Fizika 2 - izpeljave

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1 Valovna enačba

1.1

Faradejev 55 in Amperov 57 zakon lahko združimo v valovno enačbo.

1.2

•

$$ec{J}=0$$

$$ec{D}=\epsilon_0ec{E}$$

$$ec{B}=\mu_0ec{H}$$

$$\vec{E} = (0, E_y(x, t), E_z(x, t))$$

$$\vec{H} = (0, H_y(x, t), H_z(x, t))$$

1.3

$$\begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ E_x & E_y & E_z \end{vmatrix} = \left(\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z}, \frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x}, \frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) = \left(0, -\frac{\partial E_z}{\partial x}, \frac{\partial E_y}{\partial x} \right) =$$

$$= -\mu_0 \left(\frac{\partial H_x}{\partial t}, \frac{\partial H_y}{\partial t}, \frac{\partial H_z}{\partial t} \right) = -\mu_0 \left(0, \frac{\partial H_y}{\partial t}, \frac{\partial H_z}{\partial t} \right)$$
(1)

$$\frac{\partial E_z}{\partial x} = \mu_0 \frac{\partial H_y}{\partial t}$$
 (2)
$$\frac{\partial E_y}{\partial x} = -\mu_0 \frac{\partial H_z}{\partial t}$$
 (3)

$$\begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ H_x & H_y & H_z \end{vmatrix} = \left(\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z}, \frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_y}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}, \frac{\partial H_z}{\partial x} \right) = \left(0, -\frac{\partial H_z}{\partial x}$$

$$= \epsilon_0 \left(\frac{\partial H_x}{\partial t}, \frac{\partial H_y}{\partial t}, \frac{\partial H_z}{\partial t} \right) = \epsilon_0 \left(0, \frac{\partial H_y}{\partial t}, \frac{\partial H_z}{\partial t} \right)$$
 (4)

$$\frac{\partial H_z}{\partial x} = -\epsilon_0 \frac{\partial E_y}{\partial t}$$
 (5)
$$\frac{\partial H_y}{\partial x} = \epsilon_0 \frac{\partial E_z}{\partial t}$$
 (6)

1.5

$$\begin{split} \frac{\partial E_y}{\partial x} &= -\mu_0 \frac{\partial H_z}{\partial t} & \frac{\partial H_z}{\partial x} &= -\epsilon_0 \frac{\partial E_y}{\partial t} \\ \frac{\partial^2 E_y}{\partial x \partial t} &= -\mu_0 \frac{\partial^2 H_z}{\partial t^2} & \frac{\partial^2 H_z}{\partial x^2} - \epsilon_0 &= \frac{\partial^2 E_y}{\partial t \partial x} \end{split}$$

1.6

$$\frac{\partial^2 E_y}{\partial x^2} \frac{1}{-\mu_0} = -\epsilon_0 \frac{\partial^2 E_y}{\partial t^2} \tag{7}$$

1.7

$$E_y = E_0 \cos(\omega t - kx); \omega = 2\pi f, k = \frac{\omega}{c_0}$$
(8)

$$\frac{\partial^2 E_y}{\partial x^2} = -k^2 E_y; \frac{\partial^2 E_y}{\partial t^2} = -\omega^2 E_y \tag{9}$$

$$k^{2}E_{y}\frac{1}{-\epsilon_{0}\mu_{0}} = \omega^{2}E_{y} = \frac{\omega^{2}}{c_{0}^{2}}\frac{1}{-\epsilon_{0}\mu_{0}}E_{y}$$
(10)

$$\frac{1}{\epsilon_0 \mu_0} = c_0^2 \tag{11}$$

2 Lomni količnik

$$c = \frac{1}{\sqrt{\epsilon_r \epsilon_0 \mu_r \mu_0}}; c_0 = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$
 (12)

$$n = \frac{c}{c_0} = \sqrt{\frac{\epsilon_0 \mu_0}{\epsilon_r \epsilon_0 \mu_r \mu_0}} = \frac{1}{\sqrt{\epsilon_r \mu_r}}$$
 (13)

3 Lomni zakon

3.1

Minimiziramo čas preleta žarkov od točke A do točke B, ki sta v različnih medijih z različnimi n.

