_1 can be moved to cancel p_2 with $R_c > 1/g_{m_{11}}$ (needs to be verified against process variations)
 - Third pole p₃ at a high frequency
- Poles and zeros from the first stage will appear in the frequency response— $Y_{m1}(s)$ instead of g_{m1} in V_o/V_i above
 - Mirror pole and zero
 - Poles due to cascode amplifiers



Compensation cap sizing

$$p_2 \approx -rac{g_{m_{11}}rac{C_c}{C_1+C_c}}{rac{C_1C_c}{C_1+C_C}+C_L}$$
 $\omega_u \approx rac{g_{m_1}}{C_c}$

Phase margin (Ignoring $p_3, z_1, ...$)

$$\phi_{M} = \tan^{-1} \frac{|p_{2}|}{\omega_{u}}$$

$$\frac{|p_{2}|}{\omega_{u}} = \tan \phi_{M}$$

$$\frac{g_{m11}}{g_{m1}} \left(\frac{C_{c}}{C_{l}}\right)^{2} = \frac{C_{c}}{C_{l}} \left(1 + \frac{C_{1}}{C_{l}}\right) \tan \phi_{M} + \frac{C_{1}}{C_{l}} \tan \phi_{M}$$

- For a given ϕ_M , solve the quadratic to obtain C_c/C_L
- If C_1 is very small, $p_2 \approx -g_{m2}/C_L$; further simplifies

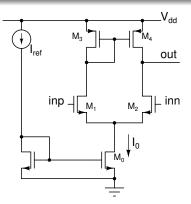
Two stage opamp

A_o	$g_{m1}g_{m11}/(g_{ds1}+g_{ds3})(g_{ds11}+g_{ds12})$				
A_{cm}	$g_{ds0}g_{m11}/2g_{m3}(g_{ds11}+g_{ds12})$				
C_i	$C_{gs1}/2$				
$\omega_{\it u}$	g_{m1}/C_c				
p_k, z_k	See previous pages				
\mathcal{S}_{vi}	$pprox 16kT/3g_{m1}(1+g_{m3}/g_{m1})$				
$\sigma_{\mathit{Vos}}^{2}$	$pprox \sigma_{VT1}^2 + (g_{m3}/g_{m1})^2 \sigma_{VT3}^2$				
V_{cm}	$\geq V_{T1} + V_{DSAT1} + V_{DSAT0}$				
	$\leq V_{dd} - V_{DSAT_3} - V_{T_3} + V_{T_1}$				
V_{out}	$\geq V_{DSAT_{12}}$				
	$\leq V_{dd} - V_{DSAT_{11}}$				
SR+	I_0/C_c				
SR-	$\min\{I_0/C_c,I_1/(C_L+C_c)\}$				
I _{supply}	$I_0 + I_1 + I_{ref}$				

Opamp comparison

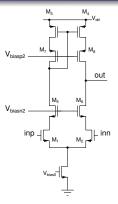
	Differential	Telescopic	Folded	Two
	pair	cascode	cascode	stage
Gain	_	++	+	++
Noise	=	=	high	=
Offset	=	=	high	=
Swing	_	_	+	++
Speed	++	+	_	+

Differential pair



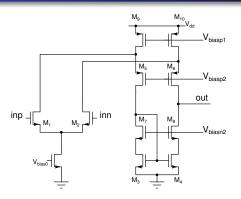
- Low accuracy (low gain) applications
- Voltage follower (capacitive load)
- Voltage follower with source follower (resistive load)
- In bias stabilization loops (effectively two stages in feedback)

Telescopic cascode



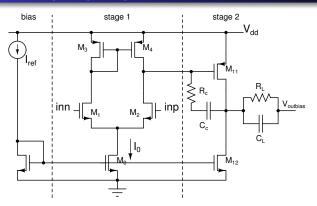
- Low swing circuits
- Switched capacitor circuits
 - Capacitive load
 - Different input and output common mode voltages
- First stage of a two stage opamp
 - Only way to get high gain in fine line processes

