EI: A(n R) Program for Ecological Inference

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Contents

1 Introduction: Ecological Inference

This program provides methods of inferring individual behavior from aggregate data. It implements the statistical procedures, diagnostics, and graphics from the Gary King, A Solution to the Ecological Inference Problem: Reconstructing Individual Behavior from Aggregate Data (Princeton: Princeton University Press, 1997), http://j.mp/ecinfbook; Ori Rosen, Wenxin Jiang, Gary King, and Martin A.. Tanner (2001) "Bayesian and Frequentist Inference for Ecological Inferece: The RxC Case." (Statistica Neerlandica, Vol.55, nr.2, pp 134-156), http://j.mp/eiRxC; and from our own ongoing work. Except where indicated, all references to page, section, chapter, table, and figure numbers in this document refer to the the first reference.

Ecological inference is the process of using aggregate (i.e., "ecological") data to infer discrete individual-level relationships of interest when individual-level data are not available. Ecological inferences are required in political science research when individual-level surveys are unavailable (e.g., local or comparative electoral politics), unreliable (racial politics), insufficient (political geography), or infeasible (political history). They are also required in public policy (e.g., for applying the Voting Rights Act) and other academic disciplines ranging from epidemiology and marketing to sociology and quantitative history. Most researchers using aggregate data have encountered some form of the ecological inference problem.

Because the ecological inference problem is caused by the lack of individual-level information, no method of ecological inference, including that estimated by this program, will always produce accurate results. However, potential difficulties are reduced by models that include more available information, diagnostics to evaluate when assumptions need to be modified, easy methods of modifying the assumptions, and uncertainty estimates for quantities of interest. We recommend reviewing Chapter 16 while using this program for actual research. Model dependence defines ecological inference when going anywhere beyond the bounds and tomography plots, and so we have added new graphical procedures for evaluating the degree of model dependence.

eiR is a unifed program that contains methods for both the 2x2 ecological inference case and the RxC case. We will begin by explaining how to use eiR in the 2x2 case, and then move on to RxC examples.

2 Overview: 2x2 R-commands

In this section we describe the basic commands for 2x2 inference. For this purpose, and without loss of generality, we use the running example from the book portrayed in Table 2.3 (page 31). This example uses the proportion of the voting age population who are black (X_i) , the proportion turning out to vote (T_i) , and the number of voting age people (N_i) in each precinct (i = 1, ..., p) to infer the fraction of blacks who vote (β_i^b) and the proportion of whites who vote (β_i^w) , also in each precinct. (For an extended example of eiR, refer to the user's guide below.) An example of a sequence of these commands are as follows:

```
> formula = t ~ x
> dbuf <- ei(formula=formula, total="n",data=data)
> summary(dbuf)
```

```
> eiread(dbuf, "betab", "betaw")
> plot(dbuf, "tomog", "betab", "betaw", "xtfit")
```

In most applications, plot and eiread would likely be run multiple times with different options chosen, and other commands would be included with these five to read in the data (t, x, and n).

• ei: To run the main procedure

Use the format, $\mathtt{dbuf} = \mathtt{ei}(\mathtt{formula,total="n",data=data})$, which takes three $p \times 1$ vectors as inputs: \mathtt{t} (e.g. the fraction of the voting age population turning out to vote); \mathtt{x} (e.g. the fraction of the voting age population who are black); and \mathtt{n} (e.g. the total number of people in the voting age population). The output of this procedure is the list \mathtt{dbuf} (i.e. an output object of class list called a "data buffer"). The data buffer includes the maximium likelihood estimates and simulated quantities of interest from the \mathtt{ei} procedure. After running \mathtt{ei} , it is a good idea to save \mathtt{dbuf} for further analysis. The output data buffer from \mathtt{ei} includes a large variety of different results useful for understanding the results of the analysis. A minimal set of nonrepetitive information is stored in this list (or data buffer), and a large variety of other information can be easily computed from it. Fortunately, you do not need to know whether the information you request is stored or computed as both are treated the same.

To extract information from the data buffer, three procedures are available:

• summary: To obtain a general summary of district-level information summary(dbuf) will produce aggregate information about the ei results. summary will produce a summary of both the maximum likelihood estimates and simulated quantities of interest. It also includes information on the values specified for the prior.

