Attention & Transformers

Ivo Verhoeven | Advanced Topics in Computational Semantics

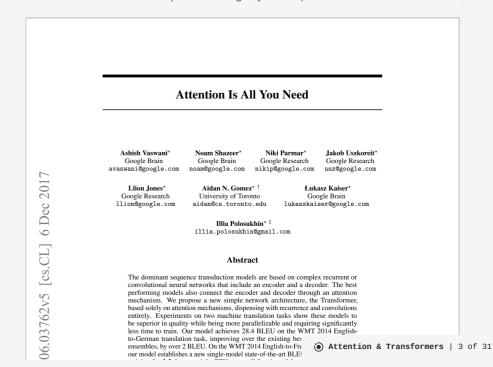
About Me



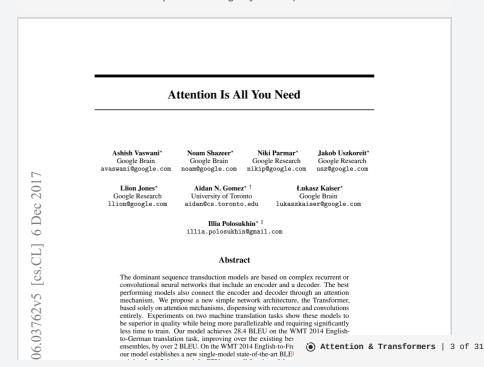
- 2017 2020: BSc. Liberal Arts & Sciences
- 2020 2022: MSc. Al at University of Amsterdam
 - Thesis on meta-learning, morphology and translation
 - Took ATCS in 2021

- 2022 ???: PhD at ILLC
 - Misinformation detection and generalisation with Katia Shutova

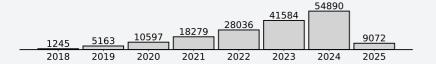
- Introduces the Transformer architecture in late 2017
 - Google Brain/Google Research collab

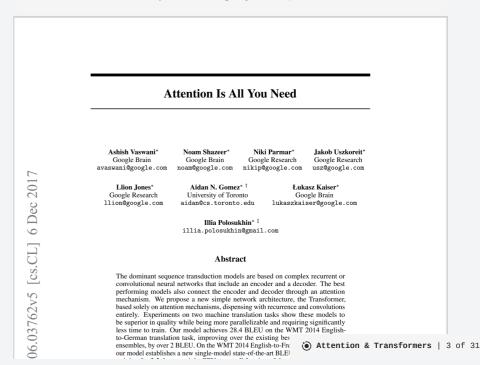


- Introduces the Transformer architecture in late 2017
 - Google Brain/Google Research collab
- Paper currently has 169 248 citations
 - Or ~64 citations a day

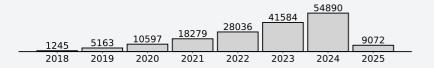


- Introduces the Transformer architecture in late 2017
 - Google Brain/Google Research collab
- Paper currently has 169 248 citations
 - Or ~64 citations a day
- Number of citations is only accelerating



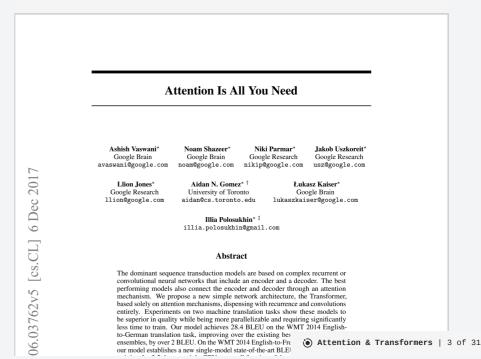


- Introduces the Transformer architecture in late 2017
 - Google Brain/Google Research collab
- Paper currently has 169 248 citations
 - Or ~64 citations a day
- Number of citations is only accelerating

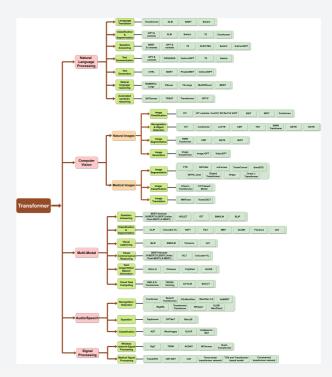


Most cited paper ever has 233 829 citations

Lowry et al. (1951) Protein measurement with the folin phenol reagent.

