

Ex1.a.

//AB1 ordin 2

```
echo off;
global kp tp zeta u;//ord 2; ord1: kp tp u; ord1sin: kp tp a omega;
//2poli 1zero: kp t1 t2 t3 u
kp=1;tp=2;zeta=0.3;tf=40;h=0.01;q=0.1;
u=1;t0=0;y10=0;y20=0;
t(1)=t0;
y(1,1)=y10;y(1,2)=y20;//ord2; ord1: y(1)=y0;
uc(1)=u;//treapta; sin: uc(1)=0
tc=t0;
yc2=[y10 y20];//ord2; ord1: yc2 = y0
yc1=yc2+h*ord2a(tc,yc2); //in functie de formula RK
tc=tc+h;
for i=2:q/h
    yc=yc1+h*(3*ord2a(tc,yc1)-ord2a(tc-h,yc2))/2; //formula AB, yk+1
//devine yc, yk devine yc1, yk-1 devine yc2, yk-2 devine yc3, yk-3
//devine yc4
    tc=tc+h;yc2=yc1;yc1=yc;
end;
t(2)=tc;
y(2,1)=yc(1);y(2,2)=yc(2);//ord2; ord1: y(2)=yc
uc(2)=u;//treapta; sin: uc(2)=a*sin(omega*tc)
for k=3:(tf-t0)/q+1
    for i=1:q/h
        yc=yc1+h*(3*ord2a(tc,yc1)-ord2a(tc-h,yc2))/2;//formula AB
        tc=tc+h;yc2=yc1;yc1=yc;
    end;
    t(k)=tc;
    y(k,1)=yc(1);y(k,2)=yc(2);//ord2, ord1: y(k)=yc
    uc(k)=u;//treapta; sin: uc(k)=a*sin(omega*tc)
end;
clf;

subplot(211);//doar la ord2
plot(t,y(:,1),'-r',t,uc,'-b');//ord2, ord1: plot(t,y,'-r',t,uc,'-b');
grid;
title('raspuns sistem ordin doi');
subplot(212);//doar la ord2
plot(t,y(:,2),'-r');//doar la ord2
grid;
title('derivata raspuns sistem ordin doi');
```

//AB3 ordin 1

```
echo off;
global kp tp u;
t(1)=t0;
y(1)=y0;uc(1)=u;
tc=t0;
yc4=y0;
k0=h*ord1(tc,yc4);
k1=h*ord1(tc+h,yc4+k0);
```

```

yc3=yc4+(k0+k1)/2;
tc=tc+h;
k0=h*ord1(tc,yc3);
k1=h*ord1(tc+h,yc3+k0);
yc2=yc3+(k0+k1)/2;
tc=tc+h;
k0=h*ord1(tc,yc2);
k1=h*ord1(tc+h,yc2+k0);
yc1=yc2+(k0+k1)/2;
tc=tc+h;
for i=4:q/h
    yc=yc1+h*(55*ord1(tc,yc1)-59*ord1(tc-h,yc2)...
        +37*ord1(tc-2*h,yc3)-9*ord1(tc-3*h,yc4))/24;
    yc4=yc3;yc3=yc2;yc2=yc1;yc1=yc;
    tc=tc+h;
end;
t(2)=tc;y(2)=yc;uc(2)=u;
for k=3:(tf-t0)/q+1,
    for i=1:q/h,
        yc=yc1+h*(55*ord1(tc,yc1)-59*ord1(tc-h,yc2)...
            +37*ord1(tc-2*h,yc3)-9*ord1(tc-3*h,yc4))/24;
        yc4=yc3;yc3=yc2;yc2=yc1;yc1=yc;
        tc=tc+h;
    end;
    t(k)=tc;y(k)=yc;uc(k)=u;
end;
clf;
plot(t,y,'-r',t,uc,'-b');
grid;
title('raspuns sistem ordin unu');

```

## //AM1 , 2 poli un zero

```

echo off;
global kp t1 t2 t3 u;
t(1)=t0;y(1,1)=y10;y(1,2)=y20;uc(1)=u;
tc=t0; yc1=[y10 y20 y30 y40];
for k=2:(tf-t0)/q+1
    for i=1:q/h
        k0=h*ord2plz(tc,yc1);
        k1=h*ord2plz(tc+h,yc1+k0);
        yc=yc1+(k0+k1)/2;
        yc=yc1+h*(ord2plz(tc+h,yc)+ord2plz(tc,yc1))/2;
        tc=tc+h;yc1=yc;
    end;
    t(k)=tc;y(k,1)=yc(1);y(k,2)=yc(2);uc(k)=u;
end;
clf;
subplot(211);
plot(t,y(:,1),'-r',t,uc,'-g');
grid;
title('raspuns sistem ordin doi');
subplot(212);
plot(t,y(:,2),'-r');
grid;
title('derivata raspuns sistem ordin doi');

