ELSEVIER

Contents lists available at ScienceDirect

# Journal of Quantitative Spectroscopy & Radiative Transfer

journal homepage: www.elsevier.com/locate/jqsrt



### High resolution study of ${}^{M}$ GeH<sub>4</sub> (M=76,74) in the dyad region



O.N. Ulenikov <sup>a,b,\*</sup>, O.V. Gromova <sup>a,b</sup>, E.S. Bekhtereva <sup>a,b</sup>, N.I. Raspopova <sup>a,b</sup>, P.G. Sennikov <sup>c</sup>, M.A. Koshelev <sup>c,d,e</sup>, I.A. Velmuzhova <sup>c</sup>, A.P. Velmuzhov <sup>c,e</sup>, A.D. Bulanov <sup>c,e</sup>

- <sup>a</sup> Institute of Physics and Technology, National Research Tomsk Polytechnic University, Tomsk 634050, Russia
- <sup>b</sup> Physics Department, National Research Tomsk State University, Tomsk 634050, Russia
- <sup>c</sup> G.G. Devyatykh Institute of Chemistry of High Purity Substances, Russian Academy of Sciences, 603950 Nizhny Novgorod, Russia
- <sup>d</sup> Institute of Applied Physics, Russian Academy of Sciences, 603950 Nizhny Novgorod, Russia
- e N.I. Lobachevsky State University of Nizhni Novgorod, National Research University, 603950 Nizhny Novgorod, Russia

#### ARTICLE INFO

#### Article history: Received 17 November 2013 Received in revised form 20 March 2014 Accepted 23 March 2014 Available online 29 March 2014

Keywords: Dyad of GeH<sub>4</sub> states High resolution spectra of GeH<sub>4</sub> Spectroscopic parameters

#### ABSTRACT

The infrared spectrum of GeH<sub>4</sub> (88.1% of <sup>76</sup>GeH<sub>4</sub>, 11.5% of <sup>74</sup>GeH<sub>4</sub>, and minor amounts of three other stable isotopic species in the sample) was measured in the 700–1080 cm<sup>-1</sup> region with a Bruker IFS 125HR Fourier transform interferometer (Nizhny Novgorod, Russia) and analyzed. 1922 transitions with  $J^{max}$  = 26 were assigned to the  $\nu_4$  and  $\nu_2$  bands of <sup>76</sup>GeH<sub>4</sub> ( $\nu_2$  is a symmetry forbidden absorption band, and its transitions appear in the spectrum only because of strong Coriolis interaction with the  $\nu_4$  band). Rotational, centrifugal distortion, tetrahedral splitting, and interaction parameters for the ground, (0100) and (0001) vibrational states were determined from the fit of experimental line positions. The obtained set of parameters reproduces the initial experimental data with an accuracy close to experimental uncertainties. The result of analogous analysis of the <sup>74</sup>GeH<sub>4</sub> isotopologue (the number of assigned transitions is 788) is also presented.

© 2014 Elsevier Ltd. All rights reserved.

#### 1. Introduction

Germane in a natural isotopic composition is used for producing high-purity germanium. Various physical devices (e.g., high-sensitivity detectors of nuclear radiation) are manufactured on its base [1]. Germane is one of the important components of the atmospheres of giant gas-planets, such as Jupiter and Saturn [2–4], and its presence should be taken into account when studying their atmospheric composition and chemistry. In particular, in the atmospheres of Jupiter and Saturn germane was detected at abundances orders of magnitude greater than their thermochemical equilibrium values in the upper

tropospheres [5]. For that reason, laboratory investigations of high resolution spectra of germane are interesting and important.

Germane in a natural isotopic composition produces complex infrared spectra, first of all because of the existence of five stable isotopologues with mass numbers 70 (20.55%), 72 (27.37%), 73 (7.67%), 74 (36.74%), and 76 (7.67%). Additional complexity of the germane spectra arises from the presence of very strong Coriolis interaction between its two deformational fundamentals  $\nu_2$  and  $\nu_4$ . GeH<sub>4</sub> is a spherical top molecule, hence, it has no permanent dipole moment, and capabilities of the Ground State Combination Differences method (which is very efficient for studying the molecules of other type) are very limited as applied to germane.

