Assignment 2

Read all instructions carefully

Work Requirements

- You must work on Assignment 2 alone. You may not work with partners.
- You may use online resources (Stack Exchange, Googling, Regex cheat sheets), including documentation and everything on Canvas. However, you may not use an LLM (ChatGPT, Copilot, etc)
- Lightly document your code, especially any decisions you make along the way. You do not need extensive documentation. You do **NOT** need a separate README file. But a person should be able to read your submission top to bottom and understand what you're doing.

Submission Instructions

- This assignment is due on Monday, October 6 at 6:59pm.
- The assignment must be submitted on Canvas as a single PDF file together with a requirements.txt file (as a text file, not PDF). The two files must be submitted as separate files, not as a zip file.
- The PDF file you submit must be named with the following format "lastname_firstname_assignment2.pdf"
- The requirements.txt file should only include the libraries you need to run your code in a Jupyter notebook, with their versions properly specified (e.g., use pip freeze with your venv activated)

Recommendations and Resources

Recommendation: Complete the assignment in a Jupyter notebook, and then convert the notebook to a PDF. If you have too much trouble converting to PDF, then convert it to HTML, open it as HTML and export that page to PDF (but this is a less preferred option).

Recommendation: As always, start by examining the data you read in and understand it. What does each row represent in each dataframe?

Helpful Documentation:

- Pandas expanding: https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.expanding.html#pandas.DataFrame.expanding
- Python re library for Regex: https://docs.python.org/3/library/re.html
- Pareto:
 https://numpy.org/doc/stable/reference/random/generated/numpy.random.pareto.html
 #numpy.random.pareto

- Gaussian: https://numpy.org/doc/stable/reference/random/generated/numpy.random.normal.htm l#numpy-random-normal
- Seaborn Boxplot: https://seaborn.pydata.org/generated/seaborn.boxplot.html
- Seaborn Scatterplot: https://seaborn.pydata.org/generated/seaborn.scatterplot.html
- Matplotlib scatterplot: https://matplotlib.org/stable/api/_as_gen/matplotlib.pyplot.scatter.html
- Matplotlib boxplot: https://matplotlib.org/stable/api/_as_gen/matplotlib.pyplot.boxplot.html#

Part 0 - Imports and CoW

```
# Import libraries
from pathlib import Path
import numpy as np
import pandas as pd
import seaborn as sns
import re
from datetime import datetime
from matplotlib import pyplot as plt
# Enforce Copy-on-Write
pd.options.mode.copy_on_write = True
```

Part 1 - Regex, EDA, and Visualization

Load the Food Safety datasets (bus.csv, ins2vio.csv, ins.csv, and vio.csv) into pandas dataframes and answer the following questions based on the dataframes.

```
#Load the datasets into Pandas DataFrames
def load_dataset_to_df(file, na_values = None):
    cwd = Path.cwd()
    assignment2 = cwd.parent
    data = assignment2.joinpath('data')
    path = data.joinpath(file)
    if path.exists():
        print(f'Found the data file {path}')
    else:
        raise Exception('Could not find that file', path)
    return pd.read_csv(path, na_values = na_values)

bus_df = load_dataset_to_df('bus.csv', na_values = [-9999])
ins_df = load_dataset_to_df('ins.csv')
isn2vio_df = load_dataset_to_df('ins2vio.csv')
vio_df = load_dataset_to_df('vio.csv')
```

Found the data file /Users/Isaia/PycharmProjects/CS-577-07-Data-Science-Fall-2025/Assignments/Assignment2/data/bus.csv
Found the data file /Users/Isaia/PycharmProjects/CS-577-07-Data-Science-Fall-2025/Assignments/Assignment2/data/ins.csv
Found the data file /Users/Isaia/PycharmProjects/CS-577-07-Data-Science-Fall-2025/Assignments/Assignment2/data/ins2vio.csv
Found the data file /Users/Isaia/PycharmProjects/CS-577-07-Data-Science-Fall-2025/Assignments/Assignment2/data/vio.csv

Use the business dataset (bus) to answer the first few questions below

1.1) Examining the entries in bus, is the bid unique for each record (i.e. each row of data)?

Hint: use value_counts() or unique() to determine if the bid series has any duplicates.

column			name	
1000	HEUNG '	YUEN RESTAU	RANT	3279
100010	ILLY C	AFFE SF_PIE	R 39	PIER 39 K-
100017	AMICI'S EAST	COAST PIZZ	ERIA	475
100026				1566 CARROLL
	_			
100030	01	JI OUI! MAC	ARON 2200 I	JERROLD AVE
y state	postal_code	latitude	longitude	
o CA	94110	37.755282	-122.420493	
o CA	94133	NaN	NaN	
o CA	94103	NaN	NaN	
o CA	94124	NaN	NaN	
o CA	94124	NaN	NaN	
	1000 100017 100026 100030 y state CA CA CA CA	1000 HEUNG N 100010 ILLY CA 1000017 AMICI'S EAST 1000026 1000030 OU y state postal_code co CA 94110 co CA 94133 co CA 94103 co CA 94124	1000 HEUNG YUEN RESTAU 100010 ILLY CAFFE SF_PIE 100017 AMICI'S EAST COAST PIZZ 100026 LOCAL CATE 100030 OUI OUI! MAC y state postal_code latitude c CA 94110 37.755282 c CA 94133 NaN c CA 94103 NaN c CA 94124 NaN	1000 HEUNG YUEN RESTAURANT 100010 ILLY CAFFE SF_PIER 39 100017 AMICI'S EAST COAST PIZZERIA 100026 LOCAL CATERING 100030 OUI OUI! MACARON 2200 3 y state postal_code latitude longitude to CA 94110 37.755282 -122.420493 to CA 94133 NaN NaN to CA 94103 NaN NaN to CA 94124 NaN NaN

