

#### **Lecture 8**

topic: Performance Measures

material: Chapters 5 (book "Data Mining for Business Intelligence")



# If you can't measure it, you can't improve it!

# Agenda

	Date	Lecture contents		Lecturer Lab topics		Test	
	Jan-27	1	Intro. to BI+ Data Management	Caron			
	Jan-30				SQL-1	1	
П	Jan-28	2	Data warehousing	Caron			
	Feb-06				SQL-2	2	
	Feb-03	3	OLAP business databases & dashboard	Caron			
	Feb-13				SQL-3 & OLAP	3a & 3b	
ı	Feb-10	4	Data mining introduction	loannou			
	Lep-10	5	Regression models	Ioannou			
	- 1 4-	6	Naïve Bayes	Ioannou			
	Feb-17	7	k nearest neighbors	Ioannou			
	Feb-20				Bayes & neighbors	4	
*	Feb-27	8	Performance measures	loannou			
	Mar-02	9	Decision trees	Ioannou			
	Mar-05				Dec. trees	5	
	Mar-09	10	Association rules	Ioannou			
	Mar-				Ass. Rules	6	
	11,12&13						
	Mar-16	11	Clustering (+20 mins exam preparation)	Ioannou			
	Mar-19				Clustering	7	

# Why shall we evaluate?

- Concerns both researchers and practitioners
- It allows you to convince others that your work is meaningful
  - Examples: clients, peers, funding agencies, company VPs, investors, teachers, ...
- Without a strong evaluation, your idea is likely to be rejected, code would not be deployed
- Empirical evaluation helps guide meaningful research and development directions

### **Evaluation** issues

"If you cannot measure it, you cannot improve it"

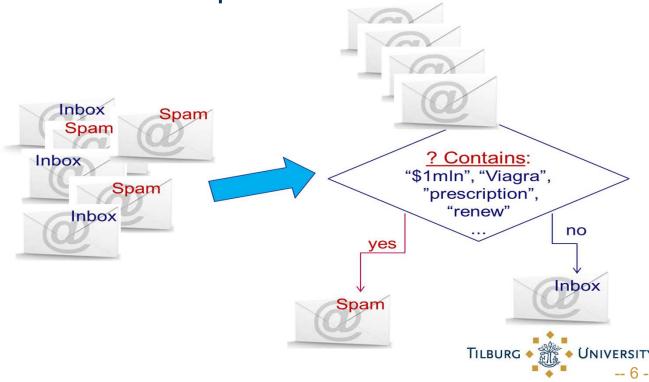
- How to evaluate the performance of a model?
- How reliable are the predicted results?
- How to obtain reliable estimates?
- How to compare the relative performance among competing models?
- How to select among models that have equal performance?

## **Evaluation issues**

- Various models, e.g.:
  - Classify instances
  - Predicting class probability
  - Predicting numeric rather than nominal values
- → Not a single methodology for the evaluation!
- → Next slides: various possible evaluation measures

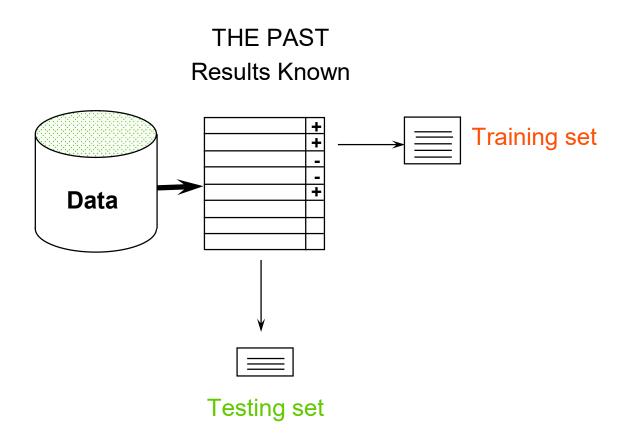
Classify e-mails to spam vs. ham

- Given (labeled) examples of both document types
- Train a classifier to discriminate between these two
- During operation, use classifier to select destination folder for new email: Inbox or Spam folder?



