

# CV1 practice exam 2

52041COV6Y Computer Vision 1 24/25 (1.1) · 4 exercises · 43.5 points

## 1 Question 1: Low Level Vision

10.0 points · 11 questions

\vspace{0.5cm}

### Camera Model

Text

Figure 1.1:

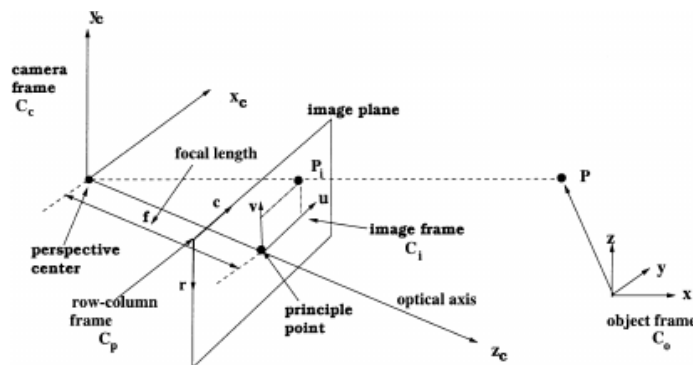


Figure 1.1 illustrates the projection from 3D space to 2D image using a pin-hole camera. The equation can be written as: \vspace{0.5cm}

$$\mathbf{x} = \mathbf{K}[\mathbf{R} \quad \mathbf{t}] \mathbf{X}$$

where  $\mathbf{X}$  is the coordinates of the 3D point in homogeneous coordinates and  $\mathbf{x}$  is the homogeneous coordinates on the 2D image.

Text

a What is the name of matrix **K**?

0.5 points · Multiple choice · 5 alternatives

- |   |     |
|---|-----|
| <input checked="" type="radio"/> Intrinsic matrix | 0.5 |
| <input type="radio"/> Extrinsic matrix            | 0.0 |
| <input type="radio"/> Rotation matrix             | 0.0 |
| <input type="radio"/> Translation matrix          | 0.0 |
| <input type="radio"/> Projection matrix           | 0.0 |

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

b Provide the expanded form of **x** and **X** :

1.0 point · Open question with final answer · 1/4 Page · 0 answers

**+0.5 points**

$$\mathbf{x} = w[u, v, 1]^T$$

Use other symbols are fine, as long as indicates homogeneous coordinates

**+0.5 points**

$$\mathbf{X} = [x, y, z, 1]^T$$

Use other symbols are fine, as long as indicates homogeneous coordinates

c The matrix  $K$  takes the form of a 3 by 3 matrix. Four elements have been provided. Can you provide the missing 5 elements for a pinhole camera model supporting non-square sensor pixels and a skew parameter:

$$K = \begin{bmatrix} \square & \square & \square \\ 0 & \square & \square \\ 0 & 0 & 1 \end{bmatrix}$$

Also, provide the meaning of the 3 elements in the first row in their correct order:

2.0 points · Open question with final answer · 1/100 Page · 0 answers

**+0.5 points**

fill in the symbols correctly. Use other symbols are acceptable if correctly explaining the meaning.

$K =$

$$\begin{bmatrix} f_x & s & u_0 \\ 0 & f_y & v_0 \\ 0 & 0 & 1 \end{bmatrix}$$

**+0.5 points**

$f_x$  is the focal length in x direction

or

$f_x$  is the scaling in x direction

**+0.5 points**

$s$  is the skew

**+0.5 points**

$u_0$  is the displacement/translation in x direction

d Given the current form of  $K$ , can we perform an arbitrary rotation using  $K$ ? If yes explain how, if not explain why?

0.5 points · Open · 1/5 Page

**+0.5 points**

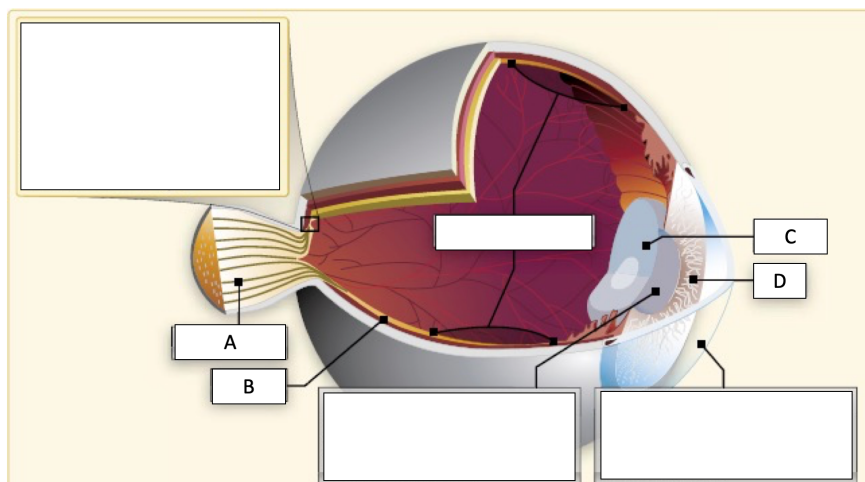
the 2nd row, 1st column of  $K$  has been fixed to be zero, and therefore cannot perform arbitrary rotation

**\vspace{4.5cm}**

**Human Vision and Color**

Text

e This is an anatomy of human eye.