• plot: To graph relevant information

For graphics, use plot(dbuf, "name");, where dbuf is the ei.object that is the output of ei or ei.sim, and name can be any number of a long list of ready-made graphs. For example, plot(dbuf, "tomog") will plot a tomography graph, and plot(dbuf, "xt") will display a scattercross graph. Any number of graphs can be selected in plot for output. For example, plot(dbuf, "tomog", "xt") will produce both a tomography graph and a scattercross graph. Some of the plots can be produced after estimating the maximum likelihood estimates using ei, but before simulating quantities of interest. These initial plots can be useful in determining which priors to include, and the user can opt to choose not to simulate quantities of interest by selecting the option simulate=FALSE. However, for some plots, plot will need the simulated quantities of interest, and therefore can only be plotted when simulate is set to the default, TRUE.

• eiread: To obtain relevant information and numerical results

For numerical information, use $v \leftarrow \text{eiread(dbuf, "name")}$, where v is the item extracted, dbuf is the data buffer output from ei, and name can be any of a list of output possibilities. For example, eiread(dbuf, "betab") will give a vector of point estimates of β_i^b ,

eiread(dbuf, "ci80w") will give 80% confidence intervals for β_i^w . Any number of items can be selected for output. For example, eiread(dbuf, "betab", "ci80b") will produce a list of the point estimates and 80% confidence intervals for β_i^b .

3 User's Guide: An Example

We now show how to use eiR through a simple example. We use data on voter registration and racial background of people from 268 counties in four Southern U.S. States: Florida, Louisiana, and South Carolina. These are the same data used in Chapter 10. The data include the total voting age population in each county (n), the proportion of the population in each county who are black (x), and the proportion of the population in each county who are registered to vote (t). The proportion of whites registered can be computed by (1-x). You can load the data into R using the command

```
> library(ei)
> data(matproii)
```

The statistical goal is to estimate the fraction of blacks registered (β_i^b) and the fraction of whites registered (β_i^w) in each county. These quantities of interest are generally unknown. However, eiR also includes an option that allows the user to assess the reliability of the eiR algorithm when the true quantities of interest are known. To illustrate the use of this "truth" option, the data also include the true fractions of registered blacks (tb) and the true fraction of registered whites (tw).

3.1 The Basic EI Algorithm

To begin, we perform ecological inference by calling the function ei. ei first computes and maximizes a likelihood distribution based on the inputed data, then estimates the county-level quantities of interest based on the possible values, or "bounds", for each county and the overall likelihood distribution.

To run this algorithm, at a minimum we need to have three vectors. Two vectors, \mathbf{t} and \mathbf{x} , contain the aggregate known information about the counties of interest. In this example, \mathbf{t} is the proportion of voters registered in each county, and \mathbf{x} is the proportion of blacks in each county. These two vectors contain aggregate information, since we are interested in the proportion of voters in each country who are black. The last vector we need is \mathbf{n} , the number of people of interest in each county. In this example, \mathbf{n} is the number of people of voting age.

We proceed by performing ecological inference without covariates on the data:

```
> formula = t ~ x
> dbuf = ei(formula=formula,total="n",data=matproii)
```

To include a covariate on β_i^b simply specify a covariate vector for the option Zb, or a string that refers to the name of the covariate in the dataset. Similarly, to include a covariate on β_i^w , specify a covariate vector for the option Zw, or a string that refers to the name of the covariate in the dataset.

Next, we use summary(dbuf) and summary(dbufsim) to obtain general information about the estimation.

```
> summary(dbuf)
Erho = 0.5 , Esigma = 0.5 , Ebeta = 0.5 , N = 268 , Resamp = 35
Maximum likelihood results in scale of estimation (and se's)
    Bb0
           Bw0
                  sigB
                           sigW
                                   rho Zb Zw
 1.2670 1.9348 -1.1151 -1.3272 1.6051
 0.2775 0.2757 0.2132 0.1640 0.3120
Untruncated psi's
            BW
                   SB
                           SW
     BB
                                 RHO
0.9758 1.1411 0.3325 0.2713 0.9082
Truncated psi's (ultimate scale)
     BB
            BW
                   SB
                           SW
                                 R.HO
0.6208 0.8259 0.2006 0.1425 0.7489
Aggregate Bounds
       betab betaw
lower 0.2125 0.7025
upper 0.9754 0.9200
Estimates of Aggregate Quantities of Interest
     mean
Bb 0.5714 0.0253
Bw 0.8177 0.0072
```

