Departamento de Matemáticas



1. $y = 5x^6 - 3x^5 + 3x^3 - 2$

3.
$$y = 3x^{10} + 2\sqrt{x} + \frac{3}{x}$$

Derivadas

$$5. y = 4 senx - 3 cosx$$

7.
$$y = 4x^3 + 2x^3 - x^3 + 4$$

$$9. y = \cos(3x)$$

11.
$$y = sen(3x^2-2x)$$

13.
$$y = sen^3(2x^2)$$

15.
$$y = 3 \sin^2(2x-3)$$

17.
$$y = \cos(\sin x)$$

19.
$$y = \sqrt[3]{\cos^2 x}$$

21.
$$y = \sqrt{x^2 - 3x}$$

23.
$$y = (2 \sqrt{x} - 3x)^3$$

25.
$$y = \sqrt[5]{sen(3x)}$$

27.
$$y = (3x^2 - \sqrt{1-x^2})^3$$

29.
$$y = \sqrt{sen^3 x + (x-1)^3}$$

31.
$$y = \frac{x}{5}$$

33.
$$y = \frac{x^4 - 3x}{4}$$

35.
$$y = \frac{(x^4 - 3x)^2}{3}$$

37.
$$y = \frac{x^2}{x^2 - 1}$$

$$39. \quad y = \sqrt{\frac{3}{x}}$$

41. $y = \sqrt[3]{3x^2 - senx}$

43.
$$y = l n (x^2 - 3x)$$

45.
$$y = \log_2 (3 x^2)$$

47.
$$y = 2^x$$

49.
$$y = 3^{senx}$$

51.
$$y = 3 e^{x^2-3x}$$

53.
$$y = 3 tg^2 x$$

55.
$$y = x^2$$
 . $l n x$

57.
$$y = x^4 \cdot e^{3x}$$

2.
$$y = x^{-4} + 2x^{-3} + x-4$$

4.
$$y = \sqrt{3} \cdot x^3 - p \cdot x + \sqrt{3}$$

6.
$$y=2\sqrt{x}+\frac{2}{x}+x^{5}$$

8.
$$y = \frac{p}{2} \cdot \cos x - 3 \sqrt{x}$$

10.
$$y = \cos^2(x^3)$$

12.
$$y = \cos(x^2)$$

14.
$$y = \cos^4(3x^4)$$

16.
$$y = \cos^5(3x^2)$$

18.
$$y = \cos^2(\sin(3x))$$

20.
$$y = \sqrt[3]{\cos^2(x^2)}$$

22.
$$y = \sqrt[3]{(x^2 - 3x)^2}$$

24.
$$y = \sqrt[3]{sen^2 x}$$

$$26. \quad y = \sqrt{3x - senx}$$

28.
$$y = sen\left(\sqrt{3x^2 - 5x}\right)$$

30.
$$y = \cos^3(x^2 - 3\sqrt{x})$$

32.
$$y = \frac{5}{x}$$

34.
$$y = \frac{x^3 - 3}{x}$$

36.
$$y = \frac{(x-1)^3}{3x}$$

$$38. \ \ y = \frac{\sqrt{3x}}{x}$$

40.
$$y = \frac{x}{\sqrt{3}x}$$
Lectividad.intergr $\sqrt{3}x$

42.
$$y = l n(3x - 1)$$

44.
$$y = l \, n \, \sqrt{x-2}$$

46.
$$y = e^{x^2}$$

48.
$$y = e^{x^2-2x}$$

50.
$$y = tg(x^3)$$

52.
$$y = \sqrt{e^{\cos x}}$$

54.
$$y = (x^2 - 1) \cdot (x - 1)$$

56.
$$y = e^{x^2} \cdot \cos x$$

58.
$$y = e^{x^4 - 3x^2}$$
 . sen x



59.
$$y = l n x^2 \cdot e^{sen x}$$

61.
$$y = \left(\frac{x^2 - 3}{x^2 + 1}\right)^3$$

63.
$$y = (\cos^2 3x - \sin^3 x) \cdot e^{x^3}$$

$$65. \ \ y = \frac{l \, n \, x}{3^x}$$

67.
$$y = l n \left(\frac{sen x}{e^x} \right)$$

69.
$$y = \frac{3x^4 - 2x^2 + 3x - 2}{2x - 1}$$

71.
$$y = arctg(x^2)$$

73.
$$y = l n (\sec x)$$

75.
$$y = arcsen x \cdot e^{cosx}$$

77.
$$y = l n \left(\frac{tgx}{e^{3x^2}} \right)$$

79.
$$y = l n (arctg(5x))$$

81.
$$y = 5 \ arctg^2(senx)$$

83.
$$y = \frac{arcsen(3x-2)}{x^2}$$

85.
$$y = x^{senx}$$

87.
