

Let (Ω, \mathcal{A}, P) be a probability space, $(\mathbb{R}^l, \mathcal{B}(\mathbb{R}^l))$ a measurable space and $\epsilon : \Omega \rightarrow \mathbb{R}^l$ a random noise with $\epsilon \sim p(\epsilon)$ independent of the variational parameter.

Let $g(\cdot; \psi) : \mathbb{R}^l \times \mathbb{R}^m \rightarrow \mathbb{R}$ be a Borel measurable function s.t.:

1) g is a differentiable bijection

2) $g(\epsilon, \mathbf{x}; \psi) = \mathbf{z}$

where ψ is the variational parameter. The image of g depends also on the values of \mathbf{x} because they are needed to evaluate the reconstruction error.