Im not sure what is bid is as there's no column named that, but business id column seems like thats what bid may be so im going to use that. Im curious what -9999 and -9999.0 means, but since there no documentation I have decided to interpret it as a NaN

```
ID = "business id column"
NAME = "name"
```

```
ADDRESS = "address"
POSTAL_CODE = "postal_code"
bid_has_duplicates = bus_df[ID].nunique() < bus_df.shape[0]
if bid_has_duplicates:
    print(f'{ID} has a duplicate ID')
else:
    print(f'{ID} has no duplicate ID')
business id column has no duplicate ID</pre>
```

1.2) In the two cells below create the following **two numpy arrays**:

- 1. Assign top_names to the top 5 most frequently used business names, from most frequent to least frequent.
- 2. Assign top_addresses to the top 5 addressses where businesses are located, from most popular to least popular.

Hint: you may find value counts () helpful.

```
top names df =
bus df[NAME].value counts().sort values(ascending=False).head(5).reset
index()
top names df
                  name count
  Peet's Coffee & Tea
                           20
      Starbucks Coffee
                           13
1
2
           McDonald's
                           10
3
           Jamba Juice
                           10
                         9
             STARBUCKS
top_names = top_names_df[NAME].to numpy()
top names
array(["Peet's Coffee & Tea", 'Starbucks Coffee', "McDonald's",
       'Jamba Juice', 'STARBUCKS'], dtype=object)
top addresses df =
bus df[ADDRESS].value counts().sort values(ascending=False).head(5).re
set index()
top addresses df
          address count
     Off The Grid
0
                      39
1
      428 11th St
                      34
  2948 Folsom St
2
                      17
3
    3251 20th Ave
                      17
4
          Pier 41
                      16
```

1.3) Look at the businesses that DO NOT have the special MISSING ZIP code value. Some of the invalid postal codes are just the full 9 digit code rather than the first 5 digits. Create a new column named postal5 in the original bus dataframe which contains only the first 5 digits of the postal_code column. Finally, for any of the likely MISSING postal5 ZIP code entries set the entry to None.

```
bus df[POSTAL CODE].unique()
array(['94110', '94133', '94103', '94124', '94123', '94118', '94121',
        '94134', '94114', '94109', '94102', '94132', '94116', nan,
'94107'
        ,
'94105', '94108', '94117', '94158', '94112', '94127', '94105-
1420',
        '94111', '94122', '94115', '94104', '94122-1909', '94131',
        '94117-3504', '94518', '95105', '94013', '94130', '941102019',
        '941', '941033148', 'CA', '92672', '94120', '94143', '94101',
        '94014', '94129', '94602', 'Ca', '94080', '00000', '94188', '64110', '94544', '94301', '94901', '95117', '95133', '95109', '95132', '95122', '94621', '94124-1917', '94102-5917',
        '94105-2907', '95112', '94123-3106'], dtype=object)
print(bus df[POSTAL CODE].value counts().sort values(ascending=True).t
o string())
postal code
94123-3106
                   1
94122 - 1909
                   1
94544
                   1
94901
                   1
95117
                   1
                   1
95133
                   1
95132
95109
                   1
                   1
95122
94621
                   1
94124-1917
                   1
                   1
94102-5917
                   1
94105-2907
                   1
95112
                   1
64110
                   1
00000
94117-3504
                   1
                   1
Ca
```

94602	1
94129	1
94014	1
94120	1
92672	1
941033148	1
941	$\bar{\bar{1}}$
941102019	1
94105 - 1420	1
95105	1
94080	1
94518	1
94188	2
CA	2
94013	2
94301	2
94101	2
	2
94143	5
94130	8
94131	49
94127	67
94134	82
94158	90
94116	97
94132	132
94104	142
94121	157
94123	177
94117	189
94112	192
94114	200
94124	218
94108	229
94115	230
94118	231
94105	249
94122	255
94111	259
94109	382
94133	398
94107	408
94102	456
94110	555
94103	562

The postal codes look suspicious:

- 1. NaN (-9999)
- 2. 94518

- 3. 95105
- 4. 94013
- 5. 941
- 6. CA
- 7. 92672
- 8. 94101
- 9. 94014
- 10. 94602
- 11. Ca
- 12. 00000
- 13. 94188
- 14. 64110
- 15. 94544
- 16. 94301
- 17. 94901
- 18. 95117
- 19. 95133
- 20. 95109
- 21. 95132
- 22. 95122
- 23. 94621
- 24. 95112

According to USPS, postal codes in San Francisco, CA and South Francisco, CA are:

- 1. 94080
- 2. 94083
- 3. 94102 94112
- 4. 94114- 94134
- 5. 94137
- 6. 94139 94147
- 7. 94151
- 8. 94158 94161
- 9. 94163 94164
- 10. 94172
- 11. 94177

