

# Assignment 3, Part 1, Specification

SFWR ENG 2AA4

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This Module Interface Specification (MIS) document contains modules, types and methods for implementing the state of a game of Forty Thieves solitaire.

[The parts that you need to fill in are marked by comments, like this one. In several of the modules local functions are specified. You can use these local functions to complete the missing specifications. —SS]

[As you edit the tex source, please leave the `wss` comments in the file. Put your answer **before** the comment. This will make grading easier. —SS]

# Card Types Module

## Module

CardTypes

## Uses

N/A

## Syntax

### Exported Constants

TOTAL\_CARDS = 104

ACE = 1

JACK = 11

QUEEN = 12

KING = 13

### Exported Types

SuitT = {Heart, Diamond, Club, Spade}

RankT = [1..13]

CategoryT = {Tableau, Foundation, Deck, Waste}

CardT = tuple of (s: SuitT, r: RankT)

### Exported Access Programs

None

## Semantics

### State Variables

None

### State Invariant

None

# Generic Stack Module

## Generic Template Module

Stack(T)

### Uses

N/A

### Syntax

#### Exported Types

Stack(T) = ? [\[What should be written here? —SS\]](#)

#### Exported Constants

None

#### Exported Access Programs

| Routine name | In       | Out      | Exceptions   |
|--------------|----------|----------|--------------|
| new Stack    | seq of T | Stack    | none         |
| push         | T        | Stack    | none         |
| pop          |          | Stack    | out_of_range |
| top          |          | T        | out_of_range |
| size         |          | N        |              |
| toSeq        |          | seq of T |              |

### Semantics

#### State Variables

$S$ : sequence of T [\[What is the type of the state variable? —SS\]](#)

#### State Invariant

None

## Assumptions & Design Decisions

- The `Stack(T)` constructor is called for each object instance before any other access routine is called for that object. The constructor can only be called once.
- Though the `toSeq()` method violates the essential property of the stack object, since this could be achieved by calling `top` and `pop` many times, this method is provided as a convenience to the client. In fact, it increases the property of separation of concerns since this means that the client does not have to worry about details of building their own sequence from the sequence of pops.

## Access Routine Semantics

`new Stack(s)`:

- transition:  $S := s$
- output:  $out := self$
- exception: none

`push(e)`:

- output:  $out := new\ Stack(S \parallel \langle e \rangle)$
- exception: none

`pop()`:

- output:  $S := S - S[|S| - 1]$  [What should go here? —SS]
- exception:  $(|S| = 0 \Rightarrow out\_of\_range)$  [What should go here? —SS]

`top()`:

- output:  $out := S[|S| - 1]$
- exception:  $(|S| = 0 \Rightarrow out\_of\_range)$  [What should go here? —SS]

`size()`:

- output:  $out := |S|$  [What should go here? —SS]
- exception: None

`toSeq()`:

- output:  $out := S$
- exception: None

## CardStack Module

### Template Module

CardStackT is Stack(cardT)[\[What should go here? —SS\]](#)

# Game Board ADT Module

## Template Module

BoardT

## Uses

CardTypes

CardStack

## Syntax

### Exported Access Programs

| Routine name      | In                                     | Out          | Exceptions                     |
|-------------------|--|--------------|--------------------------------|
| new BoardT        | seq of CardT                           | BoardT       | invalid_argument               |
| is_valid_tab_mv   | CategoryT, $\mathbb{N}$ , $\mathbb{N}$ | $\mathbb{B}$ | out_of_range                   |
| is_valid_waste_mv | CategoryT, $\mathbb{N}$                | $\mathbb{B}$ | invalid_argument, out_of_range |
| is_valid_deck_mv  |  | $\mathbb{B}$ |                                |
| tab_mv            | CategoryT, $\mathbb{N}$ , $\mathbb{N}$ |              | invalid_argument               |
| waste_mv          | CategoryT, $\mathbb{N}$                |              | invalid_argument               |
| deck_mv           |  |              | invalid_argument               |
| get_tab           | $\mathbb{N}$                           | CardStackT   | out_of_range                   |
| get_foundation    | $\mathbb{N}$                           | CardStackT   | out_of_range                   |
| get_deck          |  | CardStackT   |                                |
| get_waste         |  | CardStackT   |                                |
| valid_mv_exists   |  | $\mathbb{B}$ |                                |
| is_win_state      |  | $\mathbb{B}$ |                                |

