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## Exercise - 1

Given  $\hat{y} = [0.5 \quad -4.5 \quad -9.5]^T$   
 $y = [0 \quad -4 \quad -9]^T$

a) RMSE = 
$$\sqrt{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{n}}$$
  
$$= \sqrt{\frac{[(0.5 - 0)^2 + (-4.5 - (-4))^2 + (-9.5 - (-9))^2]}{3}}$$
  
$$= \sqrt{\frac{3 \times (0.5)^2}{3}} = 0.5$$

b) MAE = 
$$\frac{\sum_{i=1}^n |\hat{y}_i - y_i|}{n}$$
  
$$= \frac{1}{3} [ |0.5 - 0| + |-4.5 - (-4)| + |-9.5 - (-9)| ]$$
  
$$= \frac{3 \times 0.5}{3}$$
  
$$= 0.5$$

c)  $\|y\|_0$  = Total number of non-zero elements

$$= 2 \quad \text{i.e., } -4.5 \text{ and } -9.5$$

$$\begin{aligned} d) \quad \|y\|_1 &= |0| + |-4| + |-9| \\ &= 13 \end{aligned}$$

$$\begin{aligned} e) \quad \|y\|_2 &= \sqrt{0^2 + (-4)^2 + (-9)^2} \\ &= \sqrt{97} \\ &\approx 9.85 \end{aligned}$$

$$\begin{aligned} f) \quad \|y\|_\infty &= \text{Maximum absolute value} \\ &= 9 \end{aligned}$$