

Soal Latihan Transportasi

1.

dari ke	Gudang A (G ₁)	Gudang B (G ₂)	Gudang C (G ₃)	Kapasitas pabrik
pabrik W (P ₁)	Rp 20 x ₁₁	Rp 5 x ₁₂	Rp 8 x ₁₃	90
pabrik H (P ₂)	Rp 15 x ₂₁	Rp 20 x ₂₂	Rp 10 x ₂₃	60
pabrik P (P ₃)	Rp 25 x ₃₁	Rp 10 x ₃₂	Rp 19 x ₃₃	50
Kebutuhan	50	110	40	200

Biaya pengiriman minimumnya ?

Jawab

$$Z_{\min} = 20x_{11} + 5x_{12} + 8x_{13} + 15x_{21} + 20x_{22} + 10x_{23} + 25x_{31} + 10x_{32} + 19x_{33}$$

Dengan kendala :

$$\begin{aligned} x_{11} + x_{12} + x_{13} &= 90 && \text{(suplai dari P}_1\text{)} \\ x_{21} + x_{22} + x_{23} &= 60 && \text{(suplai dari P}_2\text{)} \\ x_{31} + x_{32} + x_{33} &= 50 && \text{(suplai dari P}_3\text{)} \\ x_{11} + x_{21} + x_{31} &= 50 && \text{(Permintaan dari G}_1\text{)} \\ x_{12} + x_{22} + x_{32} &= 110 && \text{(Permintaan dari G}_2\text{)} \\ x_{13} + x_{23} + x_{33} &= 40 && \text{(Permintaan dari G}_3\text{)} \end{aligned}$$

$$x_{ij} \geq 0,$$

$$i = 1, 2, 3 ; j = 1, 2, 3.$$

Tabel Transportasi

	A	B	C	Suplai
P ₁	x ₁₁ 20	x ₁₂ 5	x ₁₃ 8	90
P ₂	x ₂₁ 15	x ₂₂ 20	x ₂₃ 10	60
P ₃	x ₃₁ 25	x ₃₂ 10	x ₃₃ 19	50
Permintaan	50	110	40	200

model transportasi berimbang terbukti, yaitu :

$$\begin{aligned} \sum_{i=1}^m a_i &= \sum_{j=1}^n b_j \Rightarrow a_1 + a_2 + a_3 = b_1 + b_2 + b_3 \\ 90 + 60 + 50 &= 50 + 110 + 40 \\ 200 &= 200 \end{aligned}$$

• METODE NEW-CORNER *

	A	B	C	Suplai
P ₁	50 20	40 5		90
P ₂		60 20		60
P ₃		10 10	40 19	50
Permintaan	50	110	40	200

sel Baris nya :

$$\begin{aligned} P_1 - A & \rightarrow x_{11} \\ P_1 - B & \rightarrow x_{12} \\ P_2 - B & \rightarrow x_{22} \\ P_3 - B & \rightarrow x_{32} \\ P_3 - C & \rightarrow x_{33} \end{aligned}$$

$$(m+n)-1 = (3+3)-1$$

$$= 5$$

Sesuai dengan ketentuan.

$$\begin{aligned}
 Z_{\min} &= 50x_{11} + 40x_{12} + 60x_{21} + 10x_{32} + 40x_{33} \\
 &= 50 \cdot 20 + 40 \cdot 5 + 60 \cdot 20 + 10 \cdot 10 + 40 \cdot 19 \\
 &= 1000 + 200 + 1200 + 100 + 760 \\
 &= 3260
 \end{aligned}$$

• PENENTUAN OPTIMASI DENGAN STEPPING STONES •

Sel Bukan Basis	closed path (salurterutup)	Pengurangan biaya
$P_1 - C$	$+P_{1C} - P_{1B} + P_{2B} - P_{2C}$	$8 - 5 + 10 - 19 = -6$
$P_2 - A$	$+P_{2A} - P_{1A} + P_{1B} - P_{2B}$	$15 - 20 + 5 - 20 = -20$
$P_2 - C$	$+P_{2C} - P_{3C} + P_{3B} - P_{2B}$	$10 - 19 + 10 - 20 = -19$
$P_3 - A$	$+P_{3A} - P_{3B} + P_{1B} - P_{1A}$	$25 - 10 + 5 - 20 = 0$

Tabel awal metode new-corner belum optimum karena

$$P_2 - A = -20, \quad P_2 - C = -19, \quad P_1 - C = -6$$

• METODE NEW-CORNER (2) •

	A	B	C	Supply
P_1		90 $\begin{smallmatrix} 5 \\ 15 \end{smallmatrix}$		90
P_2	50 $\begin{smallmatrix} 15 \\ 10 \end{smallmatrix}$	10 $\begin{smallmatrix} 20 \\ 10 \end{smallmatrix}$		60
P_3		10 $\begin{smallmatrix} 10 \\ 15 \end{smallmatrix}$	40 $\begin{smallmatrix} 19 \\ 11 \end{smallmatrix}$	50
persamaan	50	110	40	200

sel paling negatif dipilih untuk masuk di basis ($P_2 - A$), sel yg akan keluar basis adalah $P_1 - A$ karena sel bertanda (-) dengan unit terkecil.

