

# PHOENIX: Pauli-based High-level Optimization Engine for Instruction Execution on NISQ Devices

---

## Algorithm 1: Pauli Strings Simplification in BSF

---

**Input :** Pauli strings list  $pls$   
**Output:** Reconfigured circuit components list  $cfg$

```

1  $cfg \leftarrow \emptyset$ ;  $bsf \leftarrow \text{BSF}(pls)$ ;  $cliffs\_with\_locals \leftarrow \emptyset$ ;
2 while  $bsf.TOTALWEIGHT() > 2$  do
3    $local\_bsf \leftarrow bsf.POPLOCALPAULIS()$ ;
4    $C \leftarrow \emptyset$ ; // Clifford2Q candidates
5    $B \leftarrow \emptyset$ ; // Each element of  $B$  results
   from applying each Clifford2Q
   candidate on  $bsf$ 
6    $costs \leftarrow \emptyset$ ; // Cost functions calculated
   on each element of  $B$ 
7   for  $cg$  in  $CLIFFORD\_2Q\_SET$  do
8     for  $i, j$  in  $COMBINATIONS(RANGE(n), 2)$  do
9        $cliff \leftarrow cg.ON(i, j)$ ; // qubits acted on
10       $bsf' \leftarrow bsf.APPLYCLIFFORD2Q(cliff)$ ;
11       $cost \leftarrow \text{CALCULATEBSFCOST}(bsf')$ ;
12       $C.APPEND(cliff)$ ;
13       $B.APPEND(bsf')$ ;
14       $costs.APPEND(cost)$ ;
15    end
16  end
17   $bsf \leftarrow \text{BSFWITHMINCOST}(B, costs)$ ;
18   $cliff \leftarrow \text{CLIFFORDWITHMINCOST}(C, costs)$ ;
19   $cliffs\_with\_locals.APPEND((cliff, local\_bsf))$ ;
20 end

21  $cfg.APPEND(bsf)$ ;
22 for  $cliff, local\_bsf$  in  $cliffs\_with\_locals$  do
   // Clifford2Q operators are added as
   conjugations, with local Pauli
   strings peeled before each epoch
23   $cfg.PREPEND(cliff)$ ;
24   $cfg.APPEND(local\_bsf)$ ;
25   $cfg.APPEND(cliff)$ ;
26 end

```

---

*Abstract—Quantum computing ...*

We propose a Pauli-based High-level Optimization Engine for Instruction eXecution (PHOENIX) of Hamiltonian simulation programs on NISQ devices

## I. INTRODUCTION

Quantum computing ...

## II. MOTIVATION

[ZY: Motivation and preliminary knowledge]

## III. OUR PROPSAL: PHOENIX

- A. Overall framework
- B. BSF simplification for each IR group
- C. Ordering of IR groups

## IV. EVALUATION

- A. Experimental settings
  - 1) Baselines:
    - TKET
    - PAULIHEDRAL
    - TETRIS
- B. Benchmarking on generic Hamiltonian simulation programs
- C. Hardware-aware benchmarking across UCCSD programs
- D. Pass-wise breakdown analysis
- E. Real system evaluation
- F. Scalability