

1. Given $F = \{a \rightarrow b, b \rightarrow c, c \rightarrow \{d, e\}\}$. What is the closure of b

$$a \rightarrow b$$

$$b \rightarrow c$$

$$c \rightarrow d$$

$$c \rightarrow e$$

$$\frac{B^+}{B, C, D, E}$$

2. Given $R(a, b, c, d, e, f)$. Given the following functional dependency:

$$F = \{ab \rightarrow cdef, c \rightarrow abdef\}$$

Identify the L M R, candidate keys, prime/non prime and normal form using the table below

$$\begin{aligned} &ab \rightarrow c \\ \times &ab \rightarrow d \\ \times &ab \rightarrow e \\ \times &ab \rightarrow f \\ &c \rightarrow a \\ &c \rightarrow b \\ &c \rightarrow d \\ &c \rightarrow e \\ &c \rightarrow f \end{aligned}$$

L	M	R	Candidate Keys	prime	Non prime	Normal Form
C	C	D	C	C	D	BCNF
A	A	E	AB	A	E	
B	B	F		B	F	

$$\begin{aligned} &\times \times \\ &A B C \\ &\downarrow \\ &AB \end{aligned}$$

3. Given $R(a,b,c,d,e,f)$. Given the following functional dependency:

$$F = \{ ab \rightarrow cdef, \quad c \rightarrow abdef, \quad e \rightarrow a \}$$

Identify the L M R, candidate keys, prime/non prime and normal form using the table below

$ab \rightarrow c$
 $\times ab \rightarrow d$
 $\times ab \rightarrow e$
 $\times ab \rightarrow f$
 $\times c \rightarrow a$
 $c \rightarrow b$
 $c \rightarrow d$
 $c \rightarrow e$
 $c \rightarrow f$
 $e \rightarrow a$

$\begin{matrix} \times & \times & \times \\ & A & B & C & E \\ & \downarrow & & & \\ & AB & & & \\ E & \swarrow & & & \end{matrix}$

L	M	R	Candidate Keys	prime	Non prime	Normal Form
	A	D	C	A	D	<u>3rd</u>
	B	F	AB	B	F	
	C		EB	C		
	E			E		

4. Given $R(a,b,c,d,e,f,g)$. Given the following functional dependency:

$$F = \{ ab \rightarrow \{cdeg, \quad c \rightarrow abdef, \quad d \rightarrow b\}$$

Identify the L M R, candidate keys, prime/non prime and normal form using the table below

$ab \rightarrow c$
 $\times ab \rightarrow d$
 $\times ab \rightarrow e$
 $\times ab \rightarrow g$
 $c \rightarrow a$
 $\times c \rightarrow b$
 $c \rightarrow d$
 $c \rightarrow e$
 $c \rightarrow f$
 $d \rightarrow b$

$\begin{matrix} \times & \times & \times \\ & A & B & C & D \\ & \downarrow & & & \\ & AB & & & \\ & \downarrow & & & \\ & AD & & & \end{matrix}$

L	M	R	Candidate Keys	prime	Non prime	Normal Form
	A	E	C	A	E	<u>3rd</u>
	B	F	AB	B	F	
	C	G	AD	C	G	
	D			D		