Spectra of different  ${}^{M}GeH_{4}$  (M=70, 72, 73, 74, 76) isotopologues of germane were the objects of study for

<sup>\*</sup>Corresponding author. Institute of Physics and Technology, National Research Tomsk Polytechnic University, Tomsk 634050, Russia.

E-mail address: Ulenikov@mail.ru (O.N. Ulenikov).

many years (see, e.g., Refs. [6-40]). Up to 1972 the spectra were recorded with low or medium resolution. Starting with 1973, Oka with co-authors extensively studied pure rotational spectra of the XH<sub>4</sub> (T<sub>d</sub> symmetry) molecules (X=C, Ge, Si) by the method of infrared-microwave double resonance [17-21]. The first high resolution infrared spectrum of germane ( $\nu_3$  and  $2\nu_3$  bands of all five isotopologues) was studied in Ref.[25]. High resolution spectra of high excited overtone stretching bands of germane were extensively discussed in a number of papers by Zhu and co-authors [34–40], in the frame of the local mode model. As to the bending bands, only the  $\nu_2$  and  $\nu_4$  fundamentals were analyzed earlier with high resolution [27,29,31,32]. Besides, only spectra in separate narrow regions of the  $\nu_2$ and  $\nu_4$  bands were discussed even for the mostly abundant germane species. For that reason, high resolution analysis of the  $\nu_2$  and  $\nu_4$  bands of any isotopic species of germane in a wide spectral region is suitable and timely.

In this paper we present results of the analysis of the high resolution Fourier transformed spectrum of  $^{M}$ GeH<sub>4</sub> (M=74, 76) in the 700–1080 cm $^{-1}$  region where the  $\nu_{2}$  and  $\nu_{4}$  bands are located. The experimental details are given in Section 2. The theoretical background of our study is briefly discussed in Section 3. Results and discussion are presented in Section 4.

#### 2. Experimental details

A sample of germane containing <sup>76</sup>GeH<sub>4</sub> (88.1%), <sup>74</sup>GeH<sub>4</sub> (11.5%), <sup>73</sup>GeH<sub>4</sub> (0.07%), <sup>72</sup>GeH<sub>4</sub> (0.17%), and <sup>70</sup>GeH<sub>4</sub> (0.12%) was used in the present study. First, the sample of germane in natural abundance was synthesized at the Institute of Chemistry of High-Purity Substances of the Russian Academy of Sciences by a reaction between GeCl<sub>4</sub> and sodium borohydride with subsequent purification by the rectification method. Then the sample was enriched with the <sup>76</sup>Ge isotope using the centrifugal method at the Joint Stock Company "Production Association Electrochemical Plant", Zelenogorsk, Russia. The enriched sample was repeatedly purified by the rectification method. Finally, the amount of hydrocarbon, carbon dioxide, di-, and tri-germane impurities in the sample enriched with  $^{76}$ Ge was less than  $10^{-5}$  mol%,  $10^{-4}$  mol%,  $10^{-1}$ – $10^{-3}$  mol %, respectively. The amount of the other impurities was less than  $3 \times 10^{-5}$  mol%

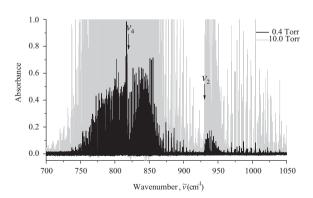
The high-resolution spectra of GeH<sub>4</sub> were recorded at room temperature in the 700–1080 cm<sup>-1</sup> wavenumber range with a Bruker IFS125HR Fourier transform spectrometer (Institute of Chemistry of High-Purity Substances, Nizhny Novgorod, Russia) equipped with a Globar source, a KBr beamsplitter and a liquid nitrogen cooled mercury-cadmium-telluride detector. The aperture size was 1.7 mm. The resolution due to the maximum optical path difference was 0.003 cm<sup>-1</sup> and the Norton-Beer (weak) apodization function was applied. A single-pass 20-cm cell equipped with ZnSe windows was permanently connected to the vacuum system with a gas sample vacuum system, a turbo-molecular pump, and pressure gauges covering the 10<sup>-3</sup>–100 Torr pressure range. The optical compartment of the spectrometer was evacuated by a mechanical pump

down to 0.02 Torr and remained at that pressure during the experiment.