3.2

 $t(\alpha,\beta)$ ima ekstrem, če je dt=0

$$t = t_1 + t_2 \tag{14}$$

$$t = \frac{s_1}{c_1} + \frac{s_2}{c_2} \tag{15}$$

$$t = \frac{h_1}{\cos(\alpha) * c_1} + \frac{h_2}{\cos(\beta) * c_2}$$
 (16)

$$dt = \frac{\partial t}{\partial \alpha} d\alpha + \frac{\partial t}{\partial \beta} d\beta = 0$$
 (17)

$$\frac{h_1 \sin(\alpha)}{\cos^2(\alpha) * c_1} d\alpha = -\frac{h_2 \sin(\beta)}{\cos^2(\beta) * c_2} d\beta \tag{18}$$

$$\frac{d\alpha}{d\beta} = -\frac{h_2}{h_1} \frac{c_1}{c_2} \frac{\sin(\beta)}{\sin(\alpha)} \frac{\cos^2(\alpha)}{\cos^2(\beta)} \tag{19}$$

3.3

L je razdalja med točkama po y osi, ker je konstantna, je dL=0

$$L = l_1 + l_2 = \frac{h_1}{\tan(\alpha)} + \frac{h_2}{\tan(\beta)}$$
 (20)

$$dL = \frac{h_1}{\cos^2(\alpha)} d\alpha + \frac{h_2}{\cos^2(\beta)} d\beta = 0$$
 (21)

$$\frac{h_1}{\cos^2(\alpha)}d\alpha = -\frac{h_2}{\cos^2(\beta)}d\beta \tag{22}$$

$$\frac{d\alpha}{d\beta} = -\frac{h_2}{h_1} \frac{\cos^2(\beta)}{\cos^2(\alpha)} \tag{23}$$

$$-\frac{h_2}{h_1}\frac{c_1}{c_2}\frac{\sin(\beta)}{\sin(\alpha)}\frac{\cos^2(\alpha)}{\cos^2(\beta)} = -\frac{h_2}{h_1}\frac{\cos^2(\beta)}{\cos^2(\alpha)}$$
(24)

$$\Rightarrow \frac{\sin(\beta)}{\sin(\alpha)} = \frac{c_1}{c_2} = \frac{\frac{c_0}{n_1}}{\frac{c_0}{n_2}} = \frac{n_2}{n_1}$$
 (25)

$$\Rightarrow n_1 \sin(\alpha) = n_2 \sin(\beta) \tag{26}$$

4 Odbojni zakon

$$t = t_1 + t_2 \tag{27}$$

$$t = \frac{s_1}{c} + \frac{s_2}{c} \tag{28}$$

$$t = \frac{h}{\cos(\alpha) * c} + \frac{h}{\cos(\beta) * c} \tag{29}$$

$$dt = \frac{\partial t}{\partial \alpha} d\alpha + \frac{\partial t}{\partial \beta} d\beta = 0$$
 (30)

$$\frac{h\sin(\alpha)}{\cos^2(\alpha)*c}d\alpha = -\frac{h\sin(\beta)}{\cos^2(\beta)*c}d\beta \tag{31}$$

$$\frac{d\alpha}{d\beta} = -\frac{\sin(\beta)}{\sin(\alpha)} \frac{\cos^2(\alpha)}{\cos^2(\beta)} \tag{32}$$

4.1

L je razdalja med točkama po y osi, ker je konstantna, je dL=0

$$L = l_1 + l_2 = \frac{h}{\tan(\alpha)} + \frac{h}{\tan(\beta)} \tag{33}$$

$$dL = \frac{h}{\cos^2(\alpha)} d\alpha + \frac{h}{\cos^2(\beta)} d\beta = 0$$
 (34)

$$\frac{h}{\cos^2(\alpha)}d\alpha = -\frac{h}{\cos^2(\beta)}d\beta \tag{35}$$

$$\frac{d\alpha}{d\beta} = -\frac{\cos^2(\beta)}{\cos^2(\alpha)} \tag{36}$$

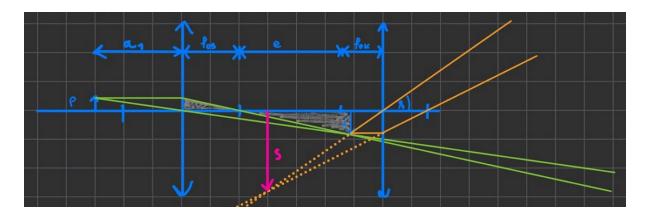
$$-\frac{\sin(\beta)}{\sin(\alpha)}\frac{\cos^2(\alpha)}{\cos^2(\beta)} = -\frac{\cos^2(\beta)}{\cos^2(\alpha)}$$
(37)