The summary function provides basic information about the ecological inference estimation, the maximum likelihood estimates on three scales, and an overall summary of the quantities of interest. First, it reports the values of the priors used in ecological inference (Erho, Esigma, Ebeta). It also reports the number of counties in the dataset (N), as well as the number of importance sampling iterations required to produce estimates of the quantities of interest (resamp).

summary also produces information both about the maximum likelihood estimates and the quantities of interest. First, it provides the maximum likelihood estimates in the scale of estimation. Next, it provides the values of the MLEs when they are transformed into an untruncated bivariate normal distribution. These estimates provide information about the location of the highest density of estimates for the proportion of blacks who are registered to vote and the proportion of whites who are registered to vote. Last, it provides the values of the MLEs on the ultimate truncated bivariate normal scale. These estimates are an unweighted average of the fraction of blacks and whites registered to vote over all the counties in the sample. In this example, the ei algorithm predicts that the unweighted average of the proportion of blacks registered to vote across counties

is 0.57 and the unweighted average of the proportion of whites registered to vote is 0.82.

Finally, summary produces information on aggregate quantities of interest. The aggregate bounds are the mean of the bounds on the proportions of black and white voters, weighted by the population in each county. The aggregate quantities of interest are the weighted mean of the proportion of registered blacks and the proportion of registered whites in each county. In this example the weighted average proportion of blacks who are registered is 0.57, and the weighted average proportion of whites who are registered is 0.82.

3.2 Extracting Quantities of Interest

eiread extracts quantities of interest in a list format from the object dbuf. For example,

```
> bb.out <- eiread(dbuf, "betab", "sbetab")</pre>
```

extracts the point estimates and estimated standard deviations for β_i^b , the estimates of the proportion of registered blacks in each county. The user can then use **bb.out\$betab** to obtain a vector of the point estimates for β_i^b , and **bb.out\$sbetab** to obtain a vector of the standard devations for β_i^b .

eiread() takes any number of arguments to extract any number of quantities of interest from the data buffer. ?eiread can be used to find a list of quantities of interest that are available in EI. Among the most useful arguments are "betab" and "betaw", which report the point estimates; "sbetab" and "sbetaw", which report the standard deviations of the point estimates; and "CI80b and "CI80w", which report the confidence intervals of the point estimates.

3.3 Plotting in EI

Plotting EI output is extremely useful for understanding the results of the ecological inference algorithm and diagnosing problems with estimation. First, we graph a tomography plot of the data (Figure 1).

```
> plot(dbuf, "tomog")
```

Each line on the map represents the possible values for β_i^b and β_i^w for one county. The contour lines identify the portion of the lines that have the highest probability of containing the true estimates of β_i^b and β_i^w . These contour lines provide information about the overall pattern of registration. Note that the area with highest probability is in the upper right-hand corner, where the proportion of whites registered is between 0.75 and 1 and the proportion of blacks registered is between 0.5 and 1. Further, we see that the lines are clustered in the upper half of the figure, indicating that the possible values of β_i^w will have a lower variance than the possible values of β_i^b .

Figure 2 is a double plot of the point estimates and their confidence intervals. To compute this, we call plot to generate two graphs: a tomography plot with the point estimates generated from the algorithm, and a tomography plot with 80% confidence intervals on the point estimate.

```
> plot(dbuf, "tomogE", "tomogCI")
```

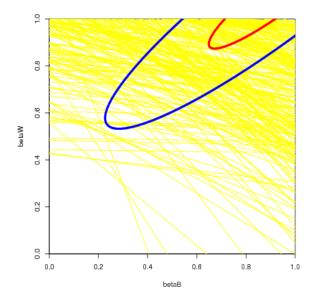


Figure 1: Tomography Plot with ML Contours

This plot is useful to visualize the estimates and confidence intervals for each county. We can see that the point estimates and confidence intervals are clustered in the same area as the contours from the previous plot. Further, the point estimates and confidence intervals only fall on the lines that indicate the possible values of β_i^b and β_i^w .

Figure 3 shows plots that indicate the distribution of β_i^b and β_i^w . To produce these plots, run:

> plot(dbuf, "betab", "betaw")

Density plots are useful to visualize the location and uncertainty of the point estimates. The green line represents the density of the simulated point estimates, and the black tick marks are a rug plot of the point estimates,s β_i^b and β_i^w . You can see that the variance of the point estimates from β_i^b is much higher than the variance of point estimates from β_i^w .