```

## //AM2 sistem de ordin 2

```
echo off;
global kp tp zeta u;
t(1)=t0;y(1,1)=y10;y(1,2)=y20;uc(1)=u;
tc=t0; yc2=[y10 y20];
yc1=yc2+h*ord2a(tc,yc2);
tc=tc+h;
for i=2:q/h
    yc=yc1+h*ord2a(tc,yc2);
    yc=yc1+h*(5*ord2a(tc+h,yc)+8*ord2a(tc,yc1)-ord2a(tc-h,yc2))/12;
    tc=tc+h;yc2=yc1;yc1=yc;
end;
t(2)=tc;y(2,1)=yc(1);y(2,2)=yc(2);uc(2)=u;
for k=3:(tf-t0)/q+1
    for i=1:q/h
        yc=yc1+h*ord2a(tc,yc2);
        yc=yc1+h*(5*ord2a(tc+h,yc)+8*ord2a(tc,yc1)-ord2a(tc-h,yc2))/12;
        tc=tc+h;yc2=yc1;yc1=yc;
    end;
    t(k)=tc;y(k,1)=yc(1);y(k,2)=yc(2);uc(k)=u;
end;
clf;
subplot(211);
plot(t,y(:,1),'-r',t,uc,'-g');
grid;
title('raspuns sistem ordin doi');
subplot(212);
plot(t,y(:,2),'-r');
grid;
title('derivata raspuns sistem ordin doi');
```

## //AM3 , sistem de ordin 2

```
echo off;
global kp tp zeta u;
t(1)=t0;y(1,1)=y10;y(1,2)=y20;uc(1)=u;
tc=t0; yc3=[y10 y20];
yc2=yc3+h*ord2a(tc,yc3);
tc=tc+h;
yc1=yc2+h*ord2a(tc,yc2);
tc=tc+h;
for i=3:q/h
    yc=yc1+h*ord2a(tc,yc2);
    yc=yc1+h*(9*ord2a(tc+h,yc)+19*ord2a(tc,yc1)-5*ord2a(tc-h,yc2)+...
        ord2a(tc-2*h,yc3))/24;
    tc=tc+h;yc3=yc2;yc2=yc1;yc1=yc;
end;
t(2)=tc;y(2,1)=yc(1);y(2,2)=yc(2);uc(2)=u;
for k=3:(tf-t0)/q+1
    for i=1:q/h
        yc=yc1+h*ord2a(tc,yc2);
        yc=yc1+h*(9*ord2a(tc+h,yc)+19*ord2a(tc,yc1)-5*ord2a(tc-h,yc2)+...
            ord2a(tc-2*h,yc3))/24;
        tc=tc+h;yc3=yc2;yc2=yc1;yc1=yc;
    end;
    t(k)=tc;y(k,1)=yc(1);y(k,2)=yc(2);uc(k)=u;
end;
```

```

end;
t(k)=tc;y(k,1)=yc(1);y(k,2)=yc(2);uc(k)=u;
end;
clf;
subplot(211);
plot(t,y(:,1),'-r',t,uc,'-g');
grid;
title('raspuns sistem ordin doi');
subplot(212);
plot(t,y(:,2),'-r');
grid;
title('derivata raspuns sistem ordin doi');

