Programming Paradigms

Lecture 7

Slides are from Prof. Chin Wei-Ngan from NUS

Types, ADT, Components

Reminder of Last Lecture

- Tupled Recursion
- Exceptions

Overview

- Types
- Abstract Data Types
- Haskell
- Design Methodology

Dynamic Typing

- Oz/Scheme uses dynamic typing, while Java uses static typing.
- In dynamic typing, each value can be of arbitrary types that is only checked at runtime.
- Advantage of dynamic types
 - no need to declare data types in advance
 - more flexible
- Disadvantage
 - errors detected late at runtime
 - less readable code

Type Notation

Every value has a type which can be captured by:

```
e :: type
```

- Type information helps program development/documentation
- Many functions are designed based on the type of the input arguments

List Type

- Based on the type hierarchy
 - □ (Value), (Record),...
 - \square $\langle Record \rangle \subset \langle Value \rangle$
 - The Record type is a subtype of the Value type
 - List is either nil or X|Xr where xr is a list and x is an arbitrary value
 - □ ⟨List⟩ ::= nil | ⟨Value⟩' | '⟨List⟩

Polymorphic List

- Usually all elements of the same type
- Polymorphic list with elements of T type \(\langle \text{List T} \rangle ::= \text{nil} \ \langle \text{T} \rangle' \rangle' \text{List T} \rangle
 - T is a type variable
 - □ (List ?) is a type constructor
 - □ ⟨List ⟨Int⟩⟩ : a list whose elements are integers
 - □ ⟨List ⟨Value⟩⟩ is equal to ⟨List⟩

Polymorphic Binary Tree

Binary trees

- Binary tree representing a dictionary mapping keys to values
- Binary tree is:
 - either a leaf (atom leaf), or
 - an internal node with label tree, with left and right subtrees, a key and a value
- Key is of literal type and the value is of type T

Types for procedures and functions

The type of a procedure where T₁ ... T_n are the types of its arguments can be represented by:

```
\langle \text{proc } \{\$ \ T_1 \ ... \ T_n \} \rangle

or

\{T_1 \ ... \ T_n\} \longrightarrow ()
```

On Types: procedures and functions

The type of a function where T₁ ... T_n are the types of the arguments, and T is the type of the result is:

```
\langle \text{fun } \{ \$ \ T_1 \ ... \ T_n \} \ \vdots \ T \rangle
\{ T_1 \ ... \ T_n \} \ \longrightarrow \ T
```

or

Append ::{⟨List⟩ ⟨List⟩} →⟨List⟩
or precisely ::{⟨List A⟩ ⟨List A⟩} →⟨List A⟩

- Programs that takes lists has a form that corresponds to the list type
- Code should also follow type, e.g:

```
case Xs of
   nil then (expr1) % base case
[] X|Xr then (expr2) % recursive call
end
```

- Helpful when the type gets complicated
- Nested lists are lists whose elements can be lists
- Exercise: "Find the number of elements of a nested list"

```
Xs = [[1 2] 4 nil [[5] 10]]
{Length Xs} = 5
```

```
declare
Xs1=[[1 2] 4 nil]
{Browse Xs1} → [[1 2] 4 nil]
Xs2=[[1 2] 4]|nil
{Browse Xs2} → [[[1 2] 4]]
```

- Nested lists type declaration

General structure:

```
case Xs
  of nil then \( \) expr1 \( \) \( \) base case
[] X|Xr andthen \( \) IsList X\( \) then
  \( \) \( \) recursive calls for X and Xr
[] X|Xr then
  \( \) \( \) recursive call for Xr
end
```

```
Length :: \{\langle NList T \rangle\} \rightarrow \langle Int \rangle
  fun {Length Xs}
      case Xs
      of nil then 0 % base case
       [] X|Xr andthen {IsList X} then
              {Length X} + {Length Xr}
       [] X|Xr then
             1+{Length Xr}
      end
  end
fun {IsList L}
      L == nil orelse
       \{Label L\} == ' \mid ' and then \{Width L\} == 2
  end
```

Summary so far

- Type Notation
- Polymorphic Types
- Function types
- Constructing programs from type

Abstract Data Types

Data Types

- Data type
 - set of values
 - operations on these values
- Primitive data types
 - records
 - numbers
 - **.**...
- Abstract data types
 - completely defined by its operations (interface)
 - implementation can be changed without changing use

Motivation

Sufficient to understand interface only

 Software components can be developed independently when they are used through interfaces.

