Statistical Computing

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Welcome to Statistical Computing! A book designed to give undergraduate students exposure to several topics related to computational statistics and programming in R.

i Note

This book is a work in progress and will contain several grammatical errors and unfinished chapters. The final product is expected to be ready by the 2025-26 Academic Year.

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Preface

This is a book created to be used for a statistical computing course at the undergraduate level.

Installing R

R is an open-source programming language used to conduct statistical analysis. You can freely download and install R here.

Installing RStudio

RStudio is an Integrated Development Environment (IDE) used for data science. It contains several tools needed to extend your programming and project management skills.

You can download and install the open-source (free) version of RStudio here.

Installing Quarto

Quarto is a technical documentation system that allows you to embed narrative, code, and output in one document. Quarto should come automatically install from RStudio; however, you can update (or install) it here.

Installing R Packages

R Packages extends the functionality from the base functions in R. R packages contain extra functions to conduct uncommon statistical models.

As of right now, the tidyverse is a set of comprehensive packages to prepare and analyze data. To install tidyverse, use the following line in the console:

Topics

Topic	Description
R Programming	Provide with a brief introduction to R programming. Topics include basic computations, control flow statements, functional programming, and scripting tips and tricks.
Simulations	Explore different algorithms to generate random variables.
Randomizations	Learn how to implement different permutation tests.
Monte Carlo Methods	Implement Monte Carlo methods to approximate integrals and distributions.
Bootstrapping	Conduct different bootstrapping techniques to construct confidence intervals.
Data Manipulation, Summarization, and Graphics	Learn how to analyze real-world data
Reporting Data	Learn how to use Quarto to generate reports and presentations.
Debugging and Efficient Programming	Learn how write efficient R code and implement Rcpp into your programs.

Part I R Programming

1 Basic R Programming

1.1 Introduction

This chapter focuses on the basics of R programming. While most of your statistical analysis will be done with R functions, it is important to have an idea of what is going on. Additionally, we will cover other topics that you may or may not need to know. The topics we will cover are:

- 1. Basic calculations in R
- 2. Types of Data
- 3. R Objects
- 4. R Functions
- 5. R Packages

1.2 Basic Calculations

This section focuses on the basic calculation that can be done in R. This is done by using different operators in R. The table below provides some of the basic operators R can use:

Operator	Description
+	Addition
_	Subtraction
*	Multiplication
/	Divides
^ or **	Exponentiate
?	Help Documentation

1.2.1 Calculator

1.2.1.1 Addition

To add numbers in R, all you need to use the + operator. For example 2+2=4. When you type it in R you have:

2 + 2

[1] 4

When you ask R to perform a task, it prints out the result of the task. As we can see above, R prints out the number 4.

To add more than 2 numbers, you can simply just type it in.

2 + 2 + 2

[1] 6

This provides the number 6.

1.2.1.2 Subtraction

To subtract numbers, you need to use the – operator. Try $4\,$ – $\,2:$

4 - 2

[1] 2

Try 4 - 6 - 4

4 - 6 - 4

[1] -6

Notice that you get a negative number.

Now try 4 + 4 - 2 + 8:

4 + 4 - 2 + 8

[1] 14

1.2.1.3 Multiplication

To multiply numbers, you will need to use the * operator. Try 4 * 4:

4 * 4

[1] 16

1.2.1.4 Division

To divide numbers, you can use the \prime operator. Try 9 $\,/\,$ 3:

9 / 3

[1] 3

1.2.1.5 Exponents

To exponentiate a number to the power of another number, you can use the $\hat{\ }$ operator. Try 2^5:

2^5

[1] 32

If you want to find e^2 , you will use the exp() function. Try exp(2):

exp(2)

[1] 7.389056

1.2.1.6 Roots

To take the n-th root of a value, use the $^{\circ}$ operator with the / operator to take the n-th root. For example, to take $\sqrt[5]{35}$, type 32 $^{\circ}$ (1/5):

32^(1/5)

[1] 2

1.2.1.7 Logarithms

To take the natural logarithm of a value, you will use the log() function. Try log(5):

log(5)

[1] 1.609438

If you want to take the logarithm of a different base, you will use the log() function with base argument. We will discuss this more in Section 1.4.

1.2.2 Comparing Numbers

Another important part of R is comparing numbers. When you compare two numbers, R will tell if the statement is TRUE or FALSE. Below are the different comparisons you can make:

Operator	Description
>	Greater Than
<	Less Than
>=	Greater than or equal
<=	Less than or equal
==	Equals
!=	Not Equals

1.2.2.1 Less than/Greater than

To check if one number is less than or greater than another number, you will use the > or < operators. Try 5 > 4:

5 > 4

[1] TRUE

Notice that R states it's true. It evaluates the expression and tells you if it's true or not. Try 5 < 4:

5 < 4

[1] FALSE

Notice that R tells you it is false.

1.2.2.2 Less than or equal to/Greater than or equal to

To check if one number is less than or equal to/greater than or equal to another number, you will use the \geq or \leq operators. Try 5 \geq 5:

5 >= 5

[1] TRUE

Try 5 >= 4:

5 >= 4

[1] TRUE

Try $5 \le 4$

5 <= 4

[1] FALSE

1.2.2.3 Equals and Not Equals

To check if 2 numbers are equal to each other, you can use the == operator. Try 3 == 3:

3 == 3

[1] TRUE

Try 4 == 3

3 == 4

[1] FALSE

Another way to see if 2 numbers are not equal to each other, you can use the !=. Try 3 != 4:

3 != 4

[1] TRUE

Try 3 != 3:

3 != 3

[1] FALSE

You may be asking why use != instead of ==. They both provides similar results. Well the reason is that you may need the TRUE output for analysis. One is only true when they are equal, while the other is true when they are not equal.

In general, the ! operator means not or opposite. It can be used to change an TRUE to a FALSE and vice-versa.

1.2.3 Help

The last operator we will discuss is the help operator?. If you want to know more about anything we talked about you can type? in front of a function and a help page will popup in your browser or in RStudio's 'Help' tab. For example you can type ?Arithmetic or ?Comparison, to review what we talked about. For other operators we didn't talk about use ?assignOps and ?Logic.

1.3 Types of Data

In R, the type of data, also known as class, we are using dictates how the programming works. For the most part, users will use *numeric*, *logical*, *POSIX* and *character* data types. Other types of data you may encounter are *complex* and *raw*. To obtain more information on them, use the ? operator.

1.3.1 Numeric

The *numeric* class is the data that are numbers. Almost every analysis that you use will be based on the numeric class. To check if you have a numeric class, you just need to use the is.numeric() function. For example, try is.numeric(5):

```
is.numeric(5)
```

[1] TRUE

Numeric classes are essentially *double* and *integer* types of data. For example a *double* data is essentially a number with decimal value. An *integer* data are whole numbers. Try is.numeric(5.63), is.double(5.63) and is.integer(5.63):

```
is.numeric(5.63)
```

[1] TRUE

```
is.double(5.63)
```

[1] TRUE

```
is.integer(5.63)
```

[1] FALSE

Notice how the value 5.63 is a *numeric* and *double* but not *integer*. Now let's try is.numeric(7), is.double(7) and is.integer(7):

```
is.numeric(7)

[1] TRUE

is.double(7)

[1] TRUE
```

is.integer(7)

[1] FALSE

Notice how the value 7 is also considered a *numeric* and *double* but not *integer*. This is because typing a whole number will be stored as a *double*. However, if we need to store an *integer*, we will need to type the letter "L" after the number. Try is.numeric(7L), is.double(7L), and is.integer(7L):

```
is.numeric(7L)

[1] TRUE

is.double(7L)

[1] FALSE

is.integer(7L)
```

[1] TRUE

1.3.2 Logical

A *logical* class are data where the only value is TRUE or FALSE. Sometimes the data is coded as 1 for TRUE and 0 for FALSE. The data may also be coded as T or F. To check if data belongs in the *logical* class, you will need the is.logical() function. Try is.logical(3 < 4):

```
is.logical(3 < 4)
```

[1] TRUE

This is same comparison from Section 1.2.2. The output was TRUE. Now R is checking whether the output is of a *logical* class. Since it it, R returns TRUE. Now try is.logical(3 > 4):

```
is.logical(3 > 4)
```

[1] TRUE

The output is TRUE as well even though the condition 3 > 4 is FALSE. Since the output is a logical data type, it is a logical variable.

1.3.3 **POSIX**

The *POSIX* class are date-time data. Where the data value is a time component. The *POSIX* class can be very complex in how it is formatted. IF you would like to learn more try ?POSIXct or ?POSIClt. First, lets run Sys.time() to check what is today's data and time:

```
Sys.time()
```

```
[1] "2024-03-16 23:10:01 PDT"
```

Now lets check if its of POSIX class, you can use the class() function to figure out which class is it. Try class(Sys.time()):

```
class(Sys.time())
```

[1] "POSIXct" "POSIXt"

1.3.4 Character

A character value is where the data values follow a string format. Examples of character values are letters, words and even numbers. A character value is any value surrounded by quotation marks. For example, the phrase "Hello World!" is considered as one character value. Another example is if your data is coded with the actual words "yes" or "no". To check if you have character data, use the is.character() function. Try is.character("Hello World!"):

```
is.character("Hello World!")
```

[1] TRUE

Notice that the output says TRUE. *Character* values can be created with single quotations. Try is.character('Hello World!'):

```
is.character('Hello World!')
```

[1] TRUE

1.3.5 Complex Numbers

Complex numbers are data values where there is a real component and an imaginary component. The imaginary component is a number multiplied by $i = \sqrt{-1}$. To create a complex number, use the complex() function. To check if a number is complex, use the is.complex() function. Try the following to create a complex number complex(1, 4, 5):

```
complex(1, 4, 5)
```

[1] 4+5i

Now try is.complex(complex(1, 4, 5)):

```
is.complex(complex(1, 4, 5))
```

[1] TRUE

1.3.6 Raw

You will probably never use raw data. I have never used raw data in R. To create a raw value, use the raw() or charToRaw() functions. Try charToRaw('Hello World!'):

```
charToRaw('Hello World!')
```

[1] 48 65 6c 6c 6f 20 57 6f 72 6c 64 21

To check if you have raw data, use the is.raw() function. Try is.raw(charToRaw('Hello World!')):

[1] TRUE

1.3.7 Missing

The last data class in R is missing data. The table below provides a brief introduction of the different types of missing data

Value	Description	Functions
NULL	These are values indicating an object is empty. Often used for functions with values that are undefined.	is.null()
NA	Stands for "Not Available", used to indicate that the value is missing in the data.	is.na()
NaN	Stands for "Not an Number". Used to indicate a missing number.	is.nan()
Inf and -Inf	Indicating an extremely large value or a value divided by 0.	<pre>is.infinite()</pre>

1.4 R Functions

An R function is the procedure that R will execute to certain data. For example, the log(x) is an R function. It takes the value x and provides you the natural logarithm. Here x is known as an argument which needs to be specified to us the log() function. Find the log(x = 5)

$$\log(x = 5)$$

[1] 1.609438

Another argument for the log() function is the base argument. With the previous code, we did not specify the base argument, so R makes the base argument equal to the number e. If you want to use the common log with base 10, you will need to set the base argument equal to 10.

Try log(x = 5, base = 10)

```
log(x = 5, base = 10)
```

[1] 0.69897

Now try log(5,10)

```
log(5,10)
```

[1] 0.69897

Notice that it provides the same value. This is because R can set arguments based on the values position in the function, regardless if the arguments are specified. For log(5,10), R thinks that 5 corresponds to the first argument x and 10 is the second argument base.

To learn more about a functions, use the ? operator on the function: ?log.

1.5 R Objects

R objects are where most of your data will be stored. An R object can be thought of as a container of data. Each object will share some sort of characteristics that will make the unique for different types of analysis.

1.5.1 Assigning objects

To create an R object, all we need to do is assign data to a variable. The variable is the name of the R object. it can be called anything, but you can only use alphanumeric values, underscore, and periods. To assign a value to a variable, use the \leftarrow operator. This is known a left assignment. Kinda like an arrow pointing left. Try assigning 9 to 'x' (x \leftarrow 9):

```
x <- 9
```

To see if x contains 9, type x in the console:

X

[1] 9

Now x can be treated as data and we can perform data analysis on it. For example, try squaring it:

x^2

[1] 81

You can use any mathematical operation from the previous sections. Try some other operations and see what happens.

The output R prints out can be stored in a variable using the asign operator, \leftarrow . Try storing x^3 in a variable called x_cubed :

```
x_cubed <- x^3
```

To see what is stored in x_{cubed} you can either type x_{cubed} in the console or use the print() function with x_{cubed} inside the parenthesis.

x_cubed

[1] 729

print(x_cubed)

[1] 729

1.5.2 Vectors

A vector is a set data values of a certain length. The R object x is considered as a numerical vector (because it contains a number) with the length 1. To check, try is.numeric(x) and is.vector(x):

is.numeric(x)

[1] TRUE

is.vector(x)

[1] TRUE

Now let's create a logical vector that contains 4 elements (have it follow this sequence: T, F, T, F) and assign it to y. To create a vector use the $c()^1$ function and type all the values and separating them with columns. Type $y \leftarrow c(T, F, T, F)$:

Now, lets see how y looks like. Type y:

у

[1] TRUE FALSE TRUE FALSE

Now lets see if it's a logical vector:

```
is.logical(y)
```

[1] TRUE

is.vector(y)

[1] TRUE

Fortunately, this vector is really small to count how many elements it has, but what if the vector is really large? To find out how many elements a vector has, use the length() function. Try length(y):

length(y)

[1] 4

¹The c() function allows you to put any data type and as many values as you wish. The only condition of a vector is that it must be the same data type.

1.5.3 Matrices

A matrix can be thought as a square or rectangular grid of data values. This grid can be constructed can be any size. Similar to vectors they must contain the same data type. The size of a matrix is usually denoted as $n \times k$, where n represents the number of rows and k represents the number of columns. To get a rough idea of how a matrix may look like, type $\text{matrix}(\text{rep}(1,12), \text{nrow} = 4, \text{ncol} = 3)^2$:

```
matrix(rep(1, 12), nrow = 4, ncol = 3)
```

```
[,1] [,2] [,3]
[1,]
          1
                 1
[2,]
          1
                 1
                       1
[3,]
          1
                1
                       1
[4,]
          1
                 1
                       1
```

Notice that this is a 4×3 matrix. Each element in the matrix has the value 1. Now try this matrix(rbinom(12,1.5), nrow = 4, ncol = 3)³:

```
matrix(rbinom(12, 1, .5), nrow = 4, ncol = 3)
```

```
[,1] [,2] [,3]
[1,] 1 1 0
[2,] 0 1 0
[3,] 1 0 0
[4,] 1 0 1
```

Your matrix may look different, but that is to be expected. Notice that some elements in a matrix are 0's and some are 1's. Each element in a matrix can hold any value.

An alternate approach to creating matrices is with the use of rbind() and cbind() functions. Using 2 vectors, and matrices, of the same length, the rbind() will append the vectors together by each row. Similarly, the cbind() function will append vectors, and matrices, of the same length by columns.

²The function rep() creates a vector by repeating a value for a certain length. rep(1,12) creates a vector of length 12 with each element being 1. We use the nrow and ncol arguments in the function to specify the number of rows and columns, respectfully.

³The rbinom() function generates binomial random variables and stores them in a vector. rbinom(12,1,5) This creates 12 random binomial numbers with parameter n = 1 and p = 0.5.

```
x <- 1:4
y <- 5:8
z <- 9:12
cbind(x, y, z)
```

```
x y z
[1,] 1 5 9
[2,] 2 6 10
[3,] 3 7 11
[4,] 4 8 12
```

rbind(x, y, z)

```
[,1] [,2] [,3] [,4]

x 1 2 3 4

y 5 6 7 8

z 9 10 11 12
```

If you want to create a matrix of a specific size without any data, you can use the matrix() function and only specify the nrow and ncol arguments. Here we are creating a 5×11 empty matrix:

```
matrix(nrow = 5, ncol = 11)
```

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11]
[1,]
       NA
             NA
                   NA
                                          NA
                                               NA
                                                     NA
                                                            NA
                        NA
                              NA
                                    NA
                                                                   NA
[2,]
       NA
                                                            NA
                                                                   NA
             NA
                   NA
                        NA
                              NA
                                    NA
                                          NA
                                               NA
                                                     NA
[3,]
       NA
             NA
                   NA
                        NA
                              NA
                                    NA
                                          NA
                                               NA
                                                     NA
                                                            NA
                                                                   NA
[4,]
       NA
             NA
                   NA
                        NA
                              NA
                                    NA
                                          NA
                                               NA
                                                     NA
                                                            NA
                                                                   NA
[5,]
       NA
             NA
                   NA
                        NA
                              NA
                                    NA
                                          NA
                                               NA
                                                     NA
                                                            NA
                                                                   NA
```

Lastly, if you need to find out the dimensions of a matrix, you can use dim() function on a matrix:

```
dim(matrix(nrow = 5, ncol = 11))
```

[1] 5 11

This will return a vector of length 2 with the first element being the number of rows and the second element being the number of columns.

1.5.4 Arrays

Matrices can be considered as a 2-dimensional block of numbers. An array is an n-dimensional block of numbers. While you may never need to use an array for data analysis. It may come in handy when programming by hand. To create an array, use the array() function. Below is an example of a $3 \times 3 \times 3$ with the numbers 1, 2, and 3 representing the 3rd dimension stored in an R object called $first_array^4$.

```
(first_array <- array(c(rep(1, 9), rep(2, 9), rep(3, 9)), dim=c(3,3,3)))
```

```
, , 1
      [,1] [,2] [,3]
[1,]
               1
[2,]
               1
                     1
         1
[3,]
, , 2
      [,1] [,2] [,3]
[1,]
               2
                     2
         2
[2,]
               2
                     2
         2
[3,]
         2
               2
                     2
, , 3
      [,1] [,2] [,3]
[1,]
         3
               3
                     3
[2,]
         3
               3
                     3
         3
               3
                     3
[3,]
```

1.5.5 Data Frames

Data frames are similar to data set that you may encounter in an excel file. However, there are a couple of differences. First, each row represents an observation, and each column represents a characteristic of the observation. Additionally, each column in a data frame will be the same data type. To get an idea of what a data frame looks like, try head(iris) ⁵:

⁴Notice the code is surrounded by parenthesis. This tells R to store the array and print out the results. You can surround code with parenthesis every time you create an object to also print what is stored.

⁵The head() function just tells R to only print the top few components of the data frame.

head(iris)

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
	5.1	3.5	1.4	0.2	setosa
	2 4.9	3.0	1.4	0.2	setosa
;	3 4.7	3.2	1.3	0.2	setosa
4	4.6	3.1	1.5	0.2	setosa
;	5.0	3.6	1.4	0.2	setosa
(5.4	3.9	1.7	0.4	setosa

In the data frame, the rows indicate a specific observation and the columns are the values of a variable. In terms of the iris data set, we can see that row 1 is a specific flower that has a sepal length of 5.1. We can also see that flower 1 has other characteristics such as sepal width and petal length. Lastly, there are results for the other flowers.

Now try tail(iris):

tail(iris)

	Sepal.Length	${\tt Sepal.Width}$	Petal.Length	${\tt Petal.Width}$	Species
145	6.7	3.3	5.7	2.5	virginica
146	6.7	3.0	5.2	2.3	virginica
147	6.3	2.5	5.0	1.9	virginica
148	6.5	3.0	5.2	2.0	virginica
149	6.2	3.4	5.4	2.3	virginica
150	5.9	3.0	5.1	1.8	virginica

The tail() function provides the last 6 rows of the data frame.

Lastly, if you are interested in viewing a specific variable (column) from a data frame, you can use the \$ operator to specify which variable from a specific data frame. For example, if we are interested in observing the Sepal.Length variable from the iris data frame, we will type iris\$Sepal.Length:

iris\$Sepal.Length

```
[1] 5.1 4.9 4.7 4.6 5.0 5.4 4.6 5.0 4.4 4.9 5.4 4.8 4.8 4.3 5.8 5.7 5.4 5.1 [19] 5.7 5.1 5.4 5.1 4.6 5.1 4.8 5.0 5.0 5.2 5.2 4.7 4.8 5.4 5.2 5.5 4.9 5.0 [37] 5.5 4.9 4.4 5.1 5.0 4.5 4.4 5.0 5.1 4.8 5.1 4.6 5.3 5.0 7.0 6.4 6.9 5.5 [55] 6.5 5.7 6.3 4.9 6.6 5.2 5.0 5.9 6.0 6.1 5.6 6.7 5.6 5.8 6.2 5.6 5.9 6.1 [73] 6.3 6.1 6.4 6.6 6.8 6.7 6.0 5.7 5.5 5.5 5.8 6.0 5.4 6.0 6.7 6.3 5.6 5.5
```