Which one is the retina?

0.5 points · Multiple choice · 5 alternatives

- ☐ A 0.0
- ☒ B 0.5
- ☐ C 0.0
- ☐ D 0.0
- ☐ None of them 0.0

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

f Here are two statements regarding human perception. Which are correct?

A. There are more rods than cones on the human retina.

B. Rods are more sensitive in low light (darkness) than cones.

0.5 points · Multiple choice · 4 alternatives

- |   |     |
|---|-----|
| <input type="radio"/> only A                  | 0.0 |
| <input type="radio"/> only B                  | 0.0 |
| <input checked="" type="radio"/> Both of them | 0.5 |
| <input type="radio"/> None of them            | 0.0 |

Feedback

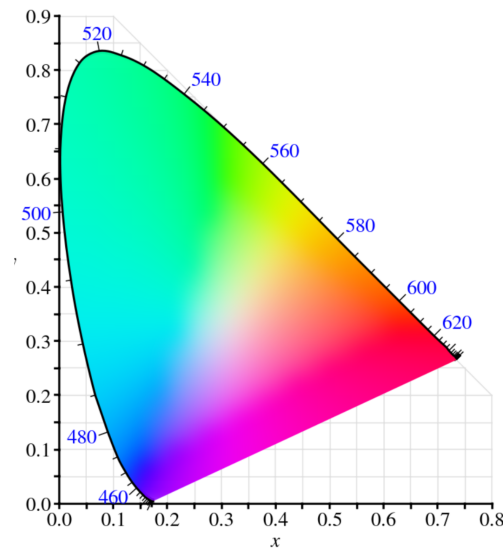
Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

g CIE systems are commonly used to study color. Assume the sunlight (ideal white) has CIE values  $X_S = Y_S = Z_S = 100$ . Further, let  $X_A = 100$ ,  $Y_A = 300$  and  $Z_A = 100$  be the values for a given artificial lamp A. Calculate the chromaticity values  $x, y$  for both S and A and plot them on the CIE-xy chart in figure 1.2 (0.5pt). (use pencil in case of correction)

Figure 1.2:



Use your plot and calculate the hue (0.5pt) and saturation (0.5pt) of A

1.5 points · Open · 7/20 Page

**+0.5 points**

$S_x = 1/3 = 0.33$ ,  $S_y = 1/3 = 0.33$ ,  $A_x = 0.2$ ,  $A_y = 0.6$

**+0.5 points**

Hue is approximately 517nm, because the result is hand plotted, it doesn't need to be very accurate, but need to show the way of doing it.

**+0.5 points**

Saturation is approximately 60%

`\vspace{0.4cm}`

**Reflection Model**

Text



Figure 1.3:

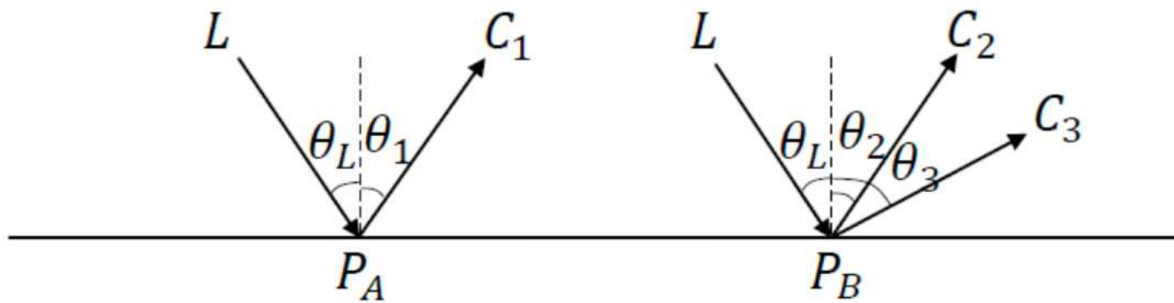


Figure 1.3 shows an image of a flat plane.  $L$  is the only light source, which is a uniform and parallel light pointing to the image plane. There is no other light source or object in the setting. There are two points  $P_A$  and  $P_B$ . And they are observed by three cameras  $C_1$ ,  $C_2$  and  $C_3$ . The angle between light source and surface normal is  $\theta_L$ , and the angle between camera and surface normal are  $\theta_1$ ,  $\theta_2$  and  $\theta_3$ . The three cameras are identical except there positions.