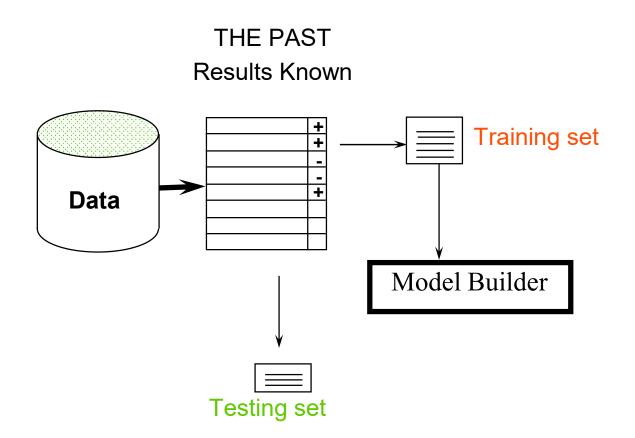
## **Classification Step 1:**

Split data into train and test sets



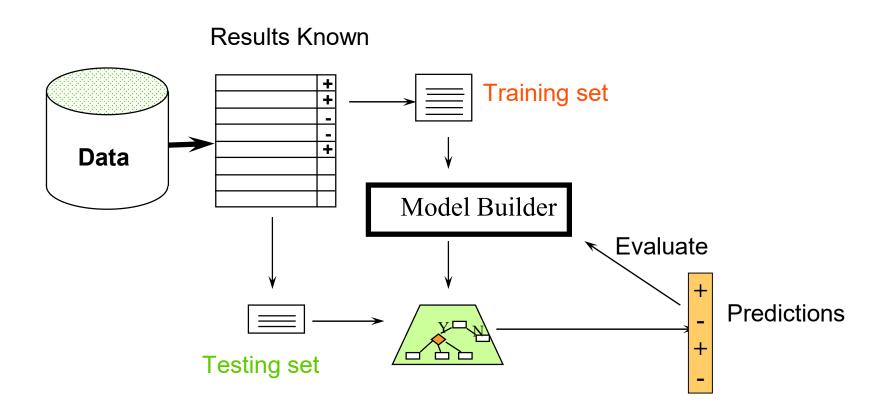
## **Classification Step 2:**

Build a model on a training set



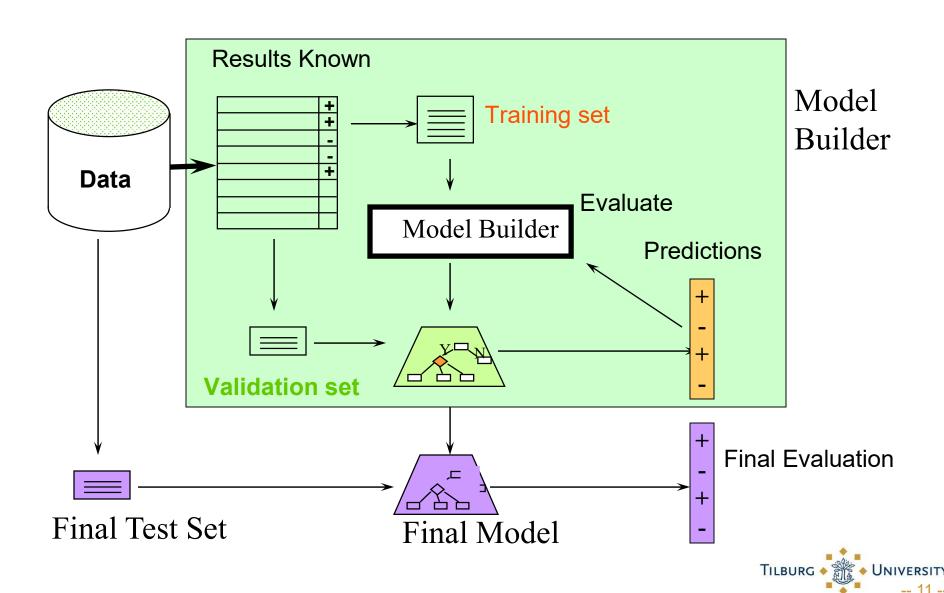
## Classification Step 3:

**Evaluate** on test set (Re-train?)



# Note on parameter tuning

- It is important that the test data is not used in any way to create the classifier
- Some training schemes operate in two stages:
  - Stage 1: build the basic structure
  - Stage 2: optimize parameter settings
- The test data cannot be used for parameter tuning!
- Proper procedure uses three sets: training data, validation data, and test data
  - Validation data is used to optimize parameters



# Making the most of the data

- Once evaluation is completed, all the data can be used to build the final classifier
- Generally, the larger the training data the better the classifier (but returns diminish)
- The larger the test data the more accurate the error estimate

# Training and Validation Performance

- Errors that are based on the training set tell us about model fit
- Errors that are based on the validation set measure the model's ability to predict new data
  - Prediction errors that measure predictive performance

What is the expected relationship between training errors and validation errors?