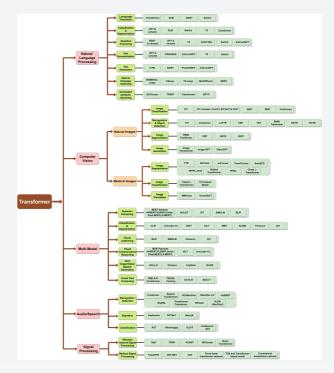


 It's hard to think of an Al area that hasn't been affected by the Transformer



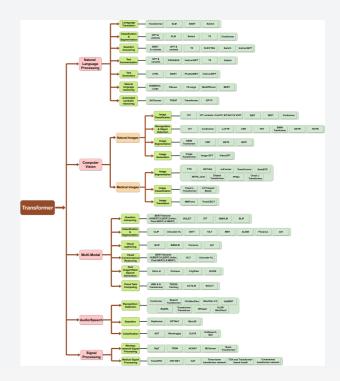
Islam, et al. (2023). A Comprehensive Survey on Application Transformers for Deep Learning Tasks. arXiv:2306.07303.

- It's hard to think of an Al area that hasn't been affected by the Transformer
 - NLP: Transformer > RNN
 - Seq-to-seq: what it was designed for
 - Classification: encoder-only transformers
 - Generation: decoder-only transformers



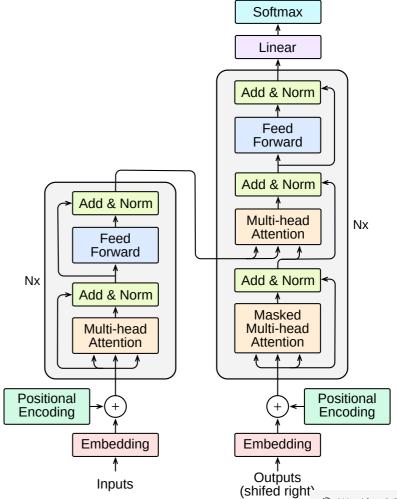
Islam, et al. (2023). A Comprehensive Survey on Application Transformers for Deep Learning Tasks. arXiv:2306.07303.

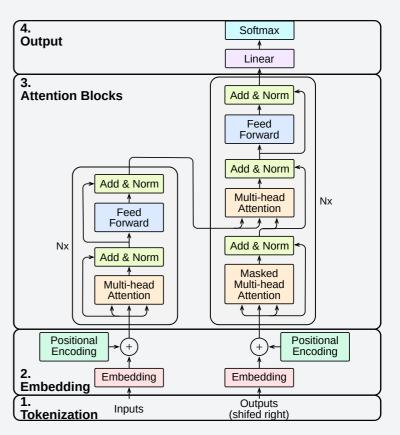
- It's hard to think of an AI area that hasn't been affected by the Transformer
 - NLP: Transformer > RNN
 - Seq-to-seq: what it was designed for
 - Classification: encoder-only transformers
 - Generation: decoder-only transformers
 - CV: ViT > CNN
 - Multi-modal: Transformer > different architectures
 - Speech: Transformer > CNN
 - Graphs: Transformer/Attention > GCN



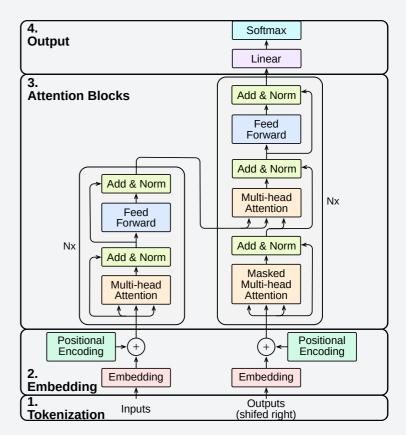
Islam, et al. (2023). A Comprehensive Survey on Application Transformers for Deep Learning Tasks. arXiv:2306.07303.