$$\begin{aligned}
 Z_{\min} &= 15x_{21} + 5x_{12} + 20x_{22} + 10x_{32} + 19x_{33} \\
 &= 15(50) + 5(90) + 20(10) + 10(10) + 19(40) \\
 &= 2260
 \end{aligned}$$

• METODE STEPPING STONE (2) •

Sel Bukan Basis	closed path	Pengurangan
$P_1 - A$	$P_{1A} - P_{1B} + P_{2B} - P_{2A}$	$20 - 5 + 20 - 15 = 20$
$P_1 - C$	$P_{1C} - P_{3C} + P_{3B} - P_{1B}$	$8 - 19 + 10 - 5 = -6$
$P_3 - A$	$P_{3A} - P_{2A} + P_{2B} - P_{3B}$	$25 - 15 + 20 - 10 = 20$
$P_2 - C$	$P_{2C} - P_{3C} + P_{3B} - P_{2B}$	$10 - 19 + 10 - 20 = -19$

Tabel ini belum optimum karena $P_1 - C = -6$, $P_2 - C = -19$.

• METODE NEW CORNER (3) •

	A	B	C	Supply
P_1		90 $\begin{smallmatrix} 15 \\ 10 \end{smallmatrix}$		90
P_2	50 $\begin{smallmatrix} 15 \\ 10 \end{smallmatrix}$		10 $\begin{smallmatrix} 19 \\ 10 \end{smallmatrix}$	60
P_3		20 $\begin{smallmatrix} 10 \\ 15 \end{smallmatrix}$	30 $\begin{smallmatrix} 19 \\ 11 \end{smallmatrix}$	50
Persamaan	50	110	40	200



$$\begin{aligned}
 Z_{\min} &= 15x_{21} + 5x_{12} + 10x_{32} + 10x_{23} + 19x_{33} \\
 &= 15(50) + 5(90) + 10(20) + 10(0) + 19(30) \\
 &= 2070
 \end{aligned}$$

* METODE STEPPING STONE (3) *

Sel Bkn Basis	closed path	Pengurangan
P_1-A	$P_1A - P_1B + P_3B - P_3C + P_2C - P_2A$	$20 - 5 + 10 - 19 + 10 - 15 = 1$
P_3-A	$P_3A - P_3C + P_2C - P_2A$	$25 - 19 + 10 - 15 = 1$
P_2-B	$P_2B - P_2C + P_3C - P_3B$	$20 - 10 + 19 - 10 = 19$
P_1-C	$P_1C - P_3C + P_3B - P_1B$	$8 - 19 + 10 - 5 = -6$

Tabel ini belum optimum karena $P_1-C = -6$

* METODE NEW CORNER (4) *

	A	B	C	Suplai
P_1		60 $\frac{15}{15}$	30 $\frac{8}{10}$	90
P_2	50 $\frac{10}{10}$		10 $\frac{10}{10}$	60
P_3		50 $\frac{10}{10}$		50
Permintaan	50	110	40	200

$$\begin{aligned}
 Z_{\min} &= 50x_{21} + 60x_{12} + 50x_{32} + 30x_{13} + 10x_{23} \\
 &= 50(15) + 60(5) + 50(10) + 30(8) + 10(10) \\
 &= 1890
 \end{aligned}$$

* METODE STEPPING STONE (4) *

Sel Bkn Basis	closed path	Pengurangan
P_1-A	$P_1A - P_1C + P_2C - P_2A$	$20 - 8 + 10 - 15 = 7$
P_3-A	$P_3A - P_2A + P_2C - P_1C + P_1B - P_3B$	$25 - 15 + 10 - 8 + 5 - 10 = 7$
P_2-B	$P_2B - P_2C + P_1C - P_1B$	$20 - 10 + 8 - 5 = 13$
P_3-C	$P_3C - P_1C + P_1B - P_3B$	$18 - 8 + 5 - 10 = 5$

Optimasi stepping stone (4) tidak ada nilai minus (-), maka nilai pada metode new corner (4) telah menunjukkan biaya alokasi pengiriman minimum yaitu 1.890

2.