The pairs with a dash 'zipcode 1 - zipcode 2' are interpolated for example 0-9 is 0,2,3,4,5,6,7,8,0 and one can use USPS tool below to verify these zip codes

https://tools.usps.com/zip-code-lookup.htm?bycitystate

and the 9 digit numbers seem to be "valid" as defined below

- 1. 94122-1909 -> 94122
- 2. 94124-1917 -> 94124

- 3. 94102-5917 -> 94102
- 4. 94105-1420 -> 94105
- 5. 94117-3504 -> 94117
- 6. 941033148 -> 94103
- 7. 941102019 -> 94110
- 8. 94105-2907 -> 94105
- 9. 94123-3106 -> 94123

From looking at bus_df from bus.csv, all rows say that the city is in San Francisco, however there some entries that have incorrect/invalid zip codes for San Francisco or South San Francisco, zip codes must be included in bullet points 1-11.

if the zip code is not numerical or doesnt contain at least 5 numbers or the first 5 digits are invalid San Francisco or South San Francisco (excluded in bullet points 1-11), then I will store None for postal5

if the zip code is numerical and contains at least 5 numbers and the first 5 digits San Francisco or South San Francisco is valid (included in bullet points 1-11), then I will keep the zip code for postal5

```
def is valid(postal code, pattern):
    if(len(str(postal code)) >= 5) and re.fullmatch(pattern,
postal code[:5]):
        return postal code[:5]
    else:
        return None
sf_postal_code_pattern = r'941(0[2-9]|1[^3]|2[0-9]|3[^5,6,8]|4[0-7]|
5[1,8,9]|6[0,1,3]|7[2,7])|940(8[0,3])
POSTAL5 = 'postal5'
bus df[POSTAL5] = bus df[POSTAL CODE].map(lambda x: is_valid(x,
sf postal code pattern))
bus df.head(5)
   business id column
                                               name
address \
                             HEUNG YUEN RESTAURANT
                 1000
                                                               3279
22nd St
               100010
                             ILLY CAFFE SF PIER 39
                                                           PIER 39 K-
106-B
               100017 AMICI'S EAST COAST PIZZERIA
                                                                475
06th St
               100026
                                    LOCAL CATERING
                                                           1566 CARROLL
AVE
                                  OUI OUI! MACARON 2200 JERROLD AVE
               100030
STE C
            city state postal code latitude
                                                 longitude
phone number \
```

0 San Francisco	CA	94110	37.755282 -	122 420493
NaN	Crt	31110	37.733202	1221 120 133
1 San Francisco	CA	94133	NaN	NaN
1.415483e+10				
2 San Francisco	CA	94103	NaN	NaN
1.415528e+10	CA	04124	NeN	NaN
3 San Francisco 1.415586e+10	CA	94124	NaN	NaN
4 San Francisco	CA	94124	NaN	NaN
1.415970e+10	CA	94124	Ivaiv	IVAIN
11 12337 00 1 10				
postal5				
0 94110				
1 94133				
2 94103				
3 94124				
4 94124				

Here we can we see that all of our values were mapped correctly based on the is_valid method

```
print(bus_df[POSTAL5].value_counts(dropna=False).sort_values(ascending
=True).to_string())
postal5
94080
           1
94120
           1
94129
           1
           5
94143
94130
           8
94131
          49
94127
          67
94134
          82
          90
94158
94116
          97
94132
         132
94104
         142
94121
         157
94123
         178
94117
         190
94112
         192
94114
         200
94124
         219
None
         222
94108
         229
94115
         230
94118
         231
94105
         251
94122
         256
94111
         259
```

```
94109 382
94133 398
94107 408
94102 457
94110 556
94103 563
```

Now using the four Food Safety datasets bus.csv, ins2vio.csv, ins.csv, and vio.csv:

1.5) Create a side-by-side boxplot that shows the distribution of the restaurant scores for each different risk category from 2017 to 2019. Use a figure size of at least 12 by 8.

