

PHOENIX: Pauli-based High-level Optimization Engine for Instruction Execution on NISQ Devices

Algorithm 1: Pauli Strings Simplification in BSF

Input : Pauli strings list pls
Output: Reconfigured circuit components list cfg

```

1  $cfg \leftarrow \emptyset$ ;  $bsf \leftarrow \text{BSF}(pls)$ ;  $cliffs\_with\_locals \leftarrow \emptyset$ ;
2 while  $bsf.TOTALWEIGHT() > 2$  do
3    $local\_bsf \leftarrow bsf.POPLOCALPAULIS()$ ;
4    $C \leftarrow \emptyset$ ; // Clifford2Q candidates
5    $B \leftarrow \emptyset$ ; // Each element of  $B$  results
   from applying each Clifford2Q
   candidate on  $bsf$ 
6    $costs \leftarrow \emptyset$ ; // Cost functions calculated
   on each element of  $B$ 
7   for  $cg$  in  $\text{CLIFFORD\_2Q\_SET}$  do
8     for  $i, j$  in  $\text{COMBINATIONS}(\text{RANGE}(n), 2)$  do
9        $cliff \leftarrow cg.ON(i, j)$ ; // qubits acted on
10       $bsf' \leftarrow bsf.APPLYCLIFFORD2Q(cliff)$ ;
11       $cost \leftarrow \text{CALCULATEBSFCOST}(bsf')$ ;
12       $C.APPEND(cliff)$ ;
13       $B.APPEND(bsf')$ ;
14       $costs.APPEND(cost)$ ;
15     end
16   end
17    $bsf \leftarrow \text{BSFWITHMINCOST}(B, costs)$ ;
18    $cliff \leftarrow \text{CLIFFORDWITHMINCOST}(C, costs)$ ;
19    $cliffs\_with\_locals.APPEND((cliff, local\_bsf))$ ;
20 end

21  $cfg.APPEND(bsf)$ ;
22 for  $cliff, local\_bsf$  in  $cliffs\_with\_locals$  do
   // Clifford2Q operators are added as
   conjugations, with local Pauli
   strings peeled before each epoch
23    $cfg.PREPEND(cliff)$ ;
24    $cfg.APPEND(local\_bsf)$ ;
25    $cfg.APPEND(cliff)$ ;
26 end

```

Abstract—Quantum computing ...

We propose a Pauli-based High-level Optimization Engine for Instruction eXecution (PHOENIX) of Hamiltonian simulation programs on NISQ devices

I. INTRODUCTION

Quantum computing ...

II. MOTIVATION

[ZY: Motivation and preliminary knowledge]

TABLE I
UCCSD BENCHMARK SUITE.

Benchmark	#Qubit	#Pauli	w_{\max}	#Gate	#CNOT	Depth	Depth-2Q
CH2_cmplt_BK	14	1488	10	37780	19574	23568	19399
CH2_cmplt_JW	14	1488	14	34280	21072	23700	19749
CH2_frz_BK	12	828	10	19880	10228	12559	10174
CH2_frz_JW	12	828	12	17658	10344	11914	9706
H2O_cmplt_BK	14	1000	10	25238	13108	15797	12976
H2O_cmplt_JW	14	1000	14	23210	14360	16264	13576
H2O_frz_BK	12	640	10	15624	8004	9691	7934
H2O_frz_JW	12	640	12	13704	8064	9332	7613
LiH_cmplt_BK	12	640	10	16762	8680	10509	8637
LiH_cmplt_JW	12	640	12	13700	8064	9342	7616
LiH_frz_BK	10	144	9	2890	1442	1868	1438
LiH_frz_JW	10	144	10	2850	1616	1985	1576
NH_cmplt_BK	12	640	10	15624	8004	9691	7934
NH_cmplt_JW	12	640	12	13704	8064	9332	7613
NH_frz_BK	10	360	9	8303	4178	5214	4160
NH_frz_JW	10	360	10	7046	3896	4640	3674

III. OUR PROPSAL: PHOENIX

- A. Overall framework
- B. BSF simplification for each IR group
- C. Ordering of IR groups

