

- 1) Give the dimension for each layer, and the number of weight parameters for each convolutional layer and the output layer**

Dimensions as set in tensorflow:

Input: data_set_size x 32 x 32 x 3

Labels: data_set_size

Weights:

$$W^1 = 5 \times 5 \times 3 \times 32$$

$$W_0^1 = \text{data_set_size} \times 28 \times 28 \times 32$$

$$W^2 = 5 \times 5 \times 32 \times 32$$

$$W_0^2 = \text{data_set_size} \times 10 \times 10 \times 32$$

$$W^3 = 3 \times 3 \times 32 \times 64$$

$$W_0^3 = \text{data_set_size} \times 3 \times 3 \times 64$$

$$W^o = 576 \times 10$$

$$W_0^o = \text{data_set_size} \times 10$$

Convolutional Layer 1: data_set_size x 28 x 28 x 32

Activation Layer 1: data_set_size x 28 x 28 x 32

Pooling Layer 1: data_set_size x 14 x 14 x 32

Convolutional Layer 2: data_set_size x 10 x 10 x 32

Activation Layer 2: data_set_size x 10 x 10 x 32

Pooling Layer 2: data_set_size x 5 x 5 x 32

Convolutional Layer 3: data_set_size x 3 x 3 x 64

Activation Layer 3: data_set_size x 3 x 3 x 64

Fully Connected Layer: data_set_size x 576

Output: data_set_size x 10

- 2) Implement in Tensorflow the back-propagation method to train the CNN. Initialize weights for all filters for the convolutional layers to small values and iteratively update them with appropriate learning rate until convergence. Plot the training and testing errors for each epoch. Save weights for all layers, as detailed in the attached instructions.**

Implementation attached as

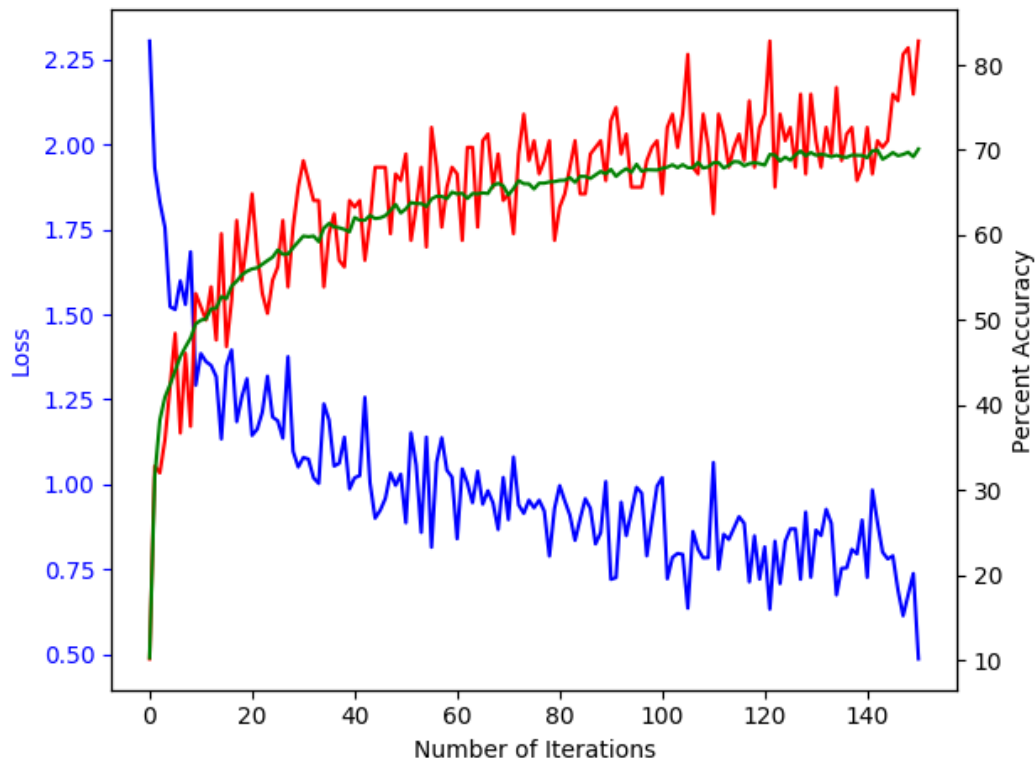
“pghw4_no_relu.py”

Plots:

Cost/Loss (Blue), Training Accuracy (Red) & Test Accuracy (Green):

x axis: Number of iterations $\div 200$

\therefore Total Number of Iterations: 30,000



All four files required (**weights**, model etc.) are attached.