Experimental spectra (see Fig. 1) were obtained by averaging 1000 scans. The spectra were recorded at significantly different pressures, 0.4 (spectrum W) and 10 (spectrum S) Torr, to cover a wider range of J numbers and to estimate the value of possible systematic errors in the line positions caused by pressure shifts. Comparison of the positions of unsaturated unblended lines in two spectra recorded at a pressure of 0.4 and 10 Torr shows a good agreement between the pairs of lines within  $\pm 10^{-5}$  cm<sup>-1</sup>, which demonstrates a negligible effect of the pressure shift. The spectra were calibrated with 400 OCS peaks of the  $\nu_1$ and  $2\nu_2$  bands (centered at 860 cm<sup>-1</sup> and 1047 cm<sup>-1</sup>, respectively), and NIST calibration tables [41], based on heterodyne frequency measurements. After calibration the standard deviation of the difference between the measured and tabulated peak positions was less than  $10^{-4}$  cm<sup>-1</sup>.

### 3. Irreducible tensorial sets and effective Hamiltonian of the $XY_4$ ( $T_d$ ) molecule

Germane is a spherical top molecule of the  $T_d$  symmetry. This molecule has a tetrahedral structure resulting in one nondegenerate  $(q_1, A_1)$ , one doubly degenerate  $(q_2, E)$ , and two triply degenerate  $(q_3 \text{ and } q_4, F_2)$  vibrational modes. In this case, the  $\nu_2$  and  $\nu_4$  fundamentals are connected by a very strong Coriolis interaction. As a consequence, the spectrum of the  $\nu_2$  and  $\nu_4$  bands may be described only in the frame of the effective Hamiltonian model which takes into account the interaction between the (0100, E) and  $(0001, F_2)$  states. On the other hand, high symmetry of the molecule necessitates using a special mathematical formalism (the theory of Irreducible Tensorial Sets, see, e.g., Refs. [45–48] and recent review in Ref. [54]) for description of its spectra. Application of the mentioned formalism to the  $XY_4$  ( $T_d$ ) molecules was discussed in the spectroscopic literature many times (see, e.g., Refs. [42-44]). For that reason we present here very briefly only the main points necessary for understanding the structure of the Fortran code discussed in Section 3.



**Fig. 1.** Survey spectrum of  $^{76}$ GeH<sub>4</sub> and  $^{74}$ GeH<sub>4</sub> in the region of the dyad. Experimental conditions: absorption path length is 20 cm; room temperature; number of scans is 1000; sample pressure is 0.4 Torr for the "black" spectrum and 10 Torr for the "grey" spectrum.

#### 3.1. Irreducible rotational operators

(a) Irreducible rotational operators of the SO(3) group: In accordance with general statements of the Irreducible Tensorial Sets Theory [45–47], the basic first-rank irreducible rotational operators  $R_m^{\Omega(K)}$   $(m=0,\pm 1,...,\pm K)$  can be chosen in the following form:

$$R_1^{1(1)} = -\frac{1}{\sqrt{2}} \left( J_x - i J_y \right) \equiv -J_+,$$

$$R_{-1}^{1(1)} = \frac{1}{\sqrt{2}} \left( J_x + i J_y \right) \equiv J_-,$$

$$R_0^{1(1)} = J_z \equiv J_0.$$
(1)

In the operators  $R_m^{\Omega(K)}$  the following notation is used:  $\Omega$  is the total degree of rotational operators  $J_\alpha$ ,  $\alpha=x$ , y, z (for example, for  $\Omega=1$ ,  $R_{...}^{1(...)}\sim J_\alpha$ ; for  $\Omega=2$ ,  $R_{...}^{2(...)}\sim J_\alpha J_\beta$ ; etc.); the indices K and m indicate the irreducible representation  $D^{(K)}$  of the SO(3) symmetry group and its line; the operators  $J_\alpha$  are conventional angular momentum components related to the molecular fixed coordinate system:

$$\begin{split} &J_{x} = i \frac{\cos \varphi}{\sin \theta} \left( \frac{\partial}{\partial \psi} - \cos \theta \frac{\partial}{\partial \varphi} \right) - i \sin \varphi \frac{\partial}{\partial \theta}, \\ &J_{y} = -i \frac{\sin \varphi}{\sin \theta} \left( \frac{\partial}{\partial \psi} - \cos \theta \frac{\partial}{\partial \varphi} \right) - i \cos \varphi \frac{\partial}{\partial \theta}, \end{split} \tag{2}$$

and

$$J_z = -i\frac{\partial}{\partial \omega}. (3)$$

The irreducible rotational operators  $R_{\tilde{m}}^{\Omega+1(K+1)}$  may be constructed from the corresponding irreducible rotational operators  $R_{m}^{\Omega(K)}$   $(n=0,\pm 1,\ldots \pm K)$  and  $R_{l}^{1(1)}$   $(l=0,\pm 1)$  of lower degrees and ranks in accordance with the general rule [49,50],

$$R_{\tilde{m}}^{\Omega+1(K+1)} = \sum_{l=-1,0,1} C_{K\ \tilde{m}-l,1\ l}^{K+1\ \tilde{m}} R_{\tilde{m}-l}^{\Omega(K)} R_{l}^{1(1)}, \tag{4}$$

where  $C_{K\ \tilde{m}-l,1\ l}^{K+1\ \tilde{m}}$  are known Clebsh–Gordan coefficients, Ref. [47]. The irreducible rotational operators  $R_m^{\Omega(K)}$  with  $K<\Omega$  (in this case, the parity of both  $\Omega$  and K must be the same [49]) are constructed as

$$R_m^{\Omega(K)} = R_m^{\Omega = K(K)} (R^{2(0)})^{(\Omega - K)/2}, \tag{5}$$

where we use the notation  $R^{2(0)} = (J_x^2 + J_y^2 + J_z^2)$ . As an illustration, Appendix A presents the operators  $R_m^{\Omega(K)}$  for  $\Omega \le 3$ .

(b) Irreducible rotational operators of the  $T_d$  group: Different rotational operators  $R_\sigma^{\Omega(K,n\Gamma)}$ , that are symmetrized in accordance with irreducible representations  $\Gamma=A_1,\,A_2,\,E,\,F_1,\,$  or  $F_2$  of the  $T_d$  symmetry group, can be easily constructed from the above discussed operators  $R_m^{\Omega(K)}$  by using the following general relations [49]:

$$R_{\sigma}^{\Omega(K,n\Gamma)} = \sum_{m}^{(K)} G_{n\Gamma\sigma}^{m} R_{m}^{\Omega(K)}.$$
 (6)

The reduction matrix elements  $^{(K)}G_{n\Gamma\sigma}^{m}$ , which are presented in Eq. (6), are determined by a concrete point symmetry group. Speaking about molecules of the  $T_d$  symmetry, only numerical representation of the  $^{(K)}G_{n\Gamma\sigma}^{m}$  values was used (see, e.g., Refs. [43,51,52]). In our case, we used a much more convenient analytical representation of G-matrix elements. For convenience of the reader, they are reproduced from Refs. [53,54] in Appendix B. We do not discuss here why the

index n is defined in the formulas of Appendix B in such a form. This issue was discussed in detail in the original papers [53,54], and we think that the reproduction of all arguments in the present paper is excessive. We will mention only that the definition of the index n for the  ${}^{(l)}G^m_{n\Gamma\sigma}$  matrix elements in the formulas of Appendix B differs from the definition used, e.g., in Refs. [43,51,52]. In the mentioned works the index n takes on the values 1, 2, 3,..., and the increase of the value n follows the increase of the energy values of states of the same symmetry. In our case, the value of n is defined exclusively by the value of the corresponding index in the right hand sides of Eqs. (14)-(18). At the same time, we would like to note that there is no contradiction between these two definitions of G-matrix elements. One should remember that the main reason for introducing the index n is to distinguish between different wave functions (or operators) of the same symmetry. From this point of view both definitions of n are equivalent. Moreover, for small values of quantum number J both definitions of G-matrix elements coincide completely. For large values of quantum number J there may appear a difference between the values of G-matrix elements. However, it does not contradict the general theory of symmetry because even different definitions of G-matrices are nothing but different reductions of irreducible representations of the SO(3) group to irreducible representations of the  $T_d$  symmetry group. As a consequence, it should not influence the final result.