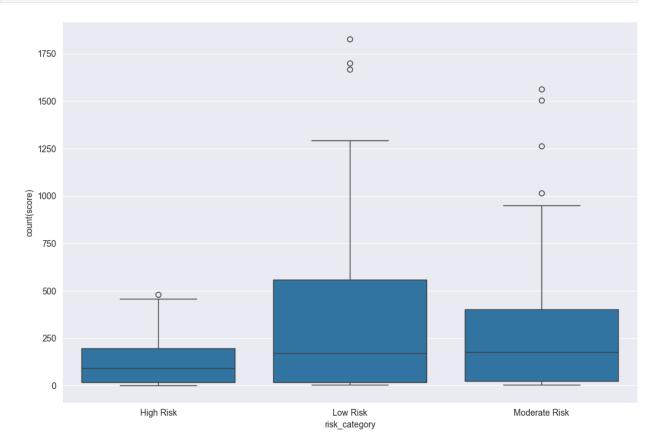
Hint: Consider using appropriate JOIN operations.

```
IID ='iid'
VID ='vid'
INNER = 'inner'
food safety df = ins df.merge(isn2vio df, on=IID,
how=INNER).merge(vio_df, on=VID, how=INNER)
food safety df[ID] =
food_safety_df[IID].str.split('_').str[0].astype('int64')
food safety df = food safety df.merge(bus df, on=ID, how=INNER)
food safety df.head()
               iid
                                      date score
type \
0 100017 20190816 08/16/2019 12:00:00 AM
                                               91
                                                   Routine -
Unscheduled
   100017 20190816
                    08/16/2019 12:00:00 AM
                                               91
                                                   Routine -
Unscheduled
                                                            New
2 100030 20190612 06/12/2019 12:00:00 AM
                                               - 1
Ownership
  100030 20190612 06/12/2019 12:00:00 AM
                                                - 1
                                                            New
0wnership
  100030 20190826
                    08/26/2019 12:00:00 AM
                                               - 1
                                                            New
Ownership
                                                 description
      vid
risk category \
0 103105
                                    Improper cooling methods
                                                                  High
Risk
1 103139
                                       Improper food storage
                                                                   Low
Risk
2 103142
                            Unclean nonfood contact surfaces
                                                                   Low
Risk
3 103154
                Unclean or degraded floors walls or ceilings
                                                                   Low
Risk
4 103149
          Wiping cloths not clean or properly stored or ...
                                                                   Low
Risk
```

```
business id column
                                               name
address \
               100017 AMICI'S EAST COAST PIZZERIA
                                                                475
06th St
               100017 AMICI'S EAST COAST PIZZERIA
                                                                475
06th St
                                  OUI OUI! MACARON 2200 JERROLD AVE
               100030
STE C
                                  OUI OUI! MACARON 2200 JERROLD AVE
               100030
STE C
                                  OUI OUI! MACARON 2200 JERROLD AVE
               100030
STE C
            city state postal code latitude longitude phone number
postal5
0 San Francisco
                    CA
                             94103
                                         NaN
                                                     NaN 1.415528e+10
94103
1 San Francisco
                    CA
                             94103
                                         NaN
                                                     NaN 1.415528e+10
94103
2 San Francisco
                                         NaN
                                                     NaN 1.415970e+10
                    CA
                             94124
94124
3 San Francisco
                    CA
                             94124
                                         NaN
                                                     NaN 1.415970e+10
94124
4 San Francisco
                    CA
                                         NaN
                                                     NaN 1.415970e+10
                             94124
94124
DATETIME = 'datetime'
DATE = 'date'
RISK_CATEGORY = 'risk_category'
SCORE = 'score'
food_safety_df[DATETIME] = pd.to_datetime(food safety df[DATE],
format='%m/%d/%Y %I:%M:%S %p')
COUNT SCORE = f'count({SCORE})'
scores df = food safety df[
    (datetime(year=2017, month=1, day=1) <= food_safety_df[DATETIME])</pre>
&
    (food safety df[DATETIME] <= datetime(year=2019, month=12,</pre>
day=31)
].groupby([RISK CATEGORY, SCORE])[SCORE].count().reset index(name=
COUNT SCORE)
scores df.head()
  risk category score count(score)
0
      High Risk
                    - 1
                                 457
1
      High Risk
                    45
                                   5
                                   4
2
      High Risk
                    46
```

```
3  High Risk 48      2
4  High Risk 51      3

plt.figure(figsize=(12, 8))
plot = sns.boxplot(data=scores_df, x=RISK_CATEGORY, y=COUNT_SCORE)
```



All risk categories look skewed top. High risk has the smallest median and IQR. low risk and moderate risk have a roughly similar median, but low risk has a larger iqr range compared to moderate risk. low risk has the outlier whisker wider than all risks, followed by moderate and high. They all have outliers, but moderate has most then low risk then high risk. but these are in respect to their outlier band.

Part II - Making a Synthetic Dataset

In this part you're going to be create a synthetic dataset (dataframe) with 1000 observations (rows). You are going to use random number generators to create the data for you.

You can use either the numpy or scipy library, whichever you find easier. Be sure to import any libraries you use at the top of the ntoebook (not down here).

```
n = 10000
```

```
#Optional: set random seed for reproducibility (how you do it depends
on whether you use numpy or scipy to generate the random numbers)
np.random.seed(n)
```

2.1) Create a variable "v1" of 10,000 numbers where y = 3x+4 is the value of the element at index x, i.e., [4, 7, 10, ...] (Done for you)

```
v1 = 3 * np.arange(n) + 4
```

2.2) Create a list of 10,000 samples from a normal (Gaussian) distribution with mean = 0 and variance = 10.

HINT: Pay attention to whether the argument to your number generator is variance or standard deviation. (It doesn't have to be a python list, it can be an array or dataframe, or whatever dtype is most convenient for you.)

```
mean = 0
variance = 10
standard_deviation = np.sqrt(variance)
noise = np.random.normal(mean, standard_deviation, n)
```

2.3) Create a variable v2 = v1 + Gaussian noise, using the noise your created above

```
v2 = v1 + noise
```

2.4) Create a variable v3 = $\exp(v1)$ that exponentiates the libear variable in v1, also sometimes denoted $e^{(v1)}$, e.g., v3[0] = e^4

```
v3 = np.exp(v1)
/var/folders/2p/bfr58x5j3q7bhsbb77vmqxbw0000gn/T/
ipykernel_1670/706569660.py:1: RuntimeWarning: overflow encountered in exp
   v3 = np.exp(v1)
```

2.5) Create a list $v4 = \exp(v1) + Gaussian$ noise, using the same noise variable you created earlier

```
v4 = v3 + noise
```

2.6) Create a list $v5 = \exp(v1 + \text{Gaussian noise})$, using the same noise variable you created earlier

```
v5 = np.exp(v2)
/var/folders/2p/bfr58x5j3q7bhsbb77vmqxbw0000gn/T/
ipykernel_1670/3036182197.py:1: RuntimeWarning: overflow encountered
in exp
   v5 = np.exp(v2)
```

v3 and v5 have overflows, This is not good, the random numbers that are generated from np.arrange(0,n) are being passed to these functions(v1,v2,v3,v4,v5), where they may to be big to represent. I will come up with a theoretical better values for np.arrange

