

Programming with Python

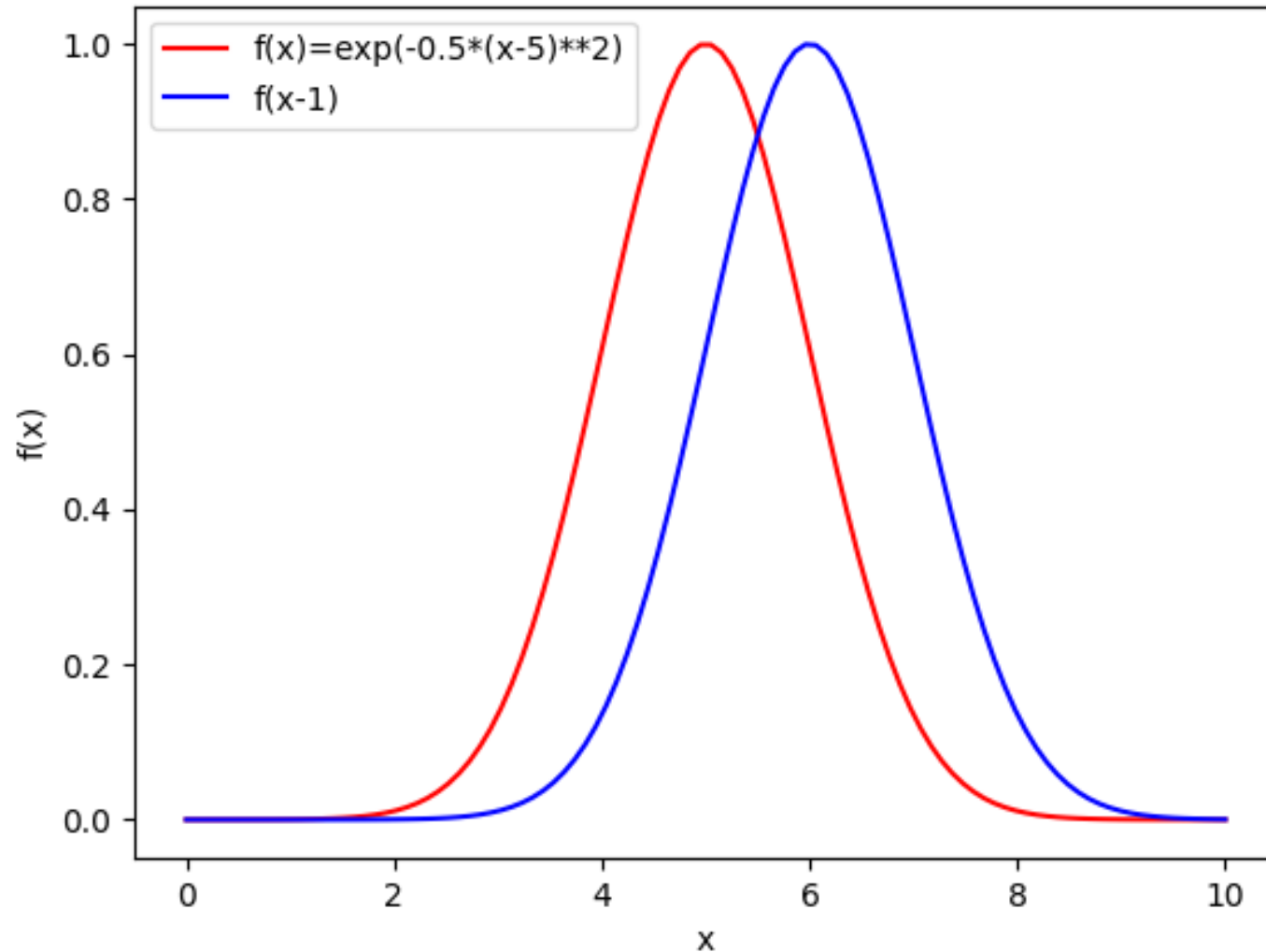
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Case 1:

Write a program that can produce this plot



Python program

```
import numpy as np
import matplotlib.pyplot as plt

xx = np.linspace(0, 10, 100)
x0 = 5
x1 = (xx - x0) ** 2
y1 = np.exp(-0.5 * x1)
# shifted Gaussian
x2 = (xx - x0 - 1) ** 2
y2 = np.exp(-0.5 * x2)
plt.plot(xx, y1, 'r-', xx, y2, 'b-')
plt.legend(['f(x) = exp(-0.5 * (x - 5) ** 2)', 'f(x - 1)'])
plt.xlabel('x')
plt.ylabel('f(x)')
plt.show()
```

Copying an array

```
In [15]: from numpy import copy
```

```
In [16]: x = linspace(0, 2, 3)           # x becomes array([ 0.,  1.,  2.])
```

```
In [17]: y = copy(x)
```

```
In [18]: y
```

```
Out[18]: array([ 0.,  1.,  2.])
```

```
In [19]: y[0] = 10.0
```

```
In [20]: y
```

```
Out[20]: array([ 10.,   1.,   2.]) # ...changed
```

```
In [21]: x
```

```
Out[21]: array([ 0.,  1.,  2.])    # ...unchanged
```

Slicing an array

```
In [1]: from numpy import linspace
```

```
In [2]: x = linspace(11, 16, 6)
```

```
In [3]: x
```

```
Out[3]: array([ 11.,  12.,  13.,  14.,  15.,  16.])
```

```
In [4]: y = x[1:5]
```

```
In [5]: y
```

```
Out[5]: array([ 12.,  13.,  14.,  15.])
```

```
In [6]: y[0] = -1.0
```

```
In [7]: y
```

```
Out[7]: array([-1.,  13.,  14.,  15.])      # ...changed
```

```
In [8]: x
```

```
Out[8]: array([ 11., -1.,  13.,  14.,  15.,  16.])  # ...changed
```

Matrix-vector multiplication

```
In [1]: import numpy as np

In [2]: I = np.zeros((3, 3))      # create matrix (note parentheses!)

In [3]: I
Out[3]:
array([[ 0.,  0.,  0.],
       [ 0.,  0.,  0.],
       [ 0.,  0.,  0.]])

In [4]: type(I)
Out[4]: numpy.ndarray

In [5]: I[0, 0] = 1.0; I[1, 1] = 1.0; I[2, 2] = 1.0 # identity matrix

In [6]: x = np.array([1.0, 2.0, 3.0]) # create vector

In [7]: y = np.dot(I, x)           # computes matrix-vector product

In [8]: y
Out[8]: array([ 1.,  2.,  3.])
```

$I = \text{np.eye}(3)$

Matrix-vector multiplication

```
In [1]: import numpy as np

In [2]: I = np.eye(3)           # create identity matrix

In [3]: I
Out[3]:
array([[ 1.,  0.,  0.],
       [ 0.,  1.,  0.],
       [ 0.,  0.,  1.]])

In [4]: type(I)                 # confirm that type is ndarray
Out[4]: numpy.ndarray

In [5]: I = np.matrix(I)        # convert to matrix object

In [6]: type(I)                 # confirm that type is matrix
Out[6]: numpy.matrixlib.defmatrix.matrix

In [7]: x = np.array([1.0, 2.0, 3.0]) # create ndarray vector

In [8]: x = np.matrix(x)        # convert to matrix object (row vector)

In [9]: x = x.transpose()       # convert to column vector

In [10]: y = I*x                # computes matrix-vector product

In [11]: y
Out[11]:
matrix([[ 1.],
        [ 2.],
        [ 3.]])
```

