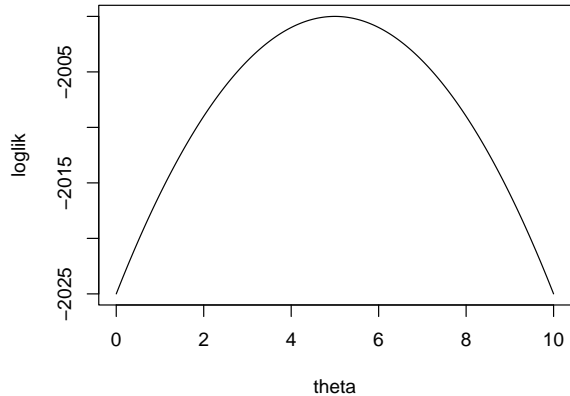


The Python function `statsmodels.tsa.arima.model.ARIMA.fit` and the R function `arima()` provide standard errors calculated by observed Fisher information. This question tests your understanding of what that means. Suppose a parametric model has a single parameter,  $\theta$ , and the log-likelihood function when fitting this model to dataset is as follows:



What is the observed Fisher information ( $I_{obs}$ ) for  $\theta$ ?

Hint 1. The observed Fisher information is accumulated over the whole dataset, not calculated per observation, so we don't have to know the number of observations,  $N$ .

Hint 2. Observations in time series models are usually not independent. Thus, the log-likelihood is not the sum of the log-likelihood for each observation. Its calculation will involve consideration of the dependence, and usually the job of calculating the log-likelihood is left to a computer.

Hint 3. The usual variance estimate for the maximum likelihood estimate,  $\hat{\theta}$ , is  $\text{Var}(\hat{\theta}) \approx 1/I_{obs}$ .

A:  $I_{obs} = 2$

B:  $I_{obs} = 1$

C:  $I_{obs} = 1/2$

D:  $I_{obs} = 1/4$

E: None of the above