```
[91] 5.5 6.1 5.8 5.0 5.6 5.7 5.7 6.2 5.1 5.7 6.3 5.8 7.1 6.3 6.5 7.6 4.9 7.3 [109] 6.7 7.2 6.5 6.4 6.8 5.7 5.8 6.4 6.5 7.7 7.7 6.0 6.9 5.6 7.7 6.3 6.7 7.2 [127] 6.2 6.1 6.4 7.2 7.4 7.9 6.4 6.3 6.1 7.7 6.3 6.4 6.0 6.9 6.7 6.9 5.8 6.8 [145] 6.7 6.7 6.3 6.5 6.2 5.9
```

1.5.6 Lists

[[1]]

Merc 450SE

Merc 450SL

Merc 450SLC

Cadillac Fleetwood

To me a list is just a container that you can store practically anything. It is compiled of elements, where each element contains an R object. For example, the first element of a list may contain a data frame, the second element may contain a vector, and the third element may contain another list. It is just a way to store things.

To create a list, use the list() function. Create a list compiled of first element with the mtcars data set, second element with a vector of zeros of size 4, and a matrix 3×3 identity matrix⁶. Store the list in an object called list one:

Type list_one to see what pops out:

16.4

17.3

15.2

10.4

```
list_one
```

```
disp hp drat
                                                  wt
                                                     qsec vs am gear carb
Mazda RX4
                     21.0
                            6 160.0 110 3.90 2.620 16.46
                                                               1
                                                                          4
                            6 160.0 110 3.90 2.875 17.02
Mazda RX4 Wag
                     21.0
                                                                    4
                                                                          4
Datsun 710
                     22.8
                            4 108.0
                                     93 3.85 2.320 18.61
                                                                    4
                                                                          1
Hornet 4 Drive
                            6 258.0 110 3.08 3.215 19.44
                                                                    3
                     21.4
                                                            1
                                                                          1
                            8 360.0 175 3.15 3.440 17.02
Hornet Sportabout
                     18.7
                                                               0
                                                                    3
                                                                          2
Valiant
                     18.1
                            6 225.0 105 2.76 3.460 20.22
                                                               0
                                                                    3
                                                                          1
                                                            1
Duster 360
                     14.3
                            8 360.0 245 3.21 3.570 15.84
                                                                    3
                                                                          4
                                                               0
Merc 240D
                     24.4
                            4 146.7
                                      62 3.69 3.190 20.00
                                                               0
                                                                    4
                                                                          2
Merc 230
                     22.8
                            4 140.8
                                     95 3.92 3.150 22.90
                                                                    4
                                                                          2
Merc 280
                     19.2
                            6 167.6 123 3.92 3.440 18.30
                                                                    4
                                                                          4
Merc 280C
                     17.8
                            6 167.6 123 3.92 3.440 18.90
                                                            1
                                                               0
                                                                          4
```

8 275.8 180 3.07 4.070 17.40

8 275.8 180 3.07 3.730 17.60

8 275.8 180 3.07 3.780 18.00

8 472.0 205 2.93 5.250 17.98

3

3

3

3

0 0

0 0

0 0

3

3

3

 $^{^6}$ An identity matrix is a matrix where the diagonal elements are 1 and the non-diagonal elements are 0

```
Lincoln Continental 10.4
                            8 460.0 215 3.00 5.424 17.82
                                                                         4
                                                                    3
                            8 440.0 230 3.23 5.345 17.42
                                                                          4
Chrysler Imperial
                     14.7
                                                            0
                                                               0
                                                                    3
Fiat 128
                     32.4
                               78.7
                                     66 4.08 2.200 19.47
                                                                    4
                                                                         1
                                                            1
                                                               1
Honda Civic
                     30.4
                               75.7
                                     52 4.93 1.615 18.52
                                                               1
                                                                    4
                                                                         2
                                                            1
                                     65 4.22 1.835 19.90
                                                                    4
Toyota Corolla
                     33.9
                               71.1
                                                               1
                                                                         1
Toyota Corona
                                     97 3.70 2.465 20.01
                                                                    3
                     21.5
                            4 120.1
                                                                          1
Dodge Challenger
                     15.5
                            8 318.0 150 2.76 3.520 16.87
                                                                    3
                                                                         2
AMC Javelin
                     15.2
                            8 304.0 150 3.15 3.435 17.30
                                                                    3
                                                                         2
Camaro Z28
                            8 350.0 245 3.73 3.840 15.41
                                                                    3
                                                                         4
                     13.3
                                                            0
Pontiac Firebird
                     19.2
                            8 400.0 175 3.08 3.845 17.05
                                                            0
                                                               0
                                                                    3
                                                                         2
                     27.3
                            4 79.0 66 4.08 1.935 18.90
                                                                    4
Fiat X1-9
                                                               1
                                                                         1
                                                            1
                     26.0
                            4 120.3 91 4.43 2.140 16.70
                                                                    5
                                                                         2
Porsche 914-2
                                                               1
                                                                          2
Lotus Europa
                     30.4
                            4 95.1 113 3.77 1.513 16.90
                                                                    5
                            8 351.0 264 4.22 3.170 14.50
                                                                    5
Ford Pantera L
                     15.8
                                                                         4
                            6 145.0 175 3.62 2.770 15.50
                                                                    5
Ferrari Dino
                     19.7
                                                                         6
Maserati Bora
                     15.0
                            8 301.0 335 3.54 3.570 14.60
                                                                    5
                                                                         8
                                                            0
                                                               1
Volvo 142E
                     21.4
                            4 121.0 109 4.11 2.780 18.60
                                                                    4
                                                                         2
[[2]]
[1] 0 0 0 0
[[3]]
     [,1] [,2] [,3]
[1,]
        1
             0
[2,]
        0
             1
                   0
[3,]
        0
             0
                   1
```

Each element in the list is labeled as a number. It is more useful to have the elements named. An element is named by typing the name in quotes followed by the = symbol before your object in the list() function (mtcars=mtcars).

Here I am creating an object called list_one, where the first element is mtcars labeled mtcars, the second element is a vector of zeros labeled vector and the last element is the identity matrix labeled identity.'

Now create a new list called list_two and store list_one labeled as list_one and first_array labeled as array.

\$list_one \$list_one\$mtcars

#IISt_one#mccars											
	mpg	cyl	disp	hp	drat	wt	qsec	٧s	\mathtt{am}	gear	carb
Mazda RX4	21.0	6	160.0	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 Wag	21.0	6	160.0	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108.0	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258.0	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360.0	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225.0	105	2.76	3.460	20.22	1	0	3	1
Duster 360	14.3	8	360.0	245	3.21	3.570	15.84	0	0	3	4
Merc 240D	24.4	4	146.7	62	3.69	3.190	20.00	1	0	4	2
Merc 230	22.8	4	140.8	95	3.92	3.150	22.90	1	0	4	2
Merc 280	19.2	6	167.6	123	3.92	3.440	18.30	1	0	4	4
Merc 280C	17.8	6	167.6	123	3.92	3.440	18.90	1	0	4	4
Merc 450SE	16.4	8	275.8	180	3.07	4.070	17.40	0	0	3	3
Merc 450SL	17.3	8	275.8	180	3.07	3.730	17.60	0	0	3	3
Merc 450SLC	15.2	8	275.8	180	3.07	3.780	18.00	0	0	3	3
Cadillac Fleetwood	10.4	8	472.0	205	2.93	5.250	17.98	0	0	3	4
Lincoln Continental	10.4	8	460.0	215	3.00	5.424	17.82	0	0	3	4
Chrysler Imperial	14.7	8	440.0	230	3.23	5.345	17.42	0	0	3	4
Fiat 128	32.4	4	78.7	66	4.08	2.200	19.47	1	1	4	1
Honda Civic	30.4	4	75.7	52	4.93	1.615	18.52	1	1	4	2
Toyota Corolla	33.9	4	71.1	65	4.22	1.835	19.90	1	1	4	1
Toyota Corona	21.5	4	120.1	97	3.70	2.465	20.01	1	0	3	1
Dodge Challenger	15.5	8	318.0	150	2.76	3.520	16.87	0	0	3	2
AMC Javelin	15.2	8	304.0	150	3.15	3.435	17.30	0	0	3	2
Camaro Z28	13.3	8	350.0	245	3.73	3.840	15.41	0	0	3	4
Pontiac Firebird	19.2	8	400.0	175	3.08	3.845	17.05	0	0	3	2
Fiat X1-9	27.3	4	79.0	66	4.08	1.935	18.90	1	1	4	1
Porsche 914-2	26.0	4	120.3	91	4.43	2.140	16.70	0	1	5	2
Lotus Europa	30.4	4	95.1	113	3.77	1.513	16.90	1	1	5	2
Ford Pantera L	15.8	8	351.0	264	4.22	3.170	14.50	0	1	5	4
Ferrari Dino	19.7	6	145.0	175	3.62	2.770	15.50	0	1	5	6
Maserati Bora	15.0	8	301.0	335	3.54	3.570	14.60	0	1	5	8
Volvo 142E	21.4	4	121.0	109	4.11	2.780	18.60	1	1	4	2

\$list_one\$vector
[1] 0 0 0 0

```
$list_one$identity
     [,1] [,2] [,3]
[1,]
         1
               0
                     0
[2,]
         0
               1
                     0
               0
[3,]
         0
                     1
$array
, , 1
      [,1] [,2] [,3]
[1,]
         1
               1
                     1
[2,]
         1
               1
                     1
         1
               1
                     1
[3,]
, , 2
     [,1] [,2] [,3]
[1,]
         2
               2
                     2
         2
               2
                     2
[2,]
               2
         2
                     2
[3,]
, , 3
     [,1] [,2] [,3]
[1,]
         3
               3
                     3
[2,]
               3
                     3
         3
         3
               3
                     3
[3,]
```

1.6 R Packages

As I stated before, R can be extended to do more things, such as create this tutorial. This is done by installing R packages. An R package can be thought of as extra software. This allows you to do more with R. To install an R package, you will need to use install.packages("NAME_OF_PACKAGE"). Once you install it, you do not need to install it again. To use the R package, use library("NAME_OF_PACKAGE"). This allows you to load the package in R. You will need to load the package every time you start R. For more information, please watch the video: https://vimeo.com/203516241.

2 Control Flow

2.1 Indexing

2.1.1 Vectors

In the Section 1.5, we discussed about different types of R objects. For example, a vector can be a certain data type with a set number of elements. Here we construct a vector called \mathbf{x} increasing from -5 to 5 by one unit:

```
(x < -5:5)
```

The vector \mathbf{x} has 11 elements. If I want to know what the 6th element of \mathbf{x} , I can index the 6th element from a vector. To do this, we use [] square brackets on \mathbf{x} to index it. For example, we index the 6th element of \mathbf{x} :

x[6]

[1] 0

When ever we use [] next to an R object, it will print out the data to a specific value inside the square brackets. We can index an R object with multiple values:

x[1:3]

[1] -5 -4 -3

x[c(3,9)]

[1] -3 3

Notice how the second line uses the c(). This is necessary when we want to specify non-contiguous elements. Now let's see how we can index a matrix

2.1.2 Matrices

A matrix can be indexed the same way as a vector using the [] brackets. However, since the matrix is a 2-dimensional objects, we will need to include a comma to represent the different dimensions: [,]. The first element indexes the row and the second element indexes the columns. To begin, we create the following 4×3 matrix:

```
(x \leftarrow matrix(1:12, nrow = 4, ncol = 3))
```

```
[,1] [,2] [,3]
[1,]
               5
         1
[2,]
         2
               6
                     10
[3,]
         3
                7
                     11
         4
[4,]
               8
                     12
```

Now to index the element at row 2 and column 3, use x[2, 3]:

```
x[2, 3]
```

[1] 10

We can also index a specific row and column:

```
x[2,]
```

[1] 2 6 10

x[,3]

[1] 9 10 11 12

2.1.3 Data Frames

There are several ways to index a data frame, since it is in a matrix format, you can index it the same way as a matrix. Here are a couple of examples using the mtcars data frame.

```
mtcars[,2]
```

mtcars[2,]

```
mpg cyl disp hp drat \, wt qsec vs am gear carb Mazda RX4 Wag 21 6 160 110 3.9 2.875 17.02 0 1 4 4
```

However, a data frame has labeled components, variables, we can index the data frame with the variable names within the brackets:

```
mtcars[, "cyl"]
```

Lastly, a data frame can be indexed to a specific variable using the \$ notation as described in Section 1.5.5.

2.1.4 Lists

As described in Section 1.5.6, lists contain elements holding different R objects. To index a specific element of a list, you will use [[]] double brackets. Below is a toy list:

To access the second element, vector element, you can type toy_list[[2]]

```
toy_list[[2]]
```

[1] 0 0 0 0

Since the elements are labeled within the list, you can place the label in quotes inside [[]]:

```
toy_list[["vector"]]
```

[1] 0 0 0 0

The element can be accessed using the \$ notation with a list:

toy_list\$vector

```
[1] 0 0 0 0
```

Lastly, you can further index the list if needed, we can access the mpg variable in mtcars from the toy_list:

```
toy_list$mtcars$mpg
```

```
[1] 21.0 21.0 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 17.8 16.4 17.3 15.2 10.4 [16] 10.4 14.7 32.4 30.4 33.9 21.5 15.5 15.2 13.3 19.2 27.3 26.0 30.4 15.8 19.7 [31] 15.0 21.4
```

```
toy_list[["mtcars"]]$mpg
```

```
[1] 21.0 21.0 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 17.8 16.4 17.3 15.2 10.4 [16] 10.4 14.7 32.4 30.4 33.9 21.5 15.5 15.2 13.3 19.2 27.3 26.0 30.4 15.8 19.7 [31] 15.0 21.4
```

```
toy_list$mtcars[,'mpg']
```

```
[1] 21.0 21.0 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 17.8 16.4 17.3 15.2 10.4 [16] 10.4 14.7 32.4 30.4 33.9 21.5 15.5 15.2 13.3 19.2 27.3 26.0 30.4 15.8 19.7 [31] 15.0 21.4
```

2.2 If/Else Statements

In R, there are control flow functions that will dictate how a program will be executed. The first set of functions we will talk about are if and else statements. First, the if statement will evaluate a task, If the conditions is satisfied, yields TRUE, then it will conduct a certain task, if it fails, yields FALSE, the else statement will guide it to a different task. Below is a general format:

```
Important Concept

if (condition) {
   TRUE task
} else {
   FALSE task
}
```

2.2.1 Example

Below is an example where we generate x from a standard normal distribution and print the statement 'positive' or 'non-positive' based on the condition x > 0.

```
x <- rnorm(1)

## if statements
if (x > 0){
  print("Positive")
} else {
  print("Non-Positive")
}
```

[1] "Non-Positive"

What if we want to print the statement 'negative' as well if the value is negative? We will then need to add another if statement after the else statement since x > 0 only lets us know if the value is positive.

```
x <- rnorm(1)

if (x > 0){
   print("Positive")
} else if (x < 0) {
   print("Negative")
}</pre>
```

[1] "Positive"

Above, we add the if statement with condition (x < 0) indicating if the number is negative. Lastly, if x is ever 0, we will want R to let us know it is 0. We can achieve this by adding one last else statement:

```
x <- rnorm(1)

if (x > 0){
   print("Positive")
} else if (x < 0) {
   print("Negative")
} else {
   print("Zero")
}</pre>
```

[1] "Negative"

2.3 for loops

A for loop is a way to repeat a task a certain amount of times. Every time a loop repeats a task, we state it is an iteration of the loop. For each iteration, we may change the inputs by a certain way, either from an indexed vector, and repeat the task. The general anatomy of a loop looks like:

```
Important Concept

for (i in vector){
   perform task
}
```

The for statement indicates that you will repeat a task inside the brackets. The i in the parenthesis controls how the task will be completed. The in statement tells R where i can look for the values, and vectorr is a vector R object that contains the values i can be. It also controls how many times the task will be repeated based on the length of the vector.

Learning about a loop is quite challenging, my recommendation is to read the section below and break the example code so you can understand how a for loop works.

2.3.1 Basic for loop

Let's say we want R to print one to five separately. We can achieve this by repeating the print() 5 times.

```
print(1); print(2); print(3); print(4); print(5)
[1] 1
[1] 2
[1] 3
[1] 4
[1] 5
```

However, this takes quite awhile to type up. Let's try to achieve the same task using a for loop.

```
for (i in 1:5){
  print(i)
}
```

[1] 1

[1] 2

[1] 3

[1] 4

[1] 5

Here, i will take a value from the vector 1:5, Then, R will print out what the value of i is.

Now, let's try another example with letters. To begin, create a new vector called letters_10 containing the first 10 letters of the alphabet. Use the vector letters to construct the neww vector.

 $^{^{1}}$ Type this in the console to see what it is.

```
letters_10 <- letters[1:10]</pre>
```

Now, we will use a loop to print out the first 10 letters:

```
for (i in 1:10) {
  print(letters_10[i])
}
```

- [1] "a"
- [1] "b"
- [1] "c"
- [1] "d"
- [1] "e"
- [1] "f"
- [1] "g"
- [1] "h"
- [1] "i"
- [1] "j"

Here, we have i take on the values 1 through 10. Using those values, we will index the vector letters_10 by i. The resulting letter will then be printed. This task repeated 10 times.

Lastly, we can replace 1:10 by letters_10 instead:

```
for (i in letters_10){
  print(i)
}
```

- [1] "a"
- [1] "b"
- [1] "c"
- [1] "d"
- [1] "e"
- [1] "f"
- [1] "g"
- [1] "h"
- [1] "i"
- [1] "j"

This is because letters_10 are the values that we want to print and i takes on the value of letters_10 each time.

2.3.2 Nested for loops

A nested for loop is a loop that contain a loop within. Below is an example of 3 for loops nested within each other. Below is a general example:

```
Important Concept

for (i in vector_1) {
   for (ii in vector_2) {
     for (iii in vector_3) {
       perform task
     }
   }
}
```

As an example, we will use the greekLetter:: 2 and use the greek_vector vector to obtain greek letters in R. Lastly, create a vector called greek_10.

```
library(greekLetters)
greek_10 <- greek_vector[1:10]</pre>
```

For this example, we want R to print "a" and " α " together as demonstrated below³:

```
print(paste0(letters_10[1], greek_10[1]))
```

[1] "a"

Now let's repeat this process to print all possible combinations of the first 3 letters and 3 greek letters:

```
for (i in 1:3){
  for (ii in 1:3){
    print(paste0(letters_10[i], greek_10[ii]))
  }
}
```

²install.packages(greekLetters)

³We will need to use pasteO() to combine the letters together.

```
[1] "a"
[1] "a"
[1] "b"
[1] "b"
[1] "c"
[1] "c"
[1] "c"
```

2.4 break

A break statement is used to stop a loop midway if a certain condition is met. A general setup of break statement goes as follows:

```
Important Concept

for (i in vector){
  if (condition) {break}
  else {
    task
  }
}
```

As you can see there is an if statement in the loop. This is used to tell R when to break the loop. If the if statement was not there, then the loop will break without iterating.

To demonstrate the break statement, we will simulate from a N(1,1) until we have 30 positive numbers or we simulate a negative number.

```
x <- rep(NA,length = 30)

for (i in seq_along(x)){
    y <- rnorm(1,1)
    if (y<0) {
        break
    }
    else {
        x[i] <- y
    }
}
print(x)</pre>
```

F.4.7		***	27.4		37.4		***
[1] (0.2822247	NA	NA	NA	NA	NA	NA
[8]	NA	NA	NA	NA	NA	NA	NA
[15]	NA	NA	NA	NA	NA	NA	NA
[22]	NA	NA	NA	NA	NA	NA	NA
[29]	NA	NA					

```
print(y)
```

```
[1] -0.06732581
```

Notice that the vector does not get filled up all the way, that is because the loop will break once a negative number is simulated

2.5 next

Similar to the break statement, the next statement is used in loops that will tell R to move on to the next iteration if a certain condition is met.

```
Important Note

for (i in vector){
   if (condition) {
     next
   } else {
     task
   }
}
```

The main difference here is that a next statement is used instead of a break statement.

Going back to simulating positive numbers, we will use the same setup but change it to a next statement.