We know

- v1 = 3x + 4
- v2 = v1 + noise
 - v2 = 3x + 4 + noise
- $v5 = e^{(v2)}$
 - v5 = e^(3x + 4 + noise)

to prevent an overflow

- v5 <= float64.max
 - e^(3x + 4 + noise) <= float64.max
 - 3x + (4 + noise) <= ln(float64.max)
 - 3x <= ln(float64.max) (4 + noise)
 - x <= (ln(float64.max) (4 + noise) / 3
- Due to the 68-95-99.7 rule
- μ = mean
 - $\mu = 0$
- variance = 10
- σ = standard deviation =
 - $\sigma = sqrt(variance)$
 - $\sigma = \operatorname{sqrt}(10)$
- z = z score
- % of samples
 - confidence interval
 - μ+- zσ

we will use the z score of 3.9 to get 99.995%

- Range
 - lower noise
 - 0 3.9 * sqrt(10)
 - upper noise
 - 0 + 3.9 * sqrt(10)

Our stop value in np arrange must be

- stop = x
 - stop = (ln(float64.max) (4 + noise) / 3
 - noise must be the upper bound of noise to account of 99.995% of data
 - stop = (ln(float64.max) (4 + upper_noise) / 3

```
z_score = 3
upper_noise = mean + (z_score * standard_deviation)
max_float64 = np.finfo(np.float64).max

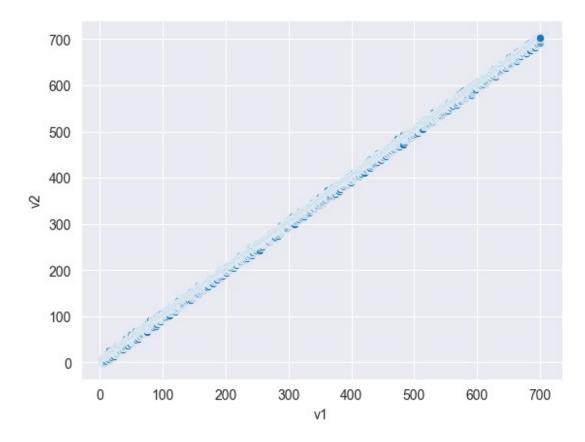
#scaling stop parameter in np.arrange
stop = ((np.log(max_float64) - (4 + upper_noise)) / 3)
print(stop)
# updating the v1,v2,v3,v4,v5
v1 = 3 * np.arange(start=0, stop=stop, step=stop / n) + 4
v2 = v1 + noise
v3 = np.exp(v1)
v4 = v3 + noise
v5 = np.exp(v2)
232.09862663762627
```

2.7) Create a dataframe with 10,000 rows and columns = [v1, v2, v3, v4, v5, noise]

```
V1 = 'v1'
V2 = 'v2'
V3 = 'v3'
V4 = 'v4'
V5 = 'v5'
NOISE = 'noise'
df_full = pd.DataFrame({V1: v1, V2: v2, V3: v3, V4: v4, V5: v5, NOISE: noise})
```

2.8) For each variable (v2, v3, v4, v5) create a separate scatter plot with v1 on the x-axis. Remark on your general observations.

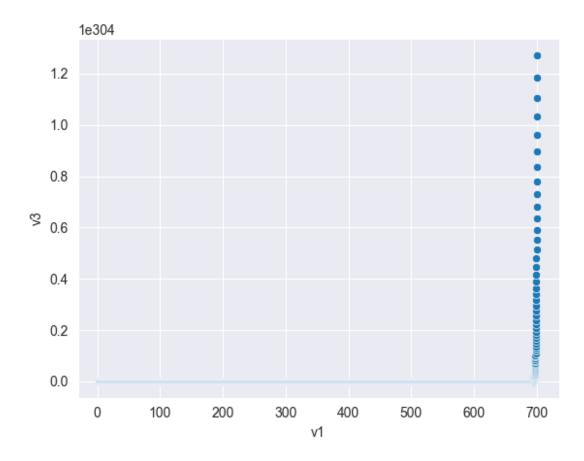
```
# Code for plots here, and remarks and observations here
sns.scatterplot(data=df_full, x=V1, y=V2)
<Axes: xlabel='v1', ylabel='v2'>
```



Will make observation later, with different view of this graph

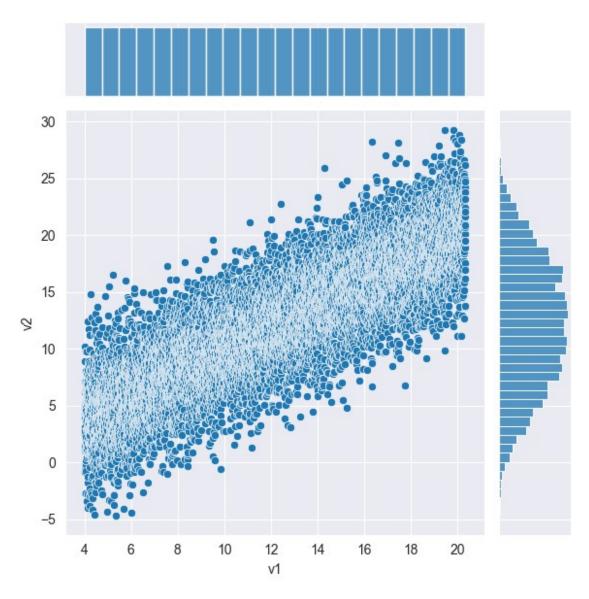
sns.scatterplot(data=df_full, x=V1, y=V3)