Folded cascode



- Higher swing circuits
- Higher noise and offset
- Lower speed than telescopic cascode
 - Low frequency pole at the drain of the input pair
- Switched capacitor circuits (Capacitive load)
- First stage of a two stage class AB opamp

Two stage opamp

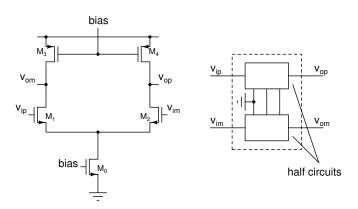


- Highest possible swing
- Resistive loads
- Capacitive loads at high speed
- "Standard" opamp: Miller compensated two stage opamp
- Class AB opamp: Always two (or more) stages

Opamps: pMOS versus nMOS input stage

- nMOS input stage
 - Higher g_m for the same current
 - Suitable for large bandwidths
 - Higher flicker noise (usually)
- pMOS input stage
 - Lower g_m for the same current
 - Lower flicker noise (usually)
 - Suitable for low noise low frequency applications

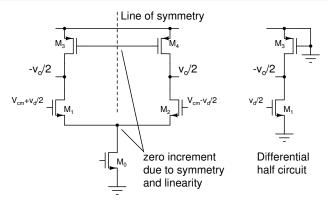
Fully differential circuits



- Two identical half circuits with some common nodes
- Two arms of the differential input applied to each half
- Two arms of the differential output taken from each half



Differential half circuit

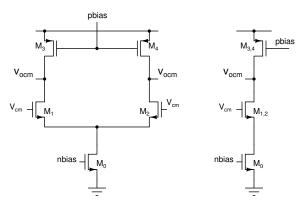


Symmetrical linear (or small signal linear) circuit under fully differential (antisymmmetric) excitation

- Nodes along the line of symmetry at 0 V (symmetry, linearity)
- Analyze only the half circuit to find the transfer function



Common mode half circuit

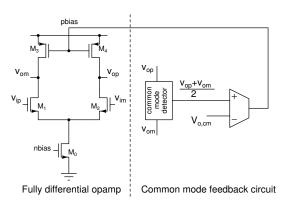


Symmetrical circuit (maybe nonlinear) under common mode (symmetric) excitation

- Nodes in each half at identical voltages (symmetry)
- Fold over the circuit and analyze the half circuit



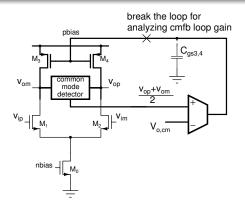
Common mode feedback



- Common mode feedback circuit for setting the bias
- Detect the output common mode and force it to be $V_{o,cm}$ via feedback



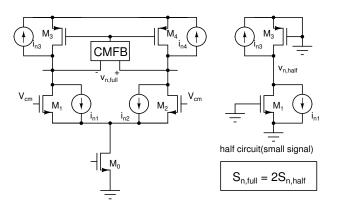
Common mode feedback loop



- Common mode feedback loop has to be stable
- Analyze it by breaking the loop and computing the loop gain with appropriate loading at the broken point
- Apply a common mode step/pulse in closed loop and ensure stability

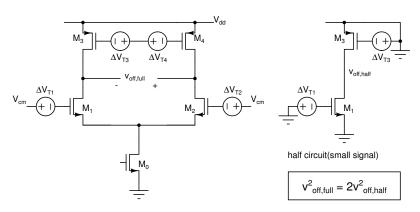


Fully differential circuits: Noise



- Calculate noise spectral density of the half circuit
- Multiply by 2×

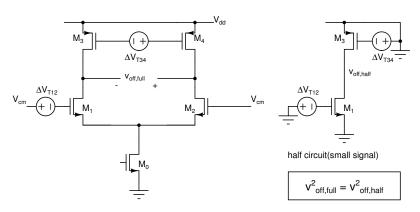
Fully differential circuits: Offset



- Calculate mean squared offset of the half circuit
- Multiply by $2 \times$ if mismatch (e.g. ΔV_T) wrt ideal device is used



Fully differential circuits: Offset



- Calculate mean squared offset of the half circuit
- Multiply by $1 \times$ if mismatch between two real devices is used