```
x <- rep(NA,length = 30)

for (i in seq_along(x)){
   y <- rnorm(1,1)
   if (y<0) {</pre>
```

```
next
}
else {
    x[i] <- y
}
print(x)</pre>
```

```
[1] 1.7209191 0.1896949 NA 1.0792022 NA 2.1369064 0.6085387 [8] NA 0.5623279 2.4101566 3.2359326 1.4701157 0.6353537 2.6892720 [15] NA 0.2331778 3.0216481 NA 1.6867428 1.0063384 0.6367926 [22] NA 3.4886272 1.3408562 0.3545091 1.5495891 0.8707791 NA [29] 1.5991112 1.3069543
```

As you can see, the vector contains missing values, these were the iterations that a negative number was simulated.

2.6 while loop

The last loop that we will discuss is a while loop. The while loop is used to keep a loop running until a certain condition is met. To construct a while loop, we will use the while statement with a condition attached to it. In general, a while loop will have the following format:

```
Important Concept

while (condition) {
  task
  update condition
}
```

Above, we see that the while statement is used followed by a condition. Then the loop will complete its task and update the condition. If the condition yields a FALSE value, then the loop will stop. Otherwise, it will continue.

2.6.1 Basic while loops

To implement a basic while loop, we will work on the previous example of simulating positive numbers. We want to simulate 30 positive numbers from N(0,1) until we have 30 values. Here, our condition is that we need to have 30 numbers. Therefore we can use the following code to simulate the values:

```
x <- c()
size <- 0
while (size < 30){
    y <- rnorm(1)
    if (y > 0) {
        x <- c(x, y)
    }
    size <- length(x)
}
print(size)</pre>
```

[1] 30

```
print(x)
```

```
[1] 0.27075614 0.68213351 0.64117300 0.09325178 0.25511193 0.84847289 [7] 0.99696727 0.49154805 1.12825620 0.03624028 0.64491023 1.61245622 [13] 0.46394449 0.05552212 0.39188109 0.50643163 0.47071310 1.19085171 [19] 0.02597452 1.33588515 0.24634318 0.28013134 0.04718407 1.46137496 [25] 0.85088606 0.31027703 1.06482412 0.28022502 1.31905554 0.28745050
```

Notice that we do not use an **else** statement. This is because we do not need R to complete a task if the condition fails.

2.6.2 Infinite while loops

With while loops, we must be weary about potential infinite loops. This occurs when the condition will never yield a FALSE value. Therfore, R will never stop the loop because it does not know when to do this.

For example, let's say we are interest if y = sin(x) will converge to a certain value. As you know it will not converge to a certain value; however, we can construct a while loop:

```
x <- 1
diff <- 1
while (diff > 1e-20) {
  old_x <- x
  x <- x + 1
  diff <- abs(sin(x) - sin(old_x))
}</pre>
```

```
print(x)
print(diff)
```

My condition above is to see if the absolute difference between sequential values is smaller than 10^{-20} . As you may know, the absolute difference will never become that small. Therefore, the loop will continue on without stopping.

To prevent an infinite while loop, we can add a counter to the condition statement. This counter will also need to be true for the loop to continue. Therefore, we can arbitrarily stop it when the loop has iterated a certain amount of times. We just need to make sure to add one to the counter every time it iterates it. Below is the code that adds a counter to the while loop:

```
x <- 1
counter <- 0
diff <- 1
while (diff > 1e-20 & counter < 10^3) {
  old_x <- x
    x <- x + 1
  diff <- abs(sin(x) - sin(old_x))
  counter <- counter + 1
}
print(x)</pre>
```

[1] 1001

```
print(diff)
```

[1] 0.09311106

```
print(counter)
```

[1] 1000

3 Functional Programming

3.1 Functions

The functionality in R is what makes it completely powerful compared to other statistical software. There are several pre-built functions, and you can extend R's functionality further with the use of R Packages.

3.1.1 Built-in Functions

There are several available functions in R to conduct specific statistical methods. The table below provides a set of commonly used functions:

Functions	Description
aov()	Fits an ANOVA Model
lm()	Fits a linear model
glm()	Fits a general linear model
t.test()	Conducts a t-test

Several of these functions have help documentation that provide the following sections:

Section	Description
Description	Provides a brief introduction of the function
Usage	Provides potential usage of the function
Arguments	Arguments that the function can take
Details	An in depth description of the function
Value	Provides information of the output produced by the function
Notes	Any need to know information about the function
Authors	Developers of the function
References	References to the model and function
See Also	Provide information of supporting functions
Examples	Examples of the function

To obtain the help documentation of each function, use the ? operator and function name in the console pane.

3.1.2 Generic Functions

Commonly used functions, such as summary() and plot() functions, are considered generic functions where their functionality is determined by the class of an R object. For example, the summary() function is a generic function for several types of functions: summary.aov(), summary.lm(), summary.glm(), and many more. Therefore, the appropriate function is needed depending the type of R object. This is where generic functions come in. We can use a generic function, ie summary(), to read the type of object and then apply to correct procedure to the object.

3.1.3 User-built Functions

While R has many capable functions that can be used to analyze your data, you may need to create a custom function for specific needs. For example, if you find yourself writing the same to repeat a task, you can wrap the code into a user-built function and use it for analysis.

To create a user-built function, you will using the function() to create an R object that is a function. To use the function Inside the funtion() parentheses, write the arguments that need to specified for your function. These are arguments you choose for the function.

3.1.3.1 Anatomy

In general function we construct a function with the following anatomy:

Here, we are creating an R function called name_of_function that will take the following arguments: data_1, data_2, argument_1, argument_2, argument_3, and From this function, it requires us to supply data for data_1 and argument_1. Arguments data_2 and argument_3 are not required, but can be utilized in the function if necessary. Argument argument_2 is also required for the function, but it it has a default setting (in this case TRUE)

if it is not specified. Lastly, the ... argument allows you to pass other arguments to R built in functions if they are present. For example, we may use the plot() to create graphics and want to manipulate the output plot further, but do not want to specify the arguments in the user-based function. In the function itself, we will complete the necessary tasks and then use the return() to return the output.

3.1.3.2 Example

To begin, let's create a function that squares any value:

```
x_{\text{square}} \leftarrow \text{function}(x)\{x^2\}
```

Above, I am creating a new function called x_{square} and it will take values of x and square it. Here are a couple of examples of x_{square} ():

```
x_square(4)
```

[1] 16

```
x_square(5)
```

[1] 25

The mtcars data set has several numeric variables that can be used for analysis. Let's say we want to apply a function (x_square()) to the sum of a specific variable and return the value. Then let's further complicate the function by allowing the sum of 2 variables, take the log of the sum and dividing the value if necessary. Below is the code for such function called summing:

```
summing <- function(vec1, vec2 = NULL, FUN, log_val = FALSE, divisor_val = NULL){
  FUN <- match.fun(FUN)
  wk_vec <- c(vec1, vec2)
  fun_sum_val <- FUN(sum(wk_vec))
  lval <- NULL
  if (isTRUE(log_val)){
    lval <- log(fun_sum_val)
  } else {
    lval <- fun_sum_val
}</pre>
```

```
if (!is.null(divisor_val)){
  dval <- divisor_val</pre>
} else {dval <- 1}</pre>
output <- lval/dval
return(output)
```

Now let's try obtaining the

```
sum(mtcars$mpg)^2
[1] 413320.4
summing(mtcars$mpg, FUN = x_square)
[1] 413320.4
log(sum(c(mtcars$mpg,mtcars$disp))^2)
[1] 17.98088
summing(mtcars$mpg, mtcars$disp, x_square, T)
[1] 17.98088
log(sum(c(mtcars$mpg,mtcars$disp))^2)/5
[1] 3.596177
summing(mtcars$mpg, mtcars$disp, x_square, T, 5)
```

[1] 3.596177

3.2 *apply Functions

*apply functions are used to iterate a function through a set of elements in a vector, matrix, or list. This will then return a vector or list depending on what is requested.

3.2.1 apply()

The apply() function is used to apply a function to the margins of an array or matrix. It will iterate between the elements, apply a function to the data, and return a vector, array or list if necessary. To use the apply() function, you will need to specify three arguments, X or the array, MARGIN which margin to apply the function on, and FUN the function.

Below we calculate the row means and column means using the apply function for a 5×4 matrix containing the elements 1 through 20:

```
x <- matrix(1:20, nrow = 5, ncol = 4)
# Row Means
apply(x, 1, mean)</pre>
```

[1] 8.5 9.5 10.5 11.5 12.5

```
# Col Means
apply(x, 2, mean)
```

[1] 3 8 13 18

3.2.2 lapply()

The lapply() function is used to apply a function to all elements in a vector or list. The lapply() function will then return a list as the output.

3.2.3 sapply()

The sapply() function is used to apply a function to all elements in a vector or list. Afterwards, the sapply() will return a "simplified" version of the list format. This could be a vector, matrix, or array.

3.3 Anonymous Functions

Anonymous functions are functions that R temporarily creates to conduct a task. They are commonly used in the *apply functions, piping or within functions. To create an anonymous function, we use the function() to create a function.

For example, let x be a vector with the values 1 through 15. Let's say we want to apply the function $f(x) = x^2 + \ln(x) + e^x/x!$. We can evaluate the function as the expression in the function:

```
x <- 1:15
x^2 + \log(x) + \exp(x)/factorial(x)
```

- [1] 3.718282 8.387675 13.446202 19.661217 27.846214 38.352077
- [7] 51.163496 66.153374 83.219555 102.308655 123.399395 146.485246
- [13] 171.565020 198.639071 227.708053

Let's say we could not do that, we need to evaluate the function for each value of x. We can use the sapply() function with an anonymous function:

```
sapply(x, function(x) x^2 + \log(x) + \exp(x) / factorial(x))
```

- [1] 3.718282 8.387675 13.446202 19.661217 27.846214 38.352077
- [7] 51.163496 66.153374 83.219555 102.308655 123.399395 146.485246
- [13] 171.565020 198.639071 227.708053

In R 4.1.0, developers introduce a shortcut approach to create functions. You can create a function using \() expression, and specify the arguments for your function within the parenthesis. Reworking the previous code, we can use \() instead of function():

```
sapply(x, (x) x^2 + \log(x) + \exp(x)/factorial(x))
```

- [1] 3.718282 8.387675 13.446202 19.661217 27.846214 38.352077
- [7] 51.163496 66.153374 83.219555 102.308655 123.399395 146.485246
- [13] 171.565020 198.639071 227.708053

```
sapply(x, (.) .^2 + log(.) + exp(.)/factorial(.))
```

- [1] 3.718282 8.387675 13.446202 19.661217 27.846214 38.352077
- [7] 51.163496 66.153374 83.219555 102.308655 123.399395 146.485246
- [13] 171.565020 198.639071 227.708053

Notice that the argument in the anonymous function can be anything.

4 Scripting and Piping in R

4.1 Commenting

A comment is used to describe your code within an R Script. To comment your code in R, you will use the # key, and R will not execute any code after the symbol. The # key can be used to anywhere in the line, from beginning to midway. It will not execute any code coming after the #.

Additionally, commenting is a great way to debug long scripts of code or functions. You comment certain lines to see if any errors are being produced. It can be used to test code line by line with out having to delete everything.

4.2 Scripting

When writing a script, it is important to follow a basic structure for you to follow your code. While this structure can be anything, the following sections below has my main recommendations for writing a script. The most important part is the **Beginning of the Script** section.

4.2.1 Beginning of the Script

Load any R packages, functions/scripts, and data that you will need for the analysis. I always like to get the date and time of the

```
## Todays data
analysis_data <- format(Sys.time(),"%Y-%m-%d-%H-%M")

## R Packages
library(tidyverse)
library(magrittr)

## Functions
source("fxs.R")</pre>
```

```
Rcpp::sourceCpp("fxs.cpp")
## Data
df1 <- read_csv("file.csv")
df2 <- load("file.RData") %>% get
```

4.2.2 Middle of the Script

Run the analysis, including pre and post analysis.

```
## Pre Analysis
df1_prep <- Prep_data(df1)
df2_prep <- Prep_data(df2)

## Analysis
df1_analysis <- analyze(df1_prep)
df2_analysis <- analyze(df2_prep)

## Post Analysis
df1_post <- Prep_post(df1_anlysis)
df2_post <- Prep_post(df2_anlysis)</pre>
```

4.2.3 End of the Script

Save your results in an R Data file:

4.3 Pipes

In R, pipes are used to transfer the output from one function to the input of another function. Piping will then allow you to chain functions to run an analysis. Since R 4.1.0, there are two version of pipes, the base R pipe and the pipes from the magrittr package. The table below provides a brief description of each type pipes

Pipe	Name	Package	Description
>	R Pipe	Base	This pipe will use the output of the previous function as the input for the first argument following function.
%>%	Forward Pipe	magrittr	The forward pipe will use the output of the previous function as the input of the following function.
%\$ 5	Exposition Pipe	magrittr	The exposition function will expose the named elements of an R object (or output) to the following function.
%T>%	Tee Pipe	magrittr	The Tee pipe will evaluate the next function using the output of the previous function, but it will not retain the output of the next function and utilize the output of the previous function.
%<>%	Assignment Pipe	magrittr	The assignment pipe will rewrite the object that is being piped into the next function.

When choosing between Base or magrittr's pipes, I recommend using magrittr's pipes due to the extended functionality. However, when writing production code or developing an R package, I recommend using the Base R pipe.

Lastly, when using the pipe, I recommend only stringing a limited amount of functions (\sim 10) to maintain code readability and conciseness. Any more functions may make the code incoherent.

If you plan to use magrittr's pipe, I recommend loading magrittr package instead of tidyverse package.

library(magrittr)

4.3.1 |>

The base pipe will use the output from the first function and use it as the input of the first argument in the second function. Below, we obtain the mpg variable from mtcars and pipe it in the mean() function.

```
mtcars$mpg |> mean()
```

[1] 20.09062

4.3.2 %>%

4.3.2.1 Uses

Magrittr's pipe is the equivalent of Base R's pipe, with some extra functionality. Below we repeat the same code as before:

```
mtcars$mpg %>% mean()
```

[1] 20.09062

Alternatively, we do not have to type the parenthesis in the second function:

```
mtcars$mpg %>% mean
```

[1] 20.09062

Below is another example where we will pipe the value 3 into the rep() with times=5, this will repeat the value 3 five times:

```
3 %>% rep(5)
```

[1] 3 3 3 3 3

If we are interested in piping the output to another argument other than the first argument, we can use the (.) placeholder in the second function to indicate which argument should take the previous output. Below, we repeat the vector c(1, 2) three times because the . is in the second argument:

```
3 %>% rep(c(1,2), .)
```

[1] 1 2 1 2 1 2

4.3.2.2 Creating Unary Functions

You can use %>% and . to create unary functions, a function with one argument, can be created. The following code will create a new function called logsqrt() which evaluates $\sqrt{\log(x)}$:

```
logsqrt <- . %>% log(base = 10) %>% sqrt
logsqrt(10000)
```

[1] 2

```
sqrt(log10(10000))
```

[1] 2

4.3.3 %\$%

The exposition pipe will expose the named elements of an object or output to the following function. For example, we will pipe the mtcars into the lm() function. However, we will use the %\$% pipe to access the variables in the data frame for the formula= argument without having to specify the data= argument:

```
mtcars %$% lm(mpg ~ hp)
```

4.3.4 %T>%

x_lm <- mtcars %\$% lm(mpg ~ hp) %T>%

The Tee pipe will pipe the contents of the previous function into the following function, but will retain the previous functions output instead of the current function. For example, we use the Tee pipe to push the results from the lm() function to print out the summary table, then use the same lm() function results to print out the model standard error:

```
(\(x) print(summary(x))) \%T>\%
  (\(x) print(sigma(x)))
Call:
lm(formula = mpg ~ hp)
Residuals:
             1Q Median
                             3Q
    Min
                                    Max
-5.7121 -2.1122 -0.8854 1.5819 8.2360
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 30.09886
                        1.63392 18.421 < 2e-16 ***
            -0.06823
                        0.01012 -6.742 1.79e-07 ***
hp
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 3.863 on 30 degrees of freedom
                                Adjusted R-squared:
Multiple R-squared: 0.6024,
F-statistic: 45.46 on 1 and 30 DF, p-value: 1.788e-07
[1] 3.862962
```

4.4 Keyboard Shortcuts

Below is a list of recommended keyboard shortcuts:

Shortcut	Windows/Linux	Mac
%>%	Ctrl+Shift+M	Cmd+Shift+M
Run Current Line	Ctrl+Enter	Cmd+Return
Run Current Chunk	Ctrl+Shift+Enter	$\operatorname{Cmd}+\operatorname{Shift}+\operatorname{Enter}$

Shortcut	Windows/Linux	Mac
Knit Document	Ctrl+Shift+K	Cmd+Shift+K
Add Cursor Below	Ctrl+Alt+Down	Cmd+Alt+Down
Comment Line	Ctrl+Shift+C	Cmd+Shift+C

I recommend modify these keyboard shortcuts in RStudio

Shortcut	Windows/Linux	Mac
%in%	Ctrl+Shift+I	Cmd+Shift+I
%\$%	Ctrl+Shift+D	Cmd+Shift+D
%T>%	Ctrl+Shift+T	Cmd+Shift+T

Note you will need to install the extraInserts package:

remotes::install_github('konradzdeb/extraInserts')

5 Further Resources

5.1 R Resources

5.1.1 Programming

Advanced R Efficient Prograaming in R

5.1.2 Reticulate and Python

Reticulate

5.1.3 Rcpp

Rcpp Website

5.2 Bayesian Programs

5.2.1 JAGS

JAGS rjags

5.2.2 Stan

Stan cmdstanr

5.3 Misc

5.3.1 Missing Semester

This is a great website containing basic information that you may need to know.

Part II Random Variables and Simulations

6 Random Variables

- **6.1 Random Experiments**
- 6.2 Probability
- 6.3 Independence
- 6.4 Random Variables
- 6.4.1 Discrete RV
- 6.4.1.1 Probability Mass Functions
- 6.4.1.2 Expectation
- **6.4.1.3** Variance
- **6.4.1.4 Moment-Generating Functions**
- 6.4.2 Continuous RV
- 6.4.2.1 Probability Density Functions
- 6.4.2.2 Expectation
- **6.4.2.3** Variance
- 6.4.2.4 Moment-Generating Functions
- 6.5 Joint Distributions
- 6.5.1 Joint Probability Density Function
- **6.5.2 Conditional Density Functions**
- 6.5.3 Marginal Density Functions
- **6.5.4 Independence and Covariance**
- 6.6 Functions of Random Variables
- 6.6.1 Method of Distribution Functions
- 6.6.2 Method of Transformations
- 6.6.3 Method of Moment-Generating Functions

7 Models

7.1	Bernoulli	Model

- 7.1.1 Distribution Functions
- 7.1.2 Expected Value
- 7.1.3 Variance

7.2 Binomial Model

- 7.2.1 Distribution Functions
- 7.2.2 Expected Value
- 7.2.3 Variance

7.3 Poisson Model

- 7.3.1 Distribution Functions
- 7.3.2 Expected Value
- 7.3.3 Variance

7.4 Negative Binomial Model

- 7.4.1 Distribution Functions
- 7.4.2 Expected Value
- 7.4.3 Variance

7.5 Multinomial Model

- 7.5.1 Distribution Functions
- 7.5.2 Expected Value
- 7.5.3 Variance

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7.6 Uniform Model

- 7.6.1 Distribution Functions
- 7.6.2 Expected Value

8 Random Number Generator

- 8.1 Random Number Generation
- 8.2 Computer Random Number Generation
- 8.2.1 Linear Congruential Generators
- 8.2.2 Multiple Recursive Generators
- 8.2.3 Modulo 2 Linear Generators

9 Monte Carlo Methods

Monte Carlo Methods are used to determine the

- 9.1 Probability Inverse Transformation
- 9.2 Composition Method
- 9.3 Acceptance-Rejection Method
- 9.4 Box-Muller Methods

10 Markov Chain Monte Carlo Methods

Part III Randomizations

11 Permutation Tests

12 Permutation Regression

Part IV Monte Carlo Methods

13 Monte Carlo Integration

14 Monte Carlo Hypothesis Testing

15 Monte Carlo Optimization

16 Monte Carlo Methods Case Study 1

17 Monte Carlo Methods Case Study 2

18 Monte Carlo Methods Case Study 3

Part V Bootstrapping

19 Parametric Bootrapping

20 Nonparametric Boostrapping

Part VI

Data Manipulation, Summarization, and Graphics

Resources

How to read this section.

Through out this Section, we use certain notations for different components in R. To begin, when something is in a gray block, _, this indicates that R code is being used. When I am talking about an R Object, it will be displayed as a word. For example, we will be using the R object mtcars. When I am talking about an R function, it will be displayed as a word followed by an open and close parentheses. For example, we will use the mean function denoted as mean() (read this as "mean function"). When I am talking about an R argument for a function, it will be displayed as a word following by an equal sign. For example, we will use the data argument denoted as data= (read this as "data argument"). When I am referencing an R package, I will use :: (two colons) after the name. For example, in this Section, I will use the ggplot2:: (read this as "ggplot2 package") Lastly, if I am displaying R code for your reference or to run, it will be displayed on its own line. There are many components in R, and my hope is that this will help you understand what components am I talking about.

21 Importing Data

21.1 Directories

21.2 Importing Data