```

### //PC1 , 2 poli un zero

```

echo off;
global kp t1 t2 t3 u;
t(1)=t0;y(1,1)=y10;y(1,2)=y20;uc(1)=u;
tc=t0; yc2=[y10 y20];
yc1=yc2+h*ord2plzb(tc,yc2);
tc=tc+h;
for i=2:q/h
    yca=yc1+h*(3*ord2plzb(tc,yc1)-ord2plzb(tc-h,yc2))/2;
    yc=yc1+h*(ord2plzb(tc+h,yca)+ord2plzb(tc,yc1))/2;
    while max(abs(yc(1)-yca(1)),abs(yc(2)-yca(2)))>prec
        yca=yc;
        yc=yc1+h*(ord2plzb(tc+h,yca)+ord2plzb(tc,yc1))/2;
    end;
    tc=tc+h;yc2=yc1;yc1=yc;
end;
t(2)=tc;y(2,1)=yc(1);y(2,2)=yc(2);uc(2)=u;
for k=3:(tf-t0)/q+1
    for i=1:q/h
        yca=yc1+h*(3*ord2plzb(tc,yc1)-ord2plzb(tc-h,yc2))/2;
        yc=yc1+h*(ord2plzb(tc+h,yca)+ord2plzb(tc,yc1))/2;
        while max(abs(yc(1)-yca(1)),abs(yc(2)-yca(2)))>prec
            yca=yc;
            yc=yc1+h*(ord2plzb(tc+h,yca)+ord2plzb(tc,yc1))/2;
        end;
        tc=tc+h;yc2=yc1;yc1=yc;
    end;
end;
t(k)=tc;y(k,1)=yc(1);y(k,2)=yc(2);uc(k)=u;
end;
clf;
subplot(211);
plot(t,y(:,1),'-r',t,uc,'-g');
grid;
title('raspuns sistem ordin doi');
subplot(212);
plot(t,y(:,2),'-r');
grid;
title('derivata raspuns sistem ordin doi');

```

```
//PC2 , un 2 poli zero [ord2plzb inlocuit cu numele  
fisierului functie]
```

```
echo off;  
global kp t1 t2 t3 u;  
t(1)=t0;y(1,1)=y10;y(1,2)=y20;uc(1)=u;  
tc=t0;yc3=[y10 y20];  
k0=h*ord2plzb(tc,yc3);  
k1=h*prd2plzb(tc+h/2,yc3+k0/2);  
k2=h*ord2plzb(tc+h,yc3+2*k1-k0);  
yc2=yc3+h*(k0+4*k1+k2)/6;  
tc=tc+h;  
k0=h*ord2plzb(tc,yc2);  
k1=h*ord2plzb(tc+h/2,yc2+k0/2);  
k2=h*ord2plzb(tc+h,yc2+2*k1-k0);  
yc1=yc2+h*k0+4*k1+k2)/6;  
tc=tc+h;  
for i=3:q/h  
    yca=yc1+h*(23*ord2plzb(tc,yc1)-16*ord2plzb(tc-h,yc2)+5*ord2plzb(tc-  
2*h,yc3)/12;  
    yc=yc1+h*(5*ord2plzb(tc+h,yca)+8*ord2plzb(tc,yc1)-ord2plzb(tc-  
h,yc2)/12;  
    while sqrt((yc(1)-yca(1))^2+(yc(2)-yca(2))^2)>prec  
        yca=yc;  
        yc=yc1+h*(5*ord2plzb(tc+h,yca)+8*ord2plzb(tc,ya)-ord2plzb(tc-  
h,yc2))/12;  
    end;  
    tc=tc+h;yc3=yc2;yc2=yca;yc1=yc;  
end;  
t(2)=tc;y(2,1)=yc(1);y(2,2)=yc(2);uc(2)=u;  
for k=3:(tf-t0)/q+1;  
    for i=1:q/h;  
        yca=yc1+h*(23*ord2plzb(tc,yc1)-16*ord2plzb(tc-  
h,yc2)+5*ord2plzb(tc-2*h,yc3))/12;  
        yc=yc1+h*(5*ord2plzb(tc+h,yca)+8*ord2plzb(tc,yc1)-ord2plzb(tc-  
h,yc2))/12;  
        while sqrt((yc(1)-yca(1))^2+(yc(2)-yca(2))^2)>prec  
            yca=yc;  
            yc=yc1+h*(5*ord2plzb(tc+h,yca)+8*ord2plzb(tc,yc1)-  
ord2plzb(tc-h,yc2))/12;  
        end;  
        tc=tc+h;yc3=yc2;yc2=yc1;yc1=yc;  
    end;  
    t(k)=tc;y(k,1)=yc(1);y(k,2)=yc2;uc(k)=u;  
end;  
clf;  
subplot(211);  
plot(t,y(:,1),'-r',t,uc,'-g');  
grid;  
title('raspuns sistem ordin doi');  
subplot(212);  
plot(t,y(:,2),'-r');  
grid;  
title('raspuns sistem ordin doi');
```

