

Abstract

Scale is not an additive property of a system — it is an *expression of constraint geometry*. This paper formalizes scale as an emergent function of entropy distribution across nested cognitive, physical, or informational layers. The Entropy Foundation defines scale as the *distance between action potentials*, not the size of the container. This reframing allows universal application across physics, cognition, AI design, and socio-technical systems.

1. Definition of Scale

Scale describes the resolution boundary at which change becomes legible.

Unlike raw magnitude or size, scale is defined by:

1. The number of meaningful distinctions a system can encode
2. The energetic cost of reading or writing those distinctions
3. The stability of that resolution boundary under entropy pressure

Thus scale = resolution × stability × energetic tolerance.

2. The Entropy Stretch Principle

A system grows not by “getting bigger,” but by stretching its resolution boundary across higher entropy without collapse.

Let:

R = resolution layer

E = entropy applied

S = structural stability

Scaling = the ability to increase R under increasing E without reducing S below failure threshold.

3. Phase Transitions of Scale

Phase 0 — Locality

Phase 1 — Projection

Phase 2 — Topology

Phase 3 — Trans-Scale Systems

4. Entropic Cost per Resolution Unit

$$\text{ECPD} = E / (R \cdot S)$$

5. The Scaling Failure Modes

1. Resolution Drift
2. Energetic Starvation
3. Entropic Shear

6. Scaling Law for Cognitive Systems

$$\Delta R < \Delta S < \Delta E$$

7. Application Across Domains

AI Development, Education, Institutions, Physics, Sociology.

8. The Symbound Interpretation

Scale is the distance between two stable changes.

9. Conclusion

Scale is a dynamic ratio of entropy, stability, and resolution.

Appendix A: Key Terms

Entropy Stretch, ECPD, Stability Layer, Resolution Layer.

Appendix B: Companion Papers

entropy_foundation_ontic, entropy_foundation_energy, entropy_foundation_scope,
entropy_foundation_stability, entropy_vectors.