The Transformer

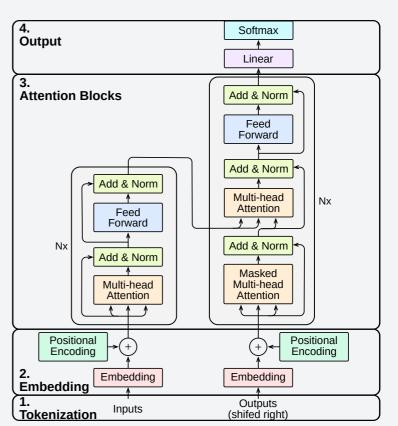




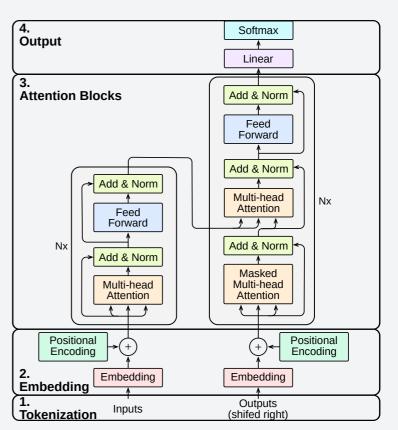
- 4. Output
 - Softmax
 - Linear



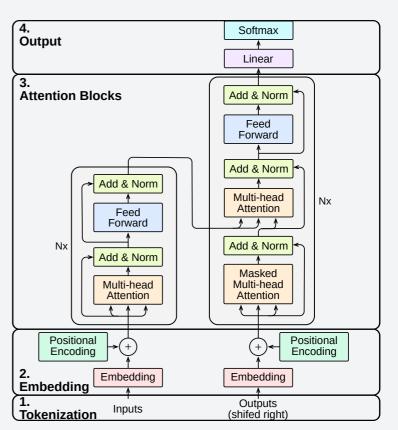
- 4. Output
 - Softmax
 - Linear
- 3. Attention Blocks
 - Multi-head Attention
 - Add & Norm
 - Feed Forward



- 4. Output
 - Softmax
 - Linear
- 3. Attention Blocks
 - Multi-head Attention
 - Add & Norm
 - Feed Forward
- 2. Embedding
 - Token Embedding
 - Positional Encoding



- 4. Output
 - Softmax
 - Linear
- 3. Attention Blocks
 - Multi-head Attention
 - Add & Norm
 - Feed Forward
- 2. Embedding
 - Token Embedding
 - Positional Encoding
- 1. Tokenization
 - (Not pictured)



- 4. Output
 - Softmax
 - Linear
- 3. Attention Blocks
 - Multi-head Attention
 - Add & Norm
 - Feed Forward
- 2. Embedding
 - Token Embedding
 - Positional Encoding
- 1. Tokenization
 - (Not pictured)

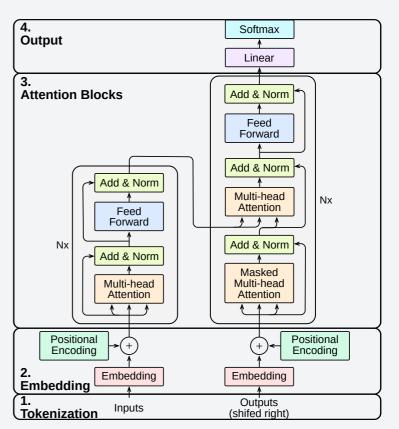
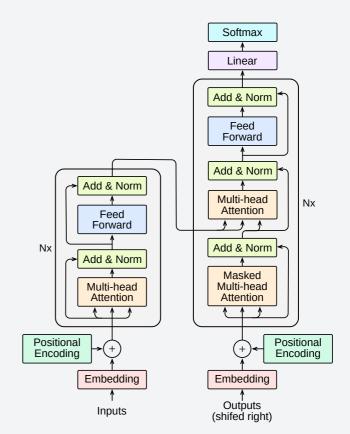