Text

h Denote the reflected light intensity to  $C_1$  from point  $P_A$  as  $I_1$  provide the simplified *Lambertian* reflection model. Please provide an equation to explain how  $I_1$  can be determined. Give extra symbols and explain them if necessary.

0.5 points · Open · 3/10 Page

**+0.5 points**

$L = a\rho LN$ ,  $a$  is a coefficient, missing it is fine.  $\rho$  is the albedo, use other symbols with proper explanation is fine.  $N$  is the surface normal and  $L$  is the light source

i Using the conditions provided in Fig. 1.3 and its descriptions but not the conditions in other questions.

In this question, assume the plane material is *Lambertian* (ideally diffusing).

We know the intensity observed by camera 1 is  $I_1 = 300$ .

Assume  $\theta_1 = \frac{\pi}{6}$ ,  $\theta_2 = \frac{\pi}{6}$  and  $\theta_3 = \frac{\pi}{3}$ .

Is the information provided so far sufficient to derive the intensity  $I_2$  and  $I_3$  captured by  $C_2$  and  $C_3$ . If so, provide the value with derivation. If not, explain why. Use illustrations if necessary.

1.0 point · Open · 3/10 Page

**+0.5 points**

$L_p \propto \rho \mathbf{LN}$ , use '=' instead of proportional is fine. Normal is assumed to be normalized, add extra normalization is fine.  $\mathbf{LN}$  is inner product between two vectors and is commutable. Use  $LN \cos \theta$  where  $\theta$  is the angle between  $L$ ,  $N$  is also fine.

**+1 point**

not possible, because the material is not uniform, the albedo is not determined.

j Using the conditions provided in Fig. 1.3 and its descriptions but not the conditions in other questions.

In this question, assume the plane material is *glossy*, which works like a mirror (ideally diffusing).

We know the intensity observed by the camera 1 is  $I_1 = 200$ .

Assume  $\theta_1 = \frac{\pi}{6}$ ,  $\theta_2 = \frac{\pi}{6}$  and  $\theta_3 = \frac{\pi}{3}$ .

Is the information provided so far sufficient to derive the intensity  $I_2$  and  $I_3$  captured by  $C_2$  and  $C_3$ . If so, provide the value with derivation. If not, explain why. Use illustrations if necessary.

1.0 point · Open · 2/5 Page

**+0.5 points**

If assume the material is perfectly reflective then  $C_2$  has the same situation as  $C_1$  and therefore  $I_2 = I_1 = 200$ .

**+0.5 points**

$I_3 = 0$ , because of the law of reflection.

k Using the conditions provided in Fig. 1.3 and its descriptions but not the conditions in other questions.

In this question, assume the plane material is *Lambertian* (ideally diffusing) and *uniform*,

We know the intensity observed by the camera 1 is  $I_1 = 100$ .

Assume  $\theta_1 = \frac{\pi}{6}$ ,  $\theta_2 = \frac{\pi}{6}$  and  $\theta_3 = \frac{\pi}{3}$ .

Is the information provided so far sufficient to derive the intensity  $I_2$  and  $I_3$  captured by  $C_2$  and  $C_3$ . If so, provide the value with derivation. If not, explain why. Use illustrations if necessary.

1.0 point · Open · 2/5 Page

**+0.5 points**

$I_2 = I_1 = 100$

**+1 point**

**+0.5 points**

$I_3 = I_1 = 100$

## 2 Question 2: Image Processing

23.5 points · 18 questions

\vspace{0.5cm}

### In Place Processing and Morphology

Consider the following image patches:

$$P = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 \\ \hline \end{array} \quad Q = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 \\ \hline 0 & 0 & 1 & 1 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

Text

a Lets do some binary morphology. Given a construction element

$$U = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Compute the results after performing *dilation* and *corrosion* separately on image  $P$  by using template  $U$ .

All elements at the image boundaries (i.e. outside image  $P$ ) are mirrored. The elements outside filter  $U$  are all zeros.

$P$  after dilation


$P$  after corrosion


2.0 points · Free formatted question

**+1 point**

no mistakes. Give only the foreground is fine

dilation:

0	0	0	0
1	1	1	1
1	1	1	1
1	1	1	1

1p for correct answer, each mistake -0.5p

**+1 point**

erosion

0 0 0 0

0 0 0 0

0 0 0 0

1 1 1 1

1p for correct answer, each mistake -0.5p

b Show the filtering result on  $Q$  by first do a *corrosion* and then do a *dilation* using  $U$ . Use zero-padding for both  $U$  and  $Q$ .


1.0 point · Open · 0/1 Page

**+1 point**

0	0	1	0
0	1	1	1
0	0	1	0
0	0	0	0

each mistake -0.5p till 0

### **\vspace{0.5cm}** Image Filtering

Text

c We have a sequence

$s = [0, 0, -2, 0, 0, 0, 0, 1, 1, 1]$ .

