

We can rewrite the conditional into $p(\mathbf{x}|\mathbf{z}) = \frac{p(\mathbf{x},\mathbf{z})}{p(\mathbf{z})}$ such that we get for the joint probability density:

$$p_{\hat{\theta}}(\mathbf{x}, \mathbf{z}) = p_{\hat{\theta}}(\mathbf{x}|\mathbf{z})p_{\hat{\theta}}(\mathbf{z}) \quad (1)$$

Let $G=(V,E)$ be a Bayesian Belief Network.

Furthermore, for every node $\mathbf{y} \in V$ its parents are random variables that \mathbf{y} is conditioned on. Let $\pi(\mathbf{y})$ be the set of parents of \mathbf{y} . Then we have that:

$$p(\mathbf{y}_1, \dots, \mathbf{y}_l) = \prod_{i=1}^l p(\mathbf{y}_i|\pi(\mathbf{y}_i)) \quad (2)$$

Every directed edge in E has a potential that is defined by a probability. If $\mathbf{y}_j \in \pi(\mathbf{y})$ the probability to reach \mathbf{y} from \mathbf{y}_j is defined by $p(\mathbf{y}|\mathbf{y}_j)$. Then the graph of a generator looks like that:

