Construction and Verification of Software

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MIEI - Integrated Master in Computer Science and Informatics

Consolidation block

Lecture 6 - Abstract Data Types
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based on previous editions by João Seco and Luís Caires



Outline

- Framing in Hoare Logic
- Modifying an Array
- ADTs and TypeStates
- Building a Queue with TypeStates

Part I Framing and Changing State

- Tracking state changes and invalidating knowledge along the proof is crucial in the verification of imperative programs.
- This is captured by the derived (constancy or frame) rule

$$\frac{\{A\}\ P\ \{B\}}{\{A \land C\}\ P\ \{B \land C\}} \text{ where } M(P) \cap V(C) = \emptyset$$

• **Crucial:** Provided that the variables modified by P (M(P)) are not referred by C (V(C)).

$$\frac{\{x > 0\} \ y := x \ \{y > 0 \land x = y\}}{\{x > 0 \land z < 0\} \ y := x \ \{y > 0 \land x = y \land z < 0\}}$$

- Tracking state changes and invalidating knowledge along the proof is crucial in the verification of imperative programs.
- This is captured by the derived (constancy or frame) rule

$$\frac{\{A\}\ P\ \{B\}}{\{A \land C\}\ P\ \{B \land C\}} \text{ where } M(P) \cap V(C) = \emptyset$$

- Crucial: Provided that the variables modified by P (M(P))
 are not referred by C (V(C)).
- Updates to variables do not allow framing the modified variables.

 method deposit(v:int)

modifies this`bal ←—like one assignment

 Tracking changes with dynamic memory is not covered by Hoare Logic. Each approach adopts some kind of strategy to make the frame rule sound:

```
predicate Valid()
  reads this`a, this`size, this`s, this.a
{ RepInv() && Sound() }

method add(x:int)
  requires Valid()
  ensures Valid()
  modifies this`a, this.a, this`size, this`s

field of contents of memory modified by
```

 Dafny refers to allocated memory areas. Objects and arrays. Modification of fields are modifications to the container object.

 Tracking state changes and invalidating knowledge along the proof is crucial in the verification of imperative programs.

$$\frac{\{A\}\ P\ \{B\}}{\{A \land C\}\ P\ \{B \land C\}}$$

 Information in the interface is important to know modified and referred memory.

```
method Main() {
  var a:Account := new Account();
  a.deposit(10);
  a.withdraw(20); <<<< ????
  if a.getBalance() > 10
   { a.withdraw(10); a.deposit(10); }
}
```

 Tracking state changes and invalidating knowledge along the proof is crucial in the verification of imperative programs.

$$\frac{\{A\}\ P\ \{B\}}{\{A \land C\}\ P\ \{B \land C\}}$$

 Information in the interface is important to know modified and referred memory.

```
requires 0 <= v <= getBal()
method Main() {
  var a:Account := new Account(); { a.bal >= 0 }
  { a.bal >= 0 } a.deposit(10); { a.bal >= 0 }
  { a.bal >= 0 } a.withdraw(20);
  if a.getBalance() > 10
  { { a.bal > 10 } a.withdraw(10); a.deposit(10); }
}
```

Part II Modifying an Array

Modifying an array

 Tracking state changes and invalidating knowledge along the proof is crucial in the verification of imperative programs.

```
method selectionSort(a:array<char>, n:int)
  requires 0 <= n <= a.Length</pre>
  modifies a
  var i := 0;
  while i < n
    decreases n - i
    invariant 0 <= i <= n
    invariant sorted(a, i)
                                           method selectSmaller(a:array<char>, i
    invariant partitioned(a, i, n)
                                             requires 0 <= i < n <= a.Length</pre>
                                             requires sorted(a, i)
    selectSmaller(a, i, n);
                                             requires partitioned(a, i, n)
    i := i + 1;
                                             modifies a
                                             ensures sorted(a, i+1)
                                             ensures partitioned(a, i+1, n)
```

It is like an assignment to all positions in the array

Modifying an array

 To have control about the positions that are indeed modified extra information is needed.

```
method sortedInsertion(a:array<char>, na:int, e:char)
returns (z:array<char>, nz:int, pos:int)
    requires 0 <= na < a.Length
    requires sorted(a, na)
    modifies this.a
    ensures sorted(a, na+1)
    ensures 0 <= pos < na+1 && a[pos] == e

    ensures forall k :: 0 <= k < pos ==> a[k] == old(a[k])
    ensures forall k :: pos < k < na+1 ==> a[k] == old(a[k-1])
```

- This allows the caller context to maintain (frame) knowledge about the unmodified positions.
- All knowledge about the array must be given by the post conditions explicitly.

Another example

The Set example

```
method add(x:int)
requires Valid() &&
ensures Valid()
ensures s == old(s) + {x}
modifies this`s, this`size, this.a
{
   var idx := find(x);
   if( idx < 0 ) {
       a[size] := x;
       size := size + 1;
       s := s + {x};
   }
}</pre>
```

The precondition about the maximum size is not nice...

Another example

A more general implementation is needed to eliminate it

```
method add(x:int)
requires Valid()
ensures Valid()
ensures s == old(s) + \{x\}
modifies this`s, this`size, this`a, this.a
{
    if( size == a.Length ) { a := Grow(); }
    var idx := find(x);
    if( idx < 0 ) {
         a[size] := x;
         size := size + 1;
         S := S + \{x\};
         assert forall i :: 0 \le i \le size-1 \Longrightarrow a[i] \Longrightarrow old(a[i]);
}
```

Set ADT (growable)

```
class ASet {
  // Abstract state
   ghost var s:set<int>;
   // Representation state
   var a:array<int>;
   var size:int;
   method Grow() returns (na:array<int>)
       requires Valid()
                                               memory not tracked before
       ensures size < na.Length</pre>
       ensures fresh(na) ◆
       ensures forall k::(0<=k<size) ==> na[k] == a[k];
   {
       na := new int[a.Length*2];
       var i := 0;
       while (i<size)</pre>
           decreases size-i
           invariant 0 <= i <= size ;</pre>
           invariant forall k::(0<=k<i) ==> na[k] == a[k];
           na[i] := a[i];
           i := i + 1;
```

Set ADT (growable)

```
class ASet {
   // Abstract state
   ghost var s:set<int>;
   // Representation state
   var a:array<int>;
   var size:int;
   method add(x:int)
   requires Valid()
   ensures Valid()
   ensures s == old(s) + \{x\}
   modifies this`s, this`size, this`a, this.a
   {
       if( size == a.Length ) { a := Grow(); }
       var idx := find(x);
       if( idx < 0 ) {
            a[size] := x;
            size := size + 1;
            S := S + \{x\};
            assert forall i :: 0 \le i \le size-1 \Longrightarrow a[i] \Longrightarrow old(a[i]);
```

Set ADT (growable)

```
class ASet {
    method del(x:int)
        modifies this, a;
         requires Valid()
         ensures Valid()
         ensures x in old(s) \leq old(s) = s + {x}
      var i:int := find(x);
      if i >= 0 {
        var pos := i;
        while (i < size-1)</pre>
           modifies a;
           decreases size - 1 - i
           invariant pos <= i <= size-1</pre>
           invariant unique(a,0,i) && unique(a,i+1,size)
           invariant forall j::(0 \le j < pos) ==> a[j] == old(a[j])
           invariant forall j::(pos <= j < i) ==> a[j] == old(a[j+1])
           invariant forall j::(i+1 \le j < size) \Longrightarrow a[j] \Longrightarrow old(a[j])
         {
             a[i] := a[i+1];
             i := i + 1;
         size := size - 1;
      > Verification of Software, FCTUNL, © (uso reservado)
```

Further hints on invariants

- We illustrate a famous issue related to using formal logic to reason about dynamical systems, the so-called "frame problem".
- There is no "purely logical" way of inferring what does not change after an action, we need in each case to specify for each action not only what changes, but also what has not (remains stable).
- E.g. this arises in reasoning about programs

```
\{x.val() == a \&\& y.val() == 0\} x.inc() \{ x.val() == a+1 \&\& y.val() == ?\}
```

How do we know changing x affects y or not?

Key Points

- The ADT operations pre / post conditions must always preserve the representation invariant
- Other operations (private helper methods) do not need to preserve the invariant, they are need to know about the ADT implementation details
- The ADT pre / post conditions should avoid referring to the concrete state, to preserve information hiding
- To do that, you may expose ghost variables
- Alternatively, use also some form of typestate, enough to express rich dynamic constraints (next).

Part III Framing

ADTs and Framing

- The ADT operations pre / post conditions must always preserve the representation invariant
- The ADT pre / post conditions should not refer to the concrete state, to preserve information hiding.
- To do that, you may expose ghost variables.
- ...but what about reads / modifies clauses?

ADTs and Framing — Counter

```
class Counter
{
    var incs: int;
    var decs: int;
    ghost var Value : int;
    predicate Valid()
        reads this
    {
        Value == incs - decs
    }
    constructor ()
        ensures Valid()
        ensures Value == 0
    {
        incs, decs, Value := 0, 0, 0;
    }
```

ADTs and Framing — Counter

```
class Counter
{
    method getValue() returns (x: int)
        requires Valid()
        ensures x == Value
    {
        x := incs - decs;
    }
    method inc()
        modifies this
        requires Valid()
        ensures Valid()
        ensures Value == old(Value) + 1
    {
        incs, Value := incs + 1, Value + 1;
    }
```

ADTs and Framing — Counter

```
class Counter
method dec()
        modifies this
        requires Valid()
        ensures Valid()
        ensures Value == old(Value) - 1
    {
        decs, Value := decs + 1, Value - 1;
    method Main()
    {
        var c := new Counter();
        c.inc(); c.inc();
        c.dec(); c.inc();
        var x := c.getValue();
        assert x == 2;
        assert c.Valid();
    }
```

ADTs and Framing

- For the Counter class, the **reads/modifies** clauses are abstract (no leaking of internal representation).
- Clients can use the Counter objects in the expected way.
- Even though Counters are dynamically allocated, they use no dynamically allocated memory!
- Lets see what happens in that case...

```
class Cell
{
    var data: int;
    constructor (n: int)
        ensures data == n
    { data := n; }
class CounterCell
{
    var incs: Cell;
    var decs: Cell;
    ghost var Value : int;
    predicate Valid()
        reads this, incs, decs
    {
        incs != decs && Value == incs.data - decs.data
    }
```

```
class Cell
{
   var data: int;
    constructor (n: int)
        ensures data == n
    { data := n; }
class CounterCell
   var incs: Cell;
    var decs: Cell;
                              API leaks the representation!
    ghost var Value : int;
    predicate Valid()
        reads this, incs, decs
    {
        incs != decs && Value == incs.data - decs.data
    }
```

```
class CounterCell
{
    constructor ()
                               API leaks the representation!
        ensures Valid()
        ensures Value == 0
        ensures fresh(incs) 4
        ensures fresh(decs)
    {
        incs := new Cell(0);
        decs := new Cell(0);
        Value := 0;
    }
  method inc()
        requires Valid()
        modifies this
        ensures Valid()/&& Value == old(Value) + 1
        modifies incs
    {
        incs.data, Value := incs.data + 1, Value + 1;
    }
```

```
class CounterCell
{
    method Main()
    {
        var c := new CounterCell();
        c.inc();
        c.inc(); //Error: Call may violate context's modifies clause
        c.dec(); //Error: Call may violate context's modifies clause
        c.inc(); //Error: Call may violate context's modifies clause
        var x := c.getValue();
        assert x == 2;
        assert c.Valid();
    }
}
```

 The issue is that after the first inc(), we lose too much information...

```
class CounterCell
{
    constructor ()
                                API leaks the representation!
        ensures Valid()
        ensures Value == 0
        ensures fresh(incs)
        ensures fresh(decs)
    {
        incs := new Cell(0);
        decs := new Cell(0);
        Value := 0;
    }
                                          Effective usage requires
  method inc()
        requires Valid()
                                              even more leaking
        modifies this
        ensures Valid()/&& Value == old(Value) + 1
        modifies incs
        ensures incs == old(incs) && decs == old(decs)
        incs.data, Value := incs.data + 1, Value + 1;
    . Ind Verification of Software, FCTUNL, © (uso reservado)
```

29

ADTs and Framing

- It seems that all hope of modularity is lost once we use "real" objects...
- Luckily, there is a better way Dynamic Frames
- A dynamic frame is an expression denoting the set of objects that is used in reads and modifies clauses.
- The frame is **dynamic** because the expr. may evaluate to different sets of objects, depending on the program state.

```
class CounterDynamicFrames
{
   var incs: Cell;
                            Set of objects in the representation!
    var decs: Cell;
    ghost var Value : int;
    ghost var Repr : set<object>;
    predicate Valid()
        reads this, Repr
    {
        this in Repr &&
        incs in Repr && decs in Repr &&
        incs != decs && Value == incs.data - decs.data
```

}

```
class CounterDynamicFrames
{
   var incs: Cell;
    var decs: Cell;
    ghost var Value : int;
    ghost var Repr : set<object>;
                                    Validity requires frame
    predicate Valid()
        reads this, Repr
                                         to be accurate
    {
        this in Repr &&
        incs in Repr && decs in Repr &&
        incs != decs && Value == incs.data - decs.data
    }
```

```
constructor ()
    ensures Valid() && fresh(Repr - {this})
    ensures Value == 0
 {
    incs := new Cell(0);
                               Constructor initializes Repr
    decs := new Cell(0);
    Value := 0;
                                   with desired objects
    Repr := {this};
    Repr := Repr + {incs, decs};
 }
method getValue() returns (x: int)
    requires Valid()
    ensures x == Value
 {
    x := incs.data - decs.data;
 }
```

```
constructor ()
    ensures Valid() && fresh(Repr - {this})
    ensures Value == 0
 {
    incs := new Cell(0);
    decs := new Cell(0);
                              All objects other than this
    Value := 0;
                        allocated after constructor invocation
    Repr := {this};
    Repr := Repr + {incs, decs};
 }
method getValue() returns (x: int)
    requires Valid()
    ensures x == Value
 {
    x := incs.data - decs.data;
```

}

```
method inc()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr))
    ensures Value == old(Value) + 1
{
    incs.data, Value := incs.data + 1, Value + 1;
}
method dec()
    requires Valid()
    modifies Repr
    ensures Valid() && fresh(Repr - old(Repr))
    ensures Value == old(Value) - 1
{
    decs.data, Value := decs.data + 1, Value - 1;
}
```

Any extra objects in Repr are fresh

Dynamic Frames

- Constructor specifies freshness of Repr {this}.
- Any extra objects in Repr are fresh.
- Otherwise (this may be fine):

```
method ShareMe(cnt: CounterDynamicFrames)
    requires Valid() && cnt.Valid()
    modifies Repr
    ensures Valid() && Value == old(Value)
{
    if (incs.data == cnt.incs.data && decs != cnt.incs) {
        incs := cnt.incs;
        Repr := Repr + {incs};
    }
}
```

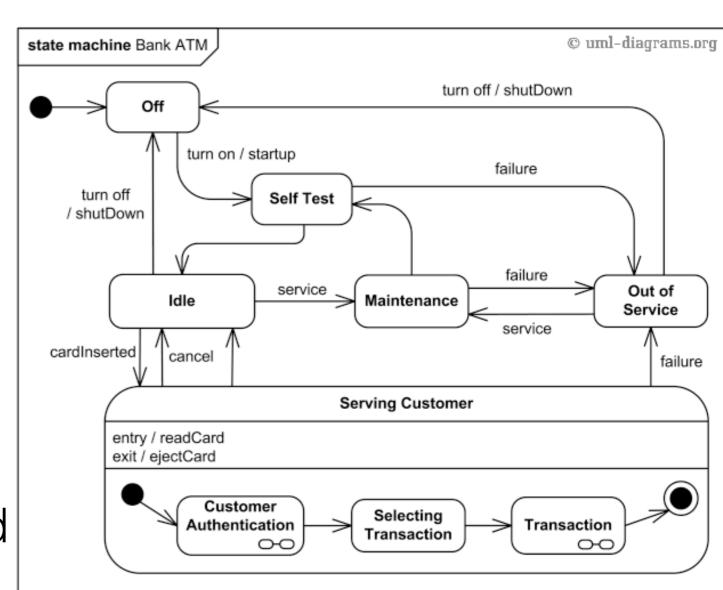
ADTs and Framing — Dynamic Frames

- Each object carries with it a (ghost) set of the objects in its memory representation (Repr).
- Invariants enforce validity of Repr.
- Constructor specifies freshness of Repr {this}.
- Methods now read / modify Repr instead of exposing internal state (generally, fresh(Repr - old(Repr)).
- Idiom supports arbitrary nesting of objects (can refer to Repr of fields and so on).

Part IV ADTs and Typestates

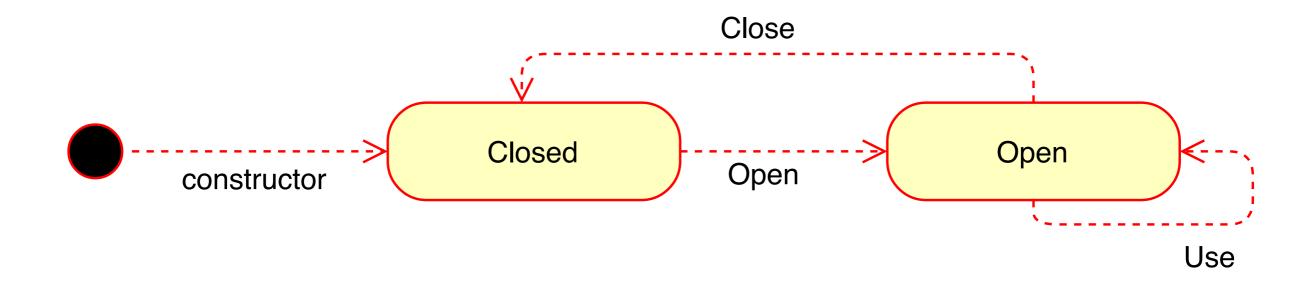
State Transition Diagrams

- Typically the connection between a state and the domain of the values for an object are based on conventions / written in documentations.
- Operations are state transitions in a state diagram.
- If a state is formally connected to conditions over the state of an object, the correction of state transitions may be mechanically checked



TypeStates

- In many situations, we may represent each abstract state of an ADT by a named assertion, that hides some set of concrete states
- We illustrate using a general Resource object with the following state diagram



TypeStates

- In many situations, we may represent each abstract state of an ADT by a named assertion, that hides some set of concrete states
- We illustrate using a general Resource object.
 - A Resource must first be created and starts on the closed state
 - A Resource can only be used after being Opened
 - A Resource may be Closed at any time
 - A Resource can only be Opened if it is in the Closed state, and Closed if it is in the Open state
- We define two abstract states (ClosedState() and OpenState())

```
class Resource {
    var h:array?<int>;
    var size:int;
    predicate OpenState()
    reads this
    { ... }
    predicate ClosedState()
    reads this
    { ... }
    constructor ()
    ensures ClosedState();
    { ... }
```

TypeStates define an abstract layer, visible to clients that can be used to verify resource usage.

```
class Resource {
    var h:array?<int>;
    var size:int;
    predicate OpenState()
    reads this
    { ... }
    predicate Clossic Character
                  method UsingTheResource()
    reads this
    { ... }
                      var r:Resource := new Resource();
                       r.Open(2);
    constructor
                       r.Use(2);
    ensures Clos
                       r.Use(9);
    { ... }
                                    Legal usage of resource,
                       r.Close();
                                    according to protocol!
                  }
```

```
class Resource {
    var h:array?<int>;
    var size:int;
    predicate OpenState()
    reads this
    { ... }
    predicate Clc method UsingTheResource()
    reads this
                      var r:Resource := new Resource();
    { ... }
                      r.Close();
                      r.Open(2);
    constructor (
                      r.Use(2);
    ensures Clos
                      r.Use(9);
    { ... }
                                    Illegal usage of resource,
                      r.Close();
                                    according to protocol!
                      r.Use(2);
```

```
class Resource {
                            TypeStates define an abstract
                            layer, that may be defined with
   var h:array?<int>;
   var size:int;
                            relation to the representation type
                            (and invariants) and be used to
   predicate OpenState()
                            verify the implementation.
       requires Valid()
       reads Repr
    { h != null && size == h.Length }
   predicate ClosedState()
       requires Valid()
       reads Repr
    { size == 0 }
   constructor ()
   ensures Valid() && fresh(Repr-{this}) && ClosedState()
    { size, h := 0 , null; Repr := this; }
```

```
class Resource {
                         Method implementations represent
                         state transitions, and must be
   var h:array?<int>;
                         implemented to correctly ensure the
   var size:int;
                         soundness of the arrival state
   method Open(N:int)
                         (assuming the departure state)
   modifies Repr
   requires Valid() && ClosedState() && N > 0
   ensures Valid() && OpenState() && fresh(Repr-old(Repr))
    { h, size := new int[N], N;
       Repr := Repr + \{h\}; \}
   method Close()
   modifies Repr
   requires Valid() && OpenState()
   ensures Valid() && ClosedState() && fresh(Repr-old(Repr))
    { h, size := null, 0;
     Repr := Repr - \{h\}; \}
```

```
class Resource {
    var h:array?<int>;
    var size:int;
    method Use(K:int)
    modifies h;
    requires OpenState()
    ensures OpenState()
       h[0] := K;
```

No execution errors can be caused by misusing the representation type. Notice that states are also used as invariants, essential to execute different methods.

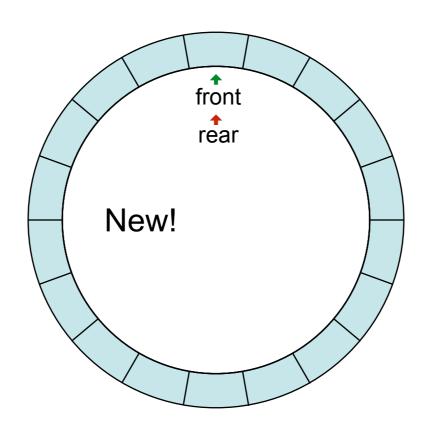
TypeStates

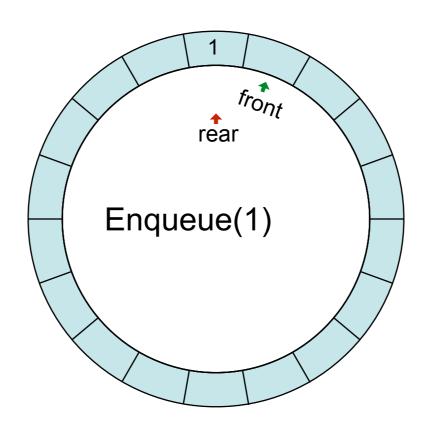
- In many situations, we may represent each abstract state of an ADT by a named assertion, that hides some set of concrete states
- It is often enough to expose Typestate assertions to ensure ADT soundness and no runtime errors
- In general, full functional specifications in terms the abstract state is too expensive and should be only adopted in high assurance code
- However, Typestate assertions are feasible and should be enforced in all ADTs:
- The simplest TypeState is the RepInv (no variants/less specific).

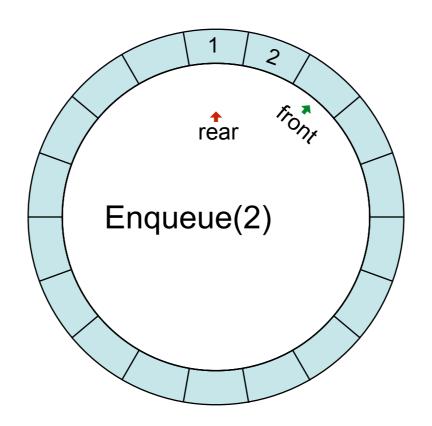
Key Points

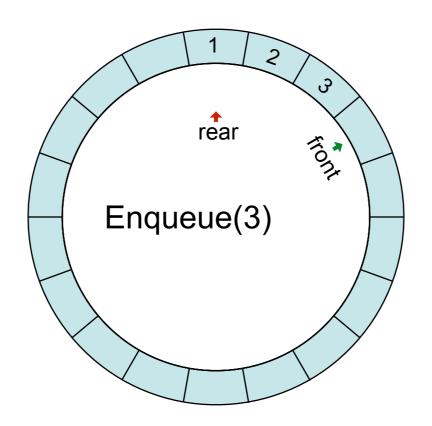
- Software Design Time
 - Abstract Data Type
 - What are the Abstract States / Concrete States?
 - What is the Representation Invariant?
 - What is the Abstraction Mapping?
- Software Construction Time
 - Make sure constructor establishes the RepInv
 - Make sure all operations preserve the RepInv
 - they may assume the RepInv
 - they may require extra pre-conditions (e.g. on op args)
 - they may enforce extra post-conditions
 - Use assertions to make sure your ADT is sound

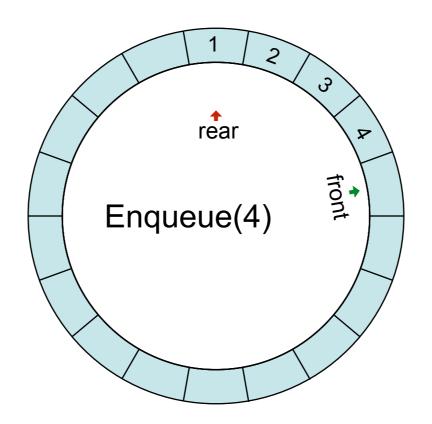
Part V Typestates (Example)

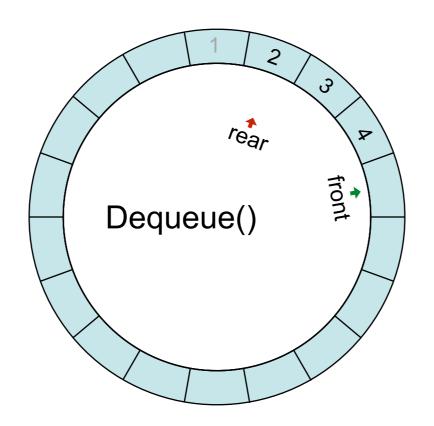


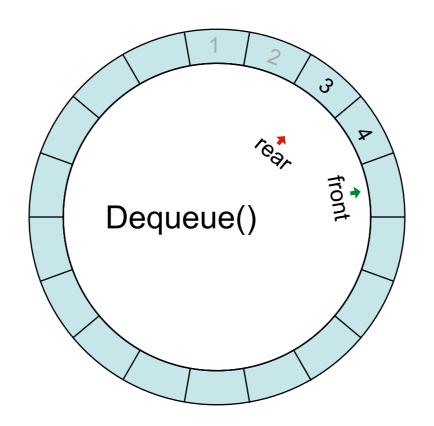


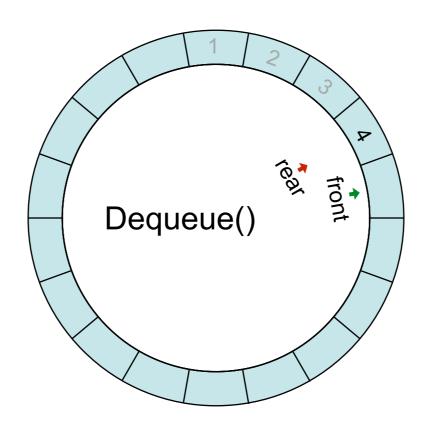


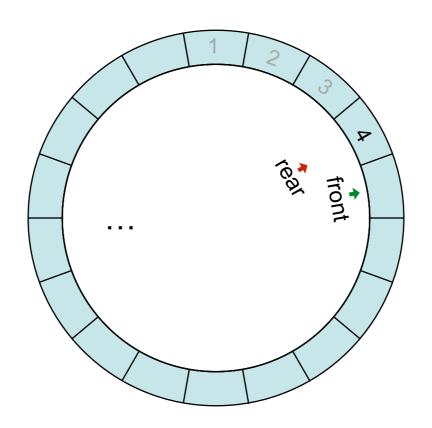


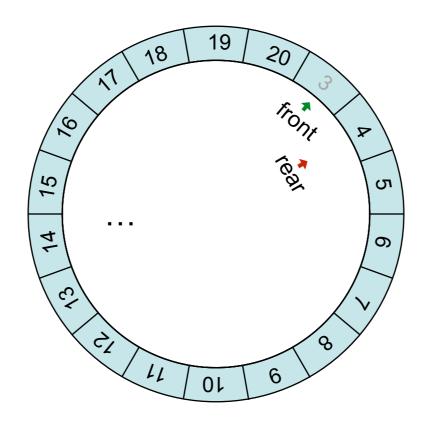


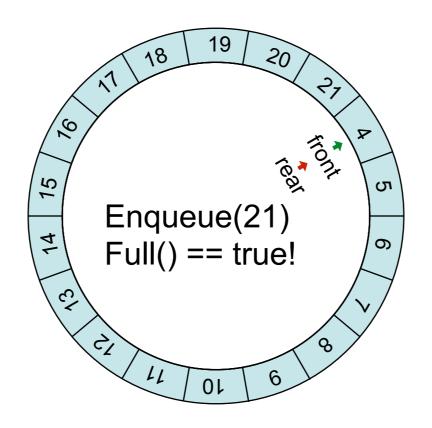












```
class {:autocontracts} Queue {
    // Representation type
    var a:array<int>;
    var front: int;
    var rear: int;
    var numberOfElements: int;
    constructor(N:int)
        requires 0 < N
    {
        a := new int[N];
        front, rear := 0 , 0;
        Repr := {this};
        numberOfElements := 0;
```

 What's wrong with it? a RepInv is necessary to maintain front and rear within bounds...

```
class {:autocontracts} Queue {
   method Enqueue(V:int)
        a[front] := V;
        front := (front + 1)%a.Length;
        numberOfElements := numberOfElements + 1;
   method Dequeue() returns (V:int)
        V := a[rear];
        rear := (rear + 1)%a.Length;
        numberOfElements := numberOfElements - 1;
```

```
class {:autocontracts} Queue {
    // Representation type
    var a:array<int>;
    var front: int;
    var rear: int;
    var numberOfElements: int;
    // Representation invariant
    predicate RepInv()
        reads Repr
    { 0 <= front < a.Length && 0 <= rear < a.Length }
    constructor(N:int)
        requires 0 < N
        ensures RepInv()
        a := new int[N];
        front, rear := 0 , 0;
        Repr := {this}
        numberOfElements := 0;
```

```
class {:autocontracts} Queue {
    method Enqueue(V:int)
        requires RepInv()
        ensures RepInv()
        a[front] := V;
        front := (front + 1)%a.Length;
        numberOfElements := numberOfElements + 1;
    }
    method Dequeue() returns (V:int)
        requires RepInv()
        ensures RepInv()
        V := a[rear];
        rear := (rear + 1)%a.Length;
        numberOfElements := numberOfElements - 1;
```

 Not enough... No runtime errors but the correct behaviour is not yet ensured... wrong values may be returned, valid elements maybe overwritten

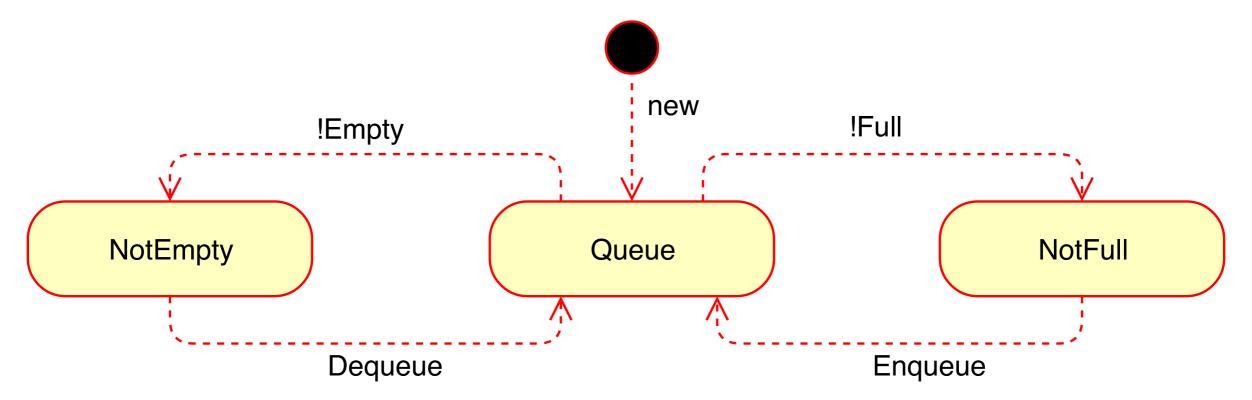
```
method Main()
{
    var q:Queue := new Queue(4);
    var r:int;

    q.Enqueue(1);
    r := q.Dequeue();
    r := q.Dequeue();
    q.Enqueue(2);
    q.Enqueue(3);
    q.Enqueue(4);
    q.Enqueue(4);
    q.Enqueue(4);
    q.Enqueue(5);
}
```

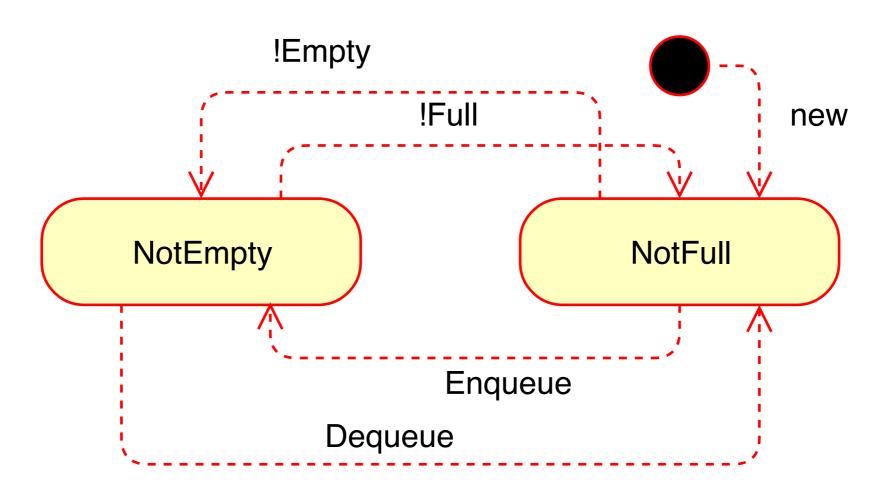
 Replnv must be refined to ensure that we stay inside the domain of valid queues...

```
predicate RepInv()
     reads this, Repr
 {
     0 <= front < a.Length &&</pre>
     0 <= rear < a.Length &&</pre>
     if front == rear then
       numberOfElements == 0 ||
       numberOfElements == a.Length
     else
       numberOfElements ==
         if front > rear
         then front - rear
         else front - rear + a.Length
 }
```

 Enqueue and Dequeue Operations are only valid in certain states... Obtained by dynamic testing operations.



 Enqueue and Dequeue Operations are only valid in certain states... Obtained by dynamic testing operations.



```
class {:autocontracts} Queue {
    predicate NotFull()
        reads this
    { RepInv() && numberOfElements < a.Length }
    predicate NotEmpty()
        reads this
    { RepInv() && numberOfElements > 0 }
    constructor(N:int)
        requires 0 < N
        ensures NotFull()
    { ... }
    method Enqueue(V:int)
        requires NotFull()
        ensures NotEmpty()
    { ... }
    method Dequeue() returns (V:int)
        requires NotEmpty()
        ensures NotFull()
    { ... }
```

```
method Main()

{
    var q:Queue := new Queue(4);
    var r:int;

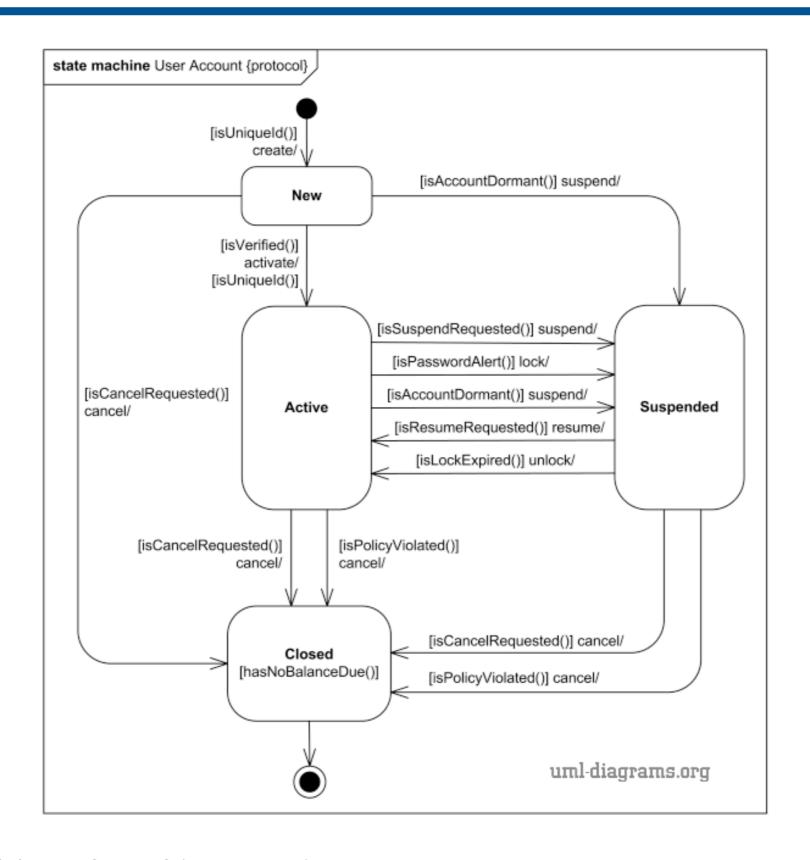
    q.Enqueue(1);
    r := q.Dequeue();
    r := q.Dequeue();
    q.Enqueue(2);
    q.Enqueue(3);
    q.Enqueue(4);
    q.Enqueue(5);
}
```

Dynamic Tests ensure the proper state for a given operation...

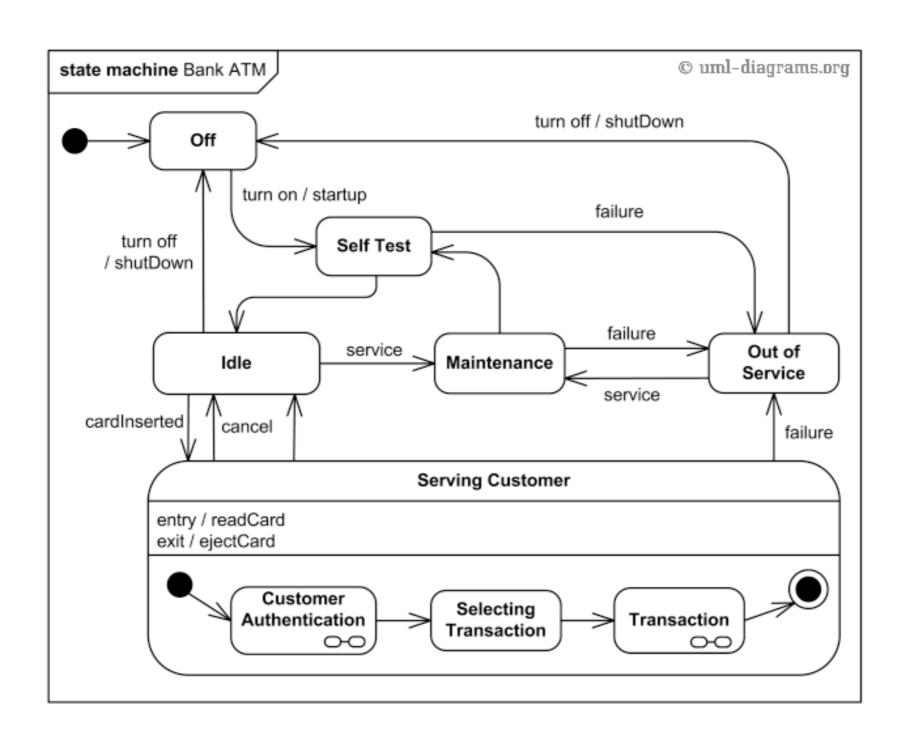
```
method Main()
{
    var q:Queue := new Queue(4);
    var r:int;

    q.Enqueue(1);
    r := q.Dequeue();
    if !q.Empty()
        { r := q.Dequeue(); q.Enqueue(2); }
        if !q.Full() { q.Enqueue(3); }
        if !q.Full() { q.Enqueue(4); r := q.Dequeue(); }
        if !q.Full() { q.Enqueue(5); }
}
```

TypeStates - UserAccount in a store



TypeStates - ATM



Exercise 14

ADT PSet

```
// Use the set implementation ASet of Lecture 3 and
// add to the representation invariants the property about
// all values being positive. Make the post-conditions
// stronger using that property
// Design some client methods and write assertions
```

// that are a consequence of the abstract invariant.

Exercise 15

Extended Bank Account that stores operations

```
// Implement a bank account whose internal
// representation is an array of bank movements
// (debit, credit).

// Make the adequate abstract representation for
// the balance and define the soundness mapping.
```

Exercise 16 (Key-Value Store)

- This exercise focuses on the development of a small but rigorously 100% bug free dictionary abstract data type (ADT). Consider that the type of keys is the K and the type of values V.
- The ADT must provide the following operations
 method assoc(k:K,v:V)
 // associates val v to key k in the dictionary
 method find(k:K) returns (r:RES)
 // returns NONE if key k is not defined in the dict, or SOME(v) if the dictionary
 method delete(k:K)

// removes any existing association of key k in the dictionary

Every dictionary entry should be represented by a record of type ENTRY

datatype ENTRY = PACK(key: K, val: V)

The result of function find should be represented with type

datatype RES = NONE | SOME(V)

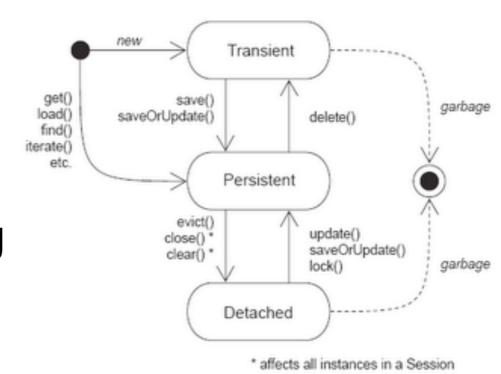
- The representation type of your ADT should be a mutable data structure (advice: start by something simple - an array, an ordered array, or a closed hashtable.
- Express the representation invariant using an auxiliary boolean function Replnv()

Exercise (2nd Handout 17/18)

Implement an ADT representing a Persistent Entity of the JPA library such that each item has the following states:

You must research about JPA states and implement two example classes that simulate such behaviour.

Persistency can be achieved by storing items in a collection/store/database represented by an array of objects.



If an item is not persistent, it does not have a valid identifier, when stored or updated the data is copied to the collection (no references).

Consider as an example a Person entity (name, age).

Exercise (2nd Handout 17/18)

To make it easier, consider the simplified state diagram.

Operation find is a method of the store class that instantiates an object (copy from the DB) with a valid id and a valid store connection.

Implement a class Person that accepts the store as parameter in methods save(store) and update(store).

When a Person is transient state, it has no valid when a Person is in detached state, It has no valid store connection (offline from the database).

new

find

save()

close()

Transient

Persistent

Detached

delete()

update()