- a) Training errors are less than the validation errors
- b) Validation errors are less than the training errors
- c) Cannot predict the relationship
- d) Exactly the same



# Types of outcomes

- Building models using training data is called Supervised Learning
- Interested in predicting the outcome variable for new records
- Three main types of outcomes
  - a. Predicted numerical value, e.g., house price
  - b. Predicted class membership, e.g., cancer or not
  - c. Probability of class membership (for categorical outcome variable), e.g., Naive Bayes

# Evaluating Predictive Performance i.e., numerical (continuous) variables

# Generating numeric predictions

- Interested in models that have high predictive accuracy when applied to new records
- Models are trained on the training data
- Applied to the validation data and
- Measures of accuracy then use the prediction errors on that validation set

• Prediction error for record i is the difference between its actual outcome value  $y_i$  and its predicted outcome value  $\hat{y}_i$ :

$$\mathbf{e}_i = \mathbf{y}_i - \hat{\mathbf{y}}_i$$

Several popular numerical measures

## Mean absolute error/deviation (MAE)

• Gives the magnitude of the average absolute error  $\frac{1}{n}\sum_{i=1}^{n}|e_{i}|$ 

#### Mean error

Same as MAE but no absolute value

$$\frac{1}{n} \sum_{i=1}^{n} e_i$$

- Negative errors cancel positive of same magnitude
- Indication of whether predictions are on average over-/under-predicting the outcome variable

## Mean absolute error/deviation (MAE)

#### Mean error

## Mean percentage error (MPE)

- Percentage score of how predictions deviate from the actual values (on average)
- Takes into account the direction of the error

$$100 \frac{1}{n} \sum_{i=1}^{n} \frac{\mathbf{e}_i}{\mathbf{y}_i}$$

#### Mean absolute percentage error (MAPE)

Percentage score of how predictions deviate (on average)
 from the actual values

$$100 \frac{1}{n} \sum_{i=1}^{n} \left| \frac{\mathbf{e}_i}{\mathbf{y}_i} \right|$$



Mean absolute error/deviation (MAE)

Mean error

Mean percentage error (MPE)

Mean absolute percentage error (MAPE)

Root mean squared error

- Intuition: (normalized) distance between the vector of predicted values and the vector of actual value
- Same units as the outcome variable

$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} e_i^2}$$

## Lift Chart

- Graphical way to assess predictive performance
- In some applications, we are not interested in predicting the outcome of value of each new record
- But the goal is to search for a subset of records that gives the highest cumulative predicted values
- Compares the model's predictive performance to a baseline model that has no predictors

### Lift chart

- In practice, costs are rarely known
- Decisions are usually made by comparing possible scenarios
- Example: promotional mailout to 1,000,000 households
  - Mail to all with response rate being 0.1% (1,000)
  - Consider a data mining tool that can identify a subset of 100,000 most promising households with response rate 0.4% (400)
  - Responses are 40% BUT cost is 10%
  - → It might pay off to restrict to these 100,000
- The increase in response rate is called lift factor
- A lift chart allows a visual comparison