IV. EVALUATION

- A. Experimental settings
- B. Benchmarks
 - 1) Metrics:
 - 2) Baselines:
 - TKET
 - PAULIHEDRAL
 - TETRIS
- C. Logical-level compilation
- D. Breakdown analysis
- E. QAOA benchmarking
- F. Hardware-aware compilation
- G. Diverse ISA comparison
- H. Real system evaluation
- I. Scalability

TABLE II
QAOA BENCHMARKING VERSUS 2QAN.

tables/qaqa.tex tab:qaqa

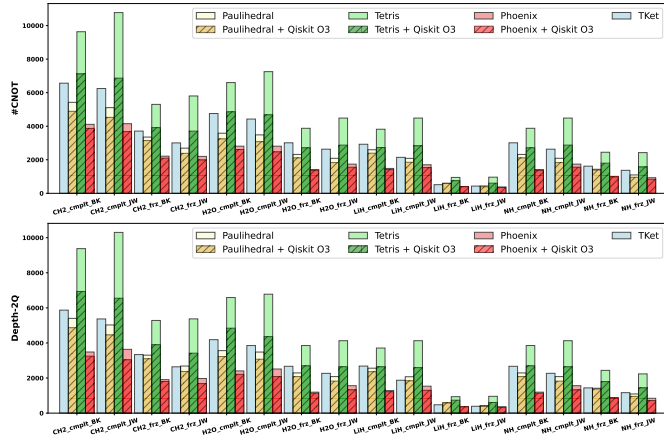


Fig. 1. Benchmarking on logical-level synthesis (all2all topology)

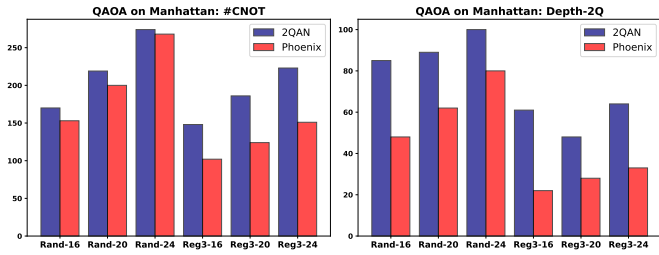


Fig. 2. QAOA benchmarking

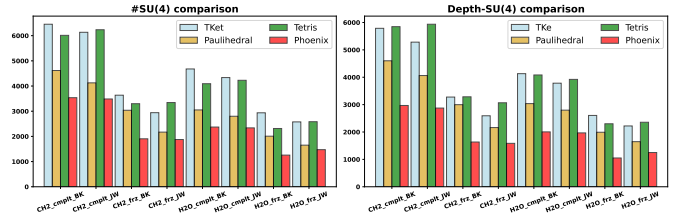


Fig. 5. SU(4) ISA comparison

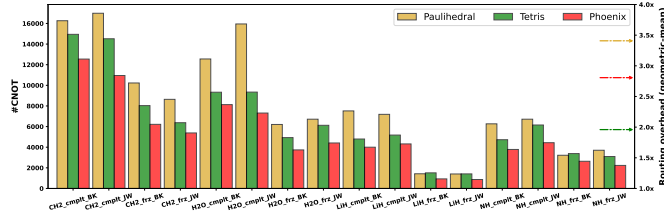


Fig. 3. Hardware-aware compilation for limited-topology NISQ device

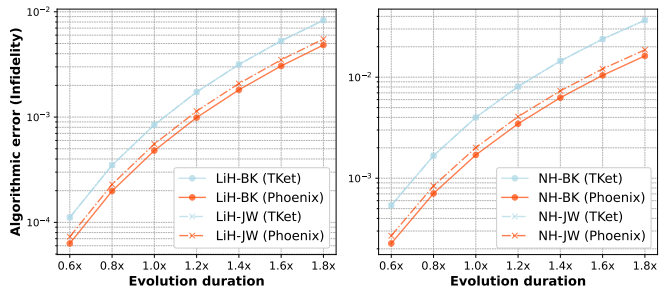


Fig. 4. Algorithmic error