Table of Contents

- 1. Encoders & Decoders
- 2. Attention Blocks
 - 1. Add & Norm
 - 1. Residual Connections
 - 2. LayerNorm
 - 2. Feed Forward
- 3. Embedding
 - 1. Position Encoding
- 4. Tokenization
- 5. Training Transformers



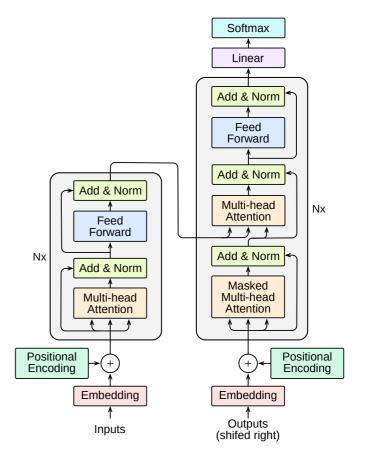
Encoders & Decoders

Text comes in, text goes out

Jakob Uszkoreit (August 31, 2017). Transformer: A Novel Neural Network Architecture for Language Understanding. https://research.google/blog/transformer-a-novel-neural-network-architecture-for-language-understanding/

Attention Blocks

What makes the Transformer what it is — and where it came from



- Let V be a matrix of (word) vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D

$$\mathbf{Attention}(?,?,\mathbf{V}) = \mathbf{AV}$$
 $\mathbf{A} \in (0,1)^{[T_V imes T_V]}$ $\mathbf{V} \in \mathbb{R}^{[T_V imes D]}$

Multi-head Attention

- Let V be a matrix of (word) vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D

- Attention is just a matrix product of V
 with an attention matrix A
 - lacksquare f A is a square matrix of size $T_V imes T_V$
 - It's elements are all between (0,1)
 - It's rows sum to 1

 $\mathbf{Attention}(?,?,\mathbf{V}) = \mathbf{AV}$ $\mathbf{A} \in (0,1)^{[T_V imes T_V]}$ $\mathbf{V} \in \mathbb{R}^{[T_V imes D]}$

Multi-head Attention

- Let V be a matrix of (word) vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D

- Attention is just a matrix product of V
 with an attention matrix A
 - lacksquare f A is a square matrix of size $T_V imes T_V$
 - It's elements are all between (0,1)
 - It's rows sum to 1

 ${\tt Attention}(?,?,\mathbf{V}) = \mathbf{AV}$

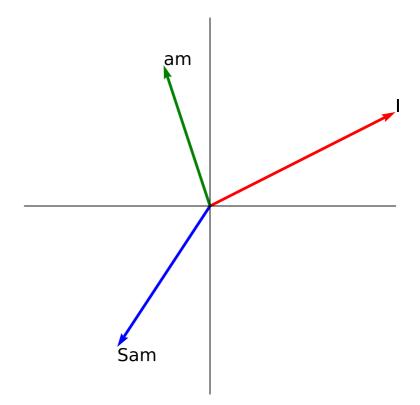
 $\mathbf{A} \in (0,1)^{[T_V imes T_V]}$

