

## Title

rdrandinf — Randomization Inference for RD Designs under Local Randomization.

#### Syntax

rdrandinf outvar runvar [if] [in] [, cutoff(#) wl(#) wr(#) statistic(stat\_name)
 p(#) evall(#) evalr(#) kernel(kerneltype) nulltau(#) ci(level [tlist])
 interfci(#) fuzzy(fuzzy\_var [fuzzy\_stat]) d(#) dscale(#) bernoulli(varname)
 reps(#) seed(#) covariates(varlist) obsmin(#) obsstep(#) wmin(#) wstep(#)
 nwindows(#) rdwstat(stat\_name) approximate rdwreps(#) level(#) plot
 graph\_options(graphopts) quietly ]

#### Description

- rdrandinf implements randomization inference and related methods for regression
   discontinuity (RD) designs, employing observations in a specified or
   data-driven selected window around the cutoff where local randomization is
   assumed to hold. See <u>Cattaneo</u>, <u>Frandsen and Titiunik (2015)</u> and <u>Cattaneo</u>,
   <u>Titiunik and Vazquez-Bare (2017)</u> for an introduction to this methodology.
- A detailed introduction to this command is given in <u>Cattaneo, Titiunik and Vazquez-Bare (2016)</u>.

  Companion <u>R</u> functions are also available <u>here</u>.
- Companion functions are <u>rdwinselect</u>, <u>rdsensitivity</u> and <u>rdrbounds</u>.
- Related Stata and R packages useful for inference in RD designs are described in the following website:

https://sites.google.com/site/rdpackages/

## <u>Options</u>

- cutoff(#) specifies the RD cutoff for the running variable runvar. Default is cutoff(0).
- wl(#) specifies the left limit of the window. Default is the minimum of the running variable.
- wr(#) specifies the right limit of the window. Default is the maximum of the running variable.
- statistic(stat\_name) specifies the statistic to be used. Options are:
   diffmeans for difference in means statistic. This is the default option.
   ksmirnov for Kolmogorov-Smirnov statistic.
   ranksum for Wilcoxon-Mann-Whitney studentized statistic.
   all for all three statistics.
   The option ttest is equivalent to diffmeans and included for backward
- compatibility.
- p(#) specifies the order of the polynomial for outcome adjustment model. Default is p(0) (constant treatment effect model).
- evall(#) specifies the point at the left of the cutoff at which the adjusted
   outcome is evaluated. Default is the cutoff value.
- evalr(#) specifies the point at the right of the cutoff at which the adjusted
   outcome is evaluated. Default is the cutoff value.
- kernel(kerneltype) specifies the type of kernel to use as weighting scheme.
  Allowed kernel types are uniform (uniform kernel), triangular (triangular kernel) and epan (Epanechnikov kernel). Default is kernel(uniform).
- nulltau(#) sets the value of the treatment effect under the null hypothesis.
  Default is nulltau(0).

rdsensitivity for details.

ci(level [tlist]) calculates a confidence interval for the treatment effect by
 test inversion, where level specifies the level of the confidence interval and

tlist indicates the grid of treatment effects to be evaluated. This option

interfci(#) sets the level for Rosenbaum's confidence interval under arbitrary
interference between units. See rdrbounds for details.

uses rdsensitivity to calculate the confidence interval; type help

- d(#) effect size for asymptotic power calculation. Default is 0.5 \* standard deviation of outcome variable for the control group.
- dscale(#) specifies fraction of the standard deviation of the outcome variable for the control group used as alternative hypothesis for asymptotic power calculation. Default is dscale(.5).
- bernoulli(varname) specifies that the randomization mechanism is Bernoulli trials
   (instead of fixed margins randomization). The values of the probability of
   treatment for each unit must be provided in the variable varname.
- reps(#) specifies the number of replications. Default is reps(1000).
- seed(#) sets the seed for the permutation test. With this option, the user can
  manually set the desired seed, or can enter the value -1 to use the system
  seed. Default is seed(666).
- NOTE: When the window around the cutoff is not specified, **rdrandinf** can select the window automatically using the companion command <u>rdwinselect</u>. The following options are available:
  - covariates(varlist) specifies the covariates employed by the companion command rdwinselect.
  - obsmin(#) specifies the minimum number of observations above and below the cutoff in the smallest window employed by the companion command rdwinselect. Default is obsmin(10).
  - obsstep(#) specifies the minimum number of observations to be added on each
     side of the cutoff for the sequence of nested windows constructed by the
     companion command <u>rdwinselect</u>. Default is obsstep(2).
  - wmin(#) specifies the smallest window to be used (if minobs(#) is not specified) by the companion command <u>rdwinselect</u>. Specifying both wmin(#) and obsmin(#) returns an error.
  - wstep(#) specifies the increment in window length (if obsstep(#) is not specified) by the companion command <u>rdwinselect</u>. Specifying both obsstep(#) and wstep(#) returns an error.
  - nwindows(#) specifies the number of windows to be used by the companion command rdwinselect. Default is nwindows(10).
  - rdwstat(#) specifies the statistic to be used by the companion command rdwinselect (see help file for options). Default option is rdwstat(ttest).
  - approximate forces the companion command <u>rdwinselect</u> to conduct the covariate balance tests using a large-sample approximation instead of finite-sample exact randomization inference methods.
  - rdwreps(#) specifies the number of replications to be used by the companion command <u>rdwinselect</u>. Default is rdwreps(1000).
  - level(#) specifies the minimum accepted value of the p-value from the
     covariate balance tests to be used by the companion command <u>rdwinselect</u>.
     Default is level(.15).

```
plot draws a scatter plot of the minimum p-value from the covariate balance
    test against window length implemented by the companion command
    rdwinselect.
```