Figure 4 portrays the results of the EI algorithm by plotting the proportion of blacks in each country by the proportion of registered voters in each country. To produce this plot, use:

> plot(dbuf, "xtfit")

The circles around each of the points in this plot are proportional to the population of each county. The graph represents the likelihood estimates by plotting the expected number of registered voters given the proportion of blacks in each county, represented by the yellow line. The red lines in the plot are the 80% confidence interval around the regression line. The higher uncertainty in the estimates of black registration can be seen by the absence of points on the right hand side of the graph and the larger confidence interval on the right hand side of the graph, where the proportion of blacks in the county is relatively large.

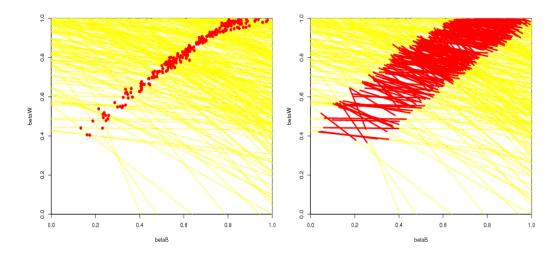


Figure 2: Tomography Plots: Point Estimates (left) and Confidence Intervals (right)

Finally, if we have data on the true proportions of registered blacks and registered whites in each county, as we do in this dataset, we can use plots in EI to assess how well the algorithm works on the given data. To do this, rerun the ei algorithm, adding the truth vectors, tb and tw as the truth argument.

```
> truth = cbind(matproii$tb,matproii$tw)
> formula = t ~ x
> dbuf = ei(formula=formula,total="n",data=matproii,truth=truth)
```

Then use plot to compare the estimates of the EI algorithm to the true proportions of white and black registered voters in each county.

```
> plot(dbuf, "truth")
```

The "truth" plot (Figure 5) has four components. The top two figures have the posterior densities of the aggregate quantities of interest B^b and B^w . These densities tell us in what range the algorithm predicts that the point estimates lie. For example, the density of B^b is wider than the density of B^w , indicating that our estimates of B^w lie in a smaller range than than our estimates of B^b . The true aggregate values, computed from the **truth** data we inputed, are indicated by the vertical bars. The fact that the true B^b and B^w are within the densities we computed confirms that the model is did a good job at predicting the true proportions of registered white and black voters.

The bottom two figures in Figure 5 plot the estimated values of β_i^b and β_i^w against the true values. The size of each of the circles plotted is proportional to the number of blacks in the county in the first graph and the number of whites in each county in the second graph. If the estimated values were exactly equal to the true values, all of the points would be on the 45° line. Because the points fall quite close to the 45° and do not deviate from the line in a systematic way, we can see that the EI algorithm predicts the point estimates quite well.

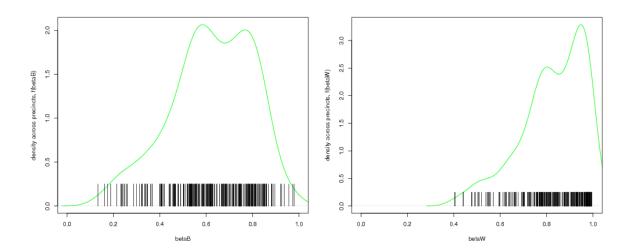


Figure 3: Plots with Distribution of Point Estimates for β_i^b (left) and β_i^w (right), for all i

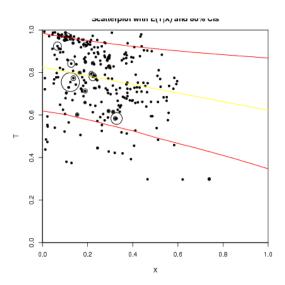


Figure 4: X and T Scatterplot with $\mathrm{E}(\mathrm{T}|\mathrm{X})$ and 80% CIs

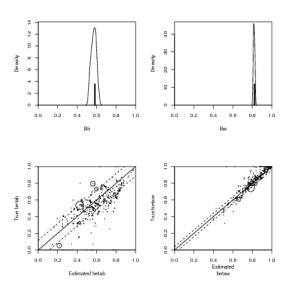


Figure 5: Comparing Estimates to the Truth at the County Level

4 Overview:eiRxC R-commands

Although the 2x2 case is useful in many circumstances, eiR also allows users to expand beyond the 2x2 case and implement RxC models. To do this, eiR contains the MCMC implementation of the multinomial-Dirichlet eiRxC model in Rosen, Jiang, King and Tanner (2001) "Bayesian and Frequentist Inference for Ecological Inferece: The RxC Case." (Statistica Neerlandica, Vol. 55, nr.2, pp 134-156), and incorporates R code from eiPack (Olivia Lau, Ryan Moore and Mike Kellermann).