$$\Rightarrow \frac{\sin(\beta)}{\sin(\alpha)} = 1 \tag{38}$$

$$\Rightarrow \sin(\alpha) = \sin(\beta) \tag{39}$$

$$\Rightarrow \alpha = \beta \tag{40}$$

5 Mikroskop



$$\tan(\varphi_1) = \frac{p}{x_0} \tag{41}$$

$$\tan(\varphi_2) = \frac{i}{f_{ch}} \tag{42}$$

$$\frac{i}{e} = \frac{p}{f_{ob}} \tag{43}$$

$$tan(\varphi_1) = \frac{p}{x_0} \tag{41}$$

$$tan(\varphi_2) = \frac{i}{f_{ok}} \tag{42}$$

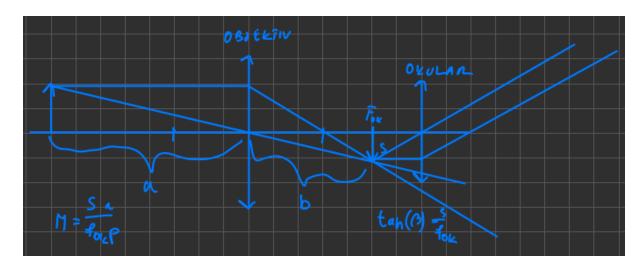
$$\frac{i}{e} = \frac{p}{f_{ob}} \tag{43}$$

$$M = \frac{\tan(\varphi_2)}{\tan(\varphi_1)} \tag{44}$$

$$M = \frac{ex_0}{f_{ok}f_{ob}} \tag{45}$$

$$M = \frac{ex_0}{f_{ok}f_{ob}} \tag{45}$$

Daljnogled



$$\tan(\varphi_1) = \frac{p}{a} = \frac{s}{b} \tag{46}$$

$$\tan(\varphi_2) = \frac{s}{f_{ok}} \tag{47}$$

$$\tan(\varphi_1) = \frac{p}{a} = \frac{s}{b}$$

$$\tan(\varphi_2) = \frac{s}{f_{ok}}$$

$$\frac{1}{f_{ob}} = \frac{1}{a} + \frac{1}{b} \Rightarrow b = \frac{af_{ob}}{a - f_{ob}}$$

$$M = \frac{\tan(\varphi_2)}{\tan(\varphi_1)} = \frac{b}{f_{ok}}$$

$$M = \frac{af_{ob}}{f_{ok}(a - f_{ob})}$$

$$(46)$$

$$(48)$$

$$(48)$$

$$(49)$$

$$M = \frac{\tan(\varphi_2)}{\tan(\varphi_1)} = \frac{b}{f_{ok}} \tag{49}$$

$$M = \frac{af_{ob}}{f_{ok}(a - f_{ob})} \tag{50}$$

Uporabljene enačbe

7.1 Matematika

Gradient

$$\vec{\nabla}f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}\right) \tag{51}$$

Divergenca

$$\vec{\nabla} \cdot \vec{F} = \frac{\partial F_x}{\partial x} + \frac{\partial F_y}{\partial y} + \frac{\partial F_z}{\partial z}$$
 (52)

Rotacija

$$ec{
abla} imes ec{F} = egin{array}{cccc} ec{i} & ec{j} & ec{k} \ rac{\partial}{\partial x} & rac{\partial}{\partial y} & rac{\partial}{\partial z} \ F_x & F_y & F_z \ \end{pmatrix}$$
 (53)

Maxwellove enačbe 7.2

Faradejev zakon v integralni obliki

$$\oint \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{S} \qquad (54)$$

Amperov zakon v integralni obliki

$$\oint \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{S} \qquad (54) \qquad \int \vec{H} \cdot d\vec{s} = \int J d\vec{S} + \int \frac{\partial \vec{D}}{\partial t} \cdot d\vec{S} \qquad (56)$$

Faradejev zakon v diferencialni obliki

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \tag{55}$$

$$\vec{\nabla} \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$
 (57)

7.3 Optika

Enačba preslikave

$$\frac{1}{f} = \frac{1}{a} + \frac{1}{b} \tag{58}$$

Mikroskop (5)

$$M = \frac{ex_0}{f_{ok}f_{ob}} \tag{61}$$

Enačba leče

$$\frac{1}{f} = (\frac{n_2}{n_1} - 1)(\frac{1}{R_1} - \frac{1}{R_2});$$
 (59)

R>0, če je središče krivulje na levi strani **Daljnogled (6)**

Lomni zakon (3)

$$n_1 \sin(\alpha) = n_2 \sin(\beta) \tag{60}$$

$$M = \frac{af_{ob}}{f_{ok}(a - f_{ob})} \tag{62}$$

Moderna fizika 7.4

Lorentzova transformacija

$$x' = \gamma(x - vt)$$
 $x = \gamma(x' + vt')$ (63)
 $y' = y$ $y = y'$ (64)
 $z' = z$ $z = z'$ (65)

$$y' = y \qquad y = y' \tag{64}$$

$$z' = z z = z' (65)$$

$$t' = \gamma(t - \frac{v}{c^2}x) \qquad t = \gamma(t' + \frac{v}{c^2}x') \quad (66)$$

Lorentzov faktor

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \tag{67}$$