graph\_options(graphopts) graph options for plot generated by the companion command rdwinselect.

quietly supress output from the companion command rdwinselect.

#### Example: Cattaneo, Frandsen and Titiunik (2015) Incumbency Data

```
Setup
```

. use rdlocrand\_senate.dta, clear

Randomization inference with user-specified window and default options

. rdrandinf demvoteshfor2 demmv, cutoff(0) wl(-.75) wr(.75)

Randomization inference with all statistics

. rdrandinf demvoteshfor2 demmv, cutoff(0) wl(-.75) wr(.75) stat(all)

Randomization inference with triangular weights

. rdrandinf demvoteshfor2 demmv, cutoff(0) wl(-.75) wr(.75) kernel(triangular)

Randomization inference on the Kolmogorov-Smirnov statistic with **rdwinselect** window options

. rdrandinf demvoteshfor2 demmv, cutoff(0) statistic(ksmirnov)
covariates(dopen population demvoteshlag1) wmin(.5) wstep(.125)

Randomization inference with linear adjustment

. rdrandinf demvoteshfor2 demmv, cutoff(0) wl(-.75) wr(.75) p(1)

Randomization inference under Bernoulli trials with .5 probability of treatment

- . gen probs=.5
- . rdrandinf demvoteshfor2 demmv, cutoff(0) w1(-.75) wr(.75) bernoulli(probs)

Confidence interval under interference

. rdrandinf demvoteshfor2 demmv, cutoff(0) wl(-.75) wr(.75) interfci(.05)

Confidence interval for the treatment effect

. rdrandinf demvoteshfor2 demmv, wl(-.75) wr(.75) ci(.05 3(1)20)

Linear adjustment with effects evaluated at the mean of the running variable

- . qui sum demmv if abs(demmv)<=.75 & demmv>=0 & demmv!=. & demvoteshfor2!=.
- . local mt=r(mean)
- . qui sum demmv if abs(demmv)<=.75 & demmv<0 & demmv!=. & demvoteshfor2!=.
- . local mc=r(mean)
- . rdrandinf demvoteshfor2 demmv, wl(-.75) wr(.75) p(1) evall('mc') evalr('mt')

# Saved results

rdrandinf saves the following in r():

```
Scalars
 r(wl)
                       left limit of window used
                       right limit of window used
 r(wr)
 r(N)
                       sample size in used window
 r(N_left)
                       sample size in used window to the left of the cutoff
 r(N_right)
                      sample size in used window to the right of the cutoff
 r(p)
                      order of polynomial in adjusted model
                      observed statistic
 r(obs_stat)
 r(randpval)
                      randomization p-value
 r(asy_pval)
                      asymptotic p-value
 r(ci_lb)
                      lower limit of confidence interval (if ci option is
                       specified)
                      upper limit of confidence interval (if ci option is
 r(ci_ub)
                       specified)
```

Locals seed used in permutations r(seed) Matrices matrix of observed statistics (when **all** is specified) matrix of asymptotic p-values (when **all** is specified) matrix of p-values (when **all** is specified) r(obs\_stat) r(asy\_pval)

## References

r(p\_val)

Cattaneo, M. D., Frandsen, B., and R. Titiunik. 2015. Randomization Inference in the Regression Discontinuity Design: An Application to Party Advantages in the U.S. Senate. Journal of Causal Inference 3(1): 1-24.

matrix of p-values (when **all** is specified)

Cattaneo, M.D., Titiunik, R. and G. Vazquez-Bare. 2016. <u>Inference in Regression</u> <u>Discontinuity Designs under Local Randomization</u>. Stata Journal 16(2): 331-367.

Cattaneo, M. D., Titiunik, R. and G. Vazquez-Bare. 2017. Comparing Inference Approaches for RD Designs: A Reexamination of the Effect of Head Start on Child Mortality. Journal of Policy Analysis and Management 36(3): 643-681.

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