

# STATS 700-002 Class 2.

## The coalescent

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Kingman, J. F. C. (1982). The coalescent. *Stochastic Processes and their Applications*, 13(3), 235-248.  
[https://doi.org/10.1016/0304-4149\(82\)90011-4](https://doi.org/10.1016/0304-4149(82)90011-4).

## Section 1

- ▶ How does the construction of section 1 relate to a genealogical tree?
- ▶ What does the assumption (1.3) mean?
- ▶ Is the relation  $\prec$  defined in (1.4) an order relation?
- ▶ Verify that  $q_\xi = \binom{|\xi|}{2}$ , as claimed in (1.6).
- ▶ In terms of genealogical trees, what is the interpretation of the  $D_t$  process introduced in (1.8)?
- ▶ In terms of genealogical trees, what does the *transit time*  $T$  introduced in (1.11) correspond to?

# Theorem 1

- ▶ What do we have to know about continuous time Markov chains to follow this proof?
- ▶ Why does equation (2.1) hold?
- ▶ Verify equation (2.2).

## Theorems 3 and 4

- ▶ Summarize, in words, what is accomplished by these results.

## Relevance to phylodynamics

- ▶ It may be hard at this point to see the relevance of Kingman's coalescent to practical phylodynamic inference.
- ▶ Given what we know at this point, conjecture how Kingman's coalescent might be used, or extended to be useful.