$$y = (\cos x)^{x^3-x}$$

89.
$$y = l n \left(\frac{x+2}{x^2} \right)^3$$

91.
$$y = 10^{\frac{senx-e^x}{3x-cosx}}$$

95.
$$y = \sqrt[3]{\frac{sen^2(e^x)}{arctg(cosx)}}$$

97.
$$y = \frac{\sqrt{\cos(e^x) \cdot x}}{\sqrt{e^{tgx}}}$$

99.
$$y = \sqrt{\frac{arctg e^x}{l n(x^2 - x)}}$$

$$60. \quad y = \frac{1}{l \, n \, \sqrt{x}}$$

62.
$$y = l n x \cdot e^{x^2 - senx}$$

64.
$$y = \left(\frac{\ln x^2}{x^3 - 2}\right)^2$$

$$66. \quad y = \frac{e^x + l \, n \, x}{x^2 - senx}$$

$$68. \quad y = \sqrt{\frac{sen x}{x-1}}$$

70.
$$y = (sen(e^{3x}))^2 \cdot cos x$$

72.
$$y = arcsen x^3$$

74.
$$y = arctg(l n x)$$

76.
$$y = arctg(e^{3x})$$

78.
$$y = arcsen\left(\frac{x+1}{e^x}\right)$$

80.
$$y = arctg \sqrt{x^3}$$

82.
$$y = 3^{arctg(x^2)}$$

84.
$$y = \frac{sen x - tg x}{\sqrt{4x - 3}}$$

86.
$$y = (sen x)^{x^2}$$

88.
$$y = 4^{arctg(ln x)}$$

90.
$$y = \left(\frac{e^{3x}}{senx}\right)^{x^2}$$

91.
$$y = I0\left(\frac{senx-e^x}{3x-cosx}\right)$$

92. $y = \cos\left(\frac{tg\sqrt{x}}{sen(lnx)}\right)$

93. $y = \frac{x^{cosx}}{(lnx)^3}$

94. $y = \cos^2(4e^x) \cdot ln\left(\frac{tgx}{3^{x^2}}\right)$

94.
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$$96. \quad y = \sqrt{\frac{e^{l \, n(\cos x)}}{5^{\cos x}}}$$

98.
$$y = (tg(e^x) + x^2)^x$$

100.
$$y = \frac{l \, n \, \sqrt{\cos x}}{sen(e^{cosx})}$$



SOLUCIONES

Todas las soluciones se dan sin simplificar

1.
$$y' = 30 x^5 - 15 x^4 + 9 x^2$$

3.
$$y' = 30 x^9 + \frac{1}{\sqrt{x}} - \frac{3}{x^2}$$

5.
$$y' = 4 \cos x + 3 \sin x$$

7.
$$y' = 15 x^2$$

9.
$$v' = -3 sen(3x)$$

11.
$$y' = \cos(3x^2 - 2x) \cdot (6x - 2)$$

13.
$$y' = 3 \operatorname{sen}^2(2x^2) \cdot \cos(2x^2) \cdot 4x$$

15.
$$y' = 6 \operatorname{sen}(2x - 3) \cdot \cos(2x - 3) \cdot 2$$

17.
$$y' = -sen(senx) \cdot cosx$$

19.
$$y' = \frac{-2 \cos x \cdot \sec x}{3 \sqrt[3]{\cos^4 x}}$$

21.
$$y' = \frac{2x-3}{2\sqrt{x^2-3x}}$$

23.
$$y' = 3 \left(2 \sqrt{x} - 3x \right)^2 \cdot \left(\frac{1}{\sqrt{x}} - 3 \right)$$
 24. $y' = \frac{2 \ senx \ cosx}{3 \sqrt[3]{sen^4 x}}$

25.
$$y' = \frac{3 \cos 3x}{5 \sqrt[5]{sen^4(3x)}}$$

27.
$$y' = 3 \left(3x^2 - \sqrt{1-x^2} \right)^2 \cdot \left(6x - \frac{-2x}{2\sqrt{1-x^2}} \right)$$

29.
$$y' = \frac{3 \operatorname{sen}^2 x \cos x + 3(x-1)^3}{2 \sqrt{\operatorname{sen}^3 x + (x-1)^3}}$$

30.
$$y' = -3\cos^2(x^2 - 3\sqrt{x})$$
. $sen(x^2 - 3\sqrt{x})$. $\left(2x - \frac{3}{2\sqrt{x}}\right)$
31. $y' = \frac{1}{5}$ 32. $y = -\frac{5}{2}$