 Developers need not know implementation details

Outlook

How to define abstract data types

How to organize abstract data types

How to use abstract data types

Abstract data types (ADTs)

- A type is abstract if it is completely defined by its set of operations/functionality.
- Possible to change the implementation of an ADT without changing its use
- ADT is described by a set of procedures
 - Including how to create a value of the ADT
- These operations are the only thing that a user of ADT can assume

Example: stack

- Assume we want to define a new data type (stack T) whose elements are of any type T
- We define the following operations (with type definitions)

```
⟨fun {NewStack}: ⟨stack T⟩⟩
⟨fun {Push ⟨stack T⟩ ⟨T⟩ }: ⟨stack T⟩⟩
⟨proc {Pop ⟨stack T⟩ ?⟨T⟩ ?⟨stack T⟩}⟩
⟨fun {IsEmpty ⟨stack T⟩}: ⟨Bool⟩⟩
```

Example: stack (algebraic properties)

- Algebraic properties are logical relations between ADT's operations
- Operations normally satisfy certain laws (properties)
- { IsEmpty {NewStack}} = true
- For any stack S, {IsEmpty {Push S}} = false
- For any E and S, {Pop {Push S E} E S} holds
- For any stack S, {Pop {NewStack} S} raises error

stack (implementation I) using lists

```
fun {NewStack} nil end
fun {Push S E} E|S end
proc {Pop E|S ?E1 ?S1}
E1 = E
S1 = S
end
fun {IsEmpty S} S==nil end
```

stack (implementation II) using tuples

```
fun {NewStack} emptyStack end
fun {Push S E} stack(E S) end
proc {Pop stack(E S) E1 S1}
  E1 = E
  S1 = S
end
fun {IsEmpty S} S==emptyStack end
```

Why is Stack Abstract?

 A program that uses the stack will work with either implementation (gives the same result)

```
declare Top S4
% ... either implementation
S1={NewStack}
S2={Push S1 2}
S3={Push S2 5}
{Pop S3 Top S4}
{Browse Top} → 5
```

What is a Dictionary?

- A dictionary is a finite mapping from a set of simple constants to a set of language entities.
- The constants are called keys because they provide a unique the path to each entity.
- We will use atoms or integers as constants.
- Goal: create the mapping dynamically, i.e., by adding new keys during the execution.

Example: Dictionaries

Designing the interface of Dictionary

```
MakeDict :: \{\} \rightarrow Dict
    returns new dictionary
DictMember :: {Dict Feature} \rightarrow Bool
    tests whether feature is member of dictionary
DictAccess :: {Dict Feature} → Value
    return value of feature in Dict
DictAdjoin :: {Dict Feature Value} \rightarrow Dict
    return adjoined dictionary with value at feature
```

Interface depends on purpose, could be richer.

Implementing the Dict ADT

- Two possible implementations are
 - based on pairlists
 - based on records
- Regardless of implementation, programs using the ADT should work!
 - the interface is a contract between use and implementation

Dict: List of Pairs

```
fun {MakeDict}
   nil
end
fun {DictMember D F}
   case D of nil then false
       [] G#X|Dr then if G==F then true
                    else {DictMember Dr F} end
   end
end
```

Example: telephone book

[name1#62565243 name2#67893421 taxi1#65221111...]

Dict: Records

end

Example: telephone book

```
d(name1:62565243 name2:67893421 taxi1:65521111...)
```

Example: Frequency Word Counting

```
local
   fun {Inc D X}
      if {DictMember D X} then
          {DictAdjoin D X {DictAccess D X}+1}
      else {DictAdjoin D X 1}
      end
   end
          {Inc mr(a:3 b:2 c:1) b} \rightarrow mr(a:3 b:3 c:1)
in
   fun {Cnt Xs}
       % returns dictionary
       {FoldL Xs Inc {MakeDict}}
   end
end
```