We would like to make here one more minor remark. In spite of the fact that the analytical presentation of G-matrix elements with n-index definition from Appendix B (as a consequence, analytical presentation of numerous intermediate results) is considerably more suitable than a numerical one, namely the n-index definition from [43,51,52] is most convenient and simple for a final description of ro-vibrational energy levels and transitions. For that reason, the analysis and all calculations in the present paper have been made with the G-matrix defined in Appendix B, but the notation of indices n/n' in the final results (Tables 2 and 8, and Supplementary materials) follows Refs. [43,51,52], *i.e.*, indices n and n' take on the values 1, 2, 3,..., and for any vibrational state increase with increasing energy values of states of the same symmetry.

#### 3.2. Ro-vibrational functions in the symmetrized form

As the  $T_d$  symmetry group has five irreducible representations  $A_1$ ,  $A_2$ , E ( $E_1$  or  $E_2$ ),  $F_1$  ( $F_{1x}$ ,  $F_{1y}$ ,  $F_{1z}$ ) and  $F_2$  ( $F_{2x}$ ,  $F_{2y}$ ,  $F_{2z}$ ), any vibrational–rotational wave function should be totally symmetric ( $A_1$ ), antisymmetric ( $A_2$ ), or be transformed under symmetry operations according to one of the two ( $E_1$  or  $E_2$ ), or three ( $F_{1x}$ ,  $F_{1y}$ ,  $F_{1z}$ ), ( $F_{2x}$ ,  $F_{2y}$ ,  $F_{2z}$ ) lines of the irreducible representations E,  $F_1$ ,  $F_2$ . In a general case, any vibrational–rotational function can be constructed in the following form [49,55]:

$$\begin{split} |\nu\gamma_{\nu}; Jn_{J}\gamma_{r}; m\gamma s\rangle &\equiv (|\nu\gamma_{\nu}\rangle \otimes |Jn_{J}\gamma_{r}\rangle)_{s}^{\gamma} \\ &= \sqrt{|\gamma|} \sum_{\sigma_{\nu}\sigma_{r}} \begin{pmatrix} \gamma & \gamma_{\nu} & \gamma_{r} \\ s & \sigma_{\nu} & \sigma_{r} \end{pmatrix} |\nu\gamma_{\nu}\sigma_{\nu}\rangle |Jn_{J}\gamma_{r}\sigma_{r}\rangle, \quad (7) \end{split}$$

where the set of indices  $v_{\gamma_{\nu}}$ ,  $J_{n_{J}\gamma_{T}}$ , and  $m_{\gamma}s$  unambiguously determines any vibrational–rotational function symmetrized

in the  $T_d$  group, and the indices  $\gamma_{\nu}$ ,  $\gamma_{\nu}$  and  $\gamma$  are the symmetry of vibrational, rotational, and vibrational–rotational functions, respectively. The  $|\nu\gamma_{\nu}\sigma_{\nu}\rangle$  and  $|Jn_{J}\gamma_{r}\sigma_{r}\rangle$  in Eq. (7) are pure vibrational and rotational wave functions symmetrized in the  $T_d$  group; the symbols  $\otimes$  and  $[\gamma]$  denote direct tensorial product and dimension of the irreducible representation  $\gamma$ , respectively; the values

$$\begin{pmatrix}
\gamma & \gamma_v & \gamma_r \\
S & \sigma_v & \sigma_r
\end{pmatrix}$$

are the so-called  $3\Gamma$ -symbols of the  $T_d$  symmetry group (nonzero  $3\Gamma$ -symbols are presented in Appendix C).

