

# Influence of hyperparameters on aggregating predictions of infinite number of experts

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# Goal of research

Prediction is very difficult,  
especially if it's about the future.

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*Niels Bohr*

## Goal

Examining the influence of hyperparameters on the accuracy of the aggregation algorithm with an infinite number of experts

## Targets

1. Time series generator implementation
2. Aggregating algorithm implementation
3. Experiments with various hyperparameters

- ▶ V. V'yugin, V. Trunov. 2023. Prediction of Locally Stationary Data Using Prediction with Expert Advice.  
<http://www.jip.ru/2023/470-487-2023.pdf>
- ▶ N. Cesa-Bianchi, G. Lugosi. 2006. Prediction, Learning, and Games.  
[https://ii.uni.wroc.pl/~lukstafi/pmwiki/uploads/AGT/Prediction\\_Learning\\_and\\_Games.pdf](https://ii.uni.wroc.pl/~lukstafi/pmwiki/uploads/AGT/Prediction_Learning_and_Games.pdf).
- ▶ Hyndman, R. J. & Athanasopoulos, G., 2nd edition. 2018. Forecasting: Principles and Practice.  
<https://otexts.com/fpp2/>

# Problem statement

There are two kinds of forecasters: those who don't know, and those who don't know they don't know.

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*John Kenneth Galbraith*

## Data

It is assumed that there are multiple generators, whose structure is unknown to the predictors. These generators switch, producing a time series that is subdivided into a sequence of segments - areas of stationarity, which can be studied using machine learning methods.

## Generators implemented:

- ▶ Linear
- ▶ ARMA

# Problem statement

## Terms

- ▶  $X$  — signals space
- ▶  $Y$  — responses space
- ▶  $\mathcal{N}$  — set of experts, indexed by natural numbers
- ▶  $D$  — decision space, to which predictions belong
- ▶  $\lambda : D \times Y \rightarrow \mathbb{R}_+$  — nonnegative loss function
- ▶  $L_T^i = \sum_{t=1}^T l_t^i$  — cumulative loss of expert  $i$  during the first  $T$  steps
- ▶  $H_T = \sum_{t=1}^T h_t$  — master's cumulative loss during the first  $T$  steps
- ▶  $R_T^i = H_T - L_T^i$  — master's regret relative to the expert  $i$

# Problem statement

## Algorithm

FOR  $t = 1, 2, \dots$ :

1. Expert  $f^t$  initialization
2. Experts' predictions  $f_t^i = f_t^i(x_t)$ ,  $1 \leq i \leq t$
3. Master's prediction evaluation  $\gamma_t = \text{Subst}(\mathbf{f}_t, \hat{\mathbf{w}}_t)$
4. Computation of master's loss  $h_t = \lambda(p_t, y_t)$  and experts' losses  $l_t^i$
5. **Loss Update** weights modification
6. **Mixing Update** weights modification

ENDFOR

# Experiments

## Initialization weights

Default weights:  $w_1^i = \frac{1}{(i+1) \ln^2(i+1)}$

Experimental:  $\frac{1}{i^\alpha}$ ,  $\frac{1}{(i+1) \ln(i+1) \ln^2 \ln(i+c)}$ ,  $\frac{1}{e^i}$ , etc.

## Window size

As the algorithm does not know the locations of generator switches, finding an optimal training window is also a challenge.

## Mixing update coefficients

Default coefficient:  $\alpha_t = \frac{1}{t+1}$

Experimental:  $\frac{1}{(t+1)^\beta}$ ,  $\frac{1}{t+c}$ , etc.

Metric - master's regret relative to the ideal expert (best partition)

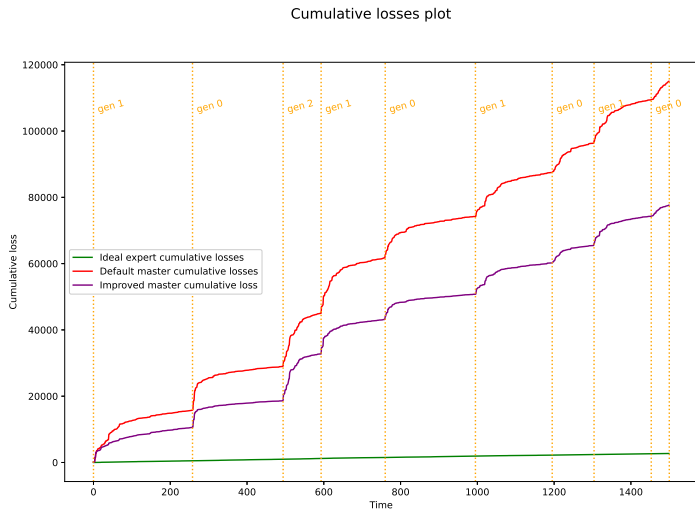
# Table

train_window	weight_function	regret
5	$1/((i + 1) * \ln^2(i + 1))$	224307.80
5	$1/(i^{1.01})$	175677.06
10	$1/((i + 1) * \ln^2(i + 1))$	142566.48
10	$1/(i^{1.01})$	98022.98
20	$1/((i + 1) * \ln^2(i + 1))$	135308.02
20	$1/(i^{1.01})$	93522.27

Table: Regret for different weight functions



# Losses plot



# Conclusion

## Summary

- ▶ Generators and algorithm implemented
- ▶ Correctness of the algorithm verified
- ▶ A series of experiments conducted
- ▶ Enhanced weight function achieved

## Further plans

- ▶ Run experiments on real data
- ▶ Theoretically prove that the obtained function is the best.

The End