<Axes: xlabel='v1', ylabel='v3'>



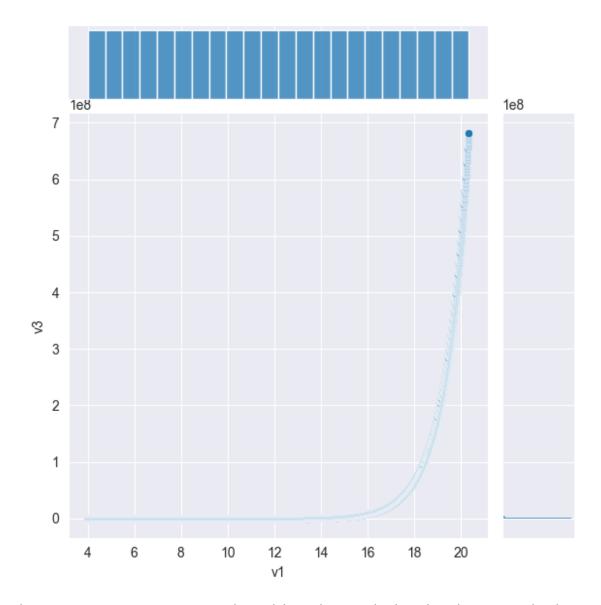
Its hard to make an observation since e^1.2e304 is close to float64.max, making the axis large, so i will scale stop down another log().

```
#scaling stop parameter in np.arrange again
stop = np.log(stop)
# updating the v1, v2, v3, v4, v5
v1 = 3 * np.arange(start=0, stop=stop, step=stop / n) + 4
v2 = v1 + noise
v3 = np.exp(v1)
v4 = v3 + noise
v5 = np.exp(v2)
#updating df full
df_full = pd.DataFrame({V1: v1, V2: v2, V3: v3, V4: v4, V5: v5, NOISE: noise})
sns.jointplot(data=df_full, x=V1 , y=V2, kind='scatter')
<seaborn.axisgrid.JointGrid at 0x1105b1f70>
```



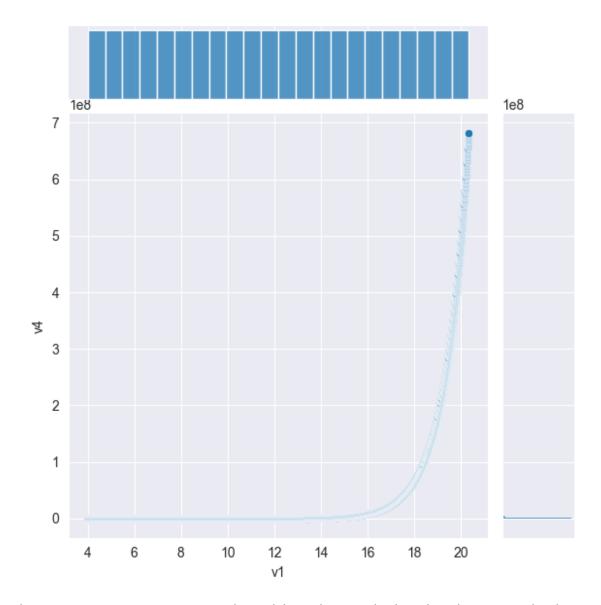
There appears to be a uniform spread across the positive linear pattern and moderate to strong relationship.

```
sns.jointplot(data=df_full, x=V1 , y=V3, kind='scatter')
<seaborn.axisgrid.JointGrid at 0x1106c28e0>
```



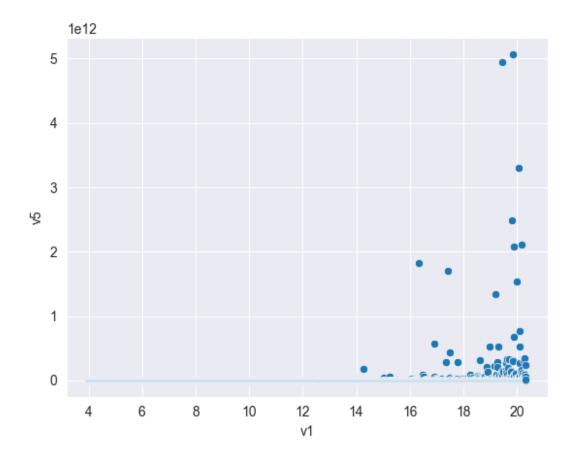
There appears positive exponential trend, but when you look at the where most the density is, trend begins to look slightly constant then skyrockets around (19e8,1e8). there appears to be a strong relationship as all the points are packed tightly, and the points are spread evenly across x = 4e8 through x = 20e8 according to distribution at the top margin. it looks like y = +0e8 might be outliers, there arent many points around that area. and lastly the variability is minimal until (16e8,0e8)

```
sns.jointplot(data=df_full, x=V1 , y=V4, kind='scatter')
<seaborn.axisgrid.JointGrid at 0x110c4bfd0>
```



There appears positive exponential trend, but when you look at the where most the density is, trend begins to look slightly constant then skyrockets around (19e8,1e8). there appears to be a strong relationship as all the points are packed tightly, and the points are spread evenly across x = 4e8 through x = 20e8 according to distribution at the top margin. it looks like y = +0e8 might be outliers, there arent many points around that area. and lastly the variability is minimal until (16e8,0e8)

