Implement Cholesky Decomposition for solving the following systems of linear equations.
n=100, n = 1000, n = 10000

$$A_1 x = b_1, \quad A_2 x = b_2$$

με $A_1, A_2 \in \mathbb{R}^{n,n}$, $b_1, b_2 \in \mathbb{R}^n$:

$$A_1 = \begin{pmatrix} 6 & -4 & 1 & 0 & \cdots & \cdots & \cdots & \cdots & \cdots & 0 \\ -4 & 6 & -4 & 1 & 0 & \cdots & \cdots & \cdots & \cdots & 0 \\ 1 & -4 & 6 & -4 & 1 & 0 & \cdots & \cdots & \cdots & 0 \\ 0 & 1 & -4 & 6 & -4 & 1 & 0 & \cdots & \cdots & 0 \\ 0 & 0 & 1 & -4 & 6 & -4 & 1 & 0 & \cdots & 0 \\ \vdots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \vdots \\ 0 & \cdots & \cdots & 0 & 1 & -4 & 6 & -4 & 1 & 0 \\ 0 & \cdots & \cdots & \cdots & 0 & 1 & -4 & 6 & -4 & 1 \\ 0 & \cdots & \cdots & \cdots & \cdots & 0 & 1 & -4 & 6 & -4 \\ 0 & \cdots & \cdots & \cdots & \cdots & \cdots & 0 & 1 & -4 & 6 \end{pmatrix}, \quad b_1 = \begin{pmatrix} 3 \\ -1 \\ 0 \\ 0 \\ 0 \\ \vdots \\ 0 \\ 0 \\ 0 \\ -1 \\ 3 \end{pmatrix},$$

$$A_2 = \begin{pmatrix} 7 & -4 & 1 & 0 & \cdots & \cdots & \cdots & \cdots & \cdots & 0 \\ -4 & 7 & -4 & 1 & 0 & \cdots & \cdots & \cdots & \cdots & 0 \\ 1 & -4 & 7 & -4 & 1 & 0 & \cdots & \cdots & \cdots & 0 \\ 0 & 1 & -4 & 7 & -4 & 1 & 0 & \cdots & \cdots & 0 \\ 0 & 0 & 1 & -4 & 7 & -4 & 1 & 0 & \cdots & 0 \\ \vdots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \ddots & \vdots \\ 0 & \cdots & \cdots & 0 & 1 & -4 & 7 & -4 & 1 & 0 \\ 0 & \cdots & \cdots & \cdots & 0 & 1 & -4 & 7 & -4 & 1 \\ 0 & \cdots & \cdots & \cdots & \cdots & 0 & 1 & -4 & 7 & -4 \\ 0 & \cdots & \cdots & \cdots & \cdots & \cdots & 0 & 1 & -4 & 7 \end{pmatrix}, \quad b_2 = \begin{pmatrix} 4 \\ 0 \\ 1 \\ 1 \\ 1 \\ \vdots \\ 1 \\ 1 \\ 1 \\ 0 \\ 4 \end{pmatrix},$$