

In *Linux* versions before 2.6.11, the capacity of a pipe was the same as the system page size (*e.g.*, 4096 bytes on *i386*). Since *Linux* 2.6.11, the pipe capacity is 16 pages (*i.e.*, 65,536 bytes in a system with a page size of 4096 bytes).

$N = 20$
 $Message = \{“ping”, “pong”, “queryPort”, “replyPort”\}$
 $MessagePairs = \{[msgIn \mapsto “ping”, msgOut \mapsto “pong”], [msgIn \mapsto “queryPort”, msgOut \mapsto “replyPort”]\}$

EXTENDS *Naturals, Sequences*

VARIABLES *inQueue, outQueue*

CONSTANT *Message, MessagePairs, N*

ASSUME $(N \in Nat) \wedge (N > 0)$ Both queues have the same number of messages

ASSUME $(\forall msgPair \in MessagePairs : \quad \wedge msgPair.msgIn \in Message$
 $\quad \wedge msgPair.msgOut \in Message$
 $\quad \wedge msgPair.msgIn \neq msgPair.msgOut)$

A simple type invariant

$TypeOK \triangleq \wedge \forall msgPair \in MessagePairs : msgPair.msgIn \neq msgPair.msgOut$

Util function

$Last(s) \triangleq s[Len(s)]$

$\backslash *$ We would usually use the existing structures, but the problem with these is that
 $\backslash *$ they have a step that chooses a random message when we advance their state using next.
 $InQueue \triangleq$ INSTANCE *BoundedFIFO* WITH $in \leftarrow inQueueIn, out \leftarrow inQueueOut, q \leftarrow inQueue$
 $OutQueue \triangleq$ INSTANCE *BoundedFIFO* WITH $in \leftarrow outQueueIn, out \leftarrow outQueueOut, q \leftarrow outQueue$

Make sure that once the message goes in, eventually it must go out as it's pair response

$MsgIncl \triangleq$
 $\forall msgPair \in MessagePairs :$
 $(Len(inQueue) > 0) \Rightarrow Last(inQueue) = msgPair.msgIn \rightsquigarrow Head(outQueue) = msgPair.msgOut$

When they start they are empty

$Init \triangleq \wedge inQueue = \langle \rangle$
 $\quad \wedge outQueue = \langle \rangle$

If the input queue is empty, we presume that the sender awaits for the response.

$BNext \triangleq \wedge$ IF $Len(inQueue) = 0$
 Append a new message to the in queue
 THEN $\exists msgPair \in MessagePairs : \quad \wedge inQueue' = Append(inQueue, msgPair.msgIn)$
 $\quad \wedge UNCHANGED (outQueue)$

$$\begin{array}{l}
\text{Advances a step, removes a message from in queue and appends it's pair to out queue} \\
\text{ELSE } \exists \text{ msgPair} \in \text{MessagePairs} : \quad \wedge \text{inQueue}' = \text{Tail}(\text{inQueue}) \\
\quad \quad \quad \wedge \text{outQueue}' = \text{Append}(\text{outQueue}, \text{msgPair.msgOut}) \\
\wedge \text{Len}(\text{inQueue}) < N \quad \text{Bounded inQueue, this gets discharged, but let's keep our invariants} \\
\wedge \text{Len}(\text{outQueue}) < N \quad \text{Bounded outQueue} \\
\\
\text{Spec} \quad \triangleq \quad \wedge \text{MsgIncl} \\
\quad \quad \wedge \text{Init} \\
\quad \quad \wedge \Box [BNext]_{\langle \text{inQueue}, \text{outQueue} \rangle} \\
\\
\hline
\text{THEOREM } \text{Spec} \Rightarrow \Box \text{TypeOK} \\
\hline
\end{array}$$