In this section we describe the basic commands needed for eiRxC. Imagine that instead of a 2x2 table where the user aims to infer the proportion of whites and non-whites who turned out to vote, for example, the user instead wants to infer the percent of turnout for white, black, and hispanic. This is a 2x3 table because the resulting estimates from this table will include two estimates (percent turnout and no turnout) for three categories of people (white, black and hispanic).

We use the data RxCdata as a running example. RxCdata has variables for each of the five marginal variables for the 2x3 table: turnout is the number of people in each precinct who turned out to vote, noturnout is the number of people in each precinct that did not turn out to vote, white is the number of people who are white in the precinct, black is the number of people who are black in the precinct, and hisp is the number of people who are hispanic in the precinct. Note that, different that the 2x2 case, these are the numbers of people rather than proportions. The user can include proportions if they want to, but then must include the argument total for the total number of people in the precinct.

To begin, we load the RxC data from the eiR library.

> data(RxCdata)

The formula for the eiRxC case tells the program which variables go on each side of the table. In this example, we have turnout and no turnout on one side of the table, and white, black and hispanic on the other side. Therefore, our formula is:

> formula <- cbind(turnout, noturnout) ~ cbind(white, black, hisp)

We can call this formula using ei:

> dbuf = ei(formula, data=RxCdata)

The MCMC output for the β 's can be found in the data buffer dbuf. dbuf\$draws\$Beta is a matrix that contains the simulations for each of the β 's for each precinct. Since there are 60 precincts in this dataset and 6 quantities of interest, the number of columns of dbuf\$draws\$Beta is 60*6=360. We can analyze the MCMC output by picking out which β we are interested at any given time. For example, to look at the MCMC output for the estimated percent white turnout for the third precinct we can use the R code:

```
> out <- dbuf$draws$Beta[,"beta.white.turnout.3"]
> summary(out)
```

Iterations = 1:1000
Thinning interval = 1
Number of chains = 1
Sample size per chain = 1000

1. Empirical mean and standard deviation for each variable, plus standard error of the mean:

Mean SD Naive SE Time-series SE 0.430233 0.035612 0.001126 0.003312

2. Quantiles for each variable:

2.5% 25% 50% 75% 97.5% 0.3615 0.4078 0.4306 0.4552 0.5007

We can also plot this MCMC output to assess convergence:

> plot(out)

From this output we can get the empirical mean and standard deviation of each of our quantities of interest. The user can add in extra arguments to specify the number of simulations, burnin, or priors for this function. For more information on this, see the documentation for eiPack and the Rosen et al (2001) paper.

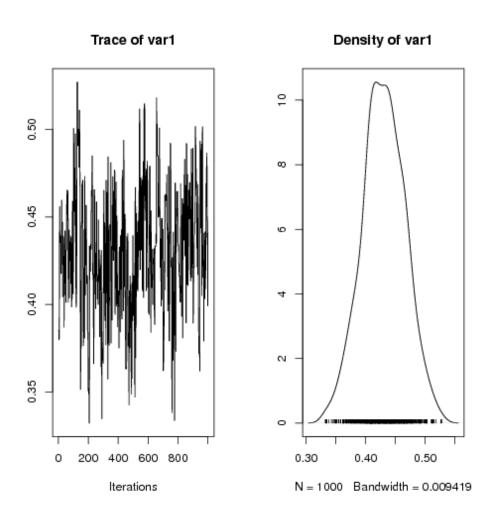


Figure 6: MCMC Output for % White Turnout in Precinct 3

5 eiRxC Tomography Plots: Assessing Model Dependence

While eiRxC model estimates are helpful, the uncertainty estimates they produce are — like all ecological inference point estimates — conditional on the model assumed. Yet, most of the actual scientific uncertainty in ei models does not stem from the sampling uncertainty given a statistical model, but rather the uncertainty associated with choosing a model — what is known as model dependence (?). A tomography plot that contains information about the possible values of the quantities of interest is therefore more useful than the model in understanding the true amount of information in the data from which the model is obtaining its estimates.

While this has not been available in the RxC case before, we have developed a method to creating and displaying tomography plots for 2x3 RxC problems and by extension examine model dependence in any RxC model.