 $\mathbf{V} \in \mathbb{R}^{[T_V imes D]}$

Multi-head Attention

■ The result of Attention is just a convex combination of **V**

$$\begin{bmatrix} 0.6 & 0.1 & 0.3 \\ 0.3 & 0.5 & 0.2 \\ 0.2 & 0.1 & 0.7 \end{bmatrix} \begin{bmatrix} 2.0 & 1.0 \\ -0.5 & 2.0 \\ -1.0 & -0.5 \end{bmatrix} \begin{bmatrix} \mathbf{I} \\ \mathbf{am} \\ \mathbf{Sam} \end{bmatrix}$$

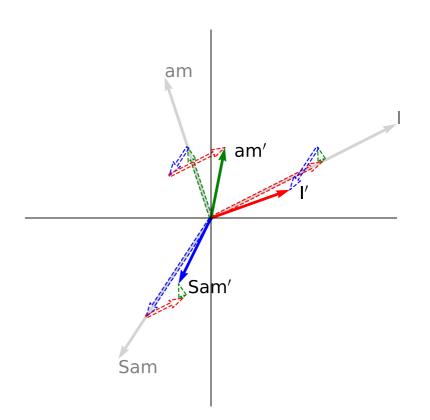


Multi-head Attention

■ The result of Attention is just a convex combination of **V**

$$\begin{bmatrix} 0.6 & 0.1 & 0.3 \\ 0.3 & 0.5 & 0.2 \\ 0.2 & 0.1 & 0.7 \end{bmatrix} \begin{bmatrix} 2.0 & 1.0 \\ -0.5 & 2.0 \\ -1.0 & -0.5 \end{bmatrix} \frac{\textbf{I}}{\text{am}}$$

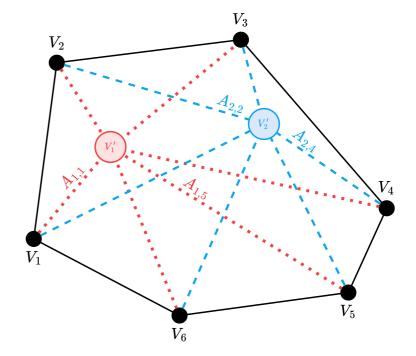
$$=egin{array}{l} 0.6*{rac{{
m I}+0.1*am+0.3*Sam}{0.3*{
m I}+0.5*am+0.2*Sam} \ 0.2*{
m I}+0.1*am+0.7*Sam \end{array}$$



Multi-head Attention

Convex Combination

The elements of V^\prime will lie inside the convex hull of all of the elements in V



Multi-head Attention

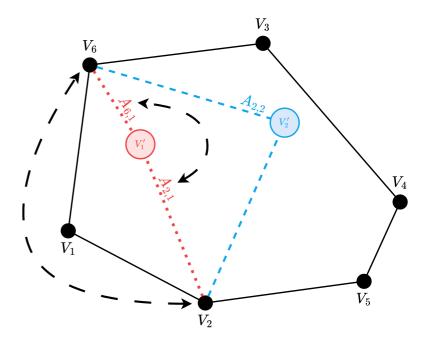
✗ Convex Combination

The elements of V^\prime will lie inside the convex hull of all of the elements in V

Permutation Equivariance

The elements of V' are *equivariant* to a change in the order of the rows of ${\bf A}$

Attention does not care about word order



Multi-head Attention

So is Attention just a linear map?

Not quite

Linear maps are:

Multi-head Attention

So is **Attention** just a linear map?

Not quite

Linear maps are:

Inflexible in terms of sequence length

Multi-head Attention

So is **Attention** just a linear map?

Not quite

Linear maps are:

- Inflexible in terms of sequence length
- Parameter inefficient

Multi-head Attention

So is **Attention** just a linear map?