Show the self correlation result by first applying a difference filter  $h = [1, 0, -1]$ . Then apply the Gaussian filter  $g = [1, 2, 1]$  as defined in the previous question. Use zero padding.

2.0 points · Open question with final answer · 1/2 Page · 0 answers

**+2 points**

first step:  $h * s = [0, 2, 0, -2, 0, 0, -1, -1, 0, 1]$ ;  
correct answer got 1pt, each mistake -0.5pt.

second step:

$g * h * s = [2, 4, 0, -4, -2, -1, -3, -3, 0, 2]$   
correct answer got 1pt, each mistake -0.5pt.

Following the above question, explain what do these operations do? Why do we need to combine a Gaussian filter with a differential filter?

1.0 point · Open question with final answer · 1/5 Page · 0 answers

**+0.5 points**

this is an edge detector / band pass filter.

**+0.5 points**

use h only is sensitive to noise, and therefore, a smoother g is applied.

e Explain the concept of a Bilateral filter:

0.5 points · Open question with final answer · 1/5 Page · 0 answers

**+0.5 points**

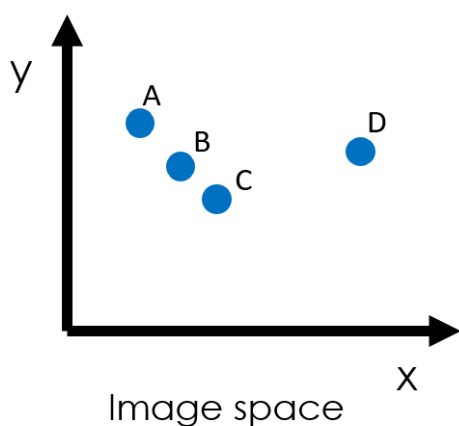
A bilateral filter is a **non-linear, edge-preserving, and noise-reducing smoothing filter for images**. It replaces the intensity of each pixel with a weighted average of intensity values from nearby pixels.

Point will be granted if mention edge/structure preserving.

## Edges and Lines

Text

f Figure 2.1:



In figure 2.1, we have 4 points in an image. The coordinates are  $A = (A_x, A_y) = (1, 3)$ ,  $B = (2, 2)$ ,  $C = (3, 1)$ ,  $D = (5, 2)$ .

Show how you can fit a line using Hough transform. For simplicity, use the linear version:  $y = ax + b$ .

To get the full points, all steps of Hough transform need to be provided.

2.0 points · Open · 1/2 Page

### +2 points

step 1 Give the four lines in Hough space (1pt)

A:  $a + b = 3$

B:  $2a + b = 2$

C:  $3a + b = 1$

D:  $5a + b = 2$

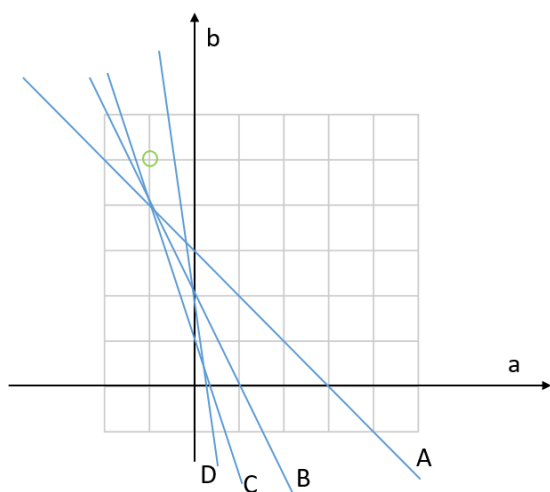
or equivalent form

Each wrong equation deduct 0.5pt, up to 1pt. It is acceptable if lines are plotted correctly without equations.

Step 2: Plot them in hough space (0.5pt)

flip axis a and b is fine

mistake other than wrong equation will deduct point. wrong equation will result in deduction in step 1.





Step 3: find  $a = -1$ ,  $b = 4$  (0.5pt) based on the voting in hough space, must mention voting in hough space.

**+1.5 points**

see grading scheme above

**+1 point**

see grading scheme above

**+0.5 points**

see grading scheme above

g Following the above question, this time, show how you can find the line using RANSAC.

1.5 points · Open · 2/5 Page

**+0.5 points**

mention random selecting two points.

**+0.5 points**

mention fitting a line based on two randomly selected points and calculate the confidence of this line.

**+0.5 points**

mention the line is found based on ranking the confidence

**\vspace{0.5cm}**

**Corners**

Text

h Harris corner detection is based on analyzing the second order differentials.