Example: Frequency Word Counting

```
local
   fun {Inc D X}
      if {DictMember D X} then
          {DictAdjoin D X
                               homework:
      else {DictAdjoin
                           understand and try
      end
   end
                              this example!
in
   fun {Cnt Xs}
      % returns diction
      {FoldL Xs Inc {MakeDict}}
   end
end
{Browse {Cnt [a b c a b a]}} \rightarrow mr(a:3 b:2 c:1)
```

Evolution of ADTs

- Important aspect of developing ADTs
 - start with simple (possibly inefficient) implementation
 - refine to better (more efficient) implementation
 - refine to carefully chosen implementation
 - hash table
 - search tree
- Evolution is local to ADT
 - no change to external programs needed!

Theoretically

Polymorphic type is related to Universal Type

```
fun {Id X} X end
Id :: A \rightarrow A
Universal type : \forall A. A \rightarrow A
```

- ADT can be implemented using existential type.
 - ∃A. type
 - where A is considered to be hidden/abstracted

Example

Say we want to Peano-number ADT

Can make into existential type using:

Haskell

Typeful and Lazy Functional Language

Typeful Programs

- Every expression has a statically determined type that can be declared or inferred
- Equations defined by pattern-matching equations

```
fact :: Integer \rightarrow Integer
fact 0 = 1
fact n | n>0 = n * fact (n-1)
```

Lazy Evaluation

 Each argument is not evaluated before the call but evaluated when needed (e.g. when matched against patterns)

```
andThen :: Bool -> Bool -> Bool
andThen True x = x
andThen False x = False
```

Type Declaration

Data types have to be declared/enumerated.

```
data Bool = True | False
data ListInt = Nil | Cons Integer ListInt
type PairInt = (Integer, Integer)
```

Polymorphic Types

Generic types can be defined with type variables.

Currying

Functions with multiple parameters may be partially applied.

```
add :: Integer -> Integer
add x y = x+y
addT :: (Integer, Integer) -> Integer
addT(x,y) = x+y
```

Valid Expressions:

```
(add 1 2) = addT(1,2)

(add 1) = y -> addT(1,y)
```

Type Classes

- Some functions work on a set of types. For example, sorting works on data values that are comparable.
- Wrong to use polymorphic types!

```
sort :: (List a) -> (List a)
```

Use type class ord a instead.

```
sort :: Ord a => (List a) -> (List a)
```

Type Classes

Class is characterized by a set of methods

```
class Eq a
== :: a -> a -> Bool
class Eq a => Ord a
>, >= :: a -> a -> Bool
a>=b = (a>b) or (a==b)
```

Type Classes

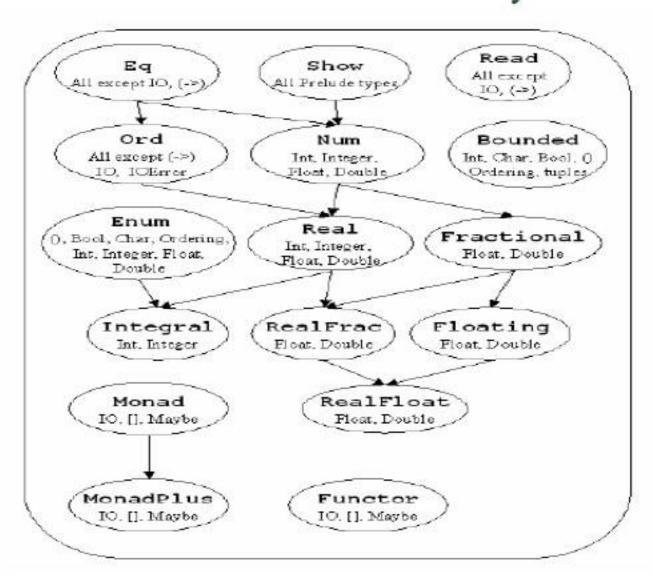
Need to define instances of given class

```
instance Ord Int
  a>b = a ><sub>Int</sub> b

instance Ord a => Ord [a]
  [] > ys = False
  x:xs > [] = True
  x:xs > y:ys = x>y or (x==y & xs>ys)
```

lexicographic ordering

Classes in Standard Library



Multi-Parameter Type Classes

Can support generic type constructors

```
class Functor f where
  fmap :: (a → b) → f a → f b

instance Functor Tree where
  fmap f (Leaf x) = Leaf (f x)
  fmap f (Node l r)
  = Node (fmap f l) (fmap f r)
```