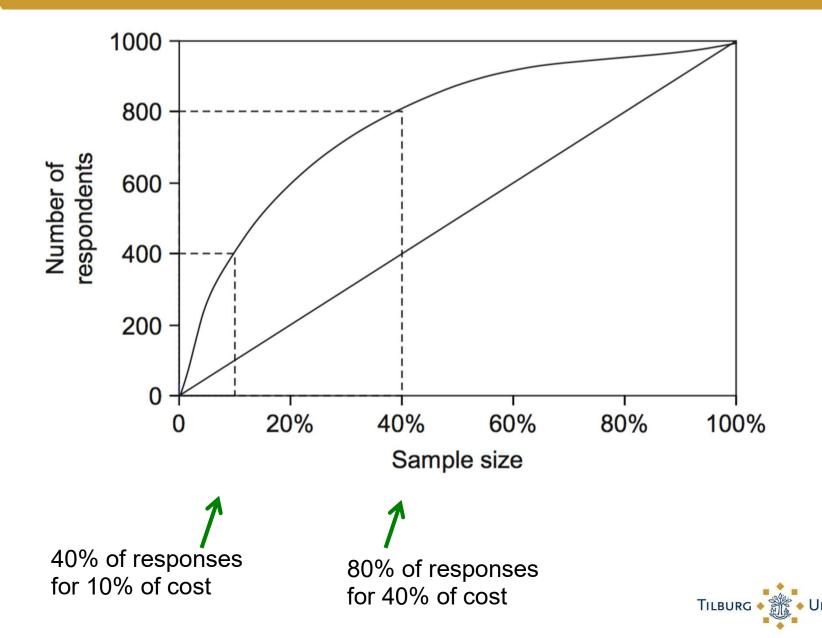
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- Take sample data set
- Apply the selected model
- Sort according to predicted probability of a yes response, i.e.,

Rank	Predicted	Actual	
1	0.95	Yes	
2	0.93	Yes	
3	0.93	No	
4	0.88	Yes	
5	0.86	Yes	
6	0.85	Yes	
7	0.82	Yes	
8	0.80	Yes	
9	0.80	No	
10	0.79	Yes	

- First instance is the one the model thinks is more likely a yes
- Next instance is the next most likely
- Etc.
- Intuition: more yes at the beginning of the list
- x-axis is sample percentage, i.e., 20% from the start of the list
- y-axis is response number, i.e., percentage where the model correctly predicts the positive class

# A hypothetical lift chart



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# Judging Classifier Performance i.e., categorical variables

## Misclassification error

- Perfect classifier makes no errors!
- But the real world has "noise" and not all the information needed to classify records precisely
- Cannot construct perfect classifiers
- Misclassification is when a record belongs to one class but the model classifies it as a member of a different class
- A natural criterion for judging the performance of a classifier is the probability of making a misclassification error



- A matrix that summarizes the correct and incorrect classifications that a classifier produced for a given dataset
- Rows and columns correspond to the predicted and true (actual) classes
- In practice, most accuracy measures are derived from this matrix

• In the two-class case (e.g., yes and no), a single prediction has four different possible outcomes

		Predicte	Predicted class	
		Yes	No	
Actual class	Yes	True Positive	False Negative	
	No	False Positive	True Negative	

- Correct classifications:
  - True Positive and True Negative
- Incorrect classifications:
  - False Positive, i.e., outcome incorrectly predicted as yes / positive
  - False Negative: i.e., outcome incorrectly predicted as no / negative



		Actual class		
	_	<b>C</b> <sub>1</sub>	C <sub>2</sub>	
Predicted Class	$C_1$	$n_{1,1}$ = number of $C_1$ records classified correctly	$n_{2,1}$ = number of $C_2$ records classified incorrectly as $C_1$	
	$C_2$	$n_{1,2}$ = number of $C_1$ records	$n_{2,2}$ = number of $C_2$ records	

classified incorrectly as C<sub>2</sub>

Actual Class

Matrix as given in the book used in our course, i.e., "Data Mining for Business Intelligence"

classified correctly

		Predicte	Predicted class		
		Yes	No		
Actual class	Yes	True Positive	False Negative		
, 1313.3.1 61616	No	False Positive	True Negative		

The prediction in the figure is a:



1. True Positive

2. False Positive

3. False Negative

4. True Negative



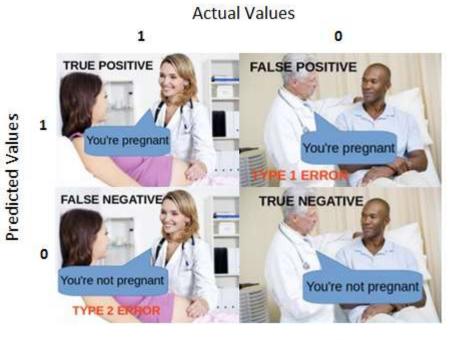
# Type I and II errors

## Type I Error → False Positive

- Predicted positive but that is incorrect
- Example: predicted that a man is pregnant, but actually he is not pregnant

# Type II Error → False Negative

- Predicted negative
   but that is incorrect
- E.g., predicted a woman
   is not pregnant when
   actually she is pregnant