Summation

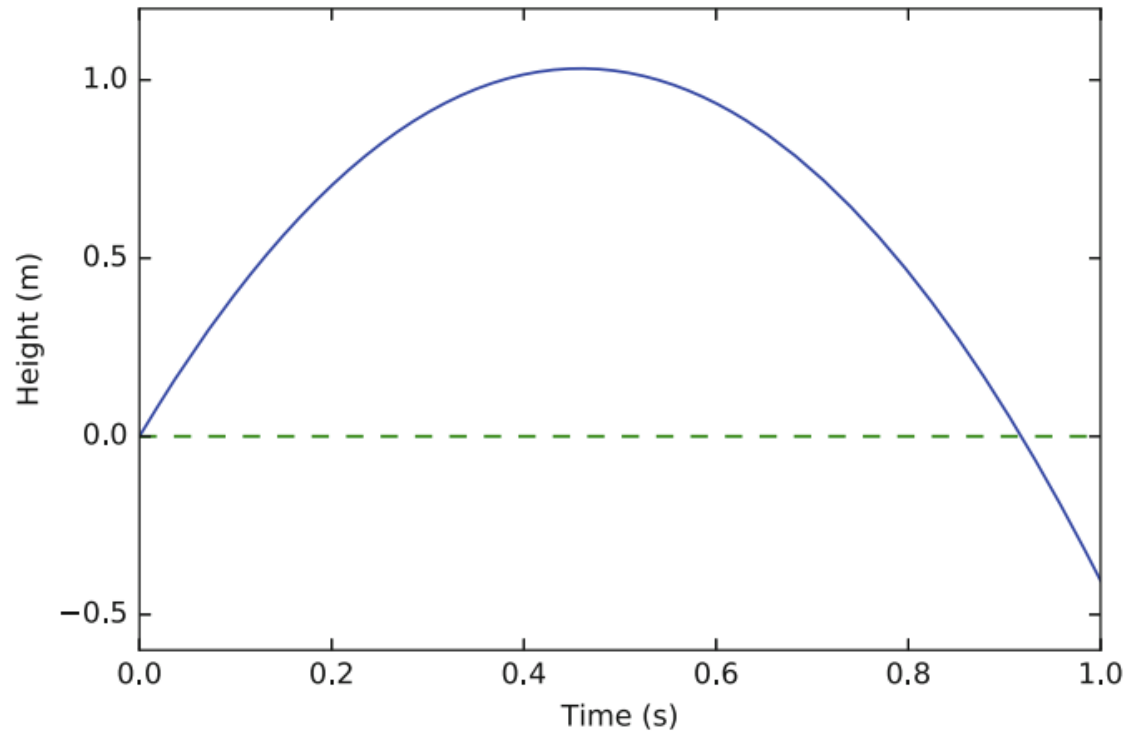
- Create a vector consisting of 100 random numbers (floats between 0 – 1)
- Compute mean of the vector:

$$\frac{1}{N} \sum_{i=1}^N x_i$$

```
import numpy as np

nn=100
data=np.random.random(nn)
ndata=len(data)
sum=0
for i in range(0,ndata):
    sum=sum+data[i]
mean=sum/ndata
```


While loop



```
import numpy as np

v0 = 4.5                # Initial velocity
g = 9.81                # Acceleration of gravity
t = np.linspace(0, 1, 1000) # 1000 points in time interval
y = v0*t - 0.5*g*t**2     # Generate all heights

# Find index where ball approximately has reached y=0
i = 0
while y[i] >= 0:
    i = i + 1

# Since y[i] is the height at time t[i], we do know the
# time as well when we have the index i...
print('Time of flight (in seconds): {:.g}'.format(t[i]))

# We plot the path again just for comparison
import matplotlib.pyplot as plt
plt.plot(t, y)
plt.plot(t, 0*t, 'g--')
plt.xlabel('Time (s)')
plt.ylabel('Height (m)')
plt.show()
```