```
# Reading Data ----
## RData ----
load("~/x.RData")
## CSV ----
library(readr)
data_3_1_csv <- read_csv("student/stat_147/data/data_3_1.csv")</pre>
View(data_3_1_csv)
## Excel ----
library(readxl)
data_3_1 <- read_excel("student/stat_147/data/data_3_1.xlsx")</pre>
View(data_3_1)
## txt ----
library(readr)
data_3_1_s <- read_table2("student/stat_147/data/data_3_1_s.txt")</pre>
View(data_3_1_s)
## Semi-colon ----
library(readr)
data_3_1_sc <- read_delim("student/stat_147/data/data_3_1_sc.txt", ";", escape_double = FALS</pre>
View(data_3_1_sc)
## SPSS ----
library(haven)
data_3_1 <- read_sav("student/stat_147/data/data_3_1.sav")</pre>
View(data_3_1)
```

```
## SAS ----
library(haven)
data_3_1 <- read_sas("student/stat_147/data/data_3_1.sas7bdat", NULL)</pre>
View(data_3_1)
## Stata ----
library(haven)
data_3_1 <- read_dta("student/stat_147/data/data_3_1.dta")</pre>
View(data_3_1)
data_3_1 <- read.csv("~/student/stat_147/data/data_3_1.csv", header=FALSE)</pre>
View(data_3_1)
# Reading Data ----
setwd("~/Repos/s147/files/Week_2")
## Base R ----
# CSV
data.csv <- read.csv("data.csv")</pre>
# STATA File
library(foreign)
read.dta("data.dta")
## RStudio packages
library(readr)
read_csv("data.csv")
library(readxl)
read_excel("data.xlsx")
library(haven)
read_dta("data.dta")
```

22 Data Manipulation

Data manipulation consists of transforming a data set to be analyzed. Certain statistical methods require data sets to be formatted in a certain way before you can apply a certain function¹. Other times, you will need to transform the data set to present to stakeholder. Therefore, being able to transform a data set is essential.

Warnings Suppressed

In order to keep the page concise, the warning messages have been suppressed. These warnings were produced because functions were applied to incorrect inputs, ie \sqrt{A} . Therefore, you may see NA as the output. There is nothing wrong with the code, it is just that the input was not valid, but R still completed the task.

22.1 Tidyverse

Tidyverse is a set of packages that make data manipulation much easier. These are functions that many individuals from the R community find useful to use for data analysis. In my opinion, once you have understand how Tidyverse packages function, it makes it much easier to work with than Base R. Many of the functions are descriptively named for easy remembrance. For the most part, you can do almost everything that Base R can do. There are just a few things you can't do, but it is rare that you will use them. One last thing is that the output from tidyverse is always formatted as a tibble class, the Tidyverse version of the data frame. This can have some ups and downs. However, think of a tibble as a lazier data frame. If you haven't done so, install tidyverse:

install.packages("tidyverse")

Then load tidyverse into R:

library(tidyverse)

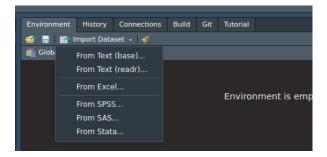
This will load the main Tidyverse packages: ggplot2, tibble, tidyr, readr, purr, dplyr, stringr, and forcats.

¹Linear Mixed-Effects Models.

22.2 Loading Data

There are three methods to load a data set in R: using base R, using Tidyverse, or using RStudio. While it is important to understand how the code works to load a data set, I recommend using RStudio to import the data. It does all the work for you. Additionally, if you decide to use Tidyverse packages, RStudio will provide corresponding code for a particular file.

To import a data set using RStudio, head over to the environment tab (usually in the upper right hand pane) and click on the Import Dataset button. A pop-up window should look something like below.



Notice how there are several options to load a data set. Depending on the format, you may want to choose one of those options. Next, notice how there are 2 "From Text". This is because it will load text data using either Base R packages or the readr package from tidyverse. Either works, but the readr package provides the necessary code to load the data set in the window. The other one provides the code in the console.

22.2.1 CSV Files

A CSV file is a type of text file that where the values are separated from commas. It is very common file that you will work with. Here I will provide the code necessary to import a CSV file using either Base R or readr package code.

22.2.1.1 Base R

read.csv("FILE_NAME_AND_LOCATION")

22.2.1.2 readr package

```
read_csv("FILE_NAME_AND_LOCATION")
```

Notice that the functions are virtually the same.

22.2.2 For This Chapter

You will need to download and extract this zip file to conduct the analysis in the chapter. The code below will load the data sets you need:

```
data1 <- read_csv("data/data_3_1.csv")
data2 <- read_csv("data/data_3_2.csv")
data3 <- read_csv("data/data_3_3.csv")
data4 <- read_csv("data/data_3_6.csv")
data5 <- read_csv("data/data_3_7.csv")
data6 <- read_csv("data/data_3_5.csv")
data7 <- read_csv("data/data_3_4.csv")</pre>
```

Make sure to change the file location as needed.

22.3 The Pipe Operator |>

The main benefit of the pipe operator is to make the code easier to read. The base pipe |> was added in R 4.0. What the pipe operator, |>, does is that it will take the output from a previous function and it will use it as the input for the next function. This prevents us from nesting functions together and overwhelm us with numerous parentheses and commas. To practice, pipe data into the glimpse().

```
data1 |> glimpse()
```

The glimpse() provides basic variable information about data1. I recommend practice reading the code in plain English to help you understand how these functions.

22.4 Data Transformation

This section focuses on manipulating the data to obtain basic statistics, such as obtaining the mean for different categories. Many of the functions used here are from the dplyr package.

22.4.1 Summarizing Data

Summarizing Data is one of the most important thing in statistics. First, let's get the mean for all the variables in data1. This is done by using the summarize_all(). All you need to do is provide the function you want R to provide. Pipe data1 into the summarize_all() and specify mean in the function.

```
data1 |> summarise_all(mean)

# A tibble: 1 x 10
    ID1 cat1 cat2    var1 var2 var3 var4 var5 var6 var7
    <dbl> >dbl> <dbl> <dbl>
```

Notice how some values are NA, this is because the variables are character data types. Therefore, it will not be able to compute the mean. Now find the standard deviation for the data set.

```
data1 |> summarise all(sd)
# A tibble: 1 x 10
  ID1
      cat1
         cat2
             var1
                 var2
                      var3
                          var4
                               var5
                                   var6
 1
   NA
       NA
              1.00 2.22 1.02 1.00 3.93
                                     0 0.489
```

Now lets create a frequency table for the cat1 variable in data1. use the count() and specify the variable you are interested in:

data1 |> count(cat1)

Now, repeat for cat2 in data1:

data1 |> count(cat2)

22.4.2 Grouping

Summarizing data is great, but sometimes you may want to group data and obtain summary statistics for those groups. This is done by using the <code>group_by()</code> and specify which variable you want to group. Try grouping data1 by cat1:

data1 |> group_by(cat1)

```
# A tibble: 1,000 x 10
# Groups:
            cat1 [3]
   ID1
             cat1
                  cat2
                           var1 var2
                                          var3
                                                 var4
                                                         var5
                                                              var6 var7
   <chr>
             <chr> <chr>
                           <dbl> <dbl>
                                         <dbl>
                                                <dbl>
                                                       <dbl> <dbl> <dbl>
1 A2b6115fd A
                   Ε
                           1.15
                                     4
                                        2.88
                                               3.54
                                                       -3.18
                                                                        1
2 Ac51c9cf1 A
                         -0.367
                                     3 0.0640 1.07
                   D
                                                       -3.18
                                                                  0
                                                                        0
3 A7534d3a0 A
                   F
                         -0.420
                                     6 -1.04
                                               0.226
                                                      -3.18
                                                                  0
                                                                        0
4 A73fc5642 A
                   F
                         -2.00
                                     5 -0.314 0.0213 -3.18
                                                                        0
                                                                  0
5 Ae020e4bd C
                   Ε
                          0.697
                                     3 0.526 2.98
                                                        6.06
                                                                  0
                                                                        0
```

```
6 AcOd3b0fe A
                            0.467
                                          2.45
                                                  1.85
                                                                            0
                    D
                                                          -3.18
                                                                      0
 7 A2edfed41 A
                                          0.514
                    Ε
                            1.36
                                                  0.529
                                                          -3.18
                                                                      0
                                                                            1
8 Ad38a4bbe C
                    F
                            0.369
                                          1.98
                                                  2.36
                                                           6.06
                                                                            1
                                                                      0
 9 A5eeOf97f B
                            1.80
                                       5
                                          0.147
                                                  2.22
                                                          -0.701
                                                                      0
                                                                            0
                    Ε
10 Ad791c03d C
                                       3 -1.05
                                                                            1
                    Ε
                            1.25
                                                  0.0289
                                                          6.06
                                                                      0
# i 990 more rows
```

Great! You now have grouped data; however, this is not helpful. We can use this output and summarize the groups. All we need to do is pipe the output to the summarise_all(). Group data1 by cat1 and find the mean:

```
data1 |> group_by(cat1) |> summarise_all(mean)
```

```
# A tibble: 3 x 10
  cat1
          ID1
               cat2
                        var1
                              var2
                                    var3
                                           var4
                                                   var5
                                                         var6
  <chr> <dbl> <dbl>
                       <dbl> <dbl> <dbl> <dbl> <
                                                  <dbl> <dbl> <dbl>
1 A
           NA
                  NA -0.0369
                              4.79 0.877
                                           1.97 -3.18
                                                             0 0.401
2 B
           NA
                  NA -0.0345
                              4.98 1.01
                                           1.97 -0.701
                                                             0 0.390
3 C
           NA
                  NA -0.0292
                              5.05 0.922
                                           1.94 6.06
                                                             0 0.391
```

If we want to group by two variables, all we need to do is specify both variables in the group_by(). Group data1 by cat1 and cat2 then find the mean:

```
data1 |> group_by(cat1,cat2) |> summarise_all(mean)
```

```
# A tibble: 9 x 10
# Groups:
            cat1 [3]
  cat1
        cat2
                 ID1
                                             var4
                                                     var5
                                                           var6
                          var1
                                var2 var3
                                                                 var7
  <chr> <chr> <dbl>
                         <dbl> <dbl> <dbl> <dbl> <dbl>
                                                    <dbl> <dbl> <dbl>
1 A
        D
                  NA -0.0186
                                4.87 0.858
                                             1.93 - 3.18
                                                              0 0.374
2 A
        Ε
                 NA -0.0265
                                4.70 0.882
                                             1.94 -3.18
                                                              0 0.393
3 A
                                             2.03 - 3.18
        F
                 NA -0.0661
                                4.79 0.890
                                                              0 0.436
4 B
        D
                 NA -0.152
                                5.21 1.01
                                             1.96 -0.701
                                                              0 0.333
5 B
        Ε
                 NA 0.0890
                                5.04 1.04
                                             1.94 -0.701
                                                              0 0.417
6 B
        F
                 NA -0.0659
                                             2.03 -0.701
                                4.72 0.979
                                                              0 0.411
7 C
        D
                 NA -0.160
                                5.01 0.927
                                             1.87
                                                    6.06
                                                              0 0.378
8 C
        Ε
                  NA -0.000228
                                             2.00
                                                              0 0.345
                                5.07 0.910
                                                    6.06
9 C
        F
                  NA 0.0662
                                5.07 0.930
                                             1.94 6.06
                                                              0 0.445
```

Now, instead of finding the mean for all variables in a data set, we are only interested in viewing var1. We can use the summarise() and type the R code for finding the mean for the particular variable. Group data1 by cat1 and find the mean for var1:

data1 |> group_by(cat1) |> summarise(mean(var1))

22.4.3 Subsets

On occasion, you may need to create a subset of your data. You may only want to work with one part of your data. To create a subset of your data, use the filter() to create the subset. This will select the rows that satisfy a certain condition. Create a subset of data1 where only the positive values of var1 are present. Use the filter() and state var1>0.

data1 |> filter(var1>0)

```
# A tibble: 484 x 10
   ID1
              cat1
                     cat2
                            var1
                                   var2
                                            var3
                                                    var4
                                                            var5
                                                                  var6
                                                                         var7
   <chr>
              <chr> <chr> <dbl> <dbl>
                                           <dbl>
                                                   <dbl>
                                                           <dbl> <dbl>
                                                                        <dbl>
 1 A2b6115fd A
                     Ε
                                          2.88
                                                          -3.18
                                                                      0
                           1.15
                                       4
                                                  3.54
                                                                             1
 2 Ae020e4bd C
                     Ε
                           0.697
                                       3
                                          0.526
                                                  2.98
                                                           6.06
                                                                      0
                                                                            0
 3 AcOd3b0fe A
                                          2.45
                                                                            0
                     D
                           0.467
                                       4
                                                  1.85
                                                          -3.18
                                                                      0
 4 A2edfed41 A
                     Ε
                           1.36
                                       5
                                          0.514
                                                  0.529
                                                         -3.18
                                                                      0
                                                                             1
 5 Ad38a4bbe C
                     F
                           0.369
                                      0
                                          1.98
                                                  2.36
                                                           6.06
                                                                             1
6 A5eeOf97f B
                     Ε
                           1.80
                                       5
                                          0.147
                                                  2.22
                                                          -0.701
                                                                      0
                                                                             0
7 Ad791c03d C
                     Ε
                           1.25
                                       3 -1.05
                                                  0.0289
                                                          6.06
                                                                      0
                                                                             1
8 Af88d3ab5 B
                     Ε
                                          3.07
                                                  3.29
                                                          -0.701
                           2.10
                                      8
                                                                      0
                                                                             1
9 A429b65a6 A
                                                                             0
                     Ε
                           1.46
                                          0.0638 2.36
                                                          -3.18
                                                                      0
10 A3638155a A
                     F
                           0.429
                                       5
                                          1.76
                                                  1.55
                                                          -3.18
                                                                      0
                                                                             1
# i 474 more rows
```

If you know which rows you want, you can use the slice() and specify the rows as a vector. Create a subset of data1 and select the rows 100 to 200 and 300 to 400.

data1 |> slice(c(100:200, 300:400))

```
# A tibble: 202 x 10
   ID1
              cat1
                    cat2
                             var1
                                   var2
                                           var3
                                                    var4
                                                           var5
                                                                 var6
                                                                        var7
   <chr>
              <chr> <chr>
                            <dbl> <dbl>
                                          <dbl>
                                                   <dbl>
                                                          <dbl> <dbl> <dbl>
 1 A568e9a48 A
                            1.88
                                          2.59
                    Ε
                                       6
                                                4.02
                                                         -3.18
                                                                     0
                                                                            1
                                                         -0.701
                            1.32
                                                                            1
2 Aa77dca83 B
                    D
                                       5
                                          0.889 3.12
                                                                     0
3 A901d56c2 C
                    F
                           -0.406
                                          0.496 3.67
                                                          6.06
                                                                     0
                                                                           0
4 Ad66ce513 A
                    D
                            1.04
                                          0.331 0.00523 -3.18
                                                                           0
5 A897a230d B
                    Ε
                           -0.616
                                          1.61 3.08
                                                         -0.701
                                                                     0
                                                                           0
6 Afbc693a4 B
                           -0.404
                                       7 -0.604 0.149
                    F
                                                         -0.701
                                                                     0
                                                                           1
7 Ae7269323 C
                    F
                           -0.176
                                          1.06 2.26
                                                          6.06
                                                                     0
                                                                           0
8 A182729af A
                    D
                            1.11
                                       7 -0.297 1.45
                                                         -3.18
                                                                     0
                                                                           1
                                          1.78 3.07
9 A1a06950b C
                    Ε
                           -1.29
                                       5
                                                          6.06
                                                                     0
                                                                            1
                                                                            0
10 A569c9d81 A
                    F
                            1.28
                                          0.683 1.53
                                                         -3.18
                                                                     0
# i 192 more rows
```

If you need random sample of your data1, use the slice_sample(n = N) and specify the number you want. It will create a data set of randomly selected rows. Create a random sample of data1 of 100 rows.

data1 |> $slice_sample(n = 100)$

```
# A tibble: 100 x 10
   ID1
              cat1
                    cat2
                             var1
                                    var2
                                            var3
                                                   var4
                                                           var5
                                                                  var6
                                                                        var7
   <chr>
              <chr> <chr>
                            <dbl> <dbl>
                                          <dbl>
                                                  <dbl>
                                                          <dbl> <dbl>
                                                                       <dbl>
 1 Dd7d5d256 C
                    F
                           -0.430
                                       3
                                          3.09
                                                  2.50
                                                          6.06
                                                                     0
                                                                            0
 2 D3638155a B
                                       5
                                          0.252
                                                  2.23
                                                         -0.701
                                                                     0
                                                                            1
                    Ε
                            1.15
 3 D59e7d00c A
                    F
                           -1.20
                                          1.95
                                                  2.21
                                                         -3.18
                                                                     0
                                                                            1
 4 A891c4eb2 B
                    F
                                          0.670
                                                  2.01
                                                         -0.701
                                                                            0
                           -0.648
                                       7
                                                                     0
 5 Acd6ee546 A
                    D
                           -0.886
                                      11
                                          0.261
                                                  0.442 - 3.18
                                                                     0
                                                                            1
 6 Bd791c03d B
                    Ε
                           -1.45
                                          1.64
                                                  1.72
                                                         -0.701
                                                                     0
                                                                            0
                                       4
7 C87a5811d A
                    Ε
                            1.74
                                          1.24
                                                  3.16
                                                        -3.18
                                                                     0
                                                                            1
                                       3
8 Dc0d3b0fe B
                    F
                            0.629
                                       4 -0.870 -0.631 -0.701
                                                                     0
                                                                            1
 9 C8882c792 A
                            0.485
                                          0.380
                                                  1.92 -3.18
                                                                     0
                                                                            0
                    D
                                       1
10 A7f2fb689 B
                    F
                            0.877
                                          1.28
                                                  0.841 - 0.701
                                                                     0
                                                                            1
# i 90 more rows
```

If you want a random sample that is proportion of your original data size, use the slice_sample(prop = X). Specify the proportion that you want from the data. Create a random sample of data1 that is only 2/7th of the original size.

data1 |> slice_sample(prop = 2/7)

```
# A tibble: 285 x 10
   TD1
             cat1
                    cat2
                             var1
                                   var2
                                            var3
                                                 var4
                                                          var5
                                                                var6
                                                                       var7
   <chr>
              <chr> <chr>
                            <dbl> <dbl>
                                           <dbl> <dbl>
                                                         <dbl> <dbl>
                                                                      <dbl>
 1 Cf0e93509 A
                           -0.184
                                                  2.41
                                                        -3.18
                                                                    0
                    D
                                       7
                                          1.68
2 D895472ca B
                    D
                           -1.38
                                       7
                                          0.710
                                                 1.36
                                                       -0.701
                                                                    0
                                                                          0
                                                                           0
3 A8e80383c A
                    F
                           -1.77
                                          0.489
                                                  1.73
                                                        -3.18
                                                                    0
                                       4
4 C22669227 C
                                                 0.863
                                                         6.06
                    F
                           -2.00
                                          0.776
                                                                    0
                                                                           0
5 C897a230d A
                    F
                           -0.372
                                       2
                                          0.150
                                                 1.45
                                                        -3.18
                                                                    0
                                                                           1
6 Ac5e3a2f3 B
                           -0.770
                                       6 - 0.415
                                                 0.173 -0.701
                                                                          0
                    D
                                                                    0
7 Cea7d3e3a C
                    D
                           0.244
                                       7
                                          2.43
                                                  3.55
                                                         6.06
                                                                    0
                                                                          0
8 B7325ee0a B
                    Ε
                            0.397
                                       3 -0.0451 1.78
                                                       -0.701
                                                                    0
                                                                          0
9 B30c73efd C
                                          0.971
                                                         6.06
                                                                           0
                    D
                           -0.409
                                       5
                                                 1.52
                                                                    0
10 Dcd9588fc C
                    Ε
                           -2.22
                                       3
                                          2.28
                                                  2.27
                                                         6.06
                                                                    0
                                                                          0
# i 275 more rows
```

22.4.4 Creating Variables

Some times you may need to transform variables to a new variable. This can be done by using the mutate() where you specify the name of the new variable and set equal to the transformation of other variables. Using the data2 data set, create a new variable called logvar1 and set that to the log of va1.

data2 |> mutate(logvar1 = log(va1))

```
# A tibble: 1,000 x 6
   ID1
             ID 1
                       ID_2
                                 va1
                                         va2 logvar1
   <chr>
             <chr>
                       <chr>
                               <dbl>
                                       <dbl>
                                               <dbl>
 1 A2b6115fd 2b6115fd A
                             0.458
                                              -0.782
                                      81.4
2 Ac51c9cf1 c51c9cf1 A
                             0.236
                                      -1.15
                                              -1.44
3 A7534d3a0 7534d3a0 A
                             0.254
                                              -1.37
                                       1.16
4 A73fc5642 73fc5642 A
                             0.0411
                                     -1.21
                                              -3.19
5 Ae020e4bd e020e4bd A
                             0.266
                                      -2.31
                                              -1.32
6 AcOd3b0fe cOd3b0fe A
                             0.00992 - 0.882
                                              -4.61
7 A2edfed41 2edfed41 A
                             0.293
                                      -0.375
                                              -1.23
8 Ad38a4bbe d38a4bbe A
                             0.261
                                      -1.09
                                              -1.34
9 A5ee0f97f 5ee0f97f A
                             0.186
                                      -6.14
                                              -1.68
10 Ad791c03d d791c03d A
                             0.0368
                                     -0.258
                                              -3.30
# i 990 more rows
```

The mutate() allows you to create multiple new variables at once. Id addition to logvar1, create a new variable called sqrtvar2 and set that equal to the square root of va2.