## Overall success rate

		Predicte	Predicted class	
		Yes	No	
Actual class	Yes	<b>True Positive</b>	False Negative	
	No	False Positive	True Negative	

## Overall success rate / Accuracy:

 Number of correct classifications divided by the total number of classifications

$$\frac{TP + TN}{TP + TN + FP + FN} \text{ or } \frac{TP + TN}{n}$$

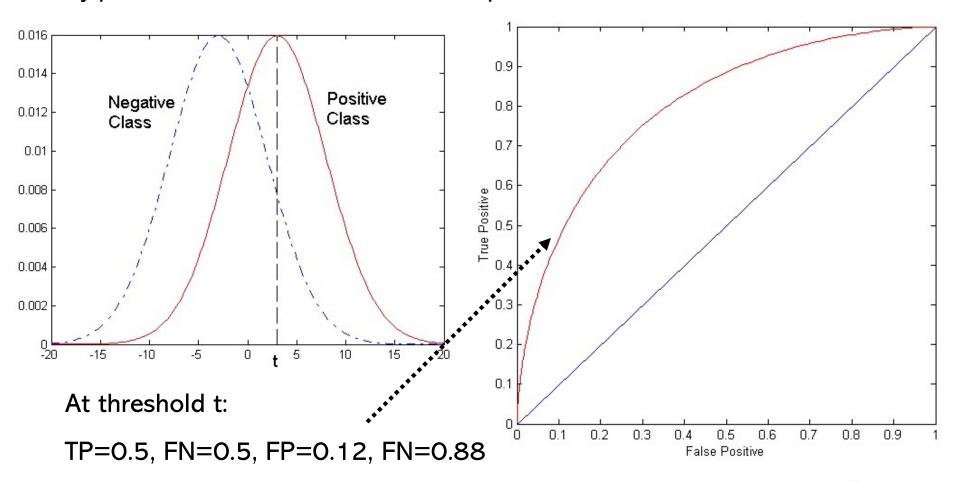
# ROC curves (Receiver Operating Characteristic)

- Developed in 1950s for signal detection theory to analyze noisy signals
- Characterize the trade-off between positive hits and false alarms

- ROC curve plots TP (on the y-axis) against
   FP (on the x-axis)
- Plots the true positive rate against the false positive rate for the different possible thresholds of a diagnostic test

# **ROC Curve**

- 1-dimensional data set containing 2 classes (positive and negative)
- any points located at x > t is classified as positive





## **ROC Curve**

## (TP,FP):

• (0,0): declare everything to be negative class

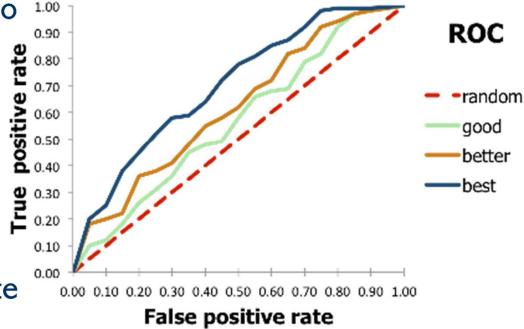
• (1,1): declare everything to be positive class

• (1,0): ideal

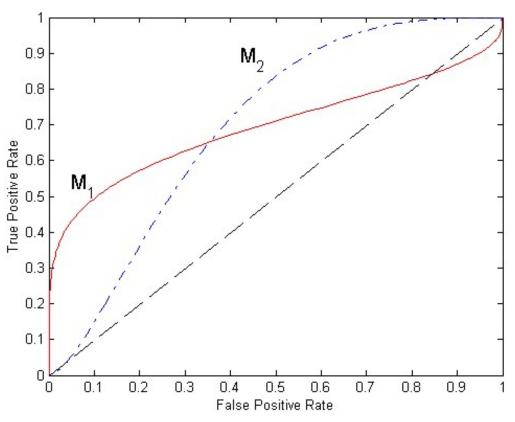
Diagonal line:

- Random guessing
- Below diagonal line:

 prediction is opposite of the true class



# Using ROC for Model Comparison



- No model consistently outperform the other
  - M1 is better for small FPR
  - M2 is better for large FPR
- Area Under the ROC curve
  - Ideal:
    - Area = 1
  - Random guess:
    - Area = 0.5