For the patch below:

0	0	1	1
1	1	1	1
0	0	1	1
0	0	0	0

compute its M matrix for the 2 \* 2 pixels in the lower right.

$$M = \begin{pmatrix} \sum f_x^2 & \sum f_x f_y \\ \sum f_x f_y & \sum f_y^2 \end{pmatrix}$$

To compute  $f_x$  use a simple derivative filter  $h_x = [-1, 1]$  in the x-direction and  $h_y = [-1, 1]^T$  in the y-direction. The center of  $h_x$  is at the first element, idem for  $h_y$ . Use cross-correlation for simplicity. Handle the out-of-boundary pixels with mirroring. To save time, assume the window size for summation over the neighborhood  $\Sigma$  is 1x1, i.e. you can ignore the summation.

2.0 points · Open · 1/2 Page

**+2 points**

$f_x =$

0 0

0 0

$f_y =$

-1 -1

0 0

$M_{33} =$

0 0

0 1

$M_{34} =$

0 0

0 1

$M_{43} =$

0 0

0 0

$M_{44} =$

0 0

0 0

Each M matrix is worth 0.5pt

**+1.5 points**

see grading scheme above

**+1 point**

see grading scheme above

**+0.5 points**

see grading scheme above

i Name two **photometric** image transformations that the SIFT descriptor is invariant to.

1.0 point · Open question with final answer · 1/20 Page · 0 answers

**+1 point**

add/subtract constant on brightness

scaling

any other reasonable answer. each worth 0.5p.

Rotation/translation are not photometric properties and are not considered correct .

**+0.5 points**

only one correct answer.

### Optical Flow

Text

j Which statements about the Lucas-Kanade optical flow method are correct?

1.5 points · Multiple choice · 6 alternatives

- ☒ The method is not robust to handle large motions (larger than the window size). 0.5
- ☒ The color or brightness of pixels is assumed to remain unchanged during motion. 0.5
- ☒ The method favors neighboring pixels to have the same flow vectors. 0.5
- ☐ The structure tensor is used to enforce local smoothness of the estimated flow field. -0.5
- ☐ The structure tensor is required to contain gradient information in at least one direction to uniquely estimate motion. -0.5
- ☒ The method fails to estimate a flow vector for homogeneously colored image regions. 0.5

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

**\vspace{0.5cm}**

**Linear Transformations**

Text

k Different types of transformations have a different degree of freedom. What is the degree of freedom of a 3D rigid body transform  $T \in SE(3)$ ?

1.0 point · Multiple choice · 4 alternatives

Model answer

Rigid body transformations are combinations of rotations and translations. These are described by the special Euclidean group.

In 2D space, that is  $[R|t] \in SE(2)$ , there is 1 degree of freedom for rotation and 2 degrees of freedom for translation.

Hence the correct answer is 3 DOF.

- |                                    |     |
|------------------------------------|-----|
| <input type="radio"/> 2            | 0.0 |
| <input type="radio"/> 3            | 0.0 |
| <input type="radio"/> 4            | 0.0 |
| <input checked="" type="radio"/> 6 | 1.0 |

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

l What is the degree of freedom of a 2D rotation  $R \in SO(2)$ ?

1.0 point · Multiple choice · 4 alternatives

Model answer

Rotations in 3D have 3 degrees of freedom: one angle for the rotation around each axis in 3 dimensions.

- |                                    |     |
|------------------------------------|-----|
| <input checked="" type="radio"/> 1 | 1.0 |
| <input type="radio"/> 2            | 0.0 |
| <input type="radio"/> 3            | 0.0 |
| <input type="radio"/> 6            | 0.0 |

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

m **Transformation composition:** Consider a kinematic chain of a human skeletal model where joint locations are described relative to each other. In particular, the joint for the hand is described by point  $H = (h_x, h_y, h_z) \in \mathbb{R}^3$  in local coordinates relative to the elbow  $E = (e_x, e_y, e_z) \in \mathbb{R}^3$ , while the elbow is defined relative to the shoulder  $S = (s_x, s_y, s_z) \in \mathbb{R}^3$ , which in turn is relative to the pelvis  $P = (p_x, p_y, p_z) \in \mathbb{R}^3$  that acts as the main anchor point for the entire skeleton.

All body joints also have locally defined relative rotations  $R_J \in SO(3)$  associated with them, where  $J \in \{H, E, S, P\}$  is a place holder for any body joint. Therefore, coordinate transformations from a local joint coordinate frame into the corresponding parent coordinate are described by a rigid body transformation  $T_J = [R_J | J] \in SE(3)$ .

Select all correct statements from the following options (multiple correct answers possible):

1.0 point · Multiple choice · 5 alternatives

Model answer

The correct answer is:

$$T_{[a_x, a_y]} R_\theta T_{[-a_x, -a_y]} B$$

The main idea is to decompose the transformation into three parts:

- 1) translate everything such that point A is in the new coordinate origin, i.e.  $T_{[-a_x, -a_y]}$ .
- 2) rotate around the coordinate origin, i.e. apply  $R_\theta$
- 3) translate everything back, i.e. , i.e.  $T_{[a_x, a_y]}$ .