The pure rotational functions,  $|Jn_J\gamma_r\sigma_r\rangle$ , being the functions symmetrized in the  $T_d$  symmetry group, can be constructed in accordance with the general equation analogous to Eq. (6):

$$|Jn_J\gamma_r\sigma_r\rangle = \sum_k^{(J)} G^k_{n_J\gamma_r\sigma_r} |Jk\rangle. \tag{8}$$

Here the coefficients  ${}^{(J)}G^k_{n_J\gamma_\tau\sigma_\tau}$  can be determined in accordance with formulas of Appendix B; the  $|Jk\rangle$   $(-J \le k \le J)$  are the conventional rotational functions for which the relations, Eq. (11) of Appendix A, are valid.

### 3.3. Effective Hamiltonian of a molecule in the presence of resonance interactions

As is known from the general vibration-rotation theory [56,57], the Hamiltonian of an arbitrary polyatomic molecule can be reduced to a set of the so-called effective Hamiltonians, or, in a more general case, to a set of effective operator matrices of the form

$$H^{vib.-rot.} = \sum_{a,b} |a\rangle\langle b| H^{a,b}. \tag{9}$$

Here  $|a\rangle$  and  $\langle b|$  are the basic vibrational functions; the operators  $H^{a,b}$  depend on the rotational operators  $J_{\alpha}$  only; and summation in Eq. (9) is performed in all degenerate and/or interacting vibrational states. When, as in our case, a molecule possesses a symmetry, Eq. (9) can be rewritten in the following form:

$$H^{vib.-rot.} = \sum_{\nu_{\gamma},\nu_{\gamma'}} \sum_{n\Gamma} [(|\nu_{\gamma}\rangle \otimes \langle \nu'_{\gamma'}|)^{n\Gamma} \otimes H^{n\Gamma}_{\nu_{\gamma},\nu_{\gamma'}}]^{A_{1}}$$

$$\equiv \sum_{\nu_{\gamma},\nu_{\gamma'}} \sum_{n\Gamma} \sum_{\Omega K} [(|\nu_{\gamma}\rangle \otimes \langle \nu'_{\gamma'}|)^{n\Gamma} \otimes R^{\Omega(K,n\Gamma)}]^{A_{1}} Y^{\Omega(K,n\Gamma)}_{\nu_{\gamma},\nu_{\gamma'}}.$$
(10)

Here  $|\nu\gamma\rangle$  are the above discussed symmetrized vibrational functions; the operators  $R^{\Omega(K,n\Gamma)}_{\sigma}$  are determined in Section 3.1; and  $Y^{\Omega(K,n\Gamma)}_{\nu\gamma,\nu'\gamma'}$  are spectroscopic parameters. When  $\nu=\nu'$  and  $\gamma=\gamma'$ , the parameters  $Y^{\Omega(K,n\Gamma)}_{\nu\gamma,\nu\gamma}$  describe the rotational structure of the vibrational state  $(\nu\gamma)$ . If  $\gamma=\gamma'$ , but  $\nu\neq\nu'$ , the parameters  $Y^{\Omega(K,n\Gamma)}_{\nu\gamma,\nu'\gamma}$  describe the Fermi-type interactions. If  $\gamma\neq\gamma'$  ( $\nu$  and  $\nu'$  are arbitrary), the parameters  $Y^{\Omega(K,n\Gamma)}_{\nu\gamma,\nu'\gamma'}$  describe the Coriolis-type interactions. The general formula, Eq. (10), is valid for an arbitrary

The general formula, Eq. (10), is valid for an arbitrary polyatomic molecule (the forms of the operators  $H^{nr}_{\nu_r,\nu_{r'}}$  for different asymmetric and symmetric top molecules are presented, *e.g.*, in [58–61] and [62–69], respectively). If we use the information from Sections 3.1 and 3.2 and Appendices A–C for the spherical top XY<sub>4</sub> (T<sub>d</sub>) molecule, then it can

be readily shown that the parameters (operators) describing the rotational structure of the ground vibrational state and the parameters (operators) responsible for description of the ro-vibrational structure of the dyad  $(0100, E)/(0001, F_2)$ , have the form presented in Table 1 (in Table 1 only parameters (operators) with  $\Omega \le 6$  are presented).