# Limitation of Accuracy

- Consider a 2-class problem
  - Number of Class 0 examples = 9990
  - Number of Class 1 examples = 10
- If model predicts everything to be class 0, accuracy is 9990/10000 = 99.9 %
  - Accuracy is misleading because model does not detect any class 1 example

### Cost Matrix

	PREDICTED CLASS						
	C( i   j )	Class=Yes	Class=No				
ACTUAL	Class=Yes	C(Yes Yes)	C(No Yes)				
CLASS	Class=No	C(Yes No)	C(No No)				

C( $i \mid j$ ): Cost of misclassifying class j example as class i

cost = C(Yes | Yes) x True Positive + C(No | Yes) x False Negative + C(Yes | No) x False Positive + C(No | No) x True Negative



# Computing Cost of Classification

Cost Matrix	PREDICTED CLASS					
	C(i j)	+	-			
ACTUAL CLASS	+	-1	100			
	-	1	0			

Model M <sub>1</sub>	PREDICTED CLASS				
		+	•		
ACTUAL CLASS	+	150	40		
	-	60	250		

Model M <sub>2</sub>	PREDICTED CLASS					
ACTUAL CLASS		+	-			
	+	250	45			
	-	5	200			

Accuracy = 80%

Cost = 3910

Accuracy = 90%

Cost = 4255

# Cost vs. Accuracy

Count	PREDICTED CLASS						
		Class=Yes	Class=No				
ACTUAL	Class=Yes	а	b				
CLASS	Class=No	С	d				

Cost	PREDICTED CLASS						
		Class=Yes	Class=No				
ACTUAL	Class=Yes	р	q				
CLASS	Class=No	q	р				

Accuracy is proportional to cost if

1. 
$$C(Yes|No) = C(No|Yes) = q$$

2. 
$$C(Yes | Yes) = C(No | No) = p$$

$$n = a + b + c + d$$

Accuracy = 
$$(a + d) / n$$

Cost = p (a + d) + q (b + c)  
= p (a + d) + q (n - a - d)  
= q n - (q - p)(a + d)  
= n [q - (q-p) 
$$\times$$
 Accuracy]

# Multiclass prediction

 Two confusion matrices for a 3-class problem: actual predictor (left) vs. random predictor (right)

	Predicted Class						Predicted Class				
(A)		а	b	С	total	(B)		а	b	С	total
Actual	a	88	10	2	100	Actual	a	60	30	10	100
class	b	14	40	6	60	Class	b	36	18	6	60
	С	18	10	12	40		С	24	12	4	40
	total	120	60	20			total	120	60	20	

- Number of successes: sum of entries in diagonal (D)
- Kappa statistic: (success rate of actual predictor success rate of random predictor) / (1 - success rate of random predictor)
- Measures relative improvement on random predictor: 1 means perfect accuracy, 0 means we are doing no better than random



### Multiclass prediction

	Predicted Class						Predicted Class				
(A)		a	b	С	total	(B)		а	b	С	total
Actual	a	88	10	2	100	Actual	a	60	30	10	100
class	b	14	40	6	60	Class	b	36	18	6	60
	С	18	10	12	40		С	24	12	4	40
	total	120	60	20			total	120	60	20	

- Number of successes: sum of entries in diagonal (D)
- Kappa statistic:
  - Success rate of actual predictor success rate of random predictor) / (1 – success rate of random predictor)
- Example:
  - Success rate of actual predictor = (88+40+12)/200 = 140/200 = 0.7
  - Success rate of random predictor = (60+18+4)/200 = 82/200 = 0.41
  - $\circ$  Kappa statistics = (0.7-0.41)/(1-0.41) = 0.492



# Precision and Recall

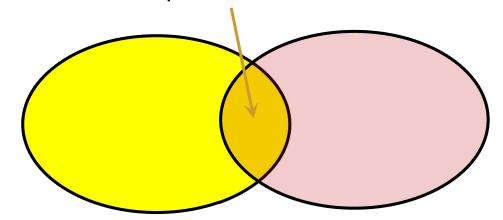


#### Precision and Recall

R: documents of a particular class from the testing set A: prediction set (answers) for the particular class, generated by a model

