Assignment 3 FMAN95

John Sun

February 2024

1 Exercises

Exercise 1.

$$f(F) = 0$$

$$F(F) = \begin{pmatrix} 0 & 0 & 2 \\ -2 & 2 & -2 \end{pmatrix} \begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 2 \\ 0 & 0 \end{pmatrix}$$

$$e_{2}^{T} F = \begin{pmatrix} 2 & 2 & 0 \end{pmatrix} \begin{pmatrix} 0 & 0 & 2 \\ 0 & 0 & -2 \\ -2 & 2 & -2 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -2 \\ -2 & 2 & -2 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Exercise 3: $X_1 \sim N_1 \times_1 \times_2 \sim N_2 \times_2 \sim N_2 \times_1 \times_2 \sim N_2 \sim N_2$

Exercise 4' F=
$$\begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

Gret e_{2} by computing nullipace of FT = $\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix}$
 $X = t$
 $X + 2 = 0$
 $X = t$
 $X + 2 = 0$
 $X = t$
 X

2 The Fundamental Matrix

Computer exercise 1

The determinant of F is very close to zero, 9.35*e(-19) (after using formula 7.33 from the lecture notes), same with the epipolar constraint with them hovering around zero. Also checked the euclidean norm of Mv to be 1.88*e-17 which is close to zero. The mean distance is 0.36 when normalized and 0.49 without normalization.

The fundamental matrix: $\begin{bmatrix} 0 & 0 & 0.0058 \\ 0 & 0 & -0.027 \\ -0.07 & 0.026 & 1 \end{bmatrix}$

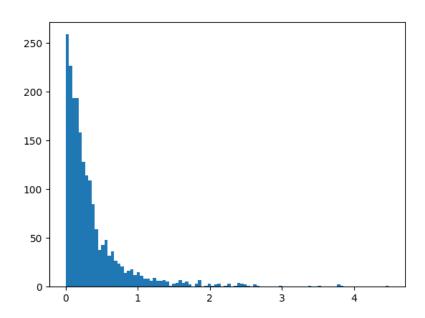


Figure 1: The distances between a point and it's epipolar line using normalized F, presented in a histogram.

Computer exercise 2

Figure 3-4 looks to be correct. Figure 5 shows the 3D points which is not at all what I expected. If the two parts of the image points are divided into the upper and lower cluster, they together form a parenthesis. I interpret it as the points being behind and in front of the camera (as the smaller cluster looks to be upside down like in figure 6.

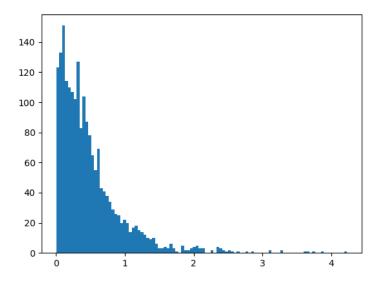


Figure 2: The distances between a point and it's epipolar line using N2=N1=1

3 The Essential Matrix

Computer exercise 3

The determinant of E is zero. The epipolar constraint is also hovering around zero ± 0.002 . We also check that Mv is close to zero being 0.0066.

The essential matrix:
$$\begin{bmatrix} -8.9 & -1005.8 & 377.1 \\ 1252.5 & 78.4 & -2448.2 \\ -472.8 & 2550.2 & 1 \end{bmatrix}$$

The mean average distance from point to epipolar line is 2.1 which is between the normalized and un-normalized values in computer exercise 1. The distances from the points x2 to epipolar lines are definitely more evenly distributed compared to the first computer exercise. The problem with rital and getting the epipolar lines to properly show still exists here.

Computer exercise 4

The camera matrix P2a

$$[UWV^Tu3]$$

had 2008 points in front of the camera.

The camera matrix P2b

$$[UWV^T - u3]$$

had 0 points in front of the camera.

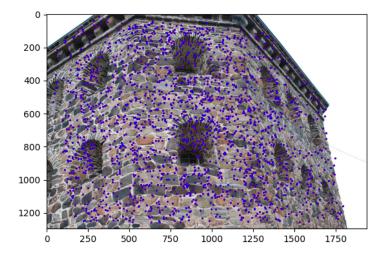


Figure 3: The image points and the projected 3D points for image 1. Blue are the projected.

The camera matrix P2c

$$[UW^TV^Tu3]$$

had 1839 points in front of the camera.

The camera matrix P2d

$$[UW^TV^T - u3]$$

had 169 points in front of the camera.

Looking at figure 7 and 8 we can see that the projected 3D points translated still looks very good compared to the original ones.

The best projection looks like figure 9 and looks like the three walls from the images. (NOTE: Python SVD returns the transpose of V)

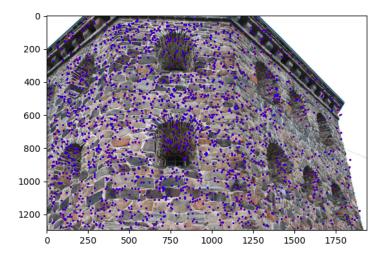


Figure 4: The image points and the projected 3D points for image 2. Blue are the projected.

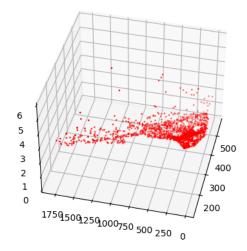


Figure 5: The 3D points

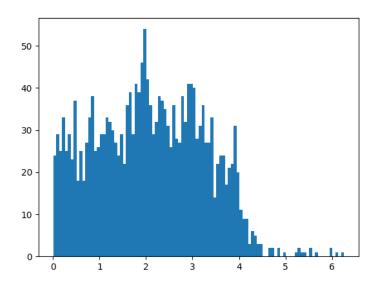


Figure 6: Distances from points to corresponding epipolar line ${\cal C}$

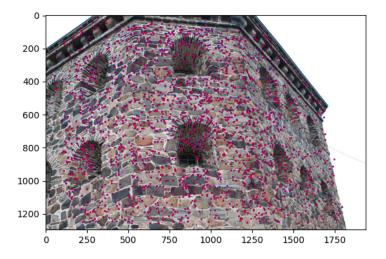


Figure 7: The projected points and the original points

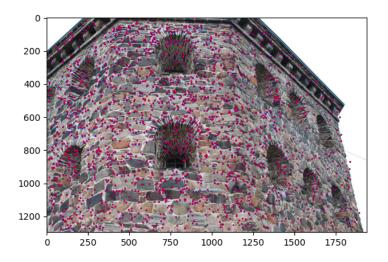


Figure 8: Projected points and the original points

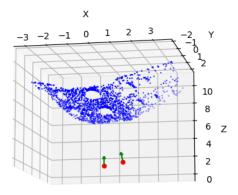


Figure 9: The projection of the image.