

## Data Mining (CSE542)

### Homework 07

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#### Task-1

Given the dataset in Figure 14.5, show the dendrogram resulting from the single-link hierarchical agglomerative clustering approach using the  $L_1$ -norm as the distance between points

$$\|\mathbf{x} - \mathbf{y}\|_1 = \sum_{d=1}^2 |x_{id} - y_{id}|$$

K=4

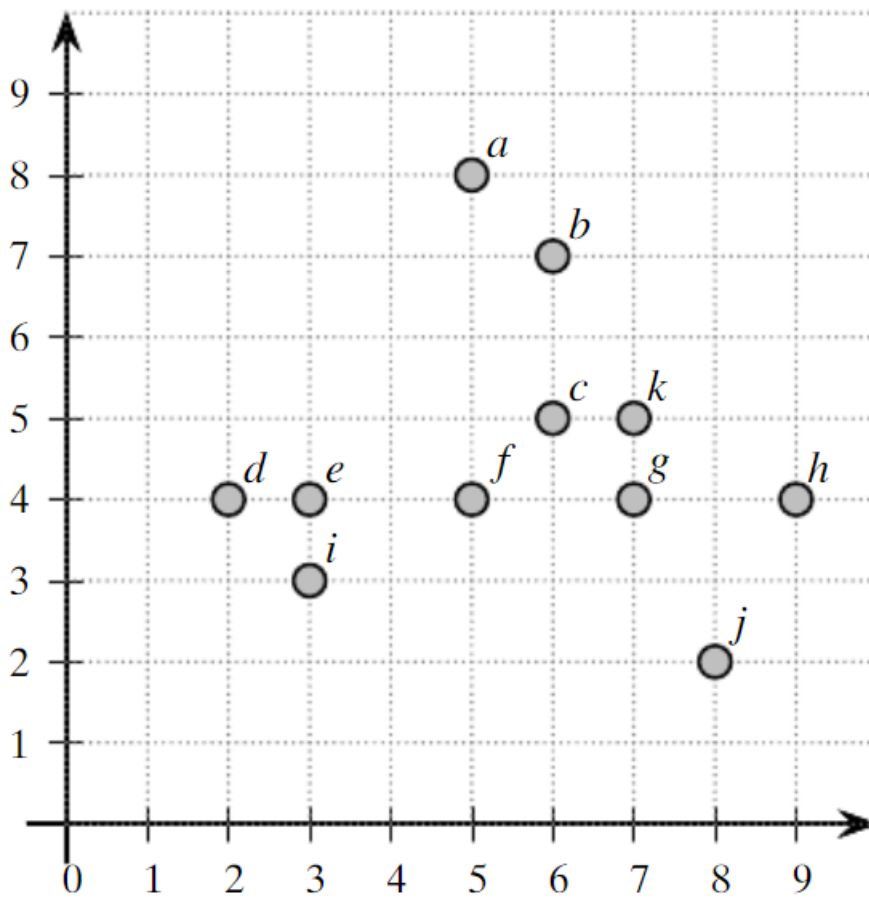


Figure 14.5. Dataset

a(5,8), b(6,7), c(6,5), d(2,4), e(3,4), f(5,4), g(7,4), h(9,4), i(3,3), j(8,2), k(7,5)

	a	b	C	D	E	F	g	h	i	j	k
a	0	2	4	7	6	4	6	8	7	9	5
b	2	0	2	7	6	4	4	6	7	7	3
c	4	2	0	5	4	2	2	4	5	5	1
d	7	7	5	0	1	3	5	7	2	8	6
e	6	6	4	1	0	2	4	6	1	7	5
f	5	4	2	3	2	0	2	4	3	5	3
g	6	4	2	5	4	2	0	2	5	3	1
h	8	6	4	7	6	4	2	0	7	3	3
i	7	7	5	2	1	3	5	7	0	6	6
j	9	7	5	8	7	5	3	3	6	0	4
k	5	3	1	6	5	3	1	3	6	4	0