31.
$$y' = \frac{1}{5}$$

33.
$$y' = \frac{4 x^3 - 3}{4}$$

35.
$$y' = \frac{2(x^4 - 3x)^2 \cdot (4x^3 - 3)}{3}$$

37.
$$y' = \frac{2x(x^2-1)-x^2.2x}{(x^2-1)^2}$$

2.
$$y' = -4 x^{-5} - 6 x^{-4} + 1$$

4.
$$y' = 3\sqrt{3} \cdot x^2 - p$$

6.
$$y' = \frac{1}{\sqrt{x}} - \frac{2}{x^2} + 5x^4$$

8.
$$y' = -\frac{p}{2} sen x - \frac{3}{2 \sqrt{x}}$$

10.
$$y' = -2 \cos(x^3)$$
. $sen(x^3)$. $3x^2$

12.
$$y' = -sen(x^2) \cdot 2x$$

14.
$$y' = 4 \cos^3(3 x^4) \cdot (-sen(3 x^4)) \cdot 12 x^3$$

16.
$$y' = 5 \cos^4(3 x^2)$$
. $(-sen(3 x^2))$. $6x$

18.
$$y' = 2\cos(sen3x) \cdot (-sen(sen3x)) \cdot \cos 3x \cdot 3$$

20.
$$y' = \frac{-2\cos(x^2) \cdot sen(x^2) \cdot 2x}{3\sqrt[3]{\cos^4(x^2)}}$$

22.
$$y' = \frac{2(x^2 - 3x)(2x - 3)}{3\sqrt[3]{(x^2 - 3x)^4}}$$

24.
$$y' = \frac{2 \ senx \ cosx}{3 \ \sqrt[3]{sen^4 x}}$$

26.
$$y' = \frac{3 - \cos x}{2 \sqrt{3x - \sin x}}$$

29.
$$y' = \frac{3 \operatorname{sen}^2 x \operatorname{cos} x + 3(x-1)^2}{2 \sqrt{\operatorname{sen}^3 x + (x-1)^3}}$$
 28. $y' = \cos\left(\sqrt{3} x^2 - 5x\right) \cdot \frac{6x - 5}{2 \sqrt{3} x^2 - 5x}$

32.
$$y = -\frac{5}{x^2}$$

34.
$$y' = 2x + \frac{3}{x^2}$$

36.
$$y' = \frac{3(x-1)^2 . 3x - 3(x-1)^3}{(3x)^2}$$

38.
$$y' = \frac{\frac{3}{2\sqrt{3x}} \cdot x - \sqrt{3x}}{x^2}$$

39.
$$y' = \frac{1}{2\sqrt{\frac{3}{x}}} \cdot \frac{-3}{x^2}$$

41.
$$y' = \frac{6 x - \cos x}{3 \sqrt[3]{(3 x^2 - \sin x)^2}}$$

43.
$$y' = \frac{2x - 3}{x^2 - 3x}$$

45.
$$y' = \frac{6 x}{3 x^2 \cdot l \, n2}$$

47.
$$y' = 2^x \cdot l \cdot n2$$

49.
$$y' = 3^{sen x} \cdot \cos x \cdot ln3$$

51.
$$y' = 3 e^{x^2-3x} \cdot (2x-3)$$

53.
$$y' = \frac{6 \ tgx}{\cos^2 x}$$

55.
$$y' = 2x \cdot l n x + \frac{x^2}{x}$$

57.
$$y' = 4 x^3 \cdot e^{3x} + x^4 e^{3x} \cdot 3$$

40.
$$y' = \frac{\sqrt{3} x - x \frac{3}{2\sqrt{3}x}}{3x}$$

42.
$$y' = \frac{3}{3x-1}$$

44.
$$y' = \frac{\frac{1}{2\sqrt{x-2}}}{\sqrt{x-2}}$$

46.
$$y' = e^{x^2}$$
. $2x$

48.
$$y' = e^{x^2-2x}$$
. $(2x-2)$

50.
$$y' = \frac{3 x^2}{\cos^2(x^3)}$$

52.
$$y' = \frac{-e^{\cos x} \ senx}{2\sqrt{e^{\cos x}}}$$

54.
$$y = 2x (x-1) + (x^2-1)$$

56.
$$y' = e^{x^2} 2x \cos x - e^{x^2} senx$$

58.
$$y' = e^{x^4 - 3x^2}$$
. $(4x^3 - 6x)$ sen $x + e^{x^4 - 3x^2}$ cos x

59.
$$y' = \frac{2x}{x^2}$$
. $e^{sen x} + l nx^2 e^{sen x} \cos x$ 60. $y' = \frac{-\frac{1}{2\sqrt{x}}}{(l n \sqrt{x})^2}$