## Semantics

### State Variables

$T$ : SeqCrdStckT # *Tableau*

$F$ : SeqCrdStckT # *Foundation*

$D$ : CardStackT # *Deck*

$W$ : CardStackT # *Waste*

## State Invariant

$|T| = 10$ [What goes here? — — — *SS*]

$|F| = 8$ [What goes here? — — — *SS*]

$\text{cnt\_cards}(T, F, D, W, \lambda t \rightarrow \text{True} \text{ [What goes here? —SS]}) = \text{TOTAL\_CARDS}$

$\text{two\_decks}(T, F, D, W) \# \text{ each card appears twice in the combined deck}$

## Assumptions & Design Decisions

- The BoardT constructor is called before any other access routine is called on that instance. Once a BoardT has been created, the constructor will not be called on it again.
- The Foundation stacks must start with an ace, but any Foundation stack can start with any suit. Once an Ace of that suit is placed there, this Foundation stack becomes that type of stack and only those type of cards can be placed there.
- Once a card has been moved to a Foundation stack, it cannot be moved again.
- For better scalability, this module is specified as an Abstract Data Type (ADT) instead of an Abstract Object. This would allow multiple games to be created and tracked at once by a client.
- The getter function is provided, though violating the property of being essential, to give a would-be view function easy access to the state of the game. This ensures that the model is able to be easily integrated with a game system in the future. Although outside of the scope of this assignment, the view function could be part of a Model View Controller design pattern implementation (<https://blog.codinghorror.com/understanding-model-view-controller/>)
- A function will be available to create a double deck of cards that consists of a random permutation of two regular decks of cards (TOTAL\_CARDS cards total). This double deck of cards can be used to build the game board.

## Access Routine Semantics

GameBoard(*deck*):

- transition:

$T, F, D, W := \text{tab\_deck}(\text{deck}[0..39]), \text{init\_seq}(8), \text{CardStackT}(\text{deck}[40..103]), \text{CardStackT}(\langle \rangle)$

- exception:  $\text{exc} := (\neg \text{two\_decks}(\text{init\_seq}(10), \text{init\_seq}(8), \text{CardStackT}(\text{deck}), \text{CardStackT}(\langle \rangle))) \Rightarrow \text{invalid\_argument}$

is\_valid\_tab\_mv( $c, n_0, n_1$ ):

- output:

|                         | $out :=$                           |
|-------------------------|------------------------------------|
| $c = \text{Tableau}$    | valid_tab_tab( $n_0, n_1$ )        |
| $c = \text{Foundation}$ | valid_tab_foundation( $n_0, n_1$ ) |
| $c = \text{Deck}$       | False [What goes here? —SS]        |
| $c = \text{Waste}$      | False [What goes here? —SS]        |

- exception:

|  | $exc :=$     |
|--|--------------|
| $c = \text{Tableau} \wedge \neg(\text{is\_valid\_pos}(\text{Tableau}, n_0) \wedge \text{is\_valid\_pos}(\text{Tableau}, n_1))$       | out_of_range |
| $c = \text{Foundation} \wedge \neg(\text{is\_valid\_pos}(\text{Tableau}, n_0) \wedge \text{is\_valid\_pos}(\text{Foundation}, n_1))$ | out_of_range |

is\_valid\_waste\_mv( $c, n$ ):

- output:

|                         | $out :=$                      |
|-------------------------|-------------------------------|
| $c = \text{Tableau}$    | valid_waste_tab( $n$ )        |
| $c = \text{Foundation}$ | valid_waste_foundation( $n$ ) |
| $c = \text{Deck}$       | False [What goes here? —SS]   |
| $c = \text{Waste}$      | False [What goes here? —SS]   |