Not quite

Linear maps are:

- Inflexible in terms of sequence length
- Parameter inefficient
- Invariant to the input content

- Let V be a matrix of value vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D_V
- Let K be a matrix of key vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D_Q
- Let Q be a matrix of query vectors
 - lacksquare It has a sequence length of T_Q
 - lacksquare It has a dimensionality of D_Q

$$ext{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \underbrace{ ext{softmax}\left(f\left(\mathbf{Q}, \mathbf{K}
ight)
ight)}_{\mathbf{A}} \mathbf{V}$$

$$\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$$

$$\mathbf{V} \in \mathbb{R}^{[T_V imes D_V]}$$

$$\mathbf{K} \in \mathbb{R}^{[T_V imes D_Q]}$$

$$\mathbf{Q} \in \mathbb{R}^{[T_Q imes D_Q]}$$

- Let V be a matrix of value vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D_V
- Let K be a matrix of key vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D_Q
- Let Q be a matrix of query vectors
 - lacksquare It has a sequence length of T_Q
 - ullet It has a dimensionality of D_Q
- lacksquare Let $f(\mathbf{Q},\mathbf{K})$ be some kernel function
 - Read: similarity function

$$ext{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \underbrace{ ext{softmax}\left(f\left(\mathbf{Q}, \mathbf{K}
ight)
ight)}_{\mathbf{A}} \mathbf{V}$$

$$\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$$

$$\mathbf{V} \in \mathbb{R}^{[T_V imes D_V]}$$

$$\mathbf{K} \in \mathbb{R}^{[T_V imes D_Q]}$$

$$\mathbf{Q} \in \mathbb{R}^{[T_Q imes D_Q]}$$

- Let V be a matrix of value vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D_V
- Let K be a matrix of key vectors
 - ullet It has a sequence length of T_V
 - ullet It has a dimensionality of D_Q
- Let Q be a matrix of query vectors
 - lacksquare It has a sequence length of T_Q
 - ullet It has a dimensionality of D_Q
- lacksquare Let $f(\mathbf{Q},\mathbf{K})$ be some kernel function
 - Read: similarity function

$$\mathtt{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \underbrace{\mathtt{softmax}\left(f\left(\mathbf{Q}, \mathbf{K}
ight)
ight)}_{\mathbf{A}} \mathbf{V}$$

$$\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$$

$$\mathbf{V} \in \mathbb{R}^{[T_V imes D_V]}$$

$$\mathbf{K} \in \mathbb{R}^{[T_V imes D_Q]}$$

$$\mathbf{Q} \in \mathbb{R}^{[T_Q imes D_Q]}$$

Non-Transformer Examples

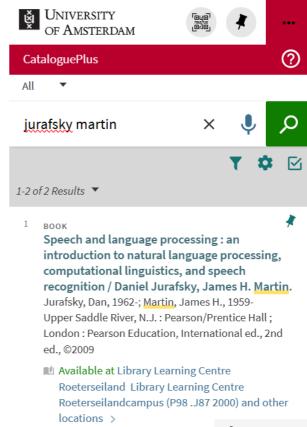
- V contains information
- **K** contains information about information (i.e, metadata)
- $lackbox{ } lackbox{ } lac$
- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}

Multi-head Attention

- V contains information
- **K** contains information about information (i.e, metadata)
- f Q contains metadata about what we want from f V
- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}

E Soft lookup

We want to find a textbook about NLP in the library (\mathbf{V}). We search for titles (\mathbf{K}) with "jurafsky" and "martin" as authors (\mathbf{Q}). The computer returns books with similar titles (f)



- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}
- ullet The output of f must a matrix of size $\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$

Multi-head Attention

- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}
- The output of f must a matrix of size $\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$

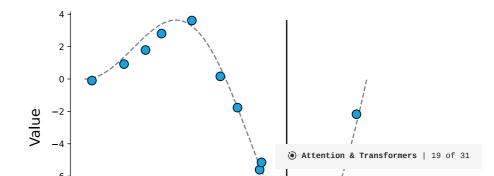
E Nadaraya-Watson Kernel Regression

We have some sequence of values $\mathcal{D} = [(1.36, 1.79), (3.40, -1.77) \dots, (6.05, -2.17)]$