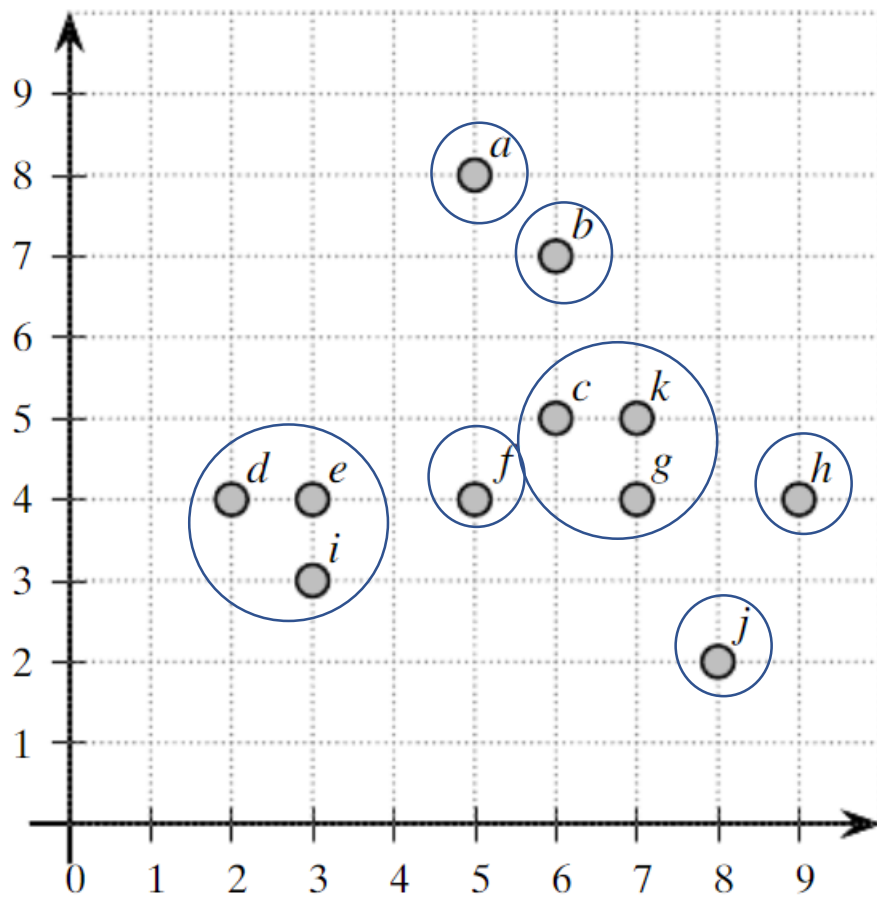
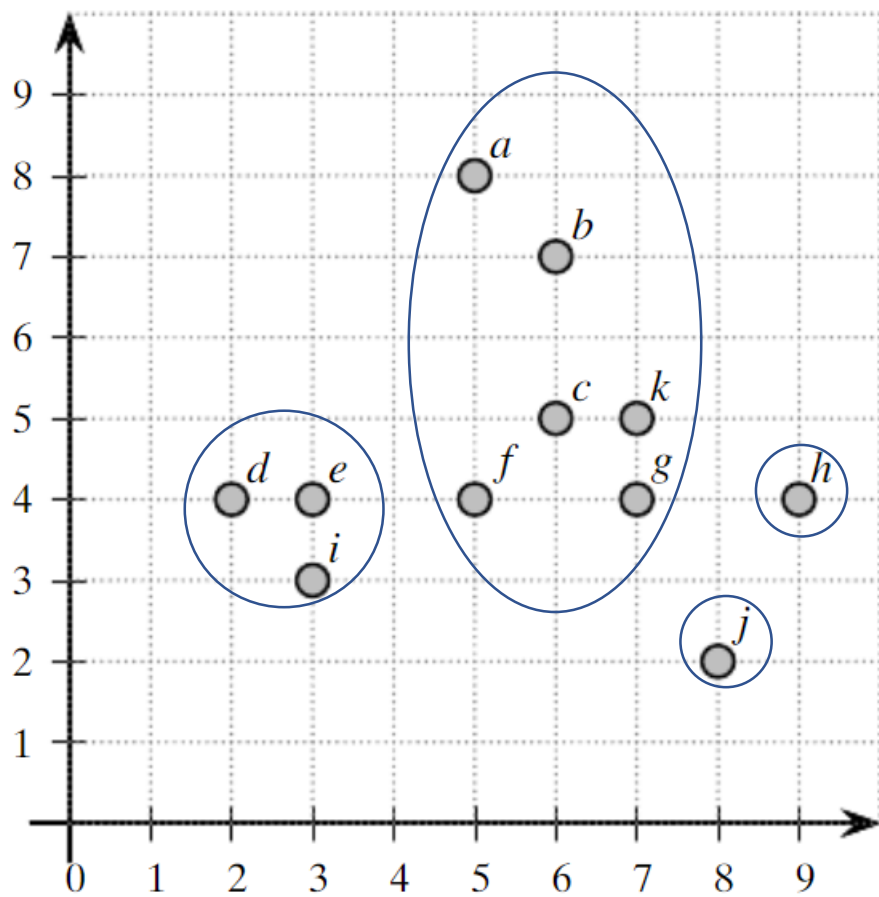


