

# Haskell les 3: Type magic

*door Pietervdvn*

# Syntax: Guards

# Guards

```
fac :: Int -> Int
```

```
fac i
```

```
  | i == 0      = 1
```

```
  | otherwise   = i * fac $ i - 1
```

Soms handig bij complexe checks

Syntax:

@

@

```
doeDingen  :: Maybe Int -> Maybe Int  
doeDingen maybe@(Just i)  
    = i + doeAndereDingen maybe
```

Syntax:  
let

# Let

```
foo :: Int -> Int -> Int -> Int
```

```
foo x y z
```

```
    = let  xy  = x + y in
```

```
      z * xy
```

# Let

```
foo :: Int -> Int -> Int -> Int
```

```
foo x y z
```

```
    = let  xy    = x + y
```

```
          zxy    = xy * xy + z in
```

```
    zxy
```



# Let

```
bar :: Maybe Int -> Int
```

```
bar maybe
```

```
  | isJust maybe
```

```
    = let (Just i) = maybe in
```

```
      i * 2
```

```
  | otherwise = 0
```

# Theorie

# fmap

`fmap :: (a -> b) -> [a] -> [b]`

`fmap :: (a -> b) -> Maybe a -> Maybe b`

`fmap :: (a -> b) -> Tree a -> Tree b`

`fmap :: (a -> b) -> Set a -> Set b`

There's a suspicious pattern here

# fmap

container met dingen van type a

Functie wordt uitgevoerd op a in die container

# Functor

container met dingen van type `a`

Functie wordt uitgevoerd op `a` in die container

Zo'n container noemt een **Functor**

# Functor

## Volgens wikipedia:

In mathematics, a **functor** is a type of mapping between categories, which is applied in category theory. Functors can be thought of as homomorphisms between categories. In the category of small categories, functors can be thought of more generally as morphisms.

Functors were first considered in algebraic topology, where algebraic objects (like the fundamental group) are associated to topological spaces, and algebraic homomorphisms are associated to continuous maps. Nowadays, functors are used throughout modern mathematics to relate various categories. Thus, functors are generally applicable in areas within mathematics that category theory can make an abstraction of.

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) -> [a] -> [c]
```

```
doublefmap f g as
```

```
    = fmap g $ fmap f as
```

```
    :: [b]
```

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) -> [a] -> [c]
```

```
doublefmap f g as
```

```
    = fmap g $ fmap f as
```

```
    :: [c]
```



# double fmap

```
doublefmap (*2) show [1,2,3]
```

```
doublefmap f      g      as  
    = fmap g $ fmap f as
```

# double fmap

```
doublefmap (*2) show [1,2,3]
```

```
doublefmap f g as  
= fmap g $ fmap f as
```

# double fmap

```
fmap show $ fmap (*2) [1,2,3]
```

```
doublefmap f      g      as  
    = fmap g $ fmap f as
```

# double fmap

```
fmap show [2,4,6]
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```

# double fmap

```
["2", "4", "6"]
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) -> [a] -> [c]
```

```
doublefmap f g  as  
    = fmap g $ fmap f as
```

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) -> [a] -> [c]
```

```
doublefmap f g
```

```
    = fmap g . fmap f
```

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) ->  
             Maybe a -> Maybe c
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```



# double fmap

```
doublefmap (*2) show $ Just 21
```

```
doublefmap f      g      as  
    = fmap g $ fmap f as
```

# double fmap

```
fmap show $ fmap (*2) $ Just 21
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```

# double fmap

```
fmap show $ Just 42
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```

# double fmap

Just “42”

```
doublefmap f g as  
    = fmap g $ map f as
```

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) ->  
            Tree a -> Tree c
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```

# double fmap

```
doublefmap :: (a -> b) -> (b -> c) ->  
              Tree a -> Tree c
```

```
doublefmap f g as  
    = fmap g $ fmap f as
```

Hoe schrijven we dit voor **elke** functor?

# double fmap

```
doublefmap :: Functor functor =>  
            (a -> b) -> (b -> c) ->  
            functor a -> functor c  
  
doublefmap f g as  
    = fmap g $ fmap f as
```

Hoe schrijven we dit voor **elke** functor?

# double fmap

```
doublefmap :: Functor f =>  
            (a -> b) -> (b -> c) ->  
            f a -> f c
```

```
doublefmap f g as  
  = fmap g $ fmap f as
```

Hoe schrijven we dit voor **elke** functor?



# Instance

# Maybe

We hebben onze eigen Maybe gemaakt

Hoe vertellen we Haskell dat dit ook een Functor is?

# Maybe

```
instance Functor Maybe where  
  fmap f (Just a) = Just $ f a  
  fmap _ Nothing  = Nothing
```

# List

We hebben onze eigen `List` gemaakt

Hoe vertellen we Haskell dat dit ook een  
`Functor` is?

# List

```
instance Functor List where
    fmap f (Cons a as)
        = Cons (f a) $ fmap f as
    fmap _ Nil = Nil
```

class

# Hoe maken we zelf functor

class **Functor** f where

fmap :: (a -> b) -> f a -> f b

# Andere nuttige klassen



# Sidenote

Waarom `fmap`? Was gewoon `map` niet genoeg?