- exception:

|   | $exc :=$         |
|---|------------------|
| $W.\text{size}() = 0$   | invalid_argument |
| $c = \text{Tableau} \wedge \neg \text{is\_valid\_pos}(\text{Tableau}, n)$       | out_of_range     |
| $c = \text{Foundation} \wedge \neg \text{is\_valid\_pos}(\text{Foundation}, n)$ | out_of_range     |

is\_valid\_deck\_mv():

- output:

|                         | $out :=$  |
|-------------------------|-----------|
| $c = \text{Tableau}$    | False     |
| $c = \text{Foundation}$ | False     |
| $c = \text{Deck}$       | False     |
| $c = \text{Waste}$      | $ D  > 0$ |

[What goes here? The deck moves involves moving a card from the deck stack to the waste stack. —SS]



- exception: None

tab\_mv( $c, n_0, n_1$ ):

- transition:

|                         |  |
|-------------------------|--|
| $c = \text{Tableau}$    | $T[n_0], T[n_1] := T[n_0].\text{pop}(), T[n_1].\text{push}(T[n_0].\text{top}())$ [What goes here? —SS] |
| $c = \text{Foundation}$ | $T[n_0], F[n_1] := T[n_0].\text{pop}(), F[n_1].\text{push}(T[n_0].\text{top}())$ [What goes here? —SS] |

- exception:  $exc := (\neg \text{is\_valid\_tab\_mv}(c, n_0, n_1) \Rightarrow \text{invalid\_argument})$

waste\_mv( $c, n$ ):

- transition:

|                         |   |
|-------------------------|---|
| $c = \text{Tableau}$    | $W, T[n] := W.\text{pop}(), T[n].\text{push}(W.\text{top}())$ [What goes here? —SS] |
| $c = \text{Foundation}$ | $W, F[n] := W.\text{pop}(), F[n].\text{push}(W.\text{top}())$ [What goes here? —SS] |

- exception:  $exc := (\neg \text{is\_valid\_waste\_mv}(c, n) \Rightarrow \text{invalid\_argument})$

deck\_mv():

- transition:  $D, W := D.\text{pop}(), W.\text{push}(D.\text{top}())$  [What goes here? —SS]
- exception:  $exc := (\neg \text{is\_valid\_deck\_mv}() \Rightarrow \text{invalid\_argument})$

get\_tab( $i$ ):

- output:  $out := T[i]$
- exception:  $exc : (\neg \text{is\_valid\_pos}(\text{Tableau}, i) \Rightarrow \text{out\_of\_range})$

get\_foundation( $i$ ):

- output:  $out := F[i]$
- exception:  $exc : (\neg \text{is\_valid\_pos}(\text{Foundation}, i) \Rightarrow \text{out\_of\_range})$

get\_deck():

- output:  $out := D$
- exception: None

get\_waste():

- output:  $out := W$

- exception: None

valid\_mv\_exists():

- output:  $out := \text{valid\_tab\_mv} \vee \text{valid\_waste\_mv} \vee \text{is\_valid\_deck\_mv}()$  where

$\text{valid\_tab\_mv} \equiv (\exists c : \text{CategoryT}, n_0 : \mathbb{N}, n_1 : \mathbb{N} | \text{is\_valid\_pos}(\text{Tableau}, n, 0) \wedge \text{is\_valid\_pos}(c, n, 1) \text{ [What goes here? — — — SS]} : \text{is\_valid\_tab\_mv}(c, n_0, n_1))$

$\text{valid\_waste\_mv} \equiv (\exists c : \text{CategoryT}, n : \mathbb{N} | \text{is\_valid\_pos}(c, n) \text{ [What goes here? — — — SS]} : \text{is\_valid\_waste\_mv}(c, n))$

- exception: None

is\_win\_state():