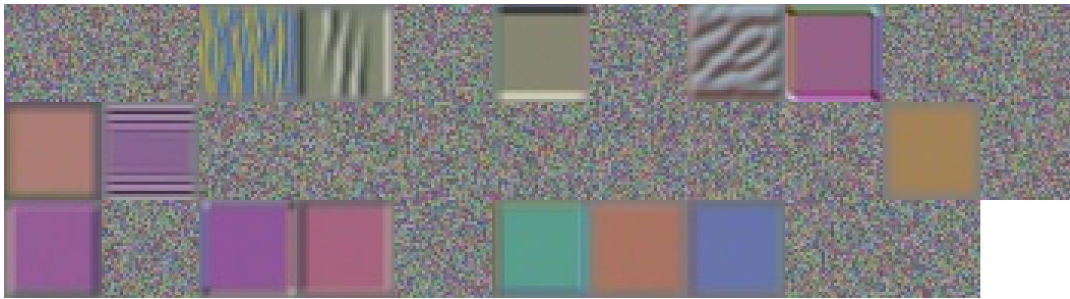
3) Visualize the learnt filters for the first convolution layer (see attached instructions).

Results with, both, before and after activation layers, respectively:

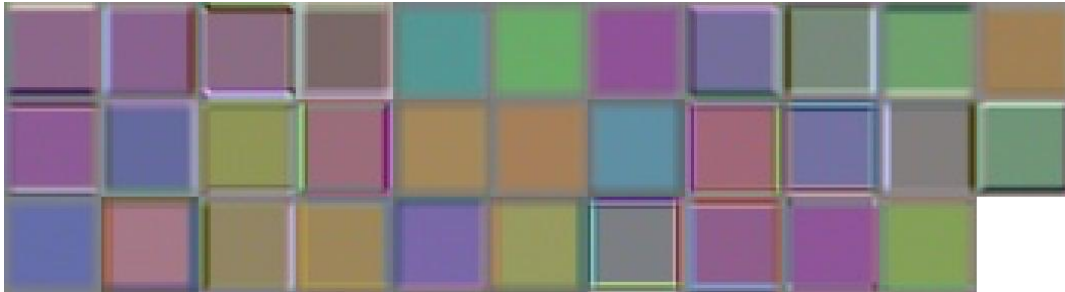
First Run, visualizing learnt filters by sending in the first convolutional layer after (ReLU) activation:



Second Run, visualizing learnt filters by sending in the first convolutional layer after (ReLU) activation but with noisy image + 100:



Last Run, visualizing learnt filters by sending in the first convolutional layer before activation:



- 4) Given the trained CNN, evaluate its performance on the testing dataset by computing its classification error for each class as well as the average classification errors for all 10 classes.

Final Cost: 0.4859

Final Average Training Accuracy: 82.8125

Final Average Test Accuracy: 70.1200

Final Average Training Error: 0.1788

Final Average Test Error: 0.2988

For classes [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

Total Number of Images for Each Class in Test Data:

$T = [488, 505, 512, 497, 507, 488, 491, 495, 504, 513]$

Number of Classification Images for Each Class in Test Data:

$I = [488, 505, 512, 497, 507, 488, 491, 495, 504, 513]$

Individual Classification Error for Each Class in Test Data:

Individual Error = $I \div T$

Individual Error: [0.250, 0.178, 0.463, 0.517, 0.387, 0.406, 0.151, 0.238, 0.167, 0.230]

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-----30000-----  
Loss: 0.48592621  
Training Accuracy: 82.8125  
Test Accuracy: 70.120000839233398  
  
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[[ 488.]  
 [ 505.]  
 [ 512.]  
 [ 497.]  
 [ 507.]  
 [ 488.]  
 [ 491.]  
 [ 495.]  
 [ 504.]  
 [ 513.]]  
[[ 366.]  
 [ 415.]  
 [ 275.]  
 [ 240.]  
 [ 311.]  
 [ 290.]  
 [ 417.]  
 [ 377.]  
 [ 420.]  
 [ 395.]]  
The Individual Errors are:  
[[ 0.25  
 [ 0.17821782]  
 [ 0.46289062]  
 [ 0.51710262]  
 [ 0.38658777]  
 [ 0.4057377 ]  
 [ 0.15071283]  
 [ 0.23838384]  
 [ 0.16666667]  
 [ 0.23001949]]  
Time Elapsed: 9053.509379863739
```