

Influence of hyperparameters on aggregating predictions of unknown number of experts

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Using aggregation of expert forecasts is one of the important methods to improve prediction accuracy. This paper focuses on examining the influence of hyperparameters on the accuracy of the aggregation algorithm with an unknown number of experts. We implemented a time series generator with specified properties and an aggregating forecasting model. We conducted a series of experiments with various hyperparameters of the algorithm. Finding optimal hyperparameters leads to high performance and wider adoption of this prediction method.

Keywords: *online learning; aggregating algorithm; prediction with experts' advice; Fixed Share, Mixing Past Posteriors (MPP)*

1 Introduction

This work is inspired by the existing algorithm [3], which is based on the Fixed Share and Mixing Past Posteriors method. In contrast to the classical statistical theory of sequential prediction, we made no assumptions about the nature of the data (which could be deterministic, stochastic, etc.). We used machine learning methods to build forecasters within a game-theoretic approach. The online learning master model considers a series of reference forecasters, referred to as experts, to build its opinion by combining their predictions. The data is presented as a time series, consisting of outcome pairs — «signal» and «response».

The general prediction algorithm with expert advice follows this structure: Learning progresses in trials at discrete points in time. During each step, expert models, based on past observational data subsamples, provide their predictions. The master model then makes a decision using the chosen aggregating algorithm. At the end of the trial, the generator presents the true outcome, and both the master and expert models are scored using a loss function. The difference between the master's cumulative losses and the expert's cumulative losses is defined as regret. The traditional goal of the aggregating algorithm is to keep it as small as possible.

We use special assumptions about the data generation structure when building forecasting strategies. It is assumed that there are multiple generators, whose structure is unknown to the predictors. These generators alternate, producing a time series that is subdivided into a sequence of segments - areas of stationarity, which can be studied using machine learning methods. Each corresponding local predictive model will be constructed based on data from the area of stationarity and can be then successfully applied in other areas of stationarity generated by the same generator.

In this formulation of the forecasting problem, the series of prediction steps is divided into segments that frame arbitrary sequences of expert strategies. The sequence of segments and its associated sequence of experts is called a partition. The modified goal of the aggregating algorithm is to perform well relative to the best partition. Accordingly, the new concept of algorithm regret is the difference between the algorithm's losses and the cumulative losses of the sequence of experts. This change allows for a more accurate modeling of real-life conditions, where the nature of outcomes may change over time and different experts may predict with varying degrees of success depending on the current trend.

The corresponding algorithm is called Fixed Share [4]. A further proposed generalization of it is the Mixing Past Posteriors (MPP) method [5]. The cumulative losses of the aggregating algorithm are related to convex combinations of expert losses. The concept of regret also changes. Now the algorithm's cumulative losses are compared to the cumulative losses of convex combinations of expert strategies.

A characteristic feature of the problem considered in [3] is the absence of a predefined set of competing expert strategies, as was the case in the works cited above. Instead, new expert strategies are constructed at each step of the online learning process. The master must aggregate the forecasts of all expert strategies constructed up to that time in real-time at each step. Algorithm GMPP, proposed in [3], is the foundation of our experiments.

2 Problem statement

References

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