- output:  $\text{cnt\_cards\_seq}(F, \lambda t \rightarrow \text{True}) = \text{TOTAL\_CARDS}$  [What goes here? —SS]
- exception: None

## Local Types

$\text{SeqCrdStckT} = \text{seq of CardStackT}$

## Local Functions

$\text{two\_decks} : \text{SeqCrdStckT} \times \text{SeqCrdStckT} \times \text{CardStackT} \times \text{CardStackT} \rightarrow \mathbb{B}$

$\text{two\_decks}(T, F, D, W) \equiv \text{[This function returns True if there is two of each card in the game —SS]}$

$(\forall st : \text{SuitT}, rk : \text{RankT} | st \in \text{SuitT} \wedge rk \in \text{RankT} : (\exists a, b : \text{CardT} | a, b \in (T[0..9].\text{toSeq()} || F[0..7].\text{toSeq()} || D.\text{toSeq()} || W.\text{toSeq}()) : a.st = b.st \wedge a.rk = b.rk) \text{ [What goes here? — — — SS]})$

$\text{cnt\_cards\_seq} : \text{SeqCrdStckT} \times (\text{CardT} \rightarrow \mathbb{B}) \rightarrow \mathbb{N}$

$\text{cnt\_cards\_seq}(S, f) \equiv (+s : \text{CardStackT} | s \in S : \text{cnt\_cards\_stack}(s, f))$

$\text{cnt\_cards\_stack} : \text{CardStackT} \times (\text{CardT} \rightarrow \mathbb{B}) \rightarrow \mathbb{N}$

$\text{cnt\_cards\_stack}(S, f) \equiv (+s : \text{CardT} | s \in S.\text{toSeq()} \wedge f(s) : 1)$

[What goes here? —SS]

$\text{cnt\_cards} : \text{SeqCrdsStckT} \times \text{SeqCrdsStckT} \times \text{CardStackT} \times \text{CardStackT} \times (\text{CardT} \rightarrow \mathbb{B}) \rightarrow \mathbb{N}$   
 $\text{cnt\_cards}(T, F, D, W, f) \equiv \text{cnt\_cards\_seq}(T, f) + \text{cnt\_cards\_seq}(F, f) + \text{cnt\_cards\_stack}(D, f) + \text{cnt\_cards\_stack}(W, f)$

$\text{init\_seq} : \mathbb{N} \rightarrow \text{SeqCrdsStckT}$   
 $\text{init\_seq}(n) \equiv s \text{ such that } (|s| = n \wedge (\forall i \in [0..n-1] : s[i] = \text{CardStackT}(\langle \rangle)))$

$\text{tab\_deck} : (\text{seq of CardT}) \rightarrow \text{SeqCrdsStckT}$   
 $\text{tab\_deck}(\text{deck}) \equiv T \text{ such that } (\forall i : \mathbb{N} | i \in [0..9] : T[i].\text{toSeq}() = \text{deck}[i * 4 \dots 4 * (i + 1) - 1 \text{ [What goes here? — — SS]})$

$\text{is\_valid\_pos} : \text{CategoryT} \times \mathbb{N} \rightarrow \mathbb{B}$   
 $\text{is\_valid\_pos}(c, n) \equiv (c = \text{Tableau} \Rightarrow n \in [0..9] | c = \text{Foundation} \Rightarrow n \in [0..7] | \text{True} \Rightarrow \text{True})$

$\text{valid\_tab\_tab} : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{B}$   
 $\text{valid\_tab\_tab}(n_0, n_1) \equiv$

|                            |                            |  |
|----------------------------|----------------------------|--|
| $T[n_0].\text{size}() > 0$ | $T[n_1].\text{size}() > 0$ | $T[n_0].\text{top}().s = T[n_1].\text{top}().s \wedge T[n_0].\text{top}().r = T[n_1].\text{top}().r - 1 \text{ [What goes here? —SS]}$ |
|                            | $T[n_1].\text{size}() = 0$ | True[What goes here? —SS]  |
| $T[n_0].\text{size}() = 0$ | $T[n_1].\text{size}() > 0$ | False[What goes here? —SS]   |
|                            | $T[n_1].\text{size}() = 0$ | False[What goes here? —SS]   |