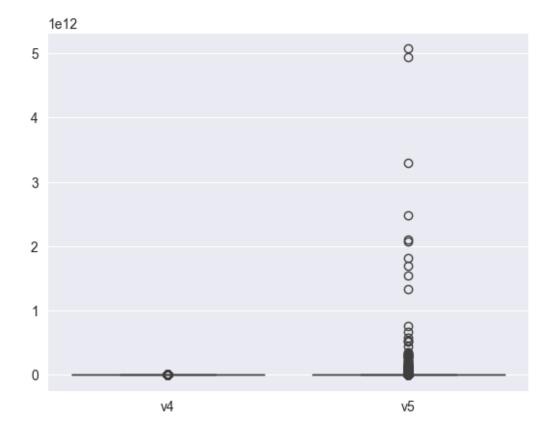
```
sns.scatterplot(data=df_full, x=V1 , y=V5)
<Axes: xlabel='v1', ylabel='v5'>
```



There appears constant trend, strong relationship as all the points are packed tightly, however the variability starts to increases after 14e12, sort of heteroscedasicity

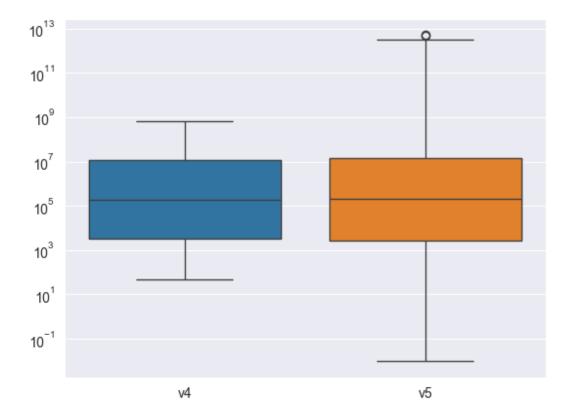
2.9) Create pair of boxplots with v4 and v5 next to each other. Remark on how v4 and v5 compare, based on the violin plots and the scatter plots. You may use other plots or tools if helpful.

```
# Pair of boxplots
sns.boxplot(data=df_full[[V4, V5]])
<Axes: >
```



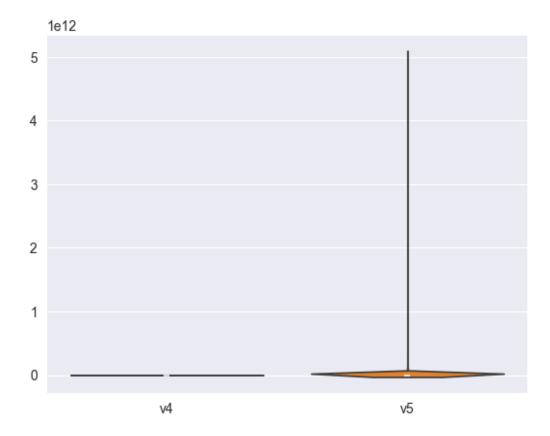
This is hard to interpret so i will log the scale

```
sns.boxplot(data=df_full[[V4, V5]], log_scale=True)
<Axes: >
```



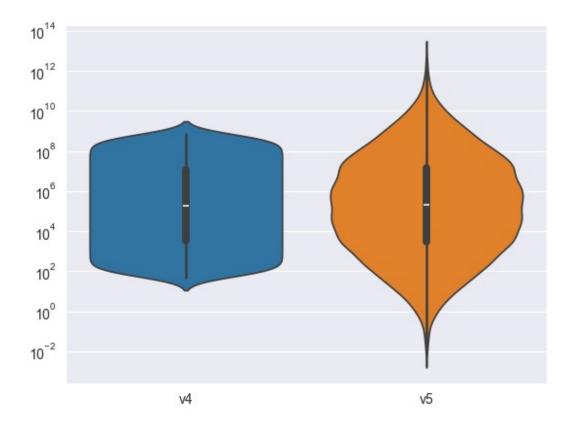
The IQR and mean seem to be roughly the same but with v5 IQR range slightly larger. There are different in a sense that v5 outlier whiskers are way larger or smaller than v4. and v5 has outliers where v4 does not.

```
# Violin plots
sns.violinplot(data=df_full[[V4, V5]])
<Axes: >
```



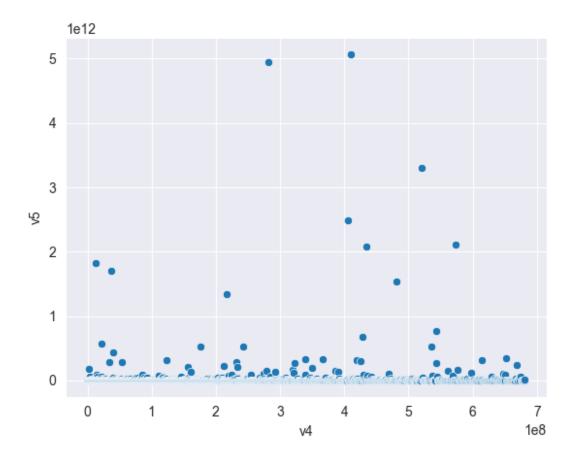
Again hard to interpret will use log scale

```
sns.violinplot(data=df_full[[V4, V5]], log_scale=True)
<Axes: >
```



v4 looks more dense than v5 in smaller range, as the outlier whiskers are wider in v5 than v4. they both look symmetric. but v5 has 3 minor modes(bumps)

```
# Scatter plot to see relationship
sns.scatterplot(data=df_full, x=V4, y=V5)
<Axes: xlabel='v4', ylabel='v5'>
```



There looks like theres a constant not positive not negative linear trend and somewhat uniform variability.