In the 2x3 case, we can do this by using the function tomogRxC. Following the code above, using the RxCdata,

```
> formula <- cbind(turnout, noturnout) ~ cbind(white, black, hisp)
> tomogRxC(formula, RxCdata)
```

Each of the polygons on the plot below represent all the possibile values in a given precinct for percent white turnout and percent black turnout. The plot follows what we call the Law of Conservation of Ink, where tomography polygons with more information (smaller polygons) are colored brighter than those with less information (larger polygons). The colors on the plot are a heat map that are brighter when polygons overlap each other. The polygons in this particular district contain a lot of information about the percent white turnout, as the vast majority of the polygons only contain low values of percent white turnout, but they contain very little information about the percent black turnout, as most of the polygons seem to cover the entire range possible for percent black turnout.

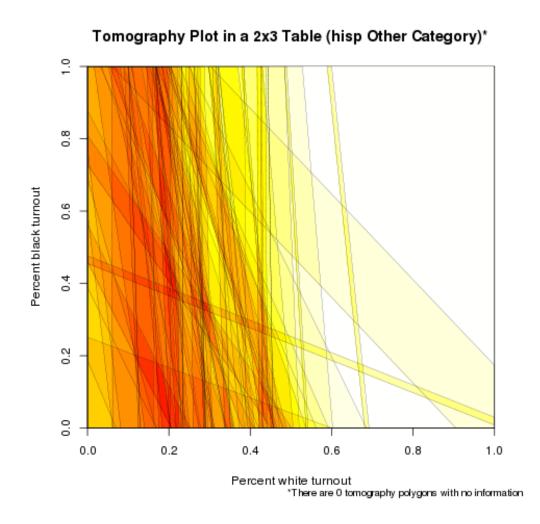


Figure 7: 2x3 Tomography Plot: % White Turnout and % Black Turnout

Figure 8: 2x3 Tomography Plot: % White Turnout and % Hispanic Turnout

Percent white turnout

*There are 1 tomography polygons with no information

The quantity of interest percent hispanic turnout is left out of this tomography plot, since we can only graph two quantities of interest simulataneously. However, if we reorganize the formula, putting white and hispanic first on the right hand side of the formula, we can create another tomography plot that expores the deterministic information for percent white turnout and percent hispanic turnout.

> formula <- cbind(turnout, noturnout) ~ cbind(white, hisp, black)
> tomogRxC(formula, RxCdata)

With this new tomography plot (in Figure 8), we find very similar results to the previous one. While we have quite a bit of information about the percent white turnout, we have less information about percent hispanic turnout. This result derives from the fact that there are very few hispanics and blacks in this particular district.

Tomography Plot in a 2x3 Table (white Other Category)* 0.4 0.0 0.0 0.0 0.2 0.4 0.6 0.8 1.0

Figure 9: 2x3 Tomography Plot: % Hispanic Turnout and % Black Turnout

Percent hisp turnout

There are 34 tomography polygons with no information

Last, we can plot the remaining two quantities of interest – percent black turnout and percent hispanic turnout– against each other:

- > formula <- cbind(turnout, noturnout) ~ cbind(hisp, black, white)
 > tomogRxC(formula, RxCdata)
- Here we see that even though the informative polygons indicate low values of percent hispanic and black turnout, we have the least information about the intersection of percent black and hispanic turnout. The polygons are spread all across the unit square space, indicating that the possible values for percent black and hispanic turnout spread over a large area. In the bottom right hand corner, and on the R console, the tomography plot reports how many of the tomography polygons have no information, or how many tomography polygons cover the entire unit square. Here we see that ther are 34 tomography polygons with no information, and since we onlyhave 60 precincts, this means that we have very little information for these quantities of interest. We

might be more confident in the estimates for white turnout in this RxC analysis than for black and hispanic turnout.

6 Reference to EI Functions

6.1 ei: Ecological Inference Estimation

Description

ei is the main command in the package EI. It gives observation-level estimates (and various related statistics) of β_i^b and β_i^w given variables T_i and X_i (i=1,...,n) in this accounting identity: $T_i = \beta_i^b * X_i + \beta_i^w * (1-X_i)$. Results are stored in an ei object, that can be read with summary() or eiread() and graphed in plot().