```
# A tibble: 1,000 x 7
   ID1
             ID_1
                       ID_2
                                         va2 logvar1 sqrtvar2
                                  va1
   <chr>
             <chr>
                       <chr>
                               <dbl>
                                       <dbl>
                                               <dbl>
                                                         <dbl>
 1 A2b6115fd 2b6115fd A
                             0.458
                                              -0.782
                                                          9.02
                                      81.4
2 Ac51c9cf1 c51c9cf1 A
                             0.236
                                      -1.15
                                              -1.44
                                                        NaN
3 A7534d3a0 7534d3a0 A
                             0.254
                                       1.16
                                              -1.37
                                                          1.08
4 A73fc5642 73fc5642 A
                             0.0411
                                     -1.21
                                              -3.19
                                                        NaN
5 Ae020e4bd e020e4bd A
                             0.266
                                              -1.32
                                      -2.31
                                                        NaN
6 AcOd3b0fe cOd3b0fe A
                             0.00992 -0.882
                                              -4.61
                                                        NaN
7 A2edfed41 2edfed41 A
                             0.293
                                      -0.375
                                              -1.23
                                                        NaN
8 Ad38a4bbe d38a4bbe A
                             0.261
                                              -1.34
                                      -1.09
                                                        NaN
9 A5ee0f97f 5ee0f97f A
                             0.186
                                      -6.14
                                              -1.68
                                                        NaN
10 Ad791c03d d791c03d A
                             0.0368
                                      -0.258
                                              -3.30
                                                        NaN
# i 990 more rows
```

If you want to create categorical variables, use the mutate() and the if_else(). The if_else() requires three arguments: condition argument, true argument, and false argument. The first argument requires a condition that will return a logical value. If true, then R will assign what is stated in the true argument, otherwise R will assign what is in the false argument. To begin, find the median of val from data2 and assign it to medval.

```
medval <- data2$va1 |> median()
```

No create a new variable called dival where if val is greater than the median of val, assign it "A", otherwise assign it "B".

```
data2 |> mutate(diva1=if_else(va1>medval, "A", "B"))
```

```
# A tibble: 1,000 x 6
   ID1
              ID_1
                                           va2 diva1
                        ID<sub>2</sub>
                                   va1
              <chr>
                                        <dbl> <chr>
   <chr>
                        <chr>
                                 <dbl>
 1 A2b6115fd 2b6115fd A
                              0.458
                                       81.4
                                               Α
2 Ac51c9cf1 c51c9cf1 A
                              0.236
                                        -1.15
                                               В
3 A7534d3a0 7534d3a0 A
                              0.254
                                         1.16
                                               В
4 A73fc5642 73fc5642 A
                              0.0411
                                       -1.21
```

```
5 Ae020e4bd e020e4bd A
                            0.266
                                    -2.31 B
6 AcOd3b0fe cOd3b0fe A
                            0.00992 -0.882 B
7 A2edfed41 2edfed41 A
                            0.293
                                    -0.375 A
8 Ad38a4bbe d38a4bbe A
                            0.261
                                    -1.09 B
9 A5ee0f97f 5ee0f97f A
                            0.186
                                    -6.14 B
10 Ad791c03d d791c03d A
                            0.0368
                                    -0.258 B
# i 990 more rows
```

22.4.5 Merging Datasets

One of the last thing is to go over how to merge data sets together. To merge the data sets, we use the full_join(). The full_join() needs two data sets (separated by commas) and the by argument which provides the variables needed (must be the same name for each data set) to merge the data sets. Merge data1 and data2 with the variable ID1.

```
full_join(data1, data2, by = "ID1")
```

```
# A tibble: 1,000 x 14
   ID1
          cat1 cat2
                         var1
                               var2
                                        var3
                                                       var5
                                                             var6
                                                                   var7 ID 1 ID 2
                                                var4
                                                      <dbl> <dbl> <chr> <chr>
   <chr>
          <chr> <chr>
                        <dbl> <dbl>
                                       <dbl>
                                               <dbl>
 1 A2b61~ A
                Ε
                        1.15
                                   4
                                      2.88
                                             3.54
                                                     -3.18
                                                                 0
                                                                       1 2b61~ A
2 Ac51c~ A
                D
                       -0.367
                                   3
                                      0.0640 1.07
                                                     -3.18
                                                                 0
                                                                       0 c51c~ A
3 A7534~ A
                F
                       -0.420
                                   6 - 1.04
                                             0.226
                                                                       0 7534~ A
                                                     -3.18
                                                                 0
4 A73fc~ A
                F
                       -2.00
                                   5 -0.314
                                             0.0213 -3.18
                                                                 0
                                                                       0 73fc~ A
5 Ae020~ C
                Ε
                                      0.526
                                             2.98
                                                                       0 e020~ A
                        0.697
                                                      6.06
                                                                 0
6 AcOd3~ A
                D
                        0.467
                                      2.45
                                              1.85
                                                     -3.18
                                                                 0
                                                                       0 c0d3~ A
7 A2edf~ A
                Ε
                                      0.514
                                             0.529
                                                                       1 2edf~ A
                        1.36
                                   5
                                                     -3.18
                                                                 0
8 Ad38a~ C
                F
                        0.369
                                   0
                                      1.98
                                             2.36
                                                      6.06
                                                                 0
                                                                       1 d38a~ A
9 A5ee0~ B
                Ε
                        1.80
                                      0.147
                                             2.22
                                                     -0.701
                                                                 0
                                                                       0 5ee0~ A
                                   5
10 Ad791~ C
                F.
                                   3 -1.05
                        1.25
                                             0.0289
                                                      6.06
                                                                 0
                                                                       1 d791~ A
# i 990 more rows
# i 2 more variables: va1 <dbl>, va2 <dbl>
```

The full_join() allows you to merge data sets using two variables instead of one. All you need to do is specify by argument with a vector specifying the arguments. Merge data2 and data3 by ID_1 and ID_2.

```
full_join(data2, data3, by = c("ID_1","ID_2"))
```

```
# A tibble: 1,000 x 8
   ID1.x
             ID_1
                       ID<sub>2</sub>
                                  va1
                                         va2 ID1.y
                                                             v1
                                                                    v2
   <chr>
              <chr>
                       <chr>
                                <dbl>
                                       <dbl> <chr>
                                                                 <dbl>
                                                          <dbl>
 1 A2b6115fd 2b6115fd A
                             0.458
                                      81.4
                                              A2b6115fd 0.361
                                                                0.278
 2 Ac51c9cf1 c51c9cf1 A
                             0.236
                                      -1.15
                                             Ac51c9cf1 0.273
                                                                2.64
3 A7534d3a0 7534d3a0 A
                             0.254
                                       1.16
                                             A7534d3a0 1.17
                                                                0.119
4 A73fc5642 73fc5642 A
                             0.0411
                                      -1.21
                                              A73fc5642 0.879
                                                                0.705
5 Ae020e4bd e020e4bd A
                             0.266
                                      -2.31
                                              Ae020e4bd 0.0268 0.297
6 AcOd3b0fe cOd3b0fe A
                             0.00992 -0.882 Ac0d3b0fe 1.18
                                                                3.16
7 A2edfed41 2edfed41 A
                             0.293
                                      -0.375 A2edfed41 0.356
                                                                0.174
8 Ad38a4bbe d38a4bbe A
                             0.261
                                      -1.09
                                              Ad38a4bbe 0.430
                                                                0.130
9 A5ee0f97f 5ee0f97f A
                                             A5ee0f97f 0.643
                             0.186
                                      -6.14
                                                                0.0231
10 Ad791c03d d791c03d A
                             0.0368
                                      -0.258 Ad791c03d 0.183
                                                                0.311
# i 990 more rows
```

22.5 Reshaping Data

This section focuses on reshaping the data to prepare it for analysis. For example, to conduct longitudinal data analysis, you will need to have long data. Reshaping data may be with converting data from wide to long, converting back from long to wide, splitting variables, splitting rows and merging variable. The functions used in this lesson are from the tidy package

22.5.1 Wide to Long Data

Converting data from wide to long is necessary when the data looks like data4, view data4:

data4

```
# A tibble: 1,000 x 5
   ID1
                  X1
                          Х2
                                ХЗ
                                       Х4
   <chr>
               <dbl>
                      <dbl> <dbl> <dbl>
 1 Ad9131ee9
               0.800
                      4.68
                              1.46
                                    5.35
 2 A9c5988ea
               1.17
                      1.50
                              4.83
                                     3.75
 3 A28a5479d
               1.85
                      2.64
                              2.39
                                     4.34
 4 Aaf5537cc
               1.55
                      2.28
                              3.35
                                     3.76
 5 A370958bd -1.36
                      2.48
                              2.06
                                    4.70
                      3.27
 6 Aea997e13
               2.37
                              3.11
                                     3.31
7 A3563646f
               2.10
                     -0.902
                              2.49
                                     2.75
 8 A9b3cfdba -0.513
                     0.271
                              2.97
                                     2.97
```

```
9 A32b6737a 1.28 2.02 3.48 4.87
10 A30e96748 1.30 1.72 2.11 2.04
# i 990 more rows
```

Let's say data4 represents biomarker data. Variable ID1 represents a unique identifier for the participant. Then X1, X2, X3, and X4 represents a value collected for a participant at different time point. This is known as repeated measurements. This data is considered wide because the repeated measurements are on the same row. To make it long, the repeated measurements must be on the same column.

To convert data from long to wide, we will use the pivot_longer() with the first argument taking variables of the repeated measurements, c(X1:X4) or X1:X4, second you will need to specify the names_to argument which specifies the variable name to store the long variables, lastly you will need to specify the values_to argument that specifies variable to store the values in the long data set. Convert the data4 to long and name the variable names column "measurement", and values column "value".

```
# A tibble: 4,000 x 3
   ID1
             measurement value
                          <dbl>
   <chr>
             <chr>
 1 Ad9131ee9 X1
                          0.800
2 Ad9131ee9 X2
                          4.68
3 Ad9131ee9 X3
                          1.46
4 Ad9131ee9 X4
                          5.35
5 A9c5988ea X1
                          1.17
                          1.50
6 A9c5988ea X2
7 A9c5988ea X3
                          4.83
8 A9c5988ea X4
                          3.75
9 A28a5479d X1
                          1.85
10 A28a5479d X2
                          2.64
# i 3,990 more rows
```

22.5.2 Long to Wide

If you need to convert data from long to wide, use the pivot_wider(). You will need to specify the names_from argument which specifies the variable names for the wide data set, and you will need to specify the values_from argument that specifies variable that contains

the values in the long data set. Convert data5 from long to wide data. Note, you must specify the arguments for this function.

```
# A tibble: 1,000 x 5
   ID1
                 X1
                         X2
                               ХЗ
                                     X4
   <chr>
              <dbl>
                     <dbl> <dbl>
                                  <dbl>
1 Ad9131ee9
              0.800
                     4.68
                             1.46
                                   5.35
2 A9c5988ea
              1.17
                     1.50
                             4.83
                                   3.75
3 A28a5479d
             1.85
                     2.64
                             2.39
                                   4.34
4 Aaf5537cc
              1.55
                     2.28
                             3.35
                                   3.76
5 A370958bd -1.36
                     2.48
                             2.06
                                   4.70
6 Aea997e13
              2.37
                     3.27
                                   3.31
                             3.11
                    -0.902
7 A3563646f
             2.10
                             2.49
                                   2.75
8 A9b3cfdba -0.513
                    0.271
                             2.97
                                   2.97
9 A32b6737a 1.28
                     2.02
                                   4.87
                             3.48
10 A30e96748 1.30
                     1.72
                             2.11 2.04
# i 990 more rows
```

22.5.3 Spliting Variables

Before we begin, look at data6:

data6

```
# A tibble: 1,000 x 4
   ID1
             merge
                            ХЗ
                                  Х4
   <chr>
             <chr>
                         <dbl> <dbl>
1 Ad9131ee9 -1.23/2.64
                          2.12
                                3.56
2 A9c5988ea 1.74/3.02
                          4.09
                                4.88
3 A28a5479d 0.87/3.56
                          3.47
                                4.47
4 Aaf5537cc 1.05/2.01
                          3.61
                                5.03
5 A370958bd -1.47/1.26
                          3.98
                                6.59
6 Aea997e13 1.66/3.51
                          1.65
                                2.72
7 A3563646f 1.81/1.7
                          4.29
                                3.13
8 A9b3cfdba 1.8/2.26
                          1.94
                                5.23
9 A32b6737a 2.38/1.68
                          3.06
                                3.3
10 A30e96748 1/2.17
                          2.59
                                3.03
# i 990 more rows
```

Notice how the merge variable has two values separated by "/". If we need to split the variable into two variables, we need to specify the separate(). All you need to specify is the variable you need to split, the name of the 2 new variables, in a character vector, and how to split the variable "/". Split the variable merge in data6 to two new variables called X1 and X2.

```
data6 |> separate(merge, c("X1", "X2"), "/")
```

```
# A tibble: 1,000 x 5
   ID1
             Х1
                   Х2
                             ХЗ
                                   Х4
   <chr>
             <chr> <chr> <dbl> <dbl>
 1 Ad9131ee9 -1.23 2.64
                           2.12
                                 3.56
2 A9c5988ea 1.74
                   3.02
                           4.09
                                 4.88
3 A28a5479d 0.87
                           3.47
                                4.47
                   3.56
4 Aaf5537cc 1.05
                   2.01
                           3.61
                                5.03
5 A370958bd -1.47 1.26
                           3.98
                                6.59
6 Aea997e13 1.66
                   3.51
                           1.65
                                2.72
7 A3563646f 1.81
                           4.29
                   1.7
                                3.13
                                5.23
8 A9b3cfdba 1.8
                   2.26
                           1.94
9 A32b6737a 2.38
                   1.68
                           3.06
                                 3.3
10 A30e96748 1
                           2.59
                                3.03
                   2.17
# i 990 more rows
```

22.5.4 Splitting Rows

The variable merge in data6 was split into different variables before, now instead of variables, let's split it into different rows instead. To do this, use the separate_rows(). All you need to specify the variable name and the sep argument (must state the argument). Split the merge variable from data6 into different rows.

```
data6 |> separate_rows(merge, sep = "/")
```

```
# A tibble: 2,000 x 4
   ID1
                             Х4
             merge
                      ХЗ
   <chr>
             <chr> <dbl> <dbl>
                          3.56
1 Ad9131ee9 -1.23
                    2.12
2 Ad9131ee9 2.64
                    2.12
                          3.56
3 A9c5988ea 1.74
                    4.09
                          4.88
4 A9c5988ea 3.02
                    4.09
                          4.88
5 A28a5479d 0.87
                          4.47
                    3.47
6 A28a5479d 3.56
                          4.47
                    3.47
7 Aaf5537cc 1.05
                    3.61 5.03
```

```
8 Aaf5537cc 2.01 3.61 5.03
9 A370958bd -1.47 3.98 6.59
10 A370958bd 1.26 3.98 6.59
# i 1,990 more rows
```

22.5.5 Merging Rows

If you need to merge variables together, similar to the merge variable, use the unite(). All you need to do is specify the variables to merge, the col argument which specifies the name of the new variable (as a character), and the sep argument which indicates the symbol for separate value, as a character. Note, you need to specify the bot the col argument and sep argument. Merge variable X3 and X4 in data6 to a new variable called merge2 and have the separator be a hyphen.

```
data6 |> unite(X3, X4, col = "merge2", sep="-")
```

```
# A tibble: 1,000 x 3
   ID1
             merge
                        merge2
   <chr>
             <chr>
                         <chr>
1 Ad9131ee9 -1.23/2.64 2.12-3.56
2 A9c5988ea 1.74/3.02 4.09-4.88
3 A28a5479d 0.87/3.56
                        3.47-4.47
4 Aaf5537cc 1.05/2.01
                        3.61-5.03
5 A370958bd -1.47/1.26 3.98-6.59
6 Aea997e13 1.66/3.51
                        1.65 - 2.72
7 A3563646f 1.81/1.7
                         4.29 - 3.13
8 A9b3cfdba 1.8/2.26
                         1.94-5.23
9 A32b6737a 2.38/1.68
                        3.06-3.3
10 A30e96748 1/2.17
                         2.59-3.03
# i 990 more rows
```

22.6 Applied Example

Here is an applied example where you will use what you learned from the previous lesson and convert data7 into data8. data7 has a wide data format which contains time points labeled as vX, where X represents the time point number. At each time point, the mean, sd, and median was taken. You will need to convert the data to long where each row represents a new time point, and each row will have 3 variables representing the mean, sd, and median. View both data7 and data8 to have a better idea on what is going on. Remember you need to convert data7 to data8.

data7

```
# A tibble: 1,000 x 13
   ID1
            `v1/mean` `v1/sd` `v1/median` `v2/mean` `v2/sd` `v2/median` `v3/mean`
   <chr>
                <dbl>
                         <dbl>
                                      <dbl>
                                                 <dbl>
                                                         <dbl>
                                                                       <dbl>
                                                                                  <dbl>
 1 Ad9131~
                3.11
                        2.86
                                       4.50
                                                 1.93
                                                         3.21
                                                                    3.27
                                                                                2.65
 2 A9c598~
                2.03
                        2.90
                                       2.08
                                                 0.709
                                                         2.27
                                                                    4.13
                                                                                1.45
 3 A28a54~
               -0.415
                         2.42
                                       2.47
                                                 2.38
                                                        -0.820
                                                                    1.22
                                                                                3.44
 4 Aaf553~
                1.25
                         2.24
                                       3.71
                                                 4.00
                                                         0.456
                                                                    4.32
                                                                                1.54
 5 A37095~
               -0.984
                        0.972
                                       3.73
                                                 2.19
                                                        -0.184
                                                                    2.14
                                                                                4.32
 6 Aea997~
                1.42
                                       2.35
                                                 2.77
                                                         4.16
                                                                   -0.00874
                                                                               -3.02
                         1.34
7 A35636~
               -0.149
                         3.26
                                       4.49
                                                 5.07
                                                         2.44
                                                                    3.85
                                                                                0.0388
8 A9b3cf~
                0.270
                         1.57
                                       3.25
                                                 2.89
                                                         0.422
                                                                    5.01
                                                                               -0.218
 9 A32b67~
                                                                               -0.784
                0.714
                         3.39
                                       5.66
                                                 2.52
                                                         3.15
                                                                    3.16
10 A30e96~
                0.467
                         2.47
                                       2.64
                                                 3.97
                                                         1.76
                                                                    4.00
                                                                                2.21
# i 990 more rows
# i 5 more variables: `v3/sd` <dbl>, `v3/median` <dbl>, `v4/mean` <dbl>,
    `v4/sd` <dbl>, `v4/median` <dbl>
```

data8

```
# A tibble: 4,000 x 5
   ID1
             time
                      mean
                                sd
                                    median
   <chr>
              <chr>
                     <dbl>
                            <dbl>
                                     <dbl>
 1 Ad9131ee9 v1
                     3.11
                            2.86
                                    4.50
 2 Ad9131ee9 v2
                     1.93
                            3.21
                                    3.27
3 Ad9131ee9 v3
                     2.65
                           -0.383
                                    3.23
4 Ad9131ee9 v4
                     0.605 0.883
                                    4.65
5 A9c5988ea v1
                            2.90
                     2.03
                                    2.08
6 A9c5988ea v2
                     0.709
                            2.27
                                    4.13
7 A9c5988ea v3
                     1.45
                            2.01
                                    2.84
8 A9c5988ea v4
                     0.710
                            3.03
                                   -0.0898
9 A28a5479d v1
                    -0.415
                           2.42
                                    2.47
10 A28a5479d v2
                     2.38
                           -0.820
                                    1.22
# i 3,990 more rows
```

Now that you viewed the data set, type the code to convert data? to data8. Try working it out before you look at the solution.