All transformations are multiplied together in right-to-left order.

- ☐ To obtain the position of the hand in the global coordinate frame one only reads out point  $H$ . -0.5
- ☒ To obtain the position of the hand in the global coordinate frame one has to compute  $T_P T_S T_E T_H \vec{0}$  0.5
- ☐ To obtain the position of the hand in the global coordinate frame one has to compute  $T_H T_E T_S T_P \vec{0}$  -0.5
- ☒ To move the entire skeleton by a given displacement vector  $D \in \mathbb{R}^3$  one has to update the relative translation only for joint  $P$ . 0.5
- ☐ To move the entire skeleton by a given displacement vector  $D \in \mathbb{R}^3$  one has to update the relative translation for all joints  $J$ . -0.5

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

A partially correct answer is not applicable here.

Feedback when the question is answered incorrectly

The main idea is to decompose the transformation into three parts:

- 1) translate everything such that point A is in the new coordinate origin, i.e.  $T_{[-a_x, -a_y]}$ .

2) rotate around the coordinate origin, i.e. apply  $R_\theta$

3) translate everything back, i.e. , i.e.  $T_{[a_x, a_y]}$ .

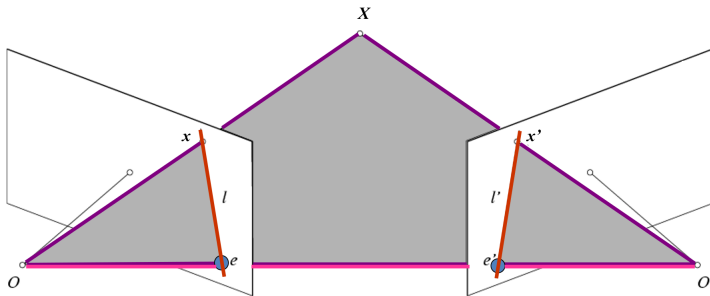
All transformations are multiplied together in right-to-left order.

$\backslash\text{space}\{12.5\text{cm}\}$

## Multiview Geometry and Reconstruction

Text

n The **epipolar geometry** is a key concept in multi-view stereo.



The figure above shows the camera centers  $O$  and  $O'$  and a 3D point  $X$  which projections on the image planes are  $x$  and  $x'$ .

Please mark correct all correct statements about epipolar geometry (multiple correct answers are possible).

2.0 points · Multiple choice · 5 alternatives

- ☒ The epipolar plane always contains the epipolar lines. 0.7
- ☒ The line through the points  $x$  and  $e$  is called epipolar line. 0.7
- ☒ The epipoles are always part of the the epipolar lines. 0.7
- ☐ The epipolar lines are always orthogonal to the line defined by the points  $o$  and  $o'$ . -0.7
- ☐ The line through the camera center  $o$  and the point  $X$  defines the principal axis. -0.7

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly



**Rectified Stereo:**

1.0 point · Multiple choice · 4 alternatives

- ☒ Image rectification reduces the correspondence search between corresponding pixels in the two input images from a 2D to a 1D search problem. 0.5
- ☒ In a rectified stereo setting all epipolar lines are parallel. 0.5
- ☐ The principal axes of two cameras are orthogonal after stereo rectification. -0.5
- ☐ Stereo rectification can be achieved by transforming both images with a rigid-body transform (i.e.  $SE(3)$ ). -0.5

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

p The following groups are generalizations of each other. Please order them from the most to the least general by entering numbers from 1 to 4.

- $\left( \quad \right)$  General linear group \newline
- $\left( \quad \right)$  Special orthogonal group \newline
- $\left( \quad \right)$  Orthogonal group \newline
- $\left( \quad \right)$  Set of square matrices

2.0 points · Free formatted question

Model answer

Solution:

2

4

3

1

because:  $SO(n) \subset O(n) \subset GL(n) \subset$  Set of square  $n \times n$  matrices.

Grading:

2p: all 4 correct

1p: 2 correct

0.5: 1 correct

alternatively, extra points are given if the order is partially correct.

**+1 point**

**Intrinsic camera calibration.** Consider the following camera model:

$$w \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f & 0 & u_0 \\ 0 & f & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{bmatrix} \begin{bmatrix} x \\ y \\ y \\ 1 \end{bmatrix}$$

How many parameters (DOF) need to be estimated for intrinsic camera calibration for the shown camera model?