Produksi pabrik perbulan

$P_1 = 50$

$P_2 = 50$

$P_3 = 45$

Permintaan perbulan

Sby = 55

mlg = 30

Diy = 60

Tabel Transportasi

	Surabaya (P_1)	Malang (P_2)	Diy (P_3)	
P_1	X_{11} 8	X_{12} 10	X_{13} 8	50
P_2	X_{21} 15	X_{22} 15	X_{23} 20	50
P_3	X_{31} 5	X_{32} 12	X_{33} 10	45
	55	30	60	145

$$Z_{min} = 8X_{11} + 10X_{12} + 8X_{13} + 15X_{21} + 15X_{22} + 20X_{23} + 5X_{31} + 12X_{32} + 10X_{33}$$

Dengan kendala :

$$X_{11} + X_{21} + X_{31}$$

= 50 (suplai dari P_1)

$$X_{21} + X_{22} + X_{23}$$

= 50 (suplai dari P_2)

$$X_{31} + X_{32} + X_{33}$$

= 45 (suplai dari P_3)

$$X_{11} + X_{21} + X_{31} = 55 \text{ (Permintaan dari } D_1)$$

$$X_{12} + X_{22} + X_{32} = 30 \text{ (Permintaan dari } D_2)$$

$$X_{13} + X_{23} + X_{33} = 60 \text{ (Permintaan dari } D_3)$$

* METODE NEW-CORNER *

	A	B	C	
P_1	50 8			50
P_2	5 15	30 15	15 20	50
P_3			45 10	45
	55	30	60	145

sel basisnya :

P_1-A X_{11}

P_2-A X_{21}

P_2-B X_{22}

P_2-C X_{23}

P_3-C X_{33}

Ada 5, sesuai dengan aturan

$$(m+n) - 1 = (3+3) - 1$$

$$= 5$$

$$Z_{min} = 50 \cdot X_{11} + 5 \cdot X_{21} + 30 \cdot X_{22} + 15 \cdot X_{23} + 45 \cdot X_{33}$$

$$= 50(8) + 5(15) + 30(15) + 15(20) + 45(10)$$

$$= 400 + 75 + 450 + 300 + 450$$

$$= 1.675$$

* METODE STEPPING STONE *

Sel Baris Basis	Closed Path	Pengurangan
P_3-A	$P_3-A - P_2-A + P_2-C - P_3-C$	$5 - 15 + 20 - 10 = 0$
P_1-B	$P_1-B - P_2-B + P_2-A - P_1-A$	$10 - 15 + 15 - 8 = 2$
P_3-B	$P_3-B - P_2-B + P_2-C - P_3-C$	$12 - 15 + 20 - 10 = 7$
P_1-C	$P_1-C - P_2-C + P_2-A - P_1-A$	$8 - 20 + 15 - 8 = -5$

(SIDU)

Tabel tersebut belum optimal karena $P_1 - C = -5$

* METODE NEW CORNER (2) *

	A	B	C	Supply
P_1	35 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$		15 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$	50
P_2	20 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$	30 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$		50
P_3			45 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$	45
	55	30	60	145

$$\begin{aligned}
 Z \text{ min} &= 35 \times 11 + 20 \times 21 + 30 \times 22 + 15 \times 13 + 45 \times 33 \\
 &= 35(8) + 20(15) + 30(15) + 15(8) + 45(10) \\
 &= 280 + 300 + 450 + 120 + 450 \\
 &= 1600
 \end{aligned}$$

* METODE STEPPING STONES (2) *

Sel Bukan Basis	Closed path	Pengurangan
$P_1 - B$	$P_1B - P_2B + P_2A - P_1A$	$10 - 15 + 15 - 8 = 2$
$P_2 - C$	$P_2C - P_1C + P_1A - P_2A$	$20 - 8 + 8 - 15 = 5$
$P_3 - A$	$P_3A - P_3C + P_1C - P_1A$	$5 - 10 + 8 - 8 = -5$
$P_3 - B$	$P_3B - P_2B + P_2A - P_1A + P_1C - P_3C$	$12 - 15 + 15 - 8 + 8 - 10 = 2$

Tabel tersebut belum optimal karena $P_3 - A = -5$

* METODE NEW CORNER (3) *

	A	B	C	Supply
P_1			50 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$	50
P_2	20 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$	30 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$		50
P_3	35 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$		10 $\begin{smallmatrix} \text{LE} \end{smallmatrix}$	45
	55	30	60	

$$\begin{aligned}
 Z \text{ min} &= 20 \times 21 + 35 \times 31 + 30 \times 22 + 50 \times 13 + 10 \times 33 \\
 &= 20(15) + 35(5) + 30(15) + 50(8) + 10(10) \\
 &= 300 + 175 + 450 + 400 + 100 \\
 &= 1425
 \end{aligned}$$

* METODE STEPPING STONES (3) *

Sel Bkn Basis	Closed path	Pengurangan
$P_1 - A$	$P_1A - P_1C + P_3C - P_3A$	$8 - 8 + 10 - 5 = 5$
$P_1 - B$	$P_1B - P_2B + P_2A - P_1A$	$10 - 15 + 15 - 8 = 2$
$P_3 - B$	$P_3B - P_3A + P_2A - P_2B$	$12 - 5 + 15 - 15 = 7$
$P_2 - C$	$P_2C - P_3C + P_3A - P_2A$	$20 - 10 + 5 - 15 = 0$

Optimasi stepping stones (3) tidak menunjukkan hasil minus (-), maka nilai pada metode new corner (3) telah menunjukkan biaya penginapan minimum, yaitu 1425.