Design methodology

Standalone applications

Design methodology

- "Programming in the large"
 - Written by more than one person, over a long period of time
- "Programming in the small"
 - Written by one person, over a short period of time

Design methodology. Recommendations

- Informal specification: inputs, outputs, relation between them
- Exploration: determine the programming technique;
 split the problem into smaller problems
- Structure and coding: determine the program's structure; group related operations into one module
- Testing and reasoning: test cases/formal semantics
- Judging the quality: Is the design correct, efficient, maintainable, extensible, simple?

Software components

- Split the program into modules (also called logical units, components)
- A module has two parts:
 - An interface = the visible part of the logical unit. It is a record that groups together related languages entities: procedures, classes, objects, etc.
 - An implementation = a set of languages entities that are accessible by the interface operations but hidden from the outside.

Module

```
declare MyList in
local
  proc {Append ... } ... end
  proc {Sort ... } ... end
  ...
in
 MyList = 'export' ( append: Append
                       sort : Sort
end
```

Modules and module specifications

- A module specification (e.g. functor) is a template that creates a module (component instance) each time it is instantiated.
- In Oz, a functor is a function whose arguments are the modules it needs and whose result is a new module.
 - Actually, the functor takes module interfaces as arguments, creates a new module, and returns that module's interface!

Functor

```
fun {MyListFunctor}
proc {Append ... } ... end
 proc {Sort ... } ... end
in
 'export' (append: Append
             sort : Sort
               ... )
end
```

Modules and module specifications

- A software component is a unit of independent deployment, and has no persistent state.
- A module is the result of installing a functor in a particular module environment.
- The module environment consists of a set of modules, each of which may have an execution state.

Functors

- A functor has three parts:
 - an import part = what other modules it needs
 - an export part = the module interface
 - a define part = the module implementation including initialization code.
- Functors in the Mozart system are compilation units.
 - source code (i.e., human-readable text, .oz)
 - object code (i.e., compiled form, .ozf).

Standalone applications (1)

- It can be run without the interactive interface.
- It has a main functor, evaluated when the program starts.
- Imports the modules it needs, which causes other functors to be evaluated.
- Evaluating (or "installing") a functor creates a new module:
 - The modules it needs are identified.
 - The initialization code is executed.
 - The module is loaded the first time it is needed during execution.

Standalone applications (2)

- This technique is called dynamic linking, as opposed to static linking, in which the modules are already loaded when execution starts.
- At any time, the set of currently installed modules is called the module environment.
- Any functor can be compiled to make a standalone program.

Functors. Example (GenericFunctor.oz)

```
functor
export generic:Generic
define
  fun {Generic Op InitVal N}
    if N == 0 then InitVal
    else {Op N {Generic Op InitVal (N-1)}}
    end
end
```

end

The compiled functor GenericFunctor.ozf is created:

```
□ ozc -c GenericFunctor.oz
```

Functors (Standalone Application)

```
GenericFunctor
                                          Browser
functor
                                    imported
import
  GenericFunctor
                                  GenericFact
  Browser
define
                                       executable
   fun {Mul X Y} X*Y end
   fun {FactUsingGeneric N}
       {GenericFunctor.generic Mul 1 N}
   end
   {Browser.browse {FactUsingGeneric 5}}
end
```

The executable functor GenericFact.exe is created:

```
ozc -x GenericFact.oz
```

Functors. Interactive Example

```
declare
[GF]={Module.link ['GenericFunctor.ozf']}
fun {Add X Y} X+Y end
fun {GenGaussSum N} {GF.generic Add 0 N} end
{Browse {GenGaussSum 5}}
```

- Function Module.link is defined in the system module Module.
- It takes a list of functors, load them from the file system, links them together
 - (i.e., evaluates them together, so that each module sees its imported modules),
- and returns a corresponding list of modules.

Summary

- Type Notation
 - Constructing programs by following the type
- Haskell
- Design methodology
 - modules/functors