61.
$$y' = 3\left(\frac{x^2-3}{x^2+1}\right)^2 \cdot \frac{2x(x^2+1)-(x^2-3)2x}{(x^2+1)^2}$$

62.
$$y' = \frac{1}{2} \cdot e^{x^2 - senx} + lnx \cdot e^{x^2 - senx} (2x - cosx)$$

62.
$$y' = \frac{1}{x} \cdot e^{x^2 - senx} + l \, nx \cdot e^{x^2 - senx} \, (2x - cosx)$$

63. $y' = \left(2\cos 3x \, \left(-sen3x \right) \, 3 - 3 \, sen^2 x \, cosx \, \right) \cdot e^{x^3} + \left(\cos^2 3x - sen^3 x \right) \, e^{x^3} \, 3 \, x^2$

64.
$$y' = 2\left(\frac{\ln x^2}{x^3 - 2}\right) \cdot \frac{\frac{2x}{x^2}(x^3 - 2) - \ln x^2 + 3x^2}{(x^3 - 2)^2}$$

65.
$$y' = \frac{\frac{1}{x} 3^x - \ln x 3^x \ln 3}{(3^x)^2}$$

67.
$$y' = \frac{e^x}{senx} \frac{\cos x \ e^x - e^x \ sen x}{(e^x)^2}$$

65.
$$y' = \frac{\frac{1}{x} 3^x - \ln x 3^x \ln 3}{(3^x)^2}$$
 66. $y' = \frac{\left(e^x + \frac{1}{x}\right)(x^2 - senx) - (e^x + \ln x)(2x - cosx)}{(x^2 - senx)^2}$

67.
$$y' = \frac{e^x}{senx} \frac{\cos x}{(e^x)^2} \frac{e^x}{(e^x)^2}$$
 68. $y' = \frac{1}{2\sqrt{\frac{sen x}{x-1}}} \cdot \frac{\cos x}{(x-1)^2} \cdot \frac{\cos x}{(x-1)^2}$



69.
$$y' = \frac{(12 x^3 - 4x + 3) (2x - 1) - (3 x^4 - 2 x^2 + 3x - 2) \cdot 2}{(2 x - 1)^2}$$

70.
$$y' = 2 \left(sen(e^{3x}) \right) . cos(e^{3x}) . e^{3x} 3 cosx - \left(sen(e^{3x}) \right)^2 . senx$$

72. $y' = \frac{3 x^2}{\sqrt{1 - x^6}}$

74. $y' = \frac{\frac{1}{x}}{(1 + (1 + x)^2)^2}$

76. $y' = \frac{e^{3x} \cdot 3}{1 + (e^{3x})^2}$

80. $y' = \frac{\frac{3x^2}{2\sqrt{x^3}}}{\frac{1}{2\sqrt{x^3}}}$

78. $y' = \frac{\frac{e^{x} - (x+1)e^{x}}{(e^{x})^{2}}}{\sqrt{1 - \left(\frac{x+1}{e^{x}}\right)^{2}}}$

82. $y' = 3^{arctg(x^2)} \frac{2x}{1+x^4} \ln 3$

71.
$$y' = \frac{2x}{1 + x^4}$$

73.
$$y' = \frac{\frac{\text{sen}x}{\cos^2 x}}{\sec x}$$

75.
$$y' = \frac{e^{\cos x}}{\sqrt{1-x^2}} - \arcsin x \quad e^{\cos x} \ sen x$$

77.
$$y' = \frac{e^{3x^2}}{tgx} \cdot \frac{e^{3x^2}}{\cos^2 x} - tgx e^{3x^2} \cdot 6x$$

79.
$$y' = \frac{1}{arctg(5x)} \frac{5}{1 + (5x)^2}$$

81.
$$y' = 10 \ arctg(senx) \ \frac{\cos x}{1 + sen^2 x}$$

83.
$$y' = \frac{3 x^2}{\sqrt{1 - (3x - 2)^2}} - arcsen(3x - 2) 2x$$

84.
$$y' = \frac{\left(\cos x - \frac{1}{\cos^2 x}\right)\sqrt{4x - 3} - (\sin x - tg x) \frac{4}{2\sqrt{4x - 3}}}{4x - 3}$$

85.
$$y' = \left(\cos x \cdot l \, n \, x + \frac{senx}{x} \right) \cdot x^{senx}$$