0.5 points · Multiple choice · 5 alternatives

Model answer

3 DOF. The provided intrinsic (/calibration) matrix has 3 parameters ( $f$ ,  $u_0$ ,  $v_0$ ). The model assumes square pixels (because  $f_x=f_y$ ) and no screw parameter (because  $s=0$ )

- ☒ 3 0.5
- ☐ 4 0.0
- ☐ 6 0.0
- ☐ 9 0.0
- ☐ 12 0.0

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

The provided intrinsic (/calibration) matrix has 3 parameters ( $f$ ,  $u_0$ ,  $v_0$ ).

r **Extrinsic camera calibration.** Using the same camera model as in the previous question:  
How many parameters (DOF) need to be estimated for extrinsic camera calibration?

0.5 points · Multiple choice · 4 alternatives

Model answer

6 DOF

- |                                    |     |
|------------------------------------|-----|
| <input type="radio"/> 5            | 0.0 |
| <input checked="" type="radio"/> 6 | 0.5 |
| <input type="radio"/> 9            | 0.0 |
| <input type="radio"/> 12           | 0.0 |

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

Although the provided matrix has 9 parameters for rotation and 3 parameters for translation (12 in total), the rotation parameters are constrained to be rotation matrices, that is, members of the special orthogonal group  $SO(3)$ . This means that the rows and column of rotation matrix need to be mutually orthogonal and the its determinant is +1. Such rotation matrices can be for example be generated from just 3 parameter, the angular rotation angles around each spatial axis. Hence, the degree of freedom (DOF) of the rotation matrix is just 3. Together with the translation parameters, the extrinsic matrix has 6 DOF.

### 3 Question 3: Image Understanding

10.0 points · 8 questions

\vspace{0.5cm}

#### Traditional Classification and Retrieval

Text

a Consider a binary classifier with the following classification results.

		Predicted class labels	
		Positive	Negative
Actual class labels	Positive	5600	40
	Negative	1900	2460

Please compute the precision and recall values for this classifier using the provided confusion matrix.

1.0 point · Open · 1/4 Page

Model answer

[0.5p] Recall =  $5600 / (5600 + 40) = 0.99$

[0.5p] Precision =  $5600 / (5600 + 1900) = 0.75$

**+1 point**

Recall =  $5600 / (5600 + 40) = 0.99$

Precision =  $5600 / (5600 + 1900) = 0.75$

**+0.5 points**

Only one of the two is correct.

b Mark all correct statements.

1.0 point · Multiple choice · 5 alternatives

- ☒ The maximum IoU score is 1. 0.5
- ☐ F1 score is not normalized and requires additional normalization to ensure a value range of [0,1]. -0.5
- ☒ A bag of words representation does not account for the frequency a word occurs. 0.5
- ☐  $F1 = 2 \times \frac{Precision + Recall}{Precision \times Recall}$  -0.5
- ☐ The bag of visual words representation describes an ordered set of visual words. -0.5

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

`\vspace{4.5cm}`

**Object Detection**

Text

c Mark all correct statements about object detection methods and their individual steps.

1.0 point · Multiple choice · 4 alternatives

☐ For given object proposals, Fast R-CNN predicts absolute bounding box coordinates. -0.5

Feedback

This is incorrect, since the method predicts coordinate updates relative to the initial proposal.

☒ All R-CNN methods require object proposals as input. 0.5

Feedback

True. All these methods require them.

☐ The major difference between Fast R-CNN and (slow) R-CNN are learned vs. non-learned region proposals. -0.5

Feedback

This is incorrect. Both methods use non-learned region proposals. In the lecture we also discussed Faster R-CNN which uses learned region proposals, but the question refers to other methods.

☒ Both Fast R-CNN and Faster R-CNN have a global feature extraction stage which is jointly computed and then used for all region proposals. 0.5

Feedback

Correct.

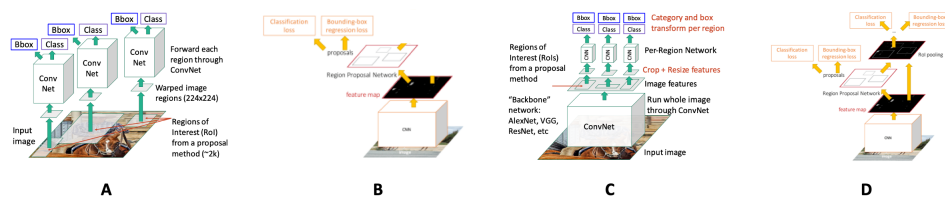
Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly

### d Object detection architectures.



Match the correct name with the architectures **A**, **B**, **C**, **D** depicted above:

- ☐ R-CNN \newline
- ☐ Fast R-CNN \newline
- ☐ Faster R-CNN \newline
- ☐ Single Stage Detector

1.0 point · Free formatted question

Model answer

- ☐ **A** - R-CNN
- ☐ **C** - Fast R-CNN
- ☐ **D** - Faster R-CNN
- ☐ **B** - Single Stage Detector

1 pt if all 4 are correct; 0.5 pts if two are correct; 0pts otherwise

**+1 point**

All four methods are correctly assigned.