We want to predict a new sample at $x=4.21\,$

We compute the negative Euclidean distance of our new sample with all training samples (f). We normalize the outputs to lie between (0,1)

We compute our predicted value as the mean of the seen values, weighted by the computed similarities



Multi-head Attention

- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}
- The output of f must a matrix of size $\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$

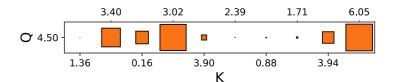
E Nadaraya-Watson Kernel Regression

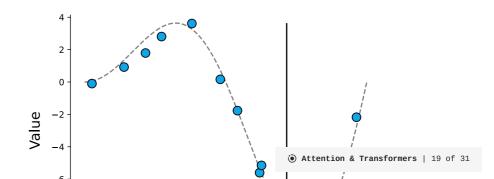
We have some sequence of values $\mathcal{D} = [(1.36, 1.79), (3.40, -1.77) \dots, (6.05, -2.17)]$

We want to predict a new sample at x=4.21

We compute the negative Euclidean distance of our new sample with all training samples (f). We normalize the outputs to lie between (0,1)

We compute our predicted value as the mean of the seen values, weighted by the computed similarities





Multi-head Attention

- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}
- The output of f must a matrix of size $\mathbf{A} \in (0,1)^{[T_Q imes T_V]}$

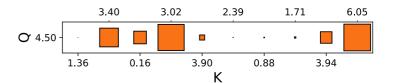
E Nadaraya-Watson Kernel Regression

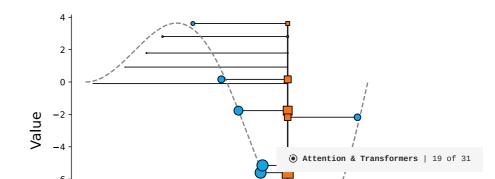
We have some sequence of values $\mathcal{D} = [(1.36, 1.79), (3.40, -1.77) \dots, (6.05, -2.17)]$

We want to predict a new sample at $x=4.21\,$

We compute the negative Euclidean distance of our new sample with all training samples (f). We normalize the outputs to lie between (0,1)

We compute our predicted value as the mean of the seen values, weighted by the computed similarities





Multi-head Attention

- $f(\mathbf{Q}, \mathbf{K})$ is high when \mathbf{Q} is similar to \mathbf{K}
- $oldsymbol{oldsymbol{ iny The output of}}$ The output of f must a matrix of size $oldsymbol{oldsymbol{A}} \in (0,1)^{[T_Q imes T_V]}$

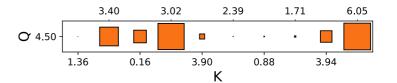
E Nadaraya-Watson Kernel Regression

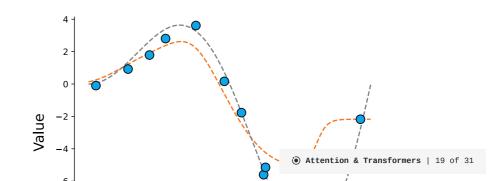
We have some sequence of values $\mathcal{D} = [(1.36, 1.79), (3.40, -1.77) \dots, (6.05, -2.17)]$

We want to predict a new sample at $x=4.21\,$

We compute the negative Euclidean distance of our new sample with all training samples (f). We normalize the outputs to lie between (0,1)

We compute our predicted value as the mean of the seen values, weighted by the computed similarities





Multi-head Attention

Attention & Transformers | 20 of 31

Attention in Transformers

Multi-head Attention

Add & Norm

Residual Connections

Add & Norm

LayerNorm

Add & Norm

These are the equations

```
egin{array}{lll} \mathbf{X}_l &= 	exttt{LayerNorm} \ \mathbf{X}_{l-1} + 	exttt{SubLayer} \left( \mathbf{X}_{l-1} 
ight) \ \end{array}
```

Feed Forward

Embedding

Position Encoding

Tokenization

Training Transformers

The End