 $R \cap A$ : the intersection of the sets R and A

 $R \cap A$ : records correctly predicted for the class



R: records of the particular class

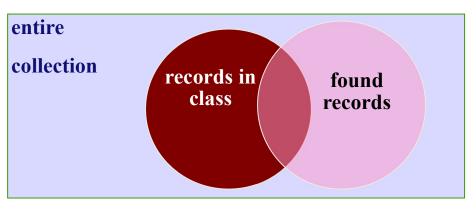
A: records predicted to belong in the class

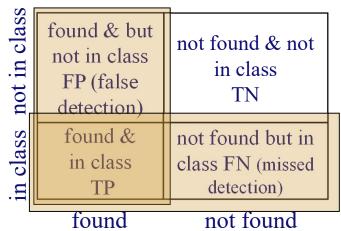
$$Recall = \frac{|R \cap A|}{|R|}$$

$$Precision = \frac{|R \cap A|}{|A|}$$



#### Precision and Recall





$$recall = \frac{number\ of\ records\ found\ that\ belong\ to\ the\ particular\ class}{number\ of\ records\ in\ class}$$

The ability of the model to find **all** of the items of the class

$$precision = \frac{number\ of\ records\ found\ that\ belong\ to\ the\ particular\ class}{number\ of\ records\ found\ for\ the\ particular\ class}$$

The ability of the model to correctly detect class items



# Determining Recall is Difficult

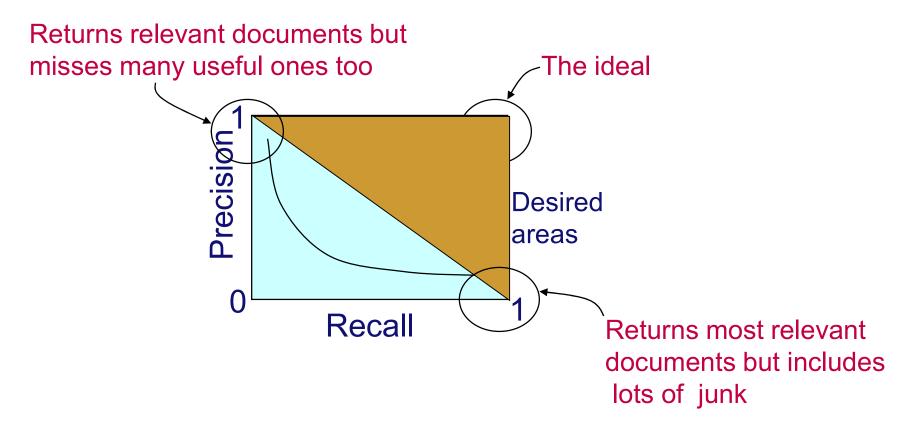
 Total number of items / records that belong to a particular class is sometimes not available

#### Solutions:

- Sample across the dataset and perform relevance judgment on these items
- Apply different models to the same dataset and then use the aggregate of relevant items as the total relevant set

### Evaluating ranked results: R&P tradeoff

- The system can return any number of results
- By taking various numbers of the top returned documents (levels of recall), the evaluator can produce a precision-recall curve



# F-Measure (F1-measure)

- One measure of performance that takes into account both recall and precision
- Harmonic mean of recall and precision:

$$F = \frac{2PR}{P + R} = \frac{2}{\frac{1}{R} + \frac{1}{P}}$$

### Question for you:

Consider two systems A and B, their IR routines are identical except that A does stemming as preprocessing.

- How precision and recall of A and B relate to each other?
  - A. B has higher precision and lower recall than A.
  - B. A and B have about the same recall.
  - C. A and B have about the same precision and about the same recall.
  - D. B has lower precision and higher recall than A.
  - E. A and B have about the same precision.
  - F. B has higher precision and higher recall than A.
  - G. B has lower precision and lower recall than A.
  - H. Impossible to say



### Training and Validation Performance

- Errors that are based on the training set tell us about model fit
- Errors that are based on the validation set measure the model's ability to predict new data
  - Prediction errors that measure predictive performance



What is the expected relationship between training errors and validation errors?

- a) Training errors are less than the validation errors
- b) Validation errors are less than the training errors
- c) Cannot predict the relationship
- d) Exactly identical



### Confusion / Classification matrix

		Predicte	Predicted class				
		Yes	No				
Actual class	Yes	True Positive	False Negative				
7.00001 01000	No	False Positive	True Negative				







- 3. False Negative
- 4. True Negative