86.
$$y' = \left(2x \ln(senx) + \frac{x^2 \cos x}{senx}\right) (sen x)^{x^2}$$

87.
$$y = \left((3x^2 - 1) \ln \cos x - \frac{(x^3 - x) senx}{\cos x} \right) \cdot (\cos x)^{x^3 - x}$$

88.
$$y' = 4^{arctg(lnx)} \cdot \frac{\frac{1}{x}}{1 + (lnx)^2} \cdot ln4$$

89.
$$y' = \frac{1}{\left(\frac{x+2}{x^2}\right)^3} \cdot 3\left(\frac{x+2}{x^2}\right)^2 \cdot \frac{x^2 - 2x(x+2)}{x^4}$$



90.
$$y' = \left(2x \ln x \left(\frac{e^{3x}}{senx} \right) + x^2 \frac{senx}{e^{3x}} \frac{3 e^{3x} senx - e^{3x} cosx}{sen^2 x} \right) \cdot \left(\frac{e^{3x}}{senx} \right)^{x^2}$$

91.
$$y' = 10 \left(\frac{senx - e^x}{3x - cosx} \right)$$
. $ln 10 \left(\frac{(cosx - e^x)(3x - cosx) - (senx - e^x)(3 + senx)}{(3x - cosx)^2} \right)$

92.
$$y' = -sen\left(\frac{tg\sqrt{x}}{sen(lnx)}\right) \cdot \frac{\frac{1}{\cos^2 \sqrt{x}} \cdot \frac{1}{2\sqrt{x}} \cdot sen(lnx) - tg\sqrt{x} \cdot \cos(lnx) \cdot \frac{1}{x}}{sen^2(lnx)}$$

93.
$$y' = \frac{\left(-senx \ l \ n \ nx + \frac{cosx}{x}\right) x^{cosx} (l \ n \ x)^3 - x^{cosx} \ 3 (l \ n \ x)^2 \frac{1}{x}}{(l \ n \ x)^6}$$

94.

$$y' = 2 \cos(4e^{x}) \cdot (-sen(4e^{x}) \cdot 4e^{x} \cdot ln\left(\frac{tgx}{3^{x^{2}}}\right) + \cos^{2}(4e^{x}) \cdot \frac{3^{x^{2}}}{tgx} \cdot \frac{3^{x^{2}}}{\cos^{2}x} - tgx \cdot 3^{x^{2}} \cdot 2x \cdot ln3$$

95.
$$y = \frac{1}{2\sqrt{\frac{e^{\ln(\cos x)}}{5^{\cos x}}}} \cdot \frac{e^{\ln(\cos x)} - \sec x}{\cos x} \cdot 5^{\cos x} - e^{\ln(\cos x)} \cdot 5^{\cos x} (-\sec x) \ln 5}{(5^{\cos x})^2}$$

96.

96.
$$y' = \frac{1}{3\sqrt[3]{\frac{sen^2(e^x)}{arctg(\cos x)}}} \cdot \frac{2 sen(e^x) \cdot \cos(e^x) \cdot e^x \cdot arctg(\cos x) - sen^2(e^x) \cdot \frac{1}{1 + \cos^2 x} \cdot (-senx)}{arctg^2(\cos x)}$$

97.
$$y' = \frac{-\frac{sen(e^x) e^x x + \cos(e^x)}{\sqrt{\cos(e^x) \cdot x}} \cdot \sqrt{e^{tgx}} - \sqrt{\cos(e^x) \cdot x}}{e^{tgx}} \cdot \frac{1}{2\sqrt{e^{tgx}}} \cdot e^{tgx}}$$

98.
$$y' = \left(\ln(tge^x + x^2) + x \frac{\frac{e^x}{\cos^2(e^x)} + 2x}{tge^x + x^2} \right) \cdot (tg(e^x) + x^2)^x$$

99.

99.
$$y' = \frac{1}{2\sqrt{\frac{arctg \, e^x \cdot \cos x}{l \, n(x^2 - x)}}} \cdot \frac{\left(\frac{e^x}{1 + (e^x)^2} \cos x - arctg \, e^x \, senx\right) l \, n(x^2 - x) - (arctg \, e^x \, cosx) \frac{2x - 1}{x^2 - x}}{l \, n^2(x^2 - x)}$$

100.
$$y' = \frac{\frac{1}{\sqrt{\cos x}} \frac{-\sin x}{2\sqrt{\cos x}} \operatorname{sen}(e^{\cos x}) - \ln \sqrt{\cos x} \cos(e^{\cos x}) e^{\cos x} (-\sin x)}{\operatorname{sen}^2(e^{\cos x})}$$