Part III - Sampling and Convergence

3.1) Create a variable "pareto" that is a list of 10,000 samples from a Pareto distribution with shape parameter = 1.2 (usually denoted a or alpha). Add this list "pareto" as a column to your dataframe from Part II

```
alpha = 1.2
pareto = np.random.pareto(a=alpha, size=n)
PARETO = 'pareto'
df full[PARETO] = pareto
df full.head()
         v1
                   v2
                              v3
                                          v4
                                                      v5
                                                             noise
pareto
0 4.000000 -0.019542
                      54.598150
                                  50.578608
                                                0.980648 -4.019542
0.718339
   4.001634
             4.558628
                       54.687444
                                  55.244439
                                               95.452475
                                                          0.556994
1.062391
                                               21.467708 -0.936718
2 4.003268
             3.066550 54.776885
                                  53.840167
0.184718
```

```
3 4.004902 5.038742 54.866472 55.900311 154.275835 1.033840 0.457977 4 4.006537 0.928314 54.956205 51.877982 2.530240 -3.078222 0.318868
```

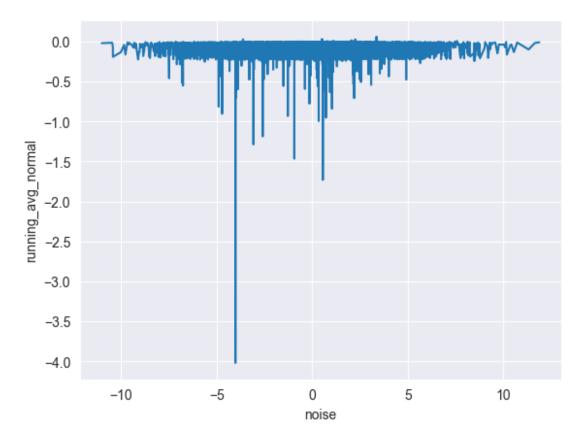
3.2) Add two more columns to your dataframe labeled "running_avg_normal" and "running_avg_pareto". In the "running_avg_normal" column put the running average of the (unsorted) values in the noise column. For example, if the values in the noise column are [0.1, 0.3, 0.5, ...] then the running average should be [0.1, 0.2, 0.3, ...]. Do the same for the Pareto column.

HINT: Check out the .expanding() and .mean() methods for pandas Series objects

```
RUNNING AVG NORMAL = 'running avg normal'
RUNNING AVG PARETO = 'running avg pareto'
df full[RUNNING AVG NORMAL] = df full[NOISE].expanding().mean()
df full[RUNNING AVG PARETO] = df full[PARETO].expanding().mean()
df full.head()
        v1
                   v2
                             v3
                                        v4
                                                    v5
                                                           noise
pareto
  4.000000 -0.019542 54.598150 50.578608
                                              0.980648 -4.019542
0.718339
  4.001634 4.558628 54.687444 55.244439
                                             95.452475 0.556994
1.062391
2 4.003268 3.066550 54.776885
                                 53.840167
                                             21.467708 -0.936718
0.184718
   4.004902 5.038742 54.866472 55.900311
                                            154.275835 1.033840
0.457977
4 4.006537
            0.928314 54.956205 51.877982
                                              2.530240 -3.078222
0.318868
   running avg normal
                       running avg pareto
0
            -4.019542
                                0.718339
            -1.731274
1
                                0.890365
2
            -1.466422
                                0.655149
3
            -0.841356
                                0.605856
4
            -1.288730
                                0.548459
```

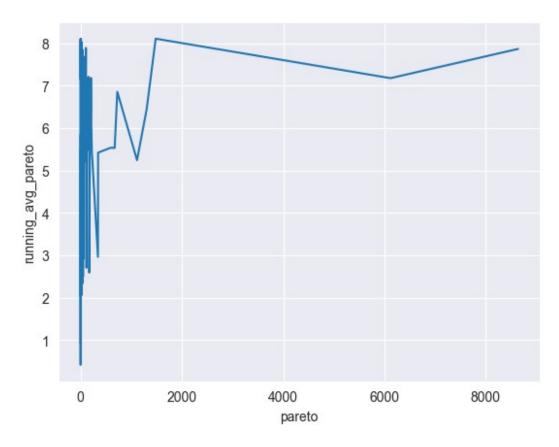
3.3) Create a lineplot for running_avg_normal and a lineplot for running_avg_Pareto. Remark on your observations.

```
sns.lineplot(data=df_full, x=NOISE, y=RUNNING_AVG_NORMAL)
<Axes: xlabel='noise', ylabel='running_avg_normal'>
```



Overall the trend is constant like with medium amount of fluctuation about the trend. The fluctuation is minimal on the edges and grows toward the center then minimizes

```
sns.lineplot(data=df_full, x=PARETO, y=RUNNING_AVG_PARETO)
<Axes: xlabel='pareto', ylabel='running_avg_pareto'>
```



There's overall a growth trend in the beginning then it stabilizes. Id also point out that there was much fluctuation and variation in the growth section of the trend.