```
# A tibble: 4,000 x 5
  ID1
            time
                            sd median
                    mean
  <chr>
            <chr> <dbl> <dbl>
                                 <dbl>
1 Ad9131ee9 v1
                   3.11
                         2.86
                                4.50
2 Ad9131ee9 v2
                   1.93
                         3.21
                                3.27
3 Ad9131ee9 v3
                   2.65 -0.383 3.23
4 Ad9131ee9 v4
                   0.605 0.883 4.65
5 A9c5988ea v1
                   2.03
                         2.90
                                2.08
6 A9c5988ea v2
                   0.709 2.27
                                4.13
7 A9c5988ea v3
                   1.45
                        2.01
                                2.84
8 A9c5988ea v4
                   0.710 3.03 -0.0898
9 A28a5479d v1
                  -0.415 2.42
                                2.47
10 A28a5479d v2
                   2.38 -0.820 1.22
# i 3,990 more rows
```

23 Data Summarization

23.1 Descriptive Statistics

Here, we will go over some of the basic syntax to obtain basic statistics. We will use the variables mpg and cyl from the mtcars data set. To view the data set use the head():

head(mtcars)

	mpg	cyl	disp	hp	drat	wt	qsec	٧s	\mathtt{am}	gear	carb
Mazda RX4	21.0	6	160	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 Wag	21.0	6	160	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225	105	2.76	3.460	20.22	1	0	3	1

The variable mpg would be used as a continuous variable, and the variable cyl would be used as a categorical variable.

23.1.1 Point Estimates

The first basic statistic you can compute are point estimates. These are your means, medians, etc. Here we will calculate these estimates.

23.1.1.1 Mean

To obtain the mean, use the mean(), you only need to specify x= for the data to compute the mean:

mean(mtcars\$mpg)

[1] 20.09062

23.1.1.2 Median

To obtain the median, use the median(), you only need to specify x= for the data to compute the median:

median(mtcars\$mpg)

[1] 19.2

23.1.1.3 Frequency

To obtain a frequency table, use the table(), you only need to specify the data as the first argument to compute the frequency table:

table(mtcars\$cyl)

4 6 8 11 7 14

23.1.1.4 Proportion

To obtain a the proportions for the frequency table, use the prop.table(). However the first argument must be the results from the table(). Use the table() inside the prop.table() to get the proportions:

prop.table(table(mtcars\$cyl))

4 6 8 0.34375 0.21875 0.43750

23.1.2 Variability

In addition to point estimates, variability is an important statistic to report to let a user know about the spread of the data. Here we will calculate certain variability statistics.

23.1.2.1 Variance

To obtain the variance, use the var(), you only need to specify x= for the data to compute the variance:

var(mtcars\$mpg)

[1] 36.3241

23.1.2.2 Standard deviation

To obtain the standard deviation, use the sd(), you only need to specify x= for the data to compute the standard deviation:

sd(mtcars\$mpg)

[1] 6.026948

23.1.2.3 Max and Min

To obtain the max and min, use the max() and min(), respectively. You only need to specify the data as the first argument to compute the max and min:

max(mtcars\$mpg)

[1] 33.9

min(mtcars\$mpg)

[1] 10.4

23.1.2.4 Q1 and Q3

To obtain the Q1 and Q3, use the quantile() and specify the desired quantile with probs=. You only need to specify the data as the first argument and probs= (as a decimal) to compute the Q1 and Q3:

```
quantile(mtcars$mpg, .25)
```

25% 15.425

```
quantile(mtcars$mpg, .75)
```

75% 22.8

23.1.3 Associations

In statistics, we may be interested on how different variables are related to each other. These associations can be represented in a numerical value.

23.1.3.1 Continuous and Continuous

When we measure the association between to continuous variables, we tend to use a correlation statistic. This statistic tells us how linearly associated are the variables are to each other. Essentially, as one variable increases, what happens to the other variable? Does it increase (positive association) or does it decrease (negative association). To find the correlation in R, use the cor(). You will need to specify the x= and y= which represents vectors for each variable. Find the correlation between mpg and hp from the mtcars data set.

```
cor(mtcars$mpg, mtcars$hp)
```

[1] -0.7761684

23.1.3.2 Categorical and Continuous

When comparing categorical variables, it becomes a bit more nuanced in how to report associations. Most of time you will discuss key differences in certain groups. Here, we will talk about how to get the means for different groups of data. Our continuous variable is the mpg variable, and our categorical variable is the cyl variable. Both are from the mtcars data set. The tapply() allows us to split the data into different groups and then calculate different statistics. We only need to specify X= of the R object to split, INDEX= which is a list of factors or categories indicating how to split the data set, and FUN= which is the function that needs to be computed. Use the tapply() and find the mean mpg for each cyl group: 4, 5, and 6.

tapply(mtcars\$mpg, list(mtcars\$cyl), mean)

4 6 8 26.66364 19.74286 15.10000

23.1.3.3 Categorical and Categorical

Reporting the association between two categorical variables is may be challenging. If you have a 2×2 table, you can report a ratio of association. However, any other case may be challenging. You can report a hypothesis test to indicate an association, but it does not provide much information about the effect of each variable. You can also report row, column, or table proportions. Here we will talk about creating cross tables and report these proportions. To create a cross table, use the table() and use the first two arguments to specify the two categorical variables. Create a cross tabulation between cyl and carb from the mtcars data set.

table(mtcars\$cyl, mtcars\$carb)

1 2 3 4 6 8 4 5 6 0 0 0 0 6 2 0 0 4 1 0 8 0 4 3 6 0 1

Notice how the first argument is represented in the rows and the second argument is in the columns. Now create table proportions using both of the variables. You first need to create the table and store it in a variable and then use the prop.table().

prop.table(table(mtcars\$cyl, mtcars\$carb))

```
1 2 3 4 6 8
4 0.15625 0.18750 0.00000 0.00000 0.00000 0.00000
6 0.06250 0.00000 0.00000 0.12500 0.03125 0.00000
8 0.00000 0.12500 0.09375 0.18750 0.00000 0.03125
```

To get the row proportions, use the argument margin = 1 within the prop.table().

To get the column proportions, use the argument margin = 2 within the prop.table().

```
1 2 3 4 6 8
4 0.7142857 0.6000000 0.0000000 0.0000000 0.0000000
6 0.2857143 0.0000000 0.0000000 0.4000000 1.0000000 0.0000000
8 0.0000000 0.4000000 1.0000000 0.6000000 0.0000000 1.0000000
```

23.2 Summarizing with Tidyverse

```
library(magrittr)
library(tidyverse)
-- Attaching packages ----- tidyverse 1.3.2 --
v ggplot2 3.4.0
                 v purrr
                         1.0.0
v tibble 3.1.8
                 v dplyr 1.0.10
v tidyr
        1.2.1
                 v stringr 1.5.0
        2.1.3
v readr
                 v forcats 0.5.2
-- Conflicts ----- tidyverse conflicts() --
x tidyr::extract() masks magrittr::extract()
x dplyr::filter()
                 masks stats::filter()
x dplyr::lag()
                 masks stats::lag()
x purrr::set_names() masks magrittr::set_names()
```

```
f <- function(x){</pre>
  mtcars %>% split(~.$cyl) %>% map(~shapiro.test(.$mpg))
  return(1)}
g <- function(x){</pre>
  mtcars %>% group_by(cyl) %>% nest() %>% mutate(shapiro = map(data, ~shapiro.test(.$mpg)))
  return(1)}
bench::mark(f(1),g(1))
# A tibble: 2 x 6
  expression
                  min median `itr/sec` mem_alloc `gc/sec`
  <bch:tm> <bch:tm> <bch:tm>
                                    <dbl> <bch:byt>
                                                       <dbl>
                                           134.23KB
                                                       16.9
1 f(1)
              402.6us 432.6us
                                  2258.
2 g(1)
              11.6ms
                        11.7ms
                                    83.5
                                             3.65MB
                                                        9.03
```

24 Graphics

Through out this chapter, we use certain notations for different components in R. To begin, when something is in a gray block, _, this indicates that R code is being used. When I am talking about an R Object, it will be displayed as a word. For example, we will be using the R object mtcars. When I am talking about an R function, it will be displayed as a word followed by an open and close parentheses. For example, we will use the mean function denoted as mean() (read this as "mean function"). When I am talking about an R argument for a function, it will be displayed as a word following by an equal sign. For example, we will use the data argument denoted as data= (read this as "data argument"). When I am referencing an R package, I will use :: (two colons) after the name. For example, in this tutorial, I will use the ggplot2:: (read this as "ggplot2 package") Lastly, if I am displaying R code for your reference or to run, it will be displayed on its own line. There are many components in R, and my hope is that this will help you understand what components am I talking about.

24.1 Base R Plotting

24.1.1 Introduction

This tutorial provides an introduction on how to create different graphics in R. For this tutorial, we will focus on plotting different components from the mtcars data set.

24.1.2 Contents

- 1. Basic
- 2. Grouping
- 3. Tweaking

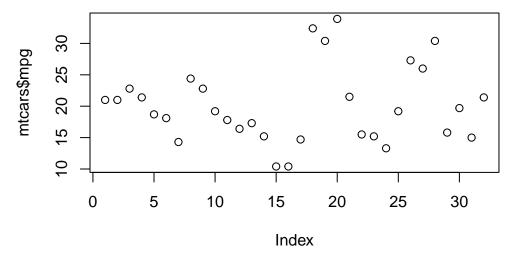
24.1.3 Basic Graphics

Here we will use the built-in R functions to create different graphics. The main function that you will use is the plot(). It contains much of the functionality to create many different plots in R. Additionally, it works well for different classes of R objects. It will provide many important plots that you will need for a certain statistical analysis.

24.1.4 Scatter Plot

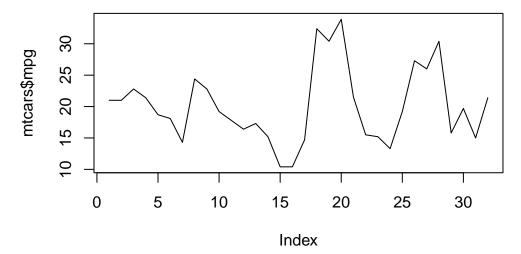
Let's first create a scatter plot for one variable using the mpg variable. This is done using the plot() and setting the first argument x= to the vector.

plot(mtcars\$mpg)



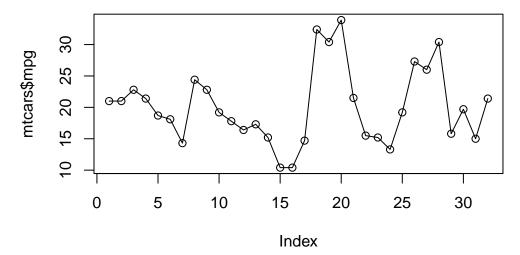
Notice that the x-axis is the index (which is not informative) and the y-axis is the mpg values. Let's connect the points with a line. This is done by setting the type= to "1".

```
plot(mtcars$mpg, type = "1")
```



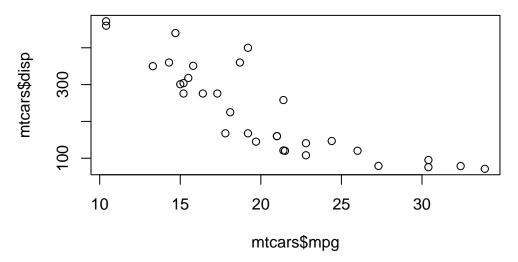
Let's add the points back to the plot and keep the lines. What we are going to do is first create the scatter plot as we did before, but we will also use the lines() to add the lines. The lines() needs the x= which is a vector of points (mpg). The two lines of code must run together.

plot(mtcars\$mpg) lines(mtcars\$mpg)



Now, let's create a more realistic scatter plot with 2 variables. This is done by specifying the y= with another variable in addition to the x= in the plot=. Plot a scatter plot between mpg and disp.

plot(mtcars\$mpg,mtcars\$disp)



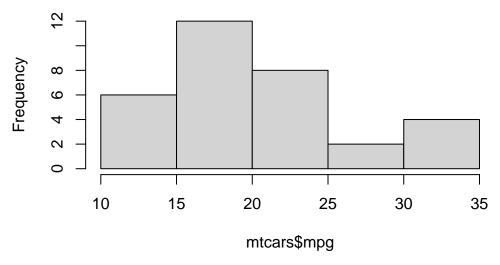
Now, let's change the the axis labels and plot title. This is done by using the arguments main=, xlab=, and ylab. The main= changes the title of the plot.

24.1.5 Histogram

To create a histogram, use the hist(). The hist() only needs x= which is numerical vector. Create a histogram with the mpg variable.

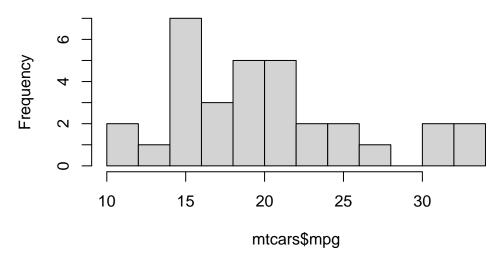
hist(mtcars\$mpg)

Histogram of mtcars\$mpg



If you want to change the number of breaks in the histogram, use the breaks=. Create a new histogram of the mpg variable with ten breaks.

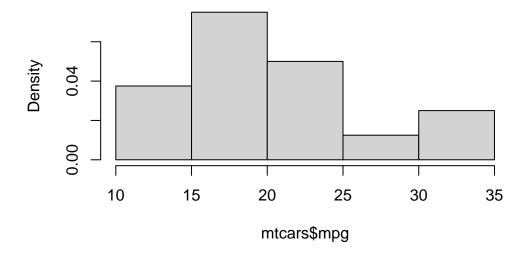
Histogram of mtcars\$mpg



The above histograms provide frequencies instead of relative frequencies. If you want relative frequencies, use the freq= and set it equal to FALSE in the hist().

hist(mtcars\$mpg, freq = FALSE)

Histogram of mtcars\$mpg

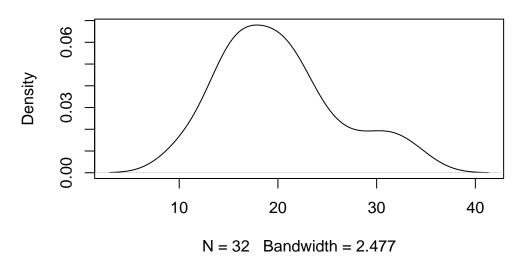


24.1.6 Density Plot

A density plot can be used instead of a histogram. This is done by using the density() to create an object containing the information to create density function. Then, use the plot() to display the plot. The only argument the density() needs is the x= which is the data to be used. Create a density plot the mpg variable.

plot(density(mtcars\$mpg))

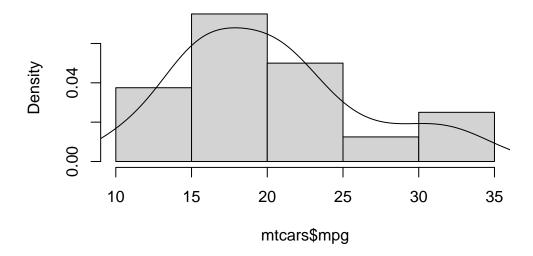
density.default(x = mtcars\$mpg)



Now, if we want to overlay the density function over a histogram, use the lines() with the output from the density() as its main input. First create the histogram using the hist() and setting the freq= to FALSE. Then use the lines() to overlay the density. Make sure to run both lines together.

hist(mtcars\$mpg, freq = FALSE)
lines(density(mtcars\$mpg))

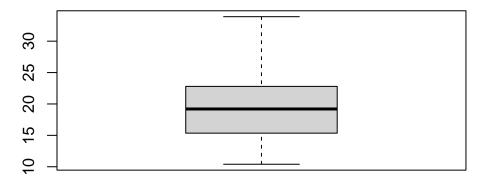
Histogram of mtcars\$mpg



24.1.7 Box Plots

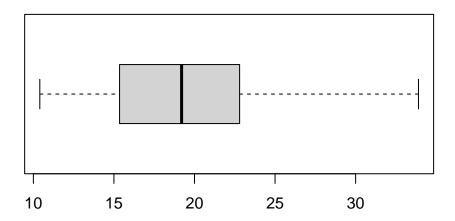
A commonly used plot to display relevant statistics is the box plot. To create a box plot use the boxplot(). The function only needs the x= which specifies the data to create the box plot. Use the box plot function to create a box plot on for the variable mpg.

boxplot(mtcars\$mpg)



If you want to make the box plot horizontal, use horizontal= and set it equal to TRUE.

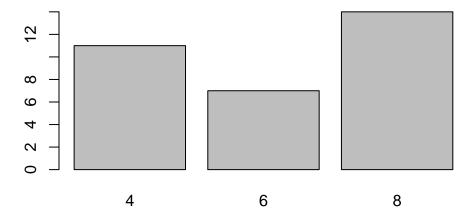
boxplot(mtcars\$mpg, horizontal = TRUE)



24.1.8 Bar Chart

A histogram shows you the frequency for a continuous variable. A bar chart will show you the frequency of a categorical or discrete variable. To create a bar chart, use the barplot(). The main argument it needs is the height= which needs to an object from the table(). Create a bar chart for the cyl variable.

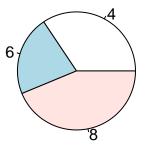
barplot(table(mtcars\$cyl))



24.1.9 Pie Chart

While I do not recommend using a pie chart, R is capable of creating one using the pie(). It only needs the x= which is a vector numerical quantities. This could be the output from the table(). Create a pie chart with the cyl variable.

pie(table(mtcars\$cyl))



24.1.10 Grouping

Similar to obtaining statistics for certain groups, plots can be grouped to reveal certain trends. We will look at a couple of methods to visualize different groups.

24.1.10.1 One Variable Grouping

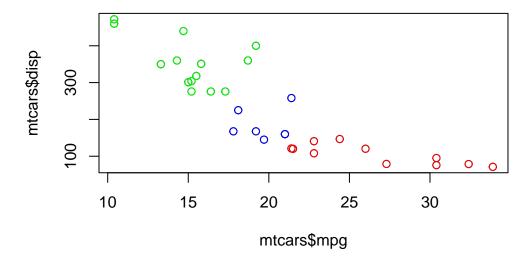
Two ways to display groups is by using color coding or panels. I will show you what I think is the best way to group variables. There may be better ways to do this, such as using the ggplot2 package. Before we begin, create three new R objects that are a subset of the mtcars data set into 3 different data sets with for the three different values of the cyl variable: "4", "6", and "8". use the subset() to create the different data sets. Name the new R objects mtcars_4, mtcars_6, and mtcars_8, respectively.

```
mtcars_4 <- subset(mtcars, cyl == 4)
mtcars_6 <- subset(mtcars, cyl == 6)
mtcars_8 <- subset(mtcars, cyl == 8)</pre>
```

24.1.10.1.1 Scatter Plot

To create different colors points for their respective label associated cyl variable. First create a base scatter plot using the plot() to set up the plot. Then one by one, overlay a set of new points on the base plot using the points(). The first two arguments should be the vectors of data from their respective R object subset. Also, use the col= to change the color of the points. The col= takes either a string or a number.

```
plot(mtcars$mpg, mtcars$disp)
points(mtcars_4$mpg, mtcars_4$disp, col = "red")
points(mtcars_6$mpg, mtcars_6$disp, col = "blue")
points(mtcars_8$mpg, mtcars_8$disp, col = "green")
```

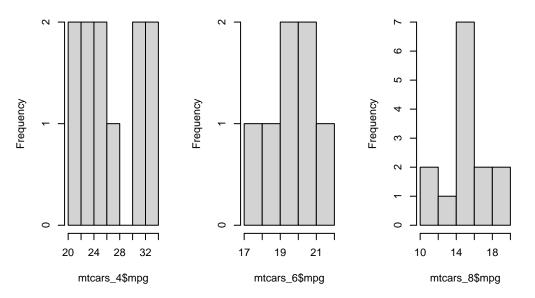


24.1.10.1.2 Histogram

Now, it us more difficult to overlay histograms on a plot to different colors. Therefore, a panel approach may be more beneficial. This can be done by setting up R to plot a grid of plots. To do this, use the par() to tell R how to set up the grid. Then use the mfrow=, which is a vector of length two, to set up a grid. The mfrow= usually has an input of c(ROWS,COLS) which states the number of rows and the number of columns. Once this is done, the next plots you create will be used to populate the grid.

