

PR 1.

a. Average Distance

- Jarak antar node :

$$0-1 = 1$$

$$0-2 = 2$$

$$0-3 = 2$$

$$1-2 = 1$$

$$1-3 = 1$$

$$2-3 = 1$$

$$\text{- Jumlah total jarak} = 1+1+2+1+1+1 = 7$$

$$\text{- jumlah pasangan} = 6$$

$$\text{- Average distance} = 7/6$$

$$= 1,17$$

Komunitas biru

data antar node

$$4-10 = 1$$

$$4-11 = 2$$

$$4-12 = 2$$

$$4-13 = 2$$

$$10-11 = 1$$

$$10-12 = 1$$

$$10-13 = 1$$

$$11-12 = 1$$

$$11-13 = 2$$

$$12-13 = 1$$

$$\text{jumlah total jarak} = 1+2+2+2+1+1+1+1+2+1 = 14$$

$$\text{jumlah pasangan} = 10$$

$$\text{Average distance} = 14/10 = 1,4$$

b. Average embeddedness

Komunitas biru

Node 0 : edge internal = 2 , degree total = 2 \rightarrow 1.0
 1 : edge internal = 3 , degree total = 4 \rightarrow $\frac{3}{4} = 0.75$
 2 : edge internal = 3 , degree total = 3 \rightarrow 1.0
 3 : edge internal = 3 , degree total = 3 \rightarrow $\frac{2}{3} = 0.67$

Average embeddedness = $(1.0 + 0.75 + 1.0 + 0.67) / 4 = 0.855$

Komunitas merah

Node 4 : ed. internal = 1 , deg. total = 2 \rightarrow 0.5
 10 : ed. internal = 4 , deg. total = 5 \rightarrow $\frac{4}{5} = 0.8$
 11 : ed. internal = 2 , deg. total = 2 \rightarrow 1.0
 12 : ed. internal = 3 , deg. total = 3 \rightarrow 1.0
 13 : ed. internal = 2 , deg. total = 3 \rightarrow $\frac{2}{3} = 0.67$

Average embeddedness = $(0.5 + 0.8 + 1.0 + 1.0 + 0.67) = 0.994$

c. Average Internal degree

Komunitas biru

node 0 : 2
 1 : 3
 2 : 3
 3 : 2

Average = $(2 + 3 + 3 + 2) / 4 = 10 / 4 = 2.5$

Komunitas merah

node 4 : 1
 10 : 4
 11 : 2

node 12 : 3
 13 : 2

PR 2

A. MI

hasil deteksi kiri

komunitas A = {0, 1, 2}

B = {3, 4, 5}

hasil deteksi kanan

komunitas X = {0, 1, 2, 3}

Y = {4, 5}

Probabilitas :

total node = 6

$$P(A) = 3/6 = 0.5, P(B) = 3/6 = 0.5$$

$$P(X) = 4/6 = 0.667, P(Y) = 2/6 = 0.333$$

$$P(A, X) = 3/6 = 0.5, P(A, Y) = 0/6 = 0$$

$$P(B, X) = 1/6 = 0.167, P(B, Y) = 2/6 = 0.333$$

Hitung kombinasi

$$(A, X) = 0.5 \times \log_2 (0.5 / (0.5 \times 0.667)) = 0.5 \times \log_2 (1.5) \\ = 0.2925$$

$$(A, Y) = 0$$

$$(B, X) = 0.167 \times \log_2 (0.167 / (0.5 \times 0.667)) = 0.667 \times \log_2 (0.5) \\ = 0.167 \times (-1) = -0.167$$

$$(B, Y) = 0.333 \times \log_2 (0.333 / (0.5 \times 0.333)) = 0.333 \times \log_2 (2) \\ = 0.333 \times 1 = 0.333$$

$$\text{TOTAL MI} = 0.2925 + 0 - 0.167 + 0.333$$

$$= 0.4585$$

$$= 0.459$$

b. NMI

1. entropy $H(x)$ dan $H(y)$

$$H(x) = -[0.5 \log_2(0.5) + 0.5 \log_2(0.5)] = -2 \times 0.5 \times (-1) = 1$$

$$\begin{aligned} H(y) &= -[0.667 \log_2(0.667) + 0.333 \log_2(0.333)] \\ &= -[0.667 \times (-0.585) + 0.333 \times (-1.585)] \\ &= 0.390 + 0.528 \\ &= 0.918 \end{aligned}$$

2. NMI Formula

$$\begin{aligned} \frac{2 \times NMI}{H(x) + H(y)} &= \frac{2 \times 0.459}{1 + 0.918} \\ &= \frac{0.918}{1.918} \\ &= 0.479 \end{aligned}$$

c. Rand Index

1. Pasangan cocok

$$\text{tot pasangan node } \binom{6}{2} = 15$$

pasangan dalam komunitas sama di kedua deteksi

$$(0,1) (0,2) (1,2) (4,5) \rightarrow 4 \text{ pasangan cocok}$$

pasangan beda komunitas di kedua deteksi

$$(0,3) (0,4) (0,5) (1,3) (1,4) (1,5) (2,3) (2,4) (2,5) (3,4) (3,5)$$

11 pasangan cocok

$$\begin{aligned} \text{jml. pasangan cocok} &= 4 + 11 \\ &= 15 \text{ pasangan cocok} \end{aligned}$$

2. Rand Index

$$RI = \frac{\text{Jml. Pasangan Cocok}}{\text{Total pasangan}} = \frac{15}{15} = 1$$

$$RI = 1.0$$

4. ARI

$$\frac{\text{Index} - \text{Expected Index}}{\text{Max Index} - \text{Expected}}$$

$$= \frac{15}{15}$$

$$= 1.0$$