//PC3 ordin 1

```
echo off;
global kp tp u;
t(1)=t0;y(1)=y0;uc(1)=u;
tc=t0; yc4=y0;
k0=h*ord1(tc,yc4);
k1=h*ord1(tc+h/2,yc4+k0/2);
k2=h*ord1(tc+h,yc4+2*k1-k0);
yc3=yc4+h*(k0+4*k1+k2)/6;
tc=tc+h;
k0=h*ord1(tc,yc3);
k1=h*ord1(tc+h/2,yc3+k0/2);
k2=h*ord1(tc+h,yc3+2*k1-k0);
yc2=yc3+h*(k0+4*k1+k2)/6;
tc=tc+h;
k0=h*ord1(tc,yc2);
k1=h*ord1(tc+h/2,yc2+k0/2);
k2=h*ord1(tc+h,yc2+2*k1-k0);
yc1=yc2+h*(k0+4*k1+k2)/6;
tc=tc+h;
for i=4:q/h
    yca=yc1+h*(55*ord1(tc,yc1)-59*ord1(tc-h,yc2)+37*ord1(tc-2*h,yc3)...
        -9*ord1(tc-3*h,yc4))/24;
    yc=yc1+h*(9*ord1(tc+h,yca)+19*ord1(tc,yc1)-5*ord1(tc-h,yc2)...
        +ord1(tc-2*h,yc3))/24;
    while abs(yc-yca)>prec
        yca=yc;
        yc=yc1+h*(9*ord1(tc+h,yca)+19*ord1(tc,yc1)-5*ord1(tc-h,yc2)...
            -5*ord1(tc-h,yc2)+ord1(tc-2*h,yc3))/24;
    end;
    tc=tc+h;yc4=yc3;yc3=yc2;yc2=yc1;yc1=yc;
end;
t(2)=tc;y(2)=yc;uc(2)=u;
for k=3:(tf-t0)/q+1
    for i=1:q/h
        yca=yc1+h*(55*ord1(tc,yc1)-59*ord1(tc-h,yc2)+37*ord1(tc-2*h,yc3)...
            -9*ord1(tc-3*h,yc4))/24;
        yc=yc1+h*(9*ord1(tc+h,yca)+19*ord1(tc,yc1)-5*ord1(tc-h,yc2)...
            +ord1(tc-2*h,yc3))/24;
        while abs(yc-yca)>prec
            yca=yc;
            yc=yc1+h*(9*ord1(tc+h,yca)+19*ord1(tc,yc1)-5*ord1(tc-h,yc2)...
                +ord1(tc-2*h,yc3))/24;
        end;
        tc=tc+h;yc4=yc3;yc3=yc2;yc2=yc1;yc1=yc;
    end;
    t(k)=tc;y(k)=yc;uc(k)=u;
end;
clf;
plot(t,y,'-r',t,uc,'-g');
grid;
title('raspuns sistem ordin unu');
```

Ex1.b.

//ode23 ordin 1 sin

```

echo off;
global kp tp a w; //pui ce variabile ai in fisierul functie
kp=2;tp=1;a=1;w=1;t0=0;tf=20;y0=0;
[t,y]=ode23('ord1sin',[t0 tf],y0);
for i=1:length(t);
    uc(i)=a*sin(w*t(i));
end;
clf;
plot(t,y,'-r',t,uc,'-b');
grid;
title('raspuns sistem ordin unu');

```

## //ode23 ordin 2

```

echo off;
global kp t1 t2 t3 u;
kp=2;t1=10;t2=1;t3=2;u=1;t0=0;tf=40;y10=0;y20=0;
[t,y]=ode23('ord2p1zb',[t0 tf],[y10 y20]);
for i=1:length(t);
    uc(i)=u;
end;
clf;
subplot(211);
plot(t,y(:,2),'-r',t,uc,'-g');
grid;
title('raspuns sistem ordin doi');
subplot(212);
plot(t,y(:,1),'-r');
grid;
title('derivata raspuns sistem ordin doi');

```

Ex2 //sisteme - apel newtraph

```

function [sol,iter]=newtraph(F,dF,x0,prec)
n=length(x0);
dx=2*prec*ones(n,1);
x_c=x0;
iter=0;
while (norm(dx)>prec),
    J=feval(nume_dF,x_c);
    dx=-inv(J)*feval(F,x_c);
    x_c=x_c+dx;
    iter=iter+1;
end;
sol=x_c;

