Assignment 4: Writing functions

Due Sunday, November 28, 2021 @ 11:59pm

Public Health 280.346, Fall 2021 Your assignment for this module is to write a series of functions for calculating 95% confidence intervals for different population parameters. To help with this, relevant entries from the formula sheet in Public Health Biostatistics are reproduced at the end of this assignment.

To complete your assignment, do the following items. You can use the Assignment4_template.Rmd file to do your work. When completed, please submit your assignment through Github.

- (1) Write a function called mean_ci() that takes the arguments listed below and returns either a 95% confidence interval for a single mean or a 95% confidence interval for the difference in means depending on those arguments. I've given default values for these arguments as well.
 - x (no default value)
- y (default value is NULL which corresponds to one.mean option for the type argument)
- type (default value is one.mean, other value is two.means)
- ... (to be able to pass the na.rm option through to any functions as needed)

Include a a way to check whether the vectors of \mathbf{x} and \mathbf{y} are numeric and thus such a confidence interval is appropriate.

If you would like a way to check that your confidence intervals are correct, here is the code I will use to check that your function works appropriately:

```
set.seed(8675309)
x \leftarrow rnorm(50)
y \leftarrow rnorm(30)
           # should get [1] -0.1404677 0.3458514
mean ci(x)
mean ci(x, y, type="two.means") # should get [1] -0.1875458 0.7320355
# checking the na.rm piece
x2 \leftarrow c(x, NA)
y2 \leftarrow c(y, NA)
mean_ci(x2, y2, type="two.means") # should get [1] NA NA
mean_ci(x2, y2, type="two.means", na.rm=TRUE) # should get [1] -0.1875458 0.7320355
# checking the numeric piece
x3 <- c("hi", "how", "are", "you", "?")
mean_ci(x3)
                                     # should get an informative error
mean_ci(x3, y2, type = "two.means") # should get an informative error
# check the type piece
mean_ci(x2, y2, type = "two.groups") # should get an informative error
```

- (2) Write a function called prop_ci() that takes the arguments listed below and returns either a 95% confidence interval for a single proportion or a 95% confidence interval for the difference in proportions depending on those arguments. I've given default values for these arguments as well.
 - x (no default value)
- y (default value is NULL which corresponds to one.mean option for the type argument)
- type (default value is one.prop, other value is two.props)
- ... (to be able to pass the na.rm option through to any functions as needed)

Include a a way to check whether the vectors of \mathbf{x} and \mathbf{y} are 0/1 vectors and thus such a confidence interval is appropriate.

If you would like a way to check that your confidence intervals are correct, here is the code I will use to check that your function works appropriately:

```
set.seed(8675309)
x \leftarrow rbinom(50, 1, .5)
y \leftarrow rbinom(30, 1, .2)
           # should get [1] 0.4196006 0.7003994
prop_ci(x)
prop_ci(x, y, type="two.props") # should get [1] 0.1978071 0.5888596
# checking the na.rm piece
x2 \leftarrow c(x, NA)
y2 <- c(y, NA)
prop_ci(x2, y2, type="two.props") # should get [1] NA NA or an error message depending
                                    # on how checked for binary vectors
prop_ci(x2, y2, type="two.props", na.rm=TRUE) # should get [1] 0.1978071 0.5888596
# checking the binary piece
x3 \leftarrow c(3,4,5,2,0,1)
prop_ci(x3)
                                      # should get an informative error message
prop_ci(x3, y2, type = "two.props") # should get an informative error message
# check the type piece
prop_ci(x2, y2, type = "two.groups") # should get an informative error message
```

- (3) Extra credit: Write a function called ratio_ci() that takes the arguments listed below and returns either a 95% confidence interval for the odds ratio or a 95% confidence interval for the relative risk between two groups depending on those arguments. I've given default values for these arguments as well.
 - p1 the sample proportion in group 1 (no default value)
 - n1 the sample size in group 1 (no default value)
 - p2 the proportion in group 2 (no default value)
 - n2 the sample size in group 2 (no default value)
 - type (default value is odds.ratio, other value is risk.ratio)

Include a a way to check whether the values of p1 and p2 that are provided are proportions between 0 and 1.

The information on the next page of this assignment is part of the formula sheet for Public Health Biostatistics, which gives the standard errors for many statistics. It may be helpful as you complete this assignment!

Standard Errors

Mean

$$se_{\bar{x}} = \sqrt{\frac{s^2}{n}}$$

Proportion

$$se_{\hat{p}} = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

Difference of two Means

$$se_{\bar{x}_1 - \bar{x}_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

Difference of two Proportions

$$se_{\hat{p}_1 - \hat{p}_2} = \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$$

Log Relative Risk

$$se_{LRR} = \sqrt{\left(\frac{1}{\hat{p}_1 n_1} + \frac{1}{\hat{p}_2 n_2}\right) - \left(\frac{1}{n_1} + \frac{1}{n_2}\right)}$$

Log Odds Ratio

$$se_{LOR} = \sqrt{\frac{1}{\hat{p}_1 n_1} + \frac{1}{(1 - \hat{p}_1) n_1} + \frac{1}{\hat{p}_2 n_2} + \frac{1}{(1 - \hat{p}_2) n_2}}$$