```
par(mfrow=c(1,3))
hist(mtcars_4$mpg)
hist(mtcars_6$mpg)
hist(mtcars_8$mpg)
```

Histogram of mtcars_4\$m| Histogram of mtcars_6\$m| Histogram of mtcars_8\$m|

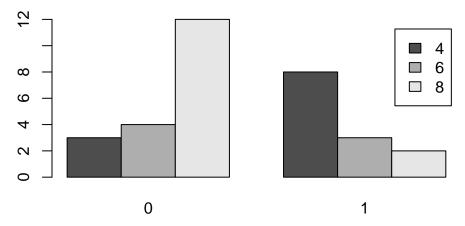


Every time you use the par(), it will change how graphics are created in an R session. Therefore, all your plots will follow the new graphic parameters. You will need to reset it by typing dev.off().

24.1.10.1.3 Bar Chart

To visualize two categorical variables, we can use a color-coded bar chart to compare the frequencies of the categories. This is simple to do with the barplot(). First, use the table() to create a cross-tabulation of the frequencies for two variables. Then use the boxplot() to visualize both variables. Then use legend= to create a label when the bar chart is color-coded. Additionally, use the beside= argument to change how the plot looks. Use the code below to compare the variables cyl and am variable.

barplot(table(mtcars\$cyl, mtcars\$am), beside = TRUE, legend = rownames(table(mtcars\$cyl, mtcars\$cyl, mtcars\$cyl)



Notice that I use the rownames() to label the legend.

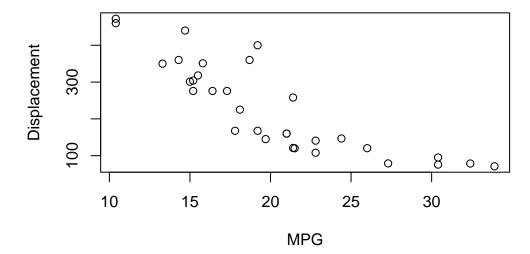
24.1.11 Tweaking

24.1.11.1 Labels

The main tweaking of plots I will talk about is changing the the axis label and titles. For the most part, each function allows you to use the main=, xlab=, and ylab=. The main= allows you to change the title. The xlab= and ylab= allow you to change the labels for the x-axis and y-axis, respectively. Create a scatter plot for the variables mpg and disp and change the labels.

plot(mtcars\$mpg, mtcars\$disp, main = "MPG vs Displacement", xlab = "MPG", ylab = "Displacement")

MPG vs Displacement



24.2 ggplot2

24.2.1 Introduction

The ggplot2:: provides a set of functions to create different graphics. For more information on plotting in ggplot2::, please visit the this excellent resource. Here we will discuss some of the basics to the ggplot2::``. To me,ggplot2::'creates a plot by adding layers to a base plot. The syntax is designed for you to change different components of a plot in an intuitive manner. For this tutorial, we will focus on plotting different components from thempg' data set.

24.2.1.1 Contents

- 1. Basic
- 2. Grouping
- 3. Themes/Tweaking

24.2.2 Basics

To begin, the ggplot2:: really works well when you are using data frames. If you have any output that you want to plot, convert into to a data frame. Once we have our data set, the first thing you would want to do is specify the main components of your base plot. This will be what will be plotted on your x-axis, and what will be plotted on your y-axis. Next, you will create the type of plot. Lastly, you will add different layers to tweak the plot for your needs. This can be changing the layout or even overlaying another plot. The 'ggplot2::" provides you with tools to do almost everything you need to create a plot easily.

Before we begin plotting, load the ggplot2:: in R.

library(ggplot2)

Now, when we create a base plot, we will use the ggplot(). This will initialize the data that we need to use with the data= and how to map it on the x and y axis with the mapping=. With the mapping=, you will need to use the aes() which constructs the mapping function for the base plot. The aes() requires the x= and optionally uses the y= to set which values represents the x and y axis. The aes() also accepts other arguments for grouping or other aesthetics.

Before we begin, create a new variable in mtcars called ind and place a numeric vector which contains integers from 1 to 32.

```
mtcars$ind <- c(1:32)
```

Now, let's create the base plot and assign it to gg_1. Use the ggplot() and set mtcars as its data and the variable ind as x= and mpg as the y=

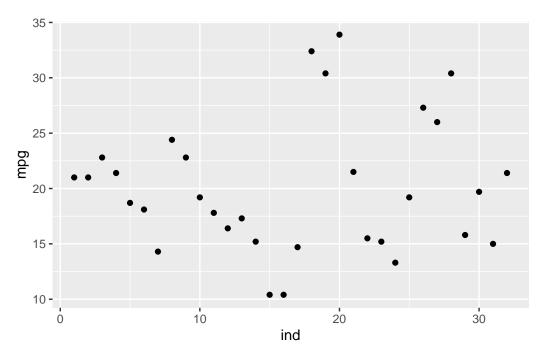
```
gg_1 <- ggplot(mtcars, aes(ind, mpg))</pre>
```

This base plot is now used to create certain plots. Plots are created by adding functions to the base plot. This is done by using the + operator and then a specific ggplot2:: function. Below we will go over some of the functions necessary.

24.2.3 Scatter Plot

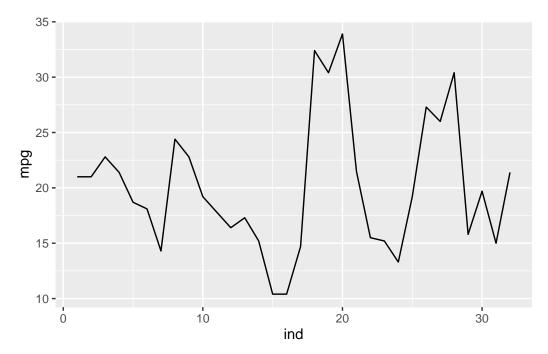
To create a scatter plot in ggplot2::, add the geom_point() to the base plot. You do not need to specify any arguments in the function. Create a scatter plot to gg_1

gg_1 + geom_point()



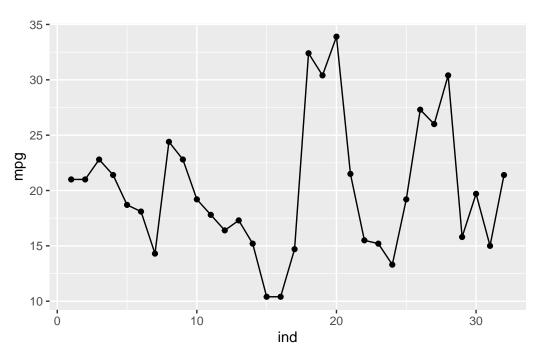
If we want to put lines instead of points, we will need to use the geom_point(). Change the points to a line.

gg_1 + geom_line()



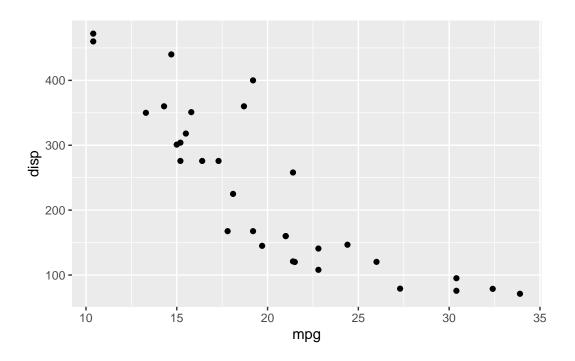
To overlay points to the plot, add <code>geom_point()</code> as well as <code>geom_line()</code>. Add points to the plot above.

gg_1 + geom_point() + geom_line()



To create a 2 variable scatter plot. You will just need to specify the x= and y= in the <code>aes()</code>. Create a base plot using the <code>mtcars</code> data set and use the <code>mpg</code> and <code>disp</code> as the x and y variables, respectively, and assign in it to <code>gg_2</code>

Now create a scatter plot using gg_2.



24.2.4 Histogram and Density Plot

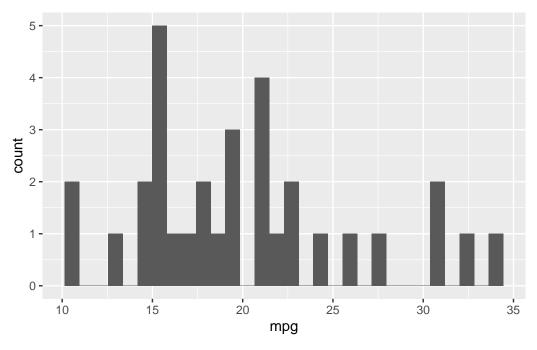
To create a histogram and density plots, create a base plot and specify the variable of interest in the <code>aes()</code>, only specify one variable. Create a base plot using the <code>mtcars</code> data set and the <code>mpg</code> variable. Assign it to <code>gg_3</code>.

```
gg_3 <- ggplot(mtcars, aes(mpg))</pre>
```

To create a histogram, use the geom_histogram().

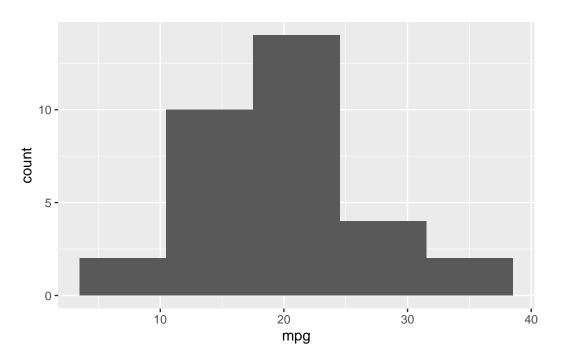
```
gg_3 + geom_histogram()
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



The above plot shows a histogram, but the number of bins is quite large. We can change the bin width argument, binwidth=, the the geom_histogram(). Change the bin width to seven.

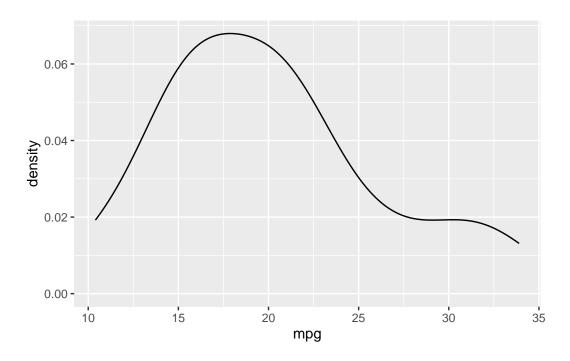
gg_3 + geom_histogram(binwidth = 7)



24.2.4.1 Density Plot

To create a density plot, use the geom_density(). Create a density plot for the mpg variable.

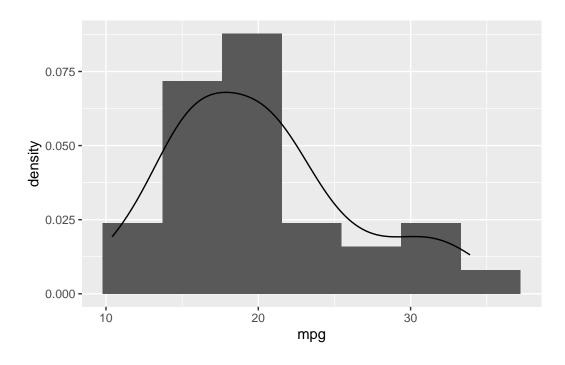
gg_3 + geom_density()



24.2.4.2 Both

Similar to adding lines and points in the same plot, you can add a histogram and a density plot by adding both the <code>geom_histogram()</code> and <code>geom_density()</code>. However, in the <code>geom_histogram()</code>, you must add <code>aes(y=..density..)</code> to create a frequency histogram. Create a plot with a histogram and a density plot.

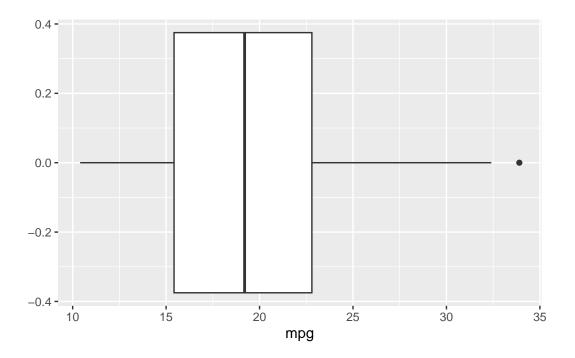
Warning: The dot-dot notation (`..density..`) was deprecated in ggplot2 3.4.0. i Please use `after_stat(density)` instead.



24.2.5 Box Plots

If you need to create a box plot, use the stat_boxplot(). Create a boxplot for the variable mpg. All you need to do is add stat_boxplot().

gg_3 + stat_boxplot()

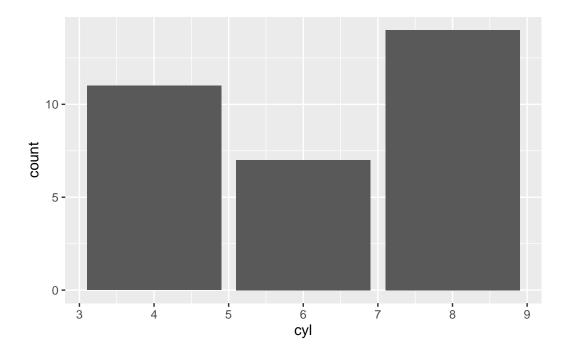


24.2.6 Bar Charts

Creating a bar chart is similar to create a box plot. All you need to do is use the stat_count(). First create a base plot using the mtcars data sets and the cyl variable for the mapping and assign it to gg_4.

Now create the bar plot by adding the stat_count().

gg_4 + stat_count()



24.2.7 Grouping

The 'ggplot2::" easily allows you to create plots from different groups. We will go over some of the arguments and functions to do this.

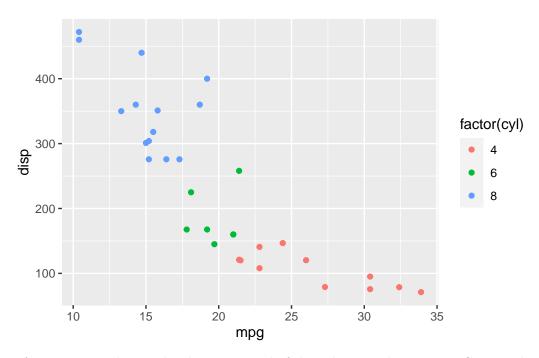
24.2.7.1 One Variable Grouping

24.2.7.1.1 Scatter Plot

To begin, we want to specify the grouping variable within the aes() with the color=. Additionally, the argument works best with a factor variable, so use the factor() to create a factor variable. Create a base plot from the mtcars data set using mpg and disp for the x and y axis, respectively, and set the color= equal to the factor(cyl). Assign it the R object gg_5.

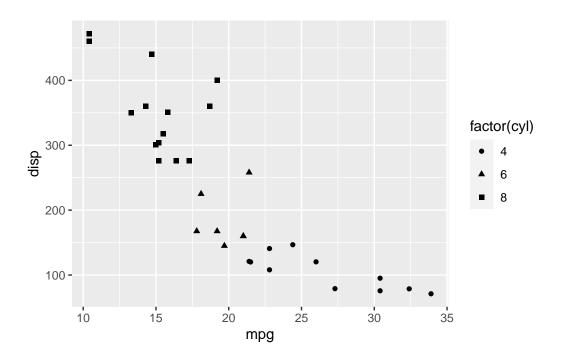
Once the base plot is created, 'ggplot2::" will automatically group the data in the plots. Create the scatter plot from the base plot.

gg_5 + geom_point()



If you want to change the shapes instead of the color, use the shape=. Create a base plot from the mtcars data set using mpg, and disp for the x and y axis, respectively, and group it by cyl with the shape=. Assign it the R object gg_6.

```
gg_6 <- ggplot(mtcars, aes(mpg, disp, shape=factor(cyl)))
gg_6 + geom_point()</pre>
```

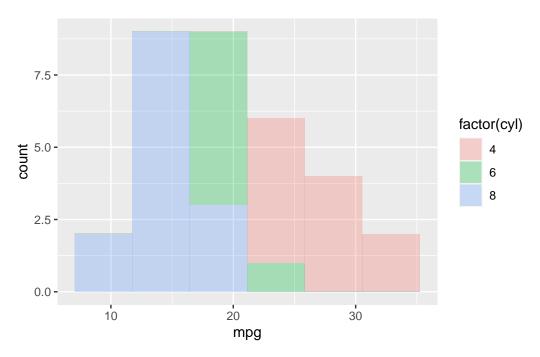


24.2.7.1.2 Histograms

Histograms can be grouped by different colors. This is done by using the fill= within the aes() in the base plot. Assign it the R object gg_7.

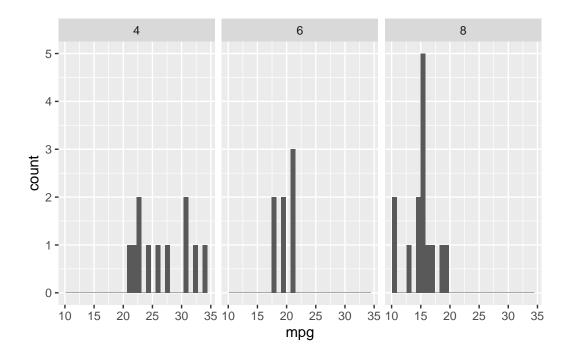
```
gg_7 <- ggplot(mtcars, aes(mpg, fill = factor(cyl)))</pre>
```

Now create a histogram from the base plot gg_7.



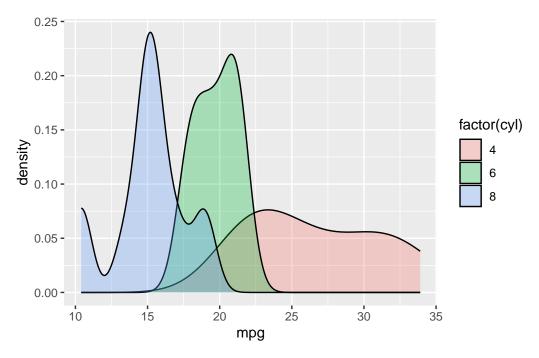
Sometimes we would like to view the histogram on separate plots. The facet_wrap() and the flact_grid() allows this. Using either function, you do not need to specify the grouping factor in the aes(). You will add facet_wrap() to the plot. It needs a formula argument with the grouping variable. Using the R object gg_3 create side by side plots using the cyl variable. Remember to add geom_histogram().

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



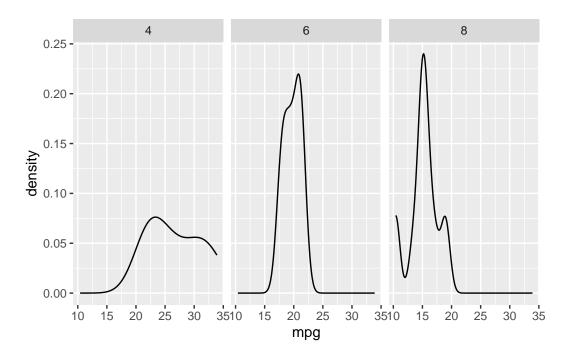
24.2.7.1.3 Density Plot

Similar to histograms, density plots can be grouped by variables the same way. Using gg_7, create color-coded density plots. All you need to do is add geom_density().



Using gg_3, create side by side density plots. You need to do is add geom_density() and facet_wrap() to group with the cyl variable.

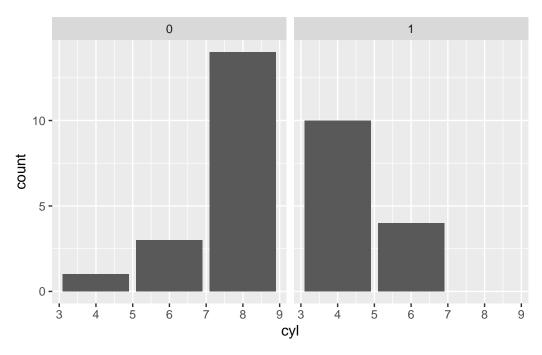
gg_3 + geom_density() + facet_wrap(~ cyl)



24.2.7.1.4 Bar Chart

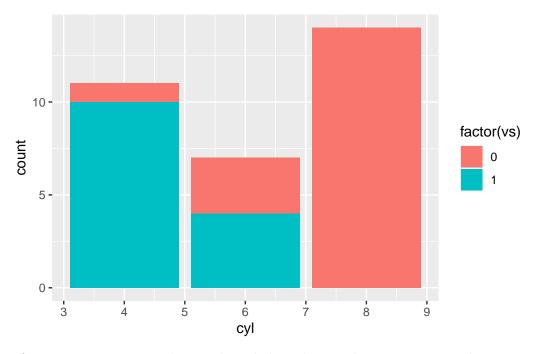
To create a side by side bar plot, you can use the facet_wrap() with a grouping variable. Using gg_4, create a side by side bar plot using vs as the grouping variable. Remember to add stat_count() as well.