**+0.5 points**

At least 2 methods correctly associated.

\vspace{0.5cm}

Neural Networks

Text

e Select all correct statements about neural network architectures.

1.0 point · Multiple choice · 4 alternatives

- ☒ Convolutional layers have fewer parameters than fully connected layers if the kernel size is smaller than the image size. 0.5
- ☐ Fully connected layers are naturally invariant to object translations in the image. -0.5
- ☐ Convolutional layers are naturally invariant to object rotations in the image. -0.5
- ☒ For patch sizes smaller than the image, convolutional layers require less computing operations and occupy less memory. 0.5

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly



- f Consider a 2D convolutional layer with RGB-D input of size  $64 \times 64$ . We apply 3 convolutional filters of size  $4 \times 4$ . All input channels are convolved together, not separately, no padding, and stride = 2.
1. What are the dimensions of the output activation layer ?
  2. How many weight parameters have to be trained in this layer ?

2.0 points · Open · 1/4 Page

Model answer

Part 1)

The output size  $W_{out}$  of a convolutional layer for **each** dimension can be computed for a given input size  $W_{inp}$ , a filter/kernel size  $k$ , padding  $p$  and stride  $s$  as follows:

$$W_{out} = \text{floor}\left(\frac{W_{inp} - k + 2p}{s}\right) + 1$$

that is, for input size 64 and kernel size  $k=4$ ,  $s=1$  and  $p=0$  we get an output size per dimension of

$$W_{out} = \text{floor}\left(\frac{64 - 4 + 0}{2}\right) + 1 = 31$$

thus for 4 conv. filters we get an output size of  $31 \times 31 \times 3$ .

Part 2)

Number of parameters = kernel height x kernel width x depth input x depth output/nr filters.

$$\text{Number of parameters} = 4 \times 4 \times 3 \times 3 = 144$$

**+1 point**

Question part 1. dimensions of output activation:  **$31 \times 31 \times 3$**  (=2883), being: height (minus kernel size) x width (minus kernel size) x number of filters.

**+0.5 points**

Question part 1. minor error (like  $30 \times 30 \times 3$ )

**+1 point**

Question part 2. Number of learnable parameters = dimensions of the kernel:

$$5 \times 5 \times 3 \times 4,$$

being:

kernel height x kernel width x depth input x depth output/nr filters.

$$\text{Number of parameters} = 4 \times 4 \times 3 \times 3 = 144$$

**+0.5 points**

Question part 2. Minor error.

g On the result of the convolutional layer of the previous question we apply a  $3 \times 3$  max pooling layer using stride = 1.

1. What are the dimensions of the output layer ?
2. How many weight parameters have to be learned in this layer ?

2.0 points · Open · 1/4 Page

Model answer

The output size  $W_{out}$  of a pooling layer can be similarly computed as for convolution layer in the previous question.

That is, for a given input size  $W_{inp}$ , a filter/kernel size  $k$ , padding  $p$  and stride  $s$  as follows:

$$W_{out} = \text{floor}\left(\frac{W_{inp} - k + 2p}{s}\right) + 1$$

that is, for input size 31 and kernel size 3,  $s=1$  and  $p=0$  we get an output size per dimension of

$$W_{out} = \text{floor}\left(\frac{31 - 3 + 0}{1}\right) + 1 = 29$$

thus for 3 conv. filters we get an **output size of  $29 \times 29 \times 3$** .

**+1 point**

Question part 1.

1pt if mentioned input conditions and corresponding output are correct:

$s=1, p=0 \rightarrow$  dimensions of output:  **$29 \times 29 \times 3$**  (=2523)

**+0.5 points**

Question part 1.

if the answer is partially correct, e.g. only one number of the output dimensions is correct or given, e.g.  $29 \times 29$  without 3 channel dimensions or a similar minor error.

**+1 point**

Question part 2.

No learnable parameters exist in (vanilla) pooling.

**+0.5 points**

Question part 2.

Minor error.

h Mark all correct statements about 2-stage and single shot object detectors.

1.0 point · Multiple choice · 5 alternatives

- ☐ 2-stage detectors require substantially less object proposals than single shot detectors. -0.5
- ☐ Non-maximum suppression is only required for 2-stage detectors. -0.5
- ☒ Single shot detectors are typically faster than 2-stage detectors. 0.5
- ☐ Single shot detectors require much less training data than 2-stage detectors. -0.5
- ☒ Single shot detectors use a small set of fixed regions as object proposals. 0.5

Feedback

Feedback when the question is answered correctly

Feedback when the question is answered partially correctly

Feedback when the question is answered incorrectly