```

```
[xstar,iter]=newtraph('F','dF',[-1,3,-2])
```

```

//gradient [minim / maxim al unei functii]
function [x,nr_it]=opt_grad(x0,epsilon)
nr_it=1;x_curent=x0;itermax=1500;

```

```

h=0.001;
p=0.001;
for k=1:n,
v=zeros(1,n);v(k)=1;
grad_curent(k)=(f1(x0+h/2*v)-f1(x0-h/2*v))/h;
end;
while (norm(grad_curent)>=epsilon)&(nr_it<=itermax)
%pentru o funcție de maximizat „-” se înlocuiește cu „+”
x_viitor=x_curent-p*grad_curent/norm(grad_curent);
for k=1:n,
v=zeros(1,n);v(k)=1;
grad_viitor(k)=(f1(x_viitor+h/2*v)-f1(x_viitor-h/2*v))/h;
end;
x_curent=x_viitor;
grad_curent=grad_viitor;
nr_it=nr_it+1;
end;
x=x_curent;

```

```

function y=f1(x)
y=5*x^2+2*x+13;

```

**//apel\_opt\_grad**

```

[x,nr_it]=opt_grad(0,1e-3)

```

```

//ex3 subpunct c) matrice monica m > n
echo off;
[m,n]=size(a);

```

```

a1=a;

```

```

q=eye(m);

```

```

for k=1:n

```

```

    sig=0;

```

```

    for i=k:m

```

```

        sig=sig+a(i,k)^2;

```

```

    end

```

```

    sig=sign(a(k,k))*sqrt(sig);

```

```

    for i=1:m

```

```

        if i<=k-1

```

```

            v(i)=0;

```

```

        elseif i==k

```



```

        v(i)=sig+a(k,k);
    else v(i)=a(i,k);
    end

end

beta=sig*(sig+a(k,k));
q1=eye(m)-(v'*v)/beta;
q=q*q1;
a=q1*a;

end

//ex3 subpunct c) matrice patratica n x n
echo off;
[m,n]=size(a);

q=eye(m);

p=eye(n);

a1=a;

k=1;

prec=1e-4;

ind=1;

for j=1:n
    norm(j)=0;
    for i=1:m
        norm(j)=norm(j)+a(i,j)^2;
    end
end

end

while ind ==1 & k<=n
    l=k;
    for j=k+1:n
        if norm(j)>norm(l)
            l=j;
        end
    end
end

```

```

end
if norm(l)==0
    ind=0;
else if l~=k
    p1=eye(n);p1(k,k)=0;p1(l,l)=0;p1(l,k)=1;p1(k,l)=1;
    a=a*p1;
    p=p1*p;
end
sig=0;
for i=k:m
    sig=sig+a(i,k)^2;
end
sig=sign(a(k,k))*sqrt(sig);
for i=1:m
    if i<=k-1
        v(i)=0;
    elseif i==k
        v(i)=sig+a(k,k);
    else v(i)=a(i,k);
    end
end
end
beta=sig*(sig+a(k,k));
q1=eye(m)-(v'*v)/beta;
a=q1*a;
q=q1*q;
for j=k+1:n
    norm(j)=0;
    for i=k+1:m
        norm(j)=norm(j)+a(i,j)^2;
    end
end

```

```

        end
    end
    k=k+1;
end
end
r=0;
for i=1:min(m,n)
    if r<=min(m,n)
        if abs(a(i,i))>prec
            r=r+1;
        end
    end
end
end
a=a';
q2=eye(n);
p2=eye(r);
for k=1:r
    sig=0;
    for i=k:n
        sig=sig+a(i,k)^2;
    end
    sig=sign(a(k,k))*sqrt(sig);
    for i=1:n
        if i<=k-1
            v(i)=0;
        elseif i==k
            v(i)=sig+a(k,k);
        else v(i)=a(i,k);
        end
    end
end

```

```

        end

        beta=sig*(sig+a(k,k));
        q1=eye(n)-(v'*v)/beta;
        a=q1*a;
        q2=q2*q1;
    end

    Z=p*q2;
    aint=a;
    for k=r:-1:1
        a(k,k)=1/a(k,k);
        for i=k-1:-1:1
            s=0;
            for j=i+1:r
                s=s+a(i,j)*a(j,k);
            end
            a(i,k)=-s/a(i,i);
        end
    end

    end

    psa=Z*a*q;

```