Usage

ei(formula, total, id, data, Zb=1, Zw=1,data=NA, erho=.5, esigma=.5, ebeta=.5, ealphab=NA, ealphaw=NA, truth=NA, precision=4)

Arguments

formula	A formula of the form t x in the $2x2$ case and $cbind(col1, col2,)$ $cbind(row1, row2,)$ in the RxC case.
n	'total' is the name of the variable in the dataset that contains the number of individuals in each unit
id	'id' is the nae of the variable in the dataset that identifies the precinct. Used for 'movie' and 'movieD' plot functions.
Zb	$p \ge k^b$ matrix of covariates or the name of covariates in the dataset
Zw	$p \ge k^w$ matrix of covariates or the name of covariates in the dataset
data	optional data frame that if specified should contain t,x,n. If using covariates and data is specified, data should also contain Zb and Zw.
erho	The standard deviation of the normal prior on ϕ_5 for the correlation. Default = 0.5.
esigma	The standard deviation of an underlying normal distribution, from which a half normal is constructed as a prior for both $\check{\sigma}_b$ and $\check{\sigma}_w$. Default = 0.5
ebeta	Standard deviation of the "flat normal" prior on \check{B}^b and \check{B}^w . The flat normal prior is uniform within the unit square and dropping outside the square according to the normal distribution. Set to zero for no prior. Setting to positive values probabilistically keeps the estimated mode within the unit square. Default= 0.5
ealphab	cols(Zb) x 2 matrix of means (in the first column) and standard deviations (in the second) of an independent normal prior distribution on elements of α^b . If you specify Zb, you should probably specify a prior, at least with mean zero and some variance (default is no prior). (See Equation 9.2, page 170, to interpret α^b).
ealphaw	$\operatorname{cols}(\operatorname{Zw}) \times 2$ matrix of means (in the first column) and standard deviations (in the second) of an independent normal prior distribution on elements of α^w .

If you specify Zw, you should probably specify a prior, at least with mean zero and some variance (default is no prior). (See Equation 9.2, page 170, to interpret α^w).

interpret α^{ω}).

truth A length(t) x 2 matrix of the true values of the quantities of interest.

precision The number of decimal places that are printed in summary and eiread func-

tions.

... see documentation in eiPack for options for RxC ei.

Details

The EI algorithm is run using the ei command. A summary of the results can be seen graphically using plot(ei.object) or numerically using summary(ei.object). Quantities of interest can be calculated using eiread(ei.object).

Author(s)

Gary King ■email: king@harvard.edu■ and Molly Roberts ■email: roberts8@fas.harvard.edu■

References

Gary King (1997). A Solution to the Ecological Inference Problem. Princeton: University Press.

Examples

```
data(sample)
form <- t ~ x
dbuf <- ei(form,total="n",data=sample)
summary(dbuf)</pre>
```

eiread: Quantities of Interest from Ecological Inference Estimation

Description

eiread is the command that pulls quantities of interest from the ei object. The command returns a list of quantities of interest requested by the user.

Usage

```
eiread(ei.object, ...)
```

Arguments

CI80w

ei.object An ei object from the function ei.

A list of quantities of interest for eiread() to return. See values below.

Value

 $p \ge 1$ point estimate of β_i^b based on its mean posterior. See section 8.2 betab $p \times 1$ point estimate of β_i^w based on its mean posterior. See section 8.2 betaw $p \times 1$ standard error for the estimate of β_i^b , based on the standard deviation of sbetab its posterior. See section 8.2 $p \times 1$ standard error for the estimate of β_i^w , based on the standard deviation of sbetaw its posterior. See section 8.2 phi Maximum posterior estimates of the CML Matrix of random simulations of ψ . See section 8.2 psisims $p \ge 4$: bounds on β_i^b and β_i^w , lower B ~ upper B ~ lower W ~ upper W. See Chapter bounds 2 x 2: aggregate bounds rows:lower, upper; columns: betab, betaw. See Chapabounds ter 5. Simulations of district-level quantities of interest \hat{B}^b and \hat{B}^w . See Section 8.3. aggs Point estimate of 2 district-level parameters, \hat{B}^b and \hat{B}^w based on the mean of maggs aggs. See Section 8.3. Variance matrix of 2 district-level parameters, \hat{B}^b and \hat{B}^w . See Section 8.3. **VCaggs** $p \ge 2$: lower upper 80% confidence intervals for β_i^b . See section 8.2. CI80b

 $p\ge 2$: lower~upper 80% confidence intervals for β_i^w . See section 8.2.

Regressions of estimated β_i^b and β_i^w on a constant term and X_i . eaggbias

Goodman's Regression. See Section 3.1 goodman

References

Gary King (1997). A Solution to the Ecological Inference Problem. Princeton: University Press.