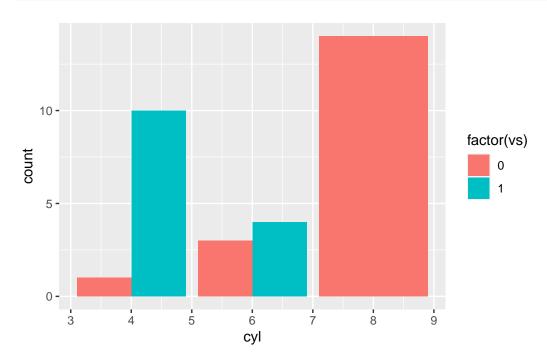
If you want to compare the bars from different group in one plot, you can use the fill= from the aes(). The fill= just needs a factor variable (use factor()). First create a base plot using the data mtcars, variable cyl and grouping variable vs. Assign it to gg_8.

Now create a bar chart by adding stat_count().



If you want to grouping bars to be side by side, use the position= in the stat_count() and set it equal to "dodge". Create the bar plot using the position = "dodge".

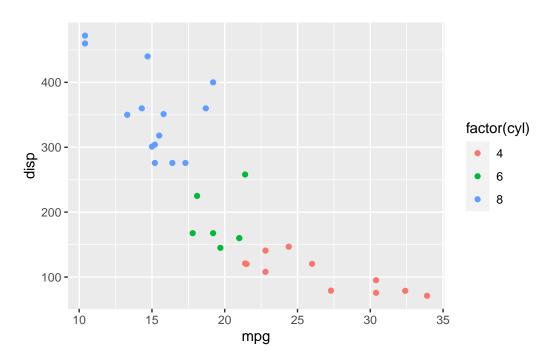




24.2.8 Themes/Tweaking

In this section, we will talk about the basic tweaks and themes to ggplot2::. However. ggplot2:: is much more powerful and can do much more. Before we begin, lets look at object gg_9 to understand the plot. To view a plot, use the plot().

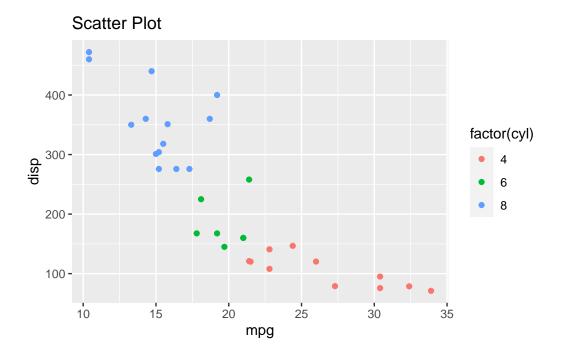




24.2.8.1 Title

To change the title, add the ggtitle() to the plot. Put the new title in quotes as the first argument. Change the title for gg_9.

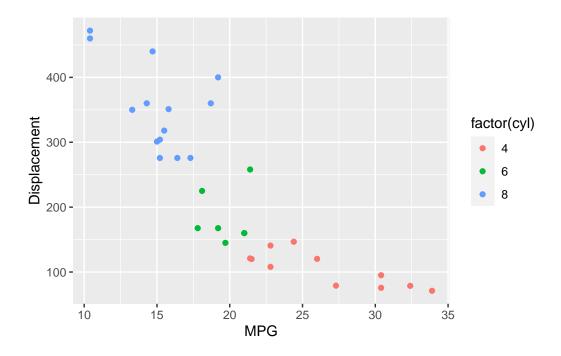
gg_9 + ggtitle("Scatter Plot")



24.2.8.2 Axis

Changing the labels for a plot, add the xlab() and ylab(), respectively. The first argument contains the phrase for the axis. Change the axis labels for gg_9.

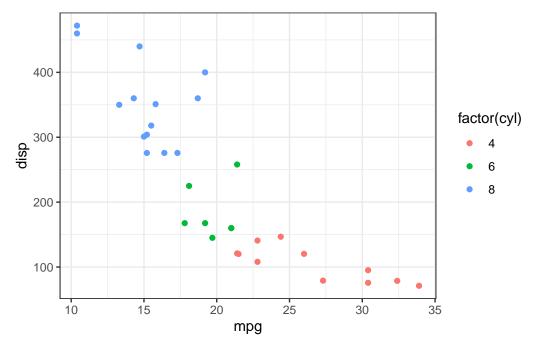
gg_9 + xlab("MPG") + ylab("Displacement")



24.2.8.3 Themes

If you don't like how the plot looks, ggplot2:: has custom themes you can add to the plot to change it. These functions usually are formatted as theme_*(), where the * indicates different possibilities. I personally like how theme_bw() looks. Change the theme of gg_9.

gg_9 + theme_bw()



Additionally, you can change certain part of the theme using the theme(). I encourage you to look at what are other possibilities.

24.2.9 Saving plot

If you want to save the plot, use the $\verb"ggsave"$ (). Read the help documentation for the functions capabilities.

Part VII Reporting Data

25 Quarto Documents

25.1 Introduction

Quarto is a file type used to create technical reports while including both R code, or other programming languages, and output in a document. A qmd¹ file is a fancy R Script containing extra capabilities. Additionally, qmd files allow for citations, footnotes, mathematical expressions, links, and much more. Once the document is finished, it can be rendered to a word file, pdf, html file, and much more. Quarto is the considered the next generation of RMarkdown.

25.2 Anatomy of a Quarto Document

There are three main components in an qmd file: the YAML header, R code, and basic text.

The YAML header contains information on how to render the document. It is located at the beginning of the document surrounded by 3 dashes (---) above and below it. For starters, the YAML header will contain a 'title', 'author', 'date', and 'output' line.

The R code is located in a block known as chunks. A chunk tells RStudio to read the next lines as code. A chunk begins with three back ticks followed by {r} and ends with three back ticks. Everything in between the back ticks will be executed by R. In RStudio, a chunk can be inserted using the keyboard shortcut ctrl+alt+I or cmd+option+I.

An example of an R chunk is shown below:

```
"" {r}
mean(mtcars$mpg)
"""
```

The R chunk will be rendered as below:

```
mean(mtcars$mpg)
```

¹QMD is the file extension to use the Quarto engine. For this document Quarto and QMD are used interchangeably.

Notice the chunk includes the code in a block followed by the output from the console.

The last component of an qmd document is the text. Write anywhere in the document, and it will be rendered as is.

25.3 Chunk Options

R chunks have options that will alter how the code or the output is rendered. The chunk options can be set either globally to affect the entire qmd document or locally to affect only an individual chunk. For more information about chunk options, visit https://yihui.org/knitr/options/

25.3.1 Global Chunk Options

To set global chunks options, add the two lines to YAML header:

```
knitr:
   opts_chunk:
---
```

Followed by the chunks and R options you want to set:

```
knitr:
  opts_chunk:
    eval: false
    tidy: styler
    R.options:
    digits: 2
```

A couple of recommended chunk options set globally are eval: false, and tidy: styler. These options make rendering the document easier.

One chunk option is tidy: styler. This tells Quarto to prevent code from printing in a long line, possibly off the page. For example, look at the output of this chunk:

```
## This comment is designed to show what happens when all your code is in 1 line. This is fi
```

Notice the comment being printed off the page. Using the options tidy: styler, the chunk is rendered as

```
## This comment is designed to show what happens when all
## your code is in 1 line. This is fine when you are
## coding, but when you are putting it in a report, it will
## run off the page.
```

The last 2 lines control how R will compute and print output. R.Options: tells Quarto that the options R will be changed, and each line after alters options. digits: 2 indicates R to use 2 significant digits.

25.3.2 Local Chunk Options

Local chunk options can be used to control an individual chunk will behave. To control a specific chunk, place the option below the $\{r\}$ identifier and use the $\#\$ chunk option indicator. An example is povided below:

```
#| eval: false
#| tidy: false
mean(mtcars$mpg)
```

The chunk option eval set to false tells Quarto to not evaluate the code within the chunk. Notice how the output was not printed the R chunk above. When we set eval to true, the output is printed:

```
"``{r}
#| eval: true
mean(mtcars$mpg)
"""
```

[1] 20.1

The echo option will control if the code within the chunk should be printed in the document. This next chunk contains #| echo: true:

```
mean(mtcars$mpg)
```

[1] 20.1

Now the chunk contains #| echo: false:

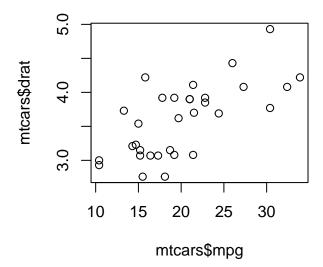
[1] 20.1

The R Code disappears.

There are chunk options for figures as well. A few options are fig-height, fig-width, fig-align, and fig-cap.

This chunk contains fig-height: 3.5; fig-width: 3.5; fig-align: left.

```
#| eval: true
#| fig-height: 3.5
#| fig-width: 3.5
#| fig-align: left
plot(mtcars$mpg, mtcars$drat)
```



The chunk options tells RStudio to create an image that is 3.5 inches in height and width, and align the image to the left.

The following chunk contains fig-height: 3.5; fig-width: 3.5; fig-align: left; fig-cap: "This is a scatter plot of MTCARS' MPG and DRAT"; label: fig-mtcars.

```
#| eval: true
#| fig-height: 3.5
#| fig-width: 3.5
#| fig-align: center
#| fig-cap: "This is a scatter plot of MTCARS' MPG and DRAT"
#| label: fig-mtcars
plot(mtcars$mpg, mtcars$drat)
```

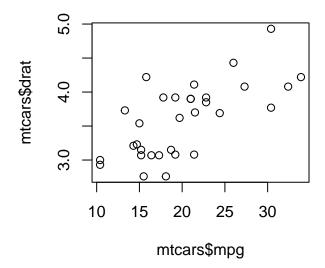


Figure 25.1: This is a scatter plot of MTCARS' MPG and DRAT

The chunk adds a caption with fig-cap and reference label with label. The label of the plot can be referenced later in the document. Figure 25.1 can be referenced with @fig-mtcars.

25.3.3 Inline Code

Instead of evaluating code in a chunk, code can evaluated in the text instead. For example, if we want to write the mean mpg in mtcars is 20.090625, one can type {r} mean(mtcars\$mpg), surrounded by back ticks (`), instead of writing the entire number and risk of miscopying the results.

25.4 Formatting

Qmd files contain basic formatting capabilities. The use of the # followed by text creates a heading. Using two or more # symbols will create subheadings based on the number of #. A text is *italicized* by surrounding the text with one asterisk (*italicized*). A text is **boldfaced** by surrounding it with 2 asterisk (**boldfaced**).

To create an unordered list, use the – symbol at the beginning of each line. To create a subitem, press the tab button twice (4 spaces), then the – symbol. Repeat this method for further sub-items.

- First Item
- Second Item
 - First Sub-Item
 - * First Sub-Sub-Item
 - · First Sub-Sub-Item

To created an ordered list, type the number followed by a period for each line. To create sub-lists, press the tab button twice and order them appropriately.

- 1. First
- 2. Second
 - a. First
 - b. Second
 - 1) First
 - 2) Second

A block quote is created with the > symbol at the beginning of a line.

Qmd files allows a table to be constructed in 2 ways, manually or using a package such as the gt package. A table is manually created by using |, :, and -. The first line contains | and the column names in between. The second line contains |:-|:-| which indicates how the table is aligned. The location of : symbol just tells RStudio about the alignment. Below is the example code of Table 25.3:

Letter	Lowercase		Code	Uppercase	Code
:	::	:	:	::	::
alpha	\$\alpha\$		`\alpha`		
beta	\$\beta\$		`\beta`		
gamma	$\gamma \$		`\gamma`		`\Gamma`
delta	\$\delta\$		`\delta`	\$\Delta\$	`\Delta`
epsilon	<pre>\$\epsilon\$</pre>		`\epsilon`		
zeta	\$\zeta\$		`\zeta`		
eta	\$\eta\$		`\eta`		
theta	\$\theta\$		`\theta`	\$\Theta\$	`\Theta`
iota	\$\iota\$		`\iota`		
kappa	\$\kappa\$		`\kappa`		
lambda	\$\lambda\$		`\lambda`	\$\Lambda\$	`\Lambda`
mu	\$\mu\$		`\mu`		
l nu l	\$\nu\$		`\nu`		
xi	\$\xi\$		`\xi`	\$\Xi\$	`\Xi`
pi	\$\pi\$		`\pi`	\$\Pi\$	`\pi`
rho	\$\rho\$		`\rho`		
sigma	\$\sigma\$		`\sigma`	\$\Sigma\$	`\Sigma`
tau	\$\tau\$		`\tau`		
upsilon	\$\upsilon\$		`\upsilon`	\$\Upsilon\$	`\Upsilon`
phi	\$\phi\$		`\phi`		`\Phi`
chi	\$\chi\$		`\chi`		
psi	\$\psi\$		`\psi`	\$\Psi\$	`\Psi`
omega	\$\omega\$	1	`\omega`	\$\Omega\$	`\Omega`
varepsilon	<pre>\$\varepsilon\$</pre>	1	`\varepsilon`		

The last line will adds a caption to the table and {#tbl-greektable} creates a label to reference the table in the text using @tbl-greektable.

The gt function from the gt package creates a table from a data frame or R object. Here is an example code to create a table from the first 6 rows of the mtcars dataset:

```
"``{r}
#| label: tbl-mtcarsdata
#| eval: true

mtcars |>
    head() |>
    gt::gt() |>
```

mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
21.0	6	160	110	3.90	2.62	16.5	0	1	4	4
21.0	6	160	110	3.90	2.88	17.0	0	1	4	4
22.8	4	108	93	3.85	2.32	18.6	1	1	4	1
21.4	6	258	110	3.08	3.21	19.4	1	0	3	1
18.7	8	360	175	3.15	3.44	17.0	0	0	3	2
18.1	6	225	105	2.76	3.46	20.2	1	0	3	1

Table 25.1

```
gt::tab_caption("The MTCARS Dataset")
```

Notice that Table 25.1 is easily produced using the gt() function with a caption

Table Table 25.1 is referenced by using the label created in the chunk and the @tbl-mtcarsdata. To install gt run the following line in your console:

```
install.packages("gt")
```

25.5 Citations and Referneces

Qmd documents contains capabilities to add citations and a bibliography. For example, to cite this textbook (mendenhallSecondCourseStatistics2012?), use the @ symbol followed by a citation identifier from the .bib file surrounded by square brackets, [@mendenhallSecondCourseStatistics2012]. To cite your textbook again (mendenhallSecondCourseStatistics2012?) without the authors names, use a - sign in front of the @ symbol, [-@mendenhallSecondCourseStatistics2012]. To cite multiple books (casellaStatisticalInference1990?; rohatgiIntroductionProbabilityStatistics2015?; resnickProbabilityPath2014?; lehmannTheoryPointEstimation1998?; lehmannTestingStatisticalHypotheses2005?), add each citation inside the square brackets with the @ symbol and separate them with semicolons, [@casellaStatisticalInference1990; @rohatgiIntroductionProbabilityStatistics2015; @resnickProbabilityPath2014; @lehmannTheoryPointEstimation1998; @lehmannTestingStatisticalHypotheses2005].

The references will be added automatically at the end of the document.

In order to use citations and references, the qmd file needs needs a .bib file containing all the information of the references. First, save the .bib file in the same folder (directory) as

your qmd file. Then add the line bibliography: NAME.bib to the YAML header. Make any changes appropriately to the line, such as the name of the .bib file.

25.5.1 .bib File

The .bib file is an ordinary text file containing "bib" entries with information about each reference. Below is an example bib entry about R:

```
@Manual{,
  title = {R: A Language and Environment for Statistical Computing},
  author = {{R Core Team}},
  organization = {R Foundation for Statistical Computing},
  address = {Vienna, Austria},
  year = {2023},
  url = {https://www.R-project.org/},
}
```

Creating a .bib file is tedious; however, there are reference managers that can help. I recommend using Zotero, an open-source reference manager designed to import and manage citations. Once a citation is in Zotero, you can export your library as a .bib file. Make sure to check your references in Zotero for any mistakes.

25.6 Math

Quarto is capable of writing mathematical formulas using LaTeX code. A mathematical symbol can be written inline using single \$ signs. For example, α in a document. To write mathematical formulas on its own line use \$\$. For example, \$\$Y=mX+b\$\$ is viewed as

$$Y = mX + b$$

.

25.6.1 Mathematical Notation

Table 25.2: LaTeX syntax for common examples.

Notation	code
$\overline{x=y}$	\$x=y\$
x > y	\$x>y\$

Notation	code
x < y	\$x <y\$< th=""></y\$<>
$x \ge y$	<pre>\$x\geq y\$</pre>
$x \le y$	<pre>\$x\leq y\$</pre>
x^y	\$x^{y}\$
x_y	\$x_{y}\$
$ar{x}$	<pre>\$\bar x\$</pre>
\hat{x}	<pre>\$\hat x\$</pre>
$ ilde{x}$	<pre>\$\tilde x\$</pre>
$\frac{x}{y}$	\$\frac{x}{y}\$
$\frac{x}{y}$ $\frac{\partial x}{\partial y}$	<pre>\$\frac{\partial x}{\partial y}\$</pre>
$x \in A$	<pre>\$x\in A\$</pre>
$x \subset A$	<pre>\$x\subset A\$</pre>
$x \subseteq A$	<pre>\$x\subseteq A\$</pre>
$x \cup A$	<pre>\$x\cup A\$</pre>
$x \cap A$	<pre>\$x\cap A\$</pre>
$\{1, 2, 3\}$	\$ \{1,2,3\}\$
$\int_a^b f(x)dx$	<pre>\$\int_a^bf(x)dx\$</pre>
$\begin{cases} \int_a^b f(x)dx \\ \left\{ \int_a^b f(x)dx \right\} \\ \sum_{i=1}^n x_i \\ \prod_{i=1}^n x_i \end{cases}$	$\left(\sum_a^b (x) dx\right) $
$\sum_{i=1}^{n} x_i$	\$\sum^n_{i=1}x_i\$
$\prod_{i=1}^{n} x_i$	<pre>\$\prod^n_{i=1}x_i\$</pre>
$\lim_{x\to 0} f(x)$	$\lim_{x\to 0} f(x)$
$X \sim \Gamma(\alpha, \beta)$	<pre>\$X\sim \Gamma(\alpha,\beta)\$</pre>

25.6.2 Greek Letters

Table 25.3: LaTeX syntax for greek letters.

Letter	Lowercase	Code	Uppercase	Code
alpha	α	\alpha	_	_
beta	β	\beta	_	_
gamma	γ	\gamma	Γ	\Gamma
delta	δ	\delta	Δ	\Delta
epsilon	ϵ	\epsilon	_	_
zeta	ζ	\zeta	_	_
eta	η	\eta	_	_
theta	heta	\theta	Θ	\Theta
iota	ι	\iota	_	_
kappa	κ	\kappa	_	_

Letter	Lowercase	Code	Uppercase	Code
lambda	λ	\lambda	Λ	\Lambda
mu	μ	\mu	_	_
nu	u	\nu	_	_
xi	ξ	\xi	Ξ	\Xi
pi	π	\pi	Π	\pi
rho	ho	\rho	_	_
sigma	σ	\sigma	Σ	\Sigma
tau	au	\tau	_	_
upsilon	v	υ	Υ	\Upsilon
phi	ϕ	\phi	Φ	\Phi
chi	χ	\chi	_	_
psi	ψ	\psi	Ψ	\Psi
omega	ω	\omega	Ω	\Omega
varepsilon	ε	$\vert varepsilon$	_	_

25.7 Rendering a Document

A qmd file can be rendered into either an html file, pdf document or word document. Rendering the qmd file to an html file or word document can be easily done using the knit button above. However, rendering the qmd file to a pdf document requires LaTeX to be installed. There are two methods to install LaTeX: from the LaTeX website or from R. I recommend installing the full LaTeX distribution from the https://www.latex-project.org/get/. This provides you with everything you may need. You can also install it from R:

```
install.packages("tinytex")
tinytex::install_tinytex()
```

You will only need to run these lines of code once and then you can render pdf documents easily.

HTML

format: html

PDF

```
format: pdf
---
```

Word Document

```
format: docx
```

25.8 Resources and Tips

Quarto

- Quarto
- Markdown Basics
- Formats

RMarkdown

- RStudio
- Bookdown

YAML

- UCLA Resource
- Reproducible Research
- RMarkdown Crash Course

Tips

- Render your document often so it easier to identify problems with rendering
- The Visual Mode in RStudio eases the process of creating a document and makes it more bearable.
- YAML is tricky with spacing. Make sure that spaces when indenting options. Also make sure that there are not extra spaces at the end of each line.

25.9 References

Presentations