$\text{valid\_tab\_foundation} : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{B}$   
 $\text{valid\_tab\_foundation}(n_0, n_1) \equiv$

|                            |                            |  |
|----------------------------|----------------------------|--|
| $T[n_0].\text{size}() > 0$ | $F[n_1].\text{size}() > 0$ | $T[n_0].\text{top}().s = T[n_1].\text{top}().s \wedge T[n_0].\text{top}().r = T[n_1].\text{top}().r - 1$ |
|                            | $F[n_1].\text{size}() = 0$ | $T[n_0].\text{top}().r = \text{ACE}$   |
| $T[n_0].\text{size}() = 0$ | $F[n_1].\text{size}() > 0$ | False  |
|                            | $F[n_1].\text{size}() = 0$ | False  |

[What goes here? You may need a table? —SS]

$\text{valid\_waste\_tab} : \mathbb{N} \rightarrow \mathbb{B}$   
 $\text{valid\_waste\_tab}(n) \equiv$

|                          |  |
|--------------------------|--|
| $T[n].\text{size}() > 0$ | $\text{tab\_placeable}(W.\text{top}(), T[n].\text{top}())$ |
| $T[n].\text{size}() = 0$ | True   |

valid\_waste\_foundation:  $\mathbb{N} \rightarrow \mathbb{B}$

valid\_waste\_foundation ( $n$ )  $\equiv$

|                   |   |
|-------------------|---|
| $F[n].size() > 0$ | $\text{foundation\_placeable}(W.\text{top}(), F[n].\text{top}())$ |
| $F[n].size() = 0$ | $W.\text{top}().r = \text{ACE}$                                   |

tab\_placeable:  $\text{CardT} \times \text{CardT} \rightarrow \mathbb{B}$

$\text{tab\_placeable}(a, b) \equiv a.s = b.s \wedge a.r = b.r - 1 \Rightarrow \text{True}$

[\[Complete this specification —SS\]](#)

foundation\_placeable:  $\text{CardT} \times \text{CardT} \rightarrow \mathbb{B}$

$\text{foundation\_placeable}(a, b) \equiv a.s = b.s \wedge a.r = b.r - 1 \Rightarrow \text{True}$

[\[Complete this specification —SS\]](#)

## Critique of Design

The interface for the modules has rigour and formality. It uses language from discrete math, which has predefined symbols formal syntax, and precise semantics, removing all ambiguity. As well, arguments are checked to see if they are valid, and if not, an exception is called. Modules exercise a proper amount of separation of concerns, with high cohesion and low coupling. All modules are components of a game, so they are closely related. However, modules only call upon each other when necessary. For example, the StackT object does not call upon any other modules, but only provides the necessary functions for itself. The StackT module exhibits generality, as the T value can be of any type. As a result, StackT can be used to represent stacks of other types. Each function only performs one task, so it is clear how each function could be, or will be used. For example, there is a function “is\_valid\_tab\_mv,” which checks to make sure the cardT values are correct, and then a “is\_valid\_pos” function which checks to make sure the arguments are valid, and then a “tab\_mv” function which actually moves the values.

A possible improvement would be making the “valid\_tab\_tab” and other valid functions more general, so that the functions could be reused for other types of solitaire. Another related improvement would be the sizes for the tableau and foundation could be a exported constant, so that the number of tableaus and foundation could be changed. Possible considerations would be limiting the size, or setting a constant for a maximum size of the stack of tableaus, as when the game is actually implemented, the tableau will show an image of the cards, and the number of cards in a tableau stack shouldn't be able to extend out of the game window. This will also limit ways the user could use the applications, and prevent possible bugs or errors

[Write a critique of the interface for the modules in this project. Is there anything missing? Is there anything you would consider changing? Why? —SS]