Examples

```
data(sample)
formula = t ~ x
dbuf <- ei(formula=formula, total="n",data=sample)
eiread(dbuf, "phi")
eiread(dbuf, "betab", "betaw")</pre>
```

6.3 plot.ei: Plotting Ecological Inference Estimates

Description

'plot' method for the class 'ei'.

Usage

```
plot.ei(ei.object, ...)
```

Arguments

ei.object An ei object from the function ei.

... A list of options to return in graphs. See values below.

Value

tomogD Tomography plot with the data only. See Figure 5.1, page 81.

tomog Tomography plot with ML contours. See Figure 10.2, page 204.

Tomography plot with 80% confidence intervals. Confidence intervals appear on the screen in red with the remainder of the tomography line in yellow. The confidence interval portion is also printed thicker than the rest of the line. See

Figure 9.5, page 179.

tomogCI95 Tomography plot with 95% confidence intervals. Confidence intervals appear

on the screen in red with the remainder of the tomography line in yellow. The confidence interval portion is also printed thicker than the rest of the line. See

Figure 9.5, page 179.

tomogE Tomography plot with estimated mean posterior β_i^b and β_i^w points.

tomogP Tomography plot with mean posterior contours.

betab Density estimate (i.e., a smooth version of a histogram) of point estimates of

 β_i^b 's with whiskers.

betaw Density estimate (i.e., a smooth version of a histogram) of point estimates of

 β_i^w 's with whiskers.

xt Basic X_i by T_i scatterplot.

xtc Basic X_i by T_i scatterplot with circles sized proportional to N_i .

xtfit X_i by T_i plot with estimated $E(T_i|X_i)$ and conditional 80% confidence intervals.

See Figure 10.3, page 206.

xtfitg xtfit with Goodman's regression line superimposed.

estsims All the simulated β_i^b 's by all the simulated β_i^w 's. The simulations should take

roughly the same shape of the mean posterior contours, except for those sam-

pled from outlier tomography lines.

boundXb X_i by the bounds on β_i^b (each precinct appears as one vertical line), see the

lines in the left graph in Figure 13.2, page 238.

boundXw X_i by the bounds on β_i^w (each precinct appears as one vertical line), see the

lines in the right graph in Figure 13.2, page 238.

truth Compares truth to estimates at the district and precinct-level. Requires truth

in the ei object. See Figures 10.4 (page 208) and 10.5 (page 210).

movieD For each observation, one tomography plot appears with the line for the partic-

ular observation darkened. After the graph for each observation appears, the user can choose to view the next observation (hit return), jump to a specific observation number (type in the number and hit return), or stop (hit "s" and

return).

References

Gary King (1997). A Solution to the Ecological Inference Problem. Princeton: University Press.

Examples

```
data(sample)
formula = t ~ x
dbuf <- ei(formula=formula, total="n",data=sample)
plot(dbuf, "tomog")
plot(dbuf, "tomog", "betab", "betaw", "xtfit")</pre>
```

6.4 tomogRxC: Plotting Ecological Inference Estimates with eiRxC information Usage

tomogRxC(formula, data, total=NULL, refine=100)

Arguments

formula A formula of the form cbind(col1, col2,...)~cbind(row1,row2,...)

data that contains the data that corresponds to the formula

total 'total' is the name of the variable in the dataset that contains the number of

individuals in each unit

refine specifies the amount of refinement for the image. Higher numbers mean better

resolution.

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References

Gary King (1997). A Solution to the Ecological Inference Problem. Princeton: University Press.

Examples

```
data(RxCsample)
formula = cbind(turnout, noturnout) ~ cbind(white, black,hisp)
tomogRxC(formula, data=RxCsample)
```

References

Gary King, A Solution to the Ecological Inference Problem: Reconstructing Individual Behaviour from Aggregate Data, Princeton University Press (1997).

Lau et al, "eiPack: Ecological Inference and Higher-Dimension Dtaa Management." http://www.olivialau.org/software.

Rosen et al, "Bayesian and Frequentist Inference for Ecological Inference: The RxC Case." *Statistica Neerlandica*, 55:2, pp 134-156, 2001.

Useful documentation also avalaible at http://GKing.Harvard.Edu.

For R language see http://www.r-project.org.

Venables, W.N., and Ripley, B.D., Statistics and Computing, Springer (2002).