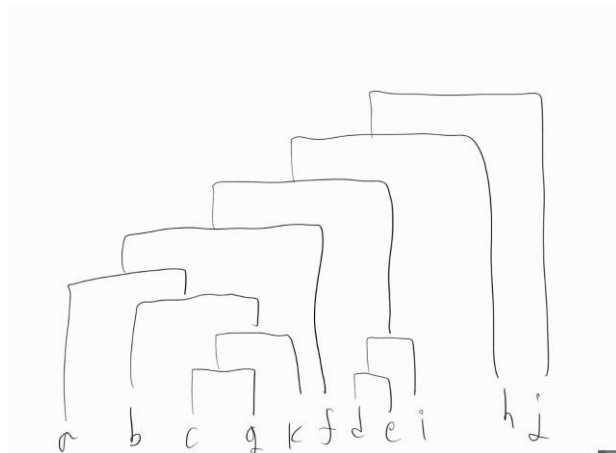
Figure 14.5. Dataset

	a	b	c,g,k	d,e,i	f	h	j
a	0	2	4	6	4	8	9
b	2	0	2	6	4	6	7
c,g,k	4	2	0	2	4	2	2
d,e,i	6	6	2	0	2	6	6
f	4	4	4	2	0	4	5
h	8	6	2	6	4	0	3
j	9	7	2	6	5	3	0



	a,b,c,f,g,k	d,e,i	h	j
a,b,c,f,g,k	0	2	2	3
d,e,i	2	0	6	6
h	2	6	0	3
j	3	6	3	0

The dendrogram is that>



## Task-2

Consider Figure 15.12 and answer the following questions, assuming that we use the Euclidean distance between points, and that  $\epsilon = 2$  and  $minpts = 3$

- List all the core points.
- Is  $a$  directly density reachable from  $d$ ?
- Is  $o$  density reachable from  $i$ ? Show the intermediate points on the chain or the point where the chain breaks.
- Is density reachable a symmetric relationship, that is, if  $x$  is density reachable from  $y$ , does it imply that  $y$  is density reachable from  $x$ ? Why or why not?
- Is  $l$  density connected to  $x$ ? Show the intermediate points that make them density connected or violate the property, respectively.
- Is density connected a symmetric relationship?
- Show the density-based clusters and the noise points.