Branching (if, elif, else)

```
if condition_1:                # testing condition 1
    <code line 1>
    <code line 2>
    ...
elif condition_2:              # testing condition 2
    <code line 1>
    <code line 2>
    ...
elif condition_3:              # testing condition 3
    <code line 1>
    <code line 2>
    ...
else:
    <code line 1>
    <code line 2>
    ...
# First line after if-elif-else construction
```

```
import numpy as np
import matplotlib.pyplot as plt

v0 = 5                        # Initial velocity
g = 9.81                      # Acceleration of gravity
t = np.linspace(0, 1, 1000)   # 1000 points in time interval
y = v0*t - 0.5*g*t**2         # Generate all heights

# At this point, the array y with all the heights is ready,
# and we need to find the largest value within y.

largest_height = y[0]         # Starting value for search
for i in range(1, len(y), 1):
    if y[i] > largest_height:
        largest_height = y[i]

print('The largest height achieved was {:g} m'.format(largest_height))

# We might also like to plot the path again just to compare
plt.plot(t,y)
plt.xlabel('Time (s)')
plt.ylabel('Height (m)')
plt.show()
```

Function

```
def y(v0, t):  
    g = 9.81                                # not in main  
    return v0*t - 0.5*g*t**2               # not in main  
  
v0 = 5  
  
time = 0.6  
print(y(v0, time))  
time = 0.9  
print(y(v0, time))
```

Function (two return values)

```
def xy(v0x, v0y, t):  
    """Compute horizontal and vertical positions at time t"""  
    g = 9.81                                # acceleration of gravity  
    return v0x*t, v0y*t - 0.5*g*t**2  
  
v_init_x = 2.0                             # initial velocity in x  
v_init_y = 5.0                             # initial velocity in y  
time = 0.6                                 # chosen point in time  
  
x, y = xy(v_init_x, v_init_y, time)  
print('Horizontal position: {:.g} , Vertical position: {:.g}'.format(x, y))
```

Exercise 3.1: A for Loop with Errors

Assume some program has been written for the task of adding all integers $i = 1, 2, \dots, 10$ and printing the final result:

```
for i in [1, 2, 3, 4, 5, 6, 7, 8, 9, 10)
    sum = Sum + x
print 'sum: ', sum
```

- Identify the errors in the program by just reading the code.
- Write a new version of the program with errors corrected. Run this program and confirm that it gives the correct output.

Exercise 3.2: The range Function

Write a slightly different version of the program in Exercise 3.1. Now, the range function should be used in the for loop header, and only the even numbers from $[2, 10]$ should be added. Also, the (only) statement within the loop should read `sum = sum + i`.

Exercise 3.3: A while Loop with Errors

Assume some program has been written for the task of adding all integers $i = 1, 2, \dots, 10$:

```
some_number = 0
i = 1
while i < 11
    some_number += 1
print some_number
```

- Identify the errors in the program by just reading the code.
- Write a new version of the program with errors corrected. Run this program and confirm that it gives the correct output.

Exercise 3.7: Frequency of Random Numbers

Write a program that takes a positive integer N as input and then draws N random integers from the interval $[1, 6]$. In the program, count how many of the numbers, M , that equal 6 and print out the fraction M/N . Also, print all the random numbers to the screen so that you can check for yourself that the counting is correct. Run the program with a small value for N (e.g., $N = 10$) to confirm that it works as intended.

Hint Use `random.randint(1,6)` to draw a random integer between 1 and 6.

Exercise 3.10: Sort Array with Numbers

Write a script that uses the `uniform` function from the `random` module to generate an array of 6 random numbers between 0 and 10.

The program should then sort the array so that numbers appear in increasing order. Let the program make a formatted print of the array to screen both before and after sorting. Confirm that the array has been sorted correctly.

Exercise 3.11: Compute π

Up through history, great minds have developed different computational schemes for the number π . We will here consider two such schemes, one by Leibniz (1646–1716), and one by Euler (1707–1783).

The scheme by Leibniz may be written

$$\pi = 8 \sum_{k=0}^{\infty} \frac{1}{(4k+1)(4k+3)},$$

while one form of the Euler scheme may appear as

$$\pi = \sqrt{6 \sum_{k=1}^{\infty} \frac{1}{k^2}}.$$

If only the first N terms of each sum are used as an approximation to π , each modified scheme will have computed π with some error.

Write a program that takes N as input from the user, and plots the error development with both schemes as the number of iterations approaches N . Your program should also print out the final error achieved with both schemes, i.e. when the number of terms is N . Run the program with $N = 100$ and explain briefly what the graphs show.