- `map` voor lijsten
- `fmap` voor functoren
- ‘noobvriendelijk’
- Wordt binnenkort veralgemeend (`mss`)

# Show

```
class Show show where  
  show :: show -> String
```

Ding met een representatie

# Eq

```
class Eq eq where  
    (==) :: eq -> eq -> Bool
```

Vergelijkbaar ding

# Ord

```
class Ord ord where  
    (>) :: ord -> ord -> Bool  
    (<) :: ord -> ord -> Bool  
    (<) a b = not (a > b)
```

Vergelijkbaar ding

# Num

```
class Num num where
```

```
...
```

Ding dat een getal is, zoals Int, Float, ...

# Monoid

```
class Monoid a where  
  mempty :: a  
  mappend :: a -> a -> a  
  mconcat :: [a] -> a
```

Ding dat een groter wordt, zoals `Int`, `[a]`, ...

# Monoid

`5 `mappend` 37 == 42`

`[1,2] `mappend` [3,4] == [1,2,3,4]`

# Type constraints

`(+) :: Num a => a -> a -> a`

`sort :: Ord a => [a] -> [a]`



# Deriving

# Deriving

Moeten we dan altijd zelf Show, Eq, Ord maken?

# Deriving

Moeten we dan altijd zelf Show, Eq, Ord maken?

```
data Maybe a = Just a | Nothing
  deriving (Show, Eq, Ord)
```

# Type synonymiemen

# HTML

Simpele html bibliotheek

`link = "a"`

`inside content tag`

`= (open tag) ++ cont ++ (close tag)`

# HTML

Simpele html bibliotheek

**link :: String**

link = "a"

**inside :: String -> String -> String**

inside content tag

= (open tag) ++ cont ++ (close tag)

# HTML

Simpele html bibliotheek

**link :: Tag**

link = "a"

**inside :: String -> Tag -> HTML**

inside content tag

= (open tag) ++ cont ++ (close tag)

# HTML

```
type HTML    = String
```

```
type Tag     = String
```



# String

```
type String = [Char]
```

# Higher order programming

# Writer

Berekening die 'en passent' verschillende waarden berekent (bv. een logbestand)

# Writer

```
berekening :: <argtypes> -> (a, [String])
```

```
berekening <args>
```

```
    = (... , ["Dingen gedaan"])
```

# Writer

Berekening die 'en passent' verschillende waarden bijhoudt (bv. een logbestand, een teller)

Constant log teruggeven wordt onhandig

# Writer

`data Writer log a = Writer log a`

# Writer

```
data Writer log a = Writer log a
```

```
tell :: log -> Writer log ()
```

```
tell entry = Writer entry ()
```

```
return :: a -> Writer log a
```

```
return a = Writer mepmty a
```

# Writer

```
andThen' :: Writer log a  
          -> Writer log b -> Writer log b  
andThen' (Writer log _) (Writer log' b)  
  = Writer (log `mappend` log') b
```



# Writer

```
andThen :: Writer log a  
        -> (a -> Writer log b) -> Writer log b  
andThen (Writer log a) a2wb  
= let    (Writer log' b)    = a2wb a in  
  Writer (log `mappend` log') b
```

# Writer

```
return 42
```

```
return a = Writer a mepmty
```

# Writer

```
Writer mempty 42
```

```
return a = Writer a mempty
```

# Writer

```
tell ["hi"]
```

```
tell log = Writer () log
```

# Writer

```
Writer ["hi"] ()
```

```
tell log = Writer () log
```

# Writer

```
tell ["hi"] `andThen` return 42
```

# Writer

```
Writer ["hi"] () `andThen` Writer mempty 42
```

# Writer

```
Writer ["hi"] () `andThen` Writer [] 42
```

```
andThen' (Writer log _) (Writer log' b)  
  = Writer (mappend log log') b
```



# Writer

```
Writer (mappend ["hi"] []) 42
```

```
andThen' (Writer log _) (Writer log' b)  
  = Writer (mappend log log') b
```

# Writer

```
Writer ["hi"] 42
```

```
andThen' (Writer log _) (Writer log' b)  
  = Writer (mappend log log') b
```

# Writer

```
tell ["hi"] `andThen`  
tell ["something happens" ] `andThen`  
someLoggingCalculation `andThen`  
(\ i -> tell ["We found "++show i] `andThen`  
         return $ i * 2)
```

# Writer

```
Writer ["hi","something happens", <logs>,  
        "we found 21"] 42
```

# Writer

```
tell 10 `andThen` return 32 `andThen` tell
```

# Writer

```
Writer 42 ()
```



# Haddock

# Haddock

```
-- | Docstring van functie/module/type  
foo :: a -> a
```



# Haddock

```
haddock File.hs --html
```

# Oefeningen

*[github.com/pietervdvn/haskell](https://github.com/pietervdvn/haskell)*