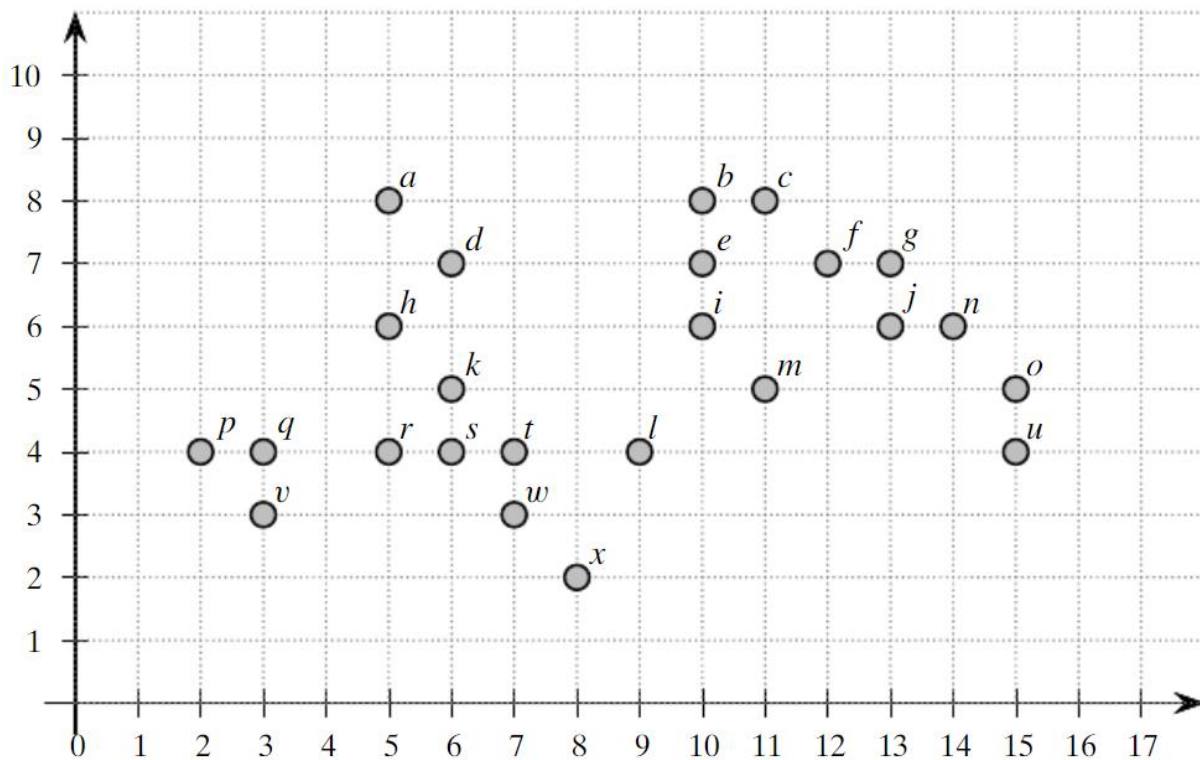


Figure 15.12. Dataset

(a) List all the points

: a, b, c, d, e, f, g, h, i, j, k, n, o, p, q, r, s, t, v, w

(b) Is 'a' directly density reachable from 'd'?

: Yes => d is a core object and a belongs to  $N_2(d)$

(c) Is 'o' density reachable from 'i'? Show the intermediate points on the chain or the point where the chain breaks.

: Yes => { i, e, b, c, f, g, j, n, o } or { i, e, f, j, n, o }

(d) Is density reachable a symmetric relationship, that is, if 'x' is density reachable from y, does it imply that 'y' is density reachable from 'x'? Why or why not?

: Density reachable is not a symmetric relationship, since a non-core object may be reachable from a core object, but the reverse is not necessarily true. For example u is density reachable from n but n is not density reachable from u.

(e) Is 'l' density connected to 'x'? Show the intermediate points that make them density connected or violate the property, respectively.

: Yes => Yes, for example, via t, since l is density-reachable from t and x is also density-reachable from t.

(f) Is density connected a symmetric relationship?

: Yes => by definition. In other words for any two points, there exists a core point that reaches both of them.

(g) Show the density-based clusters and the noise points.

:  $C_1 \Rightarrow \{ a, d, h, k, p, q, r, s, t, l, v, w, x \}$

$C_2 \Rightarrow \{ b, c, e, f, g, i, j, n, m, o, u \}$