

In *Linux* versions before 2.6.11, the capacity of a pipe was the same as the system page size (*e.g.*, 4096 bytes on *i386*). Since *Linux* 2.6.11, the pipe capacity is 16 pages (*i.e.*, 65,536 bytes in a system with a page size of 4096 bytes).

EXTENDS *Naturals*, *Sequences*

VARIABLES $inQueueIn$, $inQueueOut$, $inQueue$,
 $outQueueIn$, $outQueueOut$, $outQueue$

CONSTANT $Message$, $MessagePairs$, N

ASSUME $(N \in Nat) \wedge (N > 0)$ Both queues have the same number of messages

ASSUME $(MessagePairs \in [msgIn : Message, msgOut : Message])$

A simple type invariant

$$\begin{aligned} TypeOK &\triangleq \wedge MessagePairs \in [msgIn : Message, msgOut : Message] \\ &\quad \wedge \forall msgPair \in MessagePairs : msgPair.msgIn \neq msgPair.msgOut \\ &\quad \wedge inQueue \in Seq(Message) \\ &\quad \wedge outQueue \in Seq(Message) \end{aligned}$$

Util function

$$Last(s) \triangleq s[Len(s)]$$

$$\begin{aligned} InQueue &\triangleq \text{INSTANCE } BoundedFIFO \text{ WITH } in \leftarrow inQueueIn, out \leftarrow inQueueOut, q \leftarrow inQueue \\ OutQueue &\triangleq \text{INSTANCE } BoundedFIFO \text{ WITH } in \leftarrow outQueueIn, out \leftarrow outQueueOut, q \leftarrow outQueue \end{aligned}$$

Make sure that if the in queue is non-empty, given some length in queue of x ,
out queue will eventually reach a point where it will be at least that size, if not greater

$$\begin{aligned} MsgTrans &\triangleq \\ &\forall x \in Nat : \\ &\quad (Len(inQueue) > 0) \Rightarrow Len(inQueue) = x \leadsto Len(outQueue) \geq x \end{aligned}$$

Make sure that once the message goes in, it must go out as it's pair

$$\begin{aligned} MsgIncl &\triangleq \\ &\forall msgPair \in MessagePairs : \\ &\quad (Len(inQueue) > 0) \Rightarrow Last(inQueue) = msgPair.msgIn \leadsto Head(outQueue) = msgPair.msgOut \end{aligned}$$

$$\begin{aligned} Init &\triangleq \wedge InQueue!Init \\ &\quad \wedge OutQueue!Init \end{aligned}$$

$$\begin{aligned} BNext &\triangleq \wedge InQueue!BNext \\ &\quad \wedge OutQueue!BNext \end{aligned}$$

$$\begin{aligned} Spec &\triangleq \wedge MsgTrans \\ &\quad \wedge MsgIncl \end{aligned}$$

$$\wedge \textit{Init}$$

$$\wedge \Box [BNext]_{\langle inQueueIn, inQueueOut, inQueue, outQueueIn, outQueueOut, outQueue \rangle}$$

THEOREM $Spec \Rightarrow \Box TypeOK$