Knowledge of the rotational operators in the effective Hamiltonian, Eq. (10), and of the basic wave functions, Eqs. (7) and (8), permitted us to create an efficient Fortran code SPHETOM (SPHErical TOp Molecules) which allows both assigning ro-vibrational transitions and fitting spectroscopic parameters  $Y_{\nu_{\gamma},\nu_{\gamma'}}^{Q(K,n\Gamma)}$  of the Hamiltonian, Eq. (10). In the next section we will present results of the analysis of the high resolution spectrum of  $^{76}\text{GeH}_4/^{74}\text{GeH}_4$  in the spectral region of the dyad of strongly interacting bands  $\nu_4$  and  $\nu_2$  which was made with the SPHETOM code.

Some words should be said concerning the code used in the present study for the analysis of experimental data. Presently, the mostly efficient software for ro-vibrational analysis of high resolution spectra of spherical top molecules is the XTDS program package, Ref. [70], equipped with graphical user interface, Ref. [71]. Unfortunately, for users it is a "black box". Sometimes it is not too

**Table 1** Parameters  $Y^{\Omega(K,n\Gamma)}_{v_y,v_{y'}}$  of effective Hamiltonian of the XY<sub>4</sub> (T<sub>d</sub>) molecule.

	v/,v/				
(νγ)	$(\nu'\gamma')$	$\Omega(K,n\Gamma)$	(νγ)	$(\nu'\gamma')$	$\Omega(K, n\Gamma)$
$(0000, A_1)$	$(0000, A_1)$	$2(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	4(4, E)
$(0000, A_1)$	$(0000, A_1)$	$4(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$4(4, F_2)$
$(0000, A_1)$	$(0000, A_1)$	$4(4, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$5(1, F_1)$
$(0000, A_1)$	$(0000, A_1)$	$6(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$5(3, F_1)$
$(0000, A_1)$	$(0000, A_1)$	$6(4, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$5(5, F_1)$
$(0000, A_1)$	$(0000, A_1)$	$6(6, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$5(5, F_1)$
$(0000, A_1)$	$(0000, A_1)$	$8(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$6(0, A_1)$
$(0000, A_1)$	$(0000, A_1)$	$8(4, A_1)$	$(0001, F_2)$	$(0001, F_2)$	6(2, E)
$(0000, A_1)$	$(0000, A_1)$	$8(6, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$6(2, F_2)$
$(0000, A_1)$	$(0000, A_1)$	$8(8, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$6(4, A_1)$
(0100, E)	(0100, E)	$0(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	6(4, E)
(0100, E)	(0100, E)	$2(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$6(4, F_2)$
(0100, E)	(0100, E)	2(2, E)	$(0001, F_2)$	$(0001, F_2)$	$6(6, A_1)$
(0100, E)	(0100, E)	$3(3, A_2)$	$(0001, F_2)$	$(0001, F_2)$	6(6, E)
(0100, E)	(0100, E)	$4(0, A_1)$	$(0001, F_2)$	$(0001, F_2)$	$6(6, F_2)$
(0100, E)	(0100, E)	4(2, E)	$(0001, F_2)$	$(0001, F_2)$	$6(6, F_2)$
(0100, E)	(0100, E)	$4(4, A_1)$	(0100, E)	$(0001, F_2)$	$1(1, F_1)$
(0100, E)	(0100, E)	4(4, E)	(0100, E)	$(0001, F_2)$	$2(2, F_2)$
(0100, E)	(0100, E)	$5(3, A_2)$	(0100, E)	$(0001, F_2)$	$3(1, F_1)$
(0100, E)	(0100, E)	$6(0, A_1)$	(0100, E)	$(0001, F_2)$	$3(3, F_1)$
(0100, E)	(0100, E)	6(2, E)	(0100, E)	$(0001, F_2)$	$3(3, F_2)$
(0100, E)	(0100, E)	$6(4, A_1)$	(0100, E)	$(0001, F_2)$	$4(2, F_2)$
(0100, E)	(0100, E)	6(4, E)	(0100, E)	$(0001, F_2)$	$4(4, F_1)$
(0100, E)	(0100, E)	$6(6, A_1)$	(0100, E)	$(0001, F_2)$	$4(4, F_2)$
(0100, E)	(0100, E)	6(6, E)	(0100, E)	$(0001, F_2)$	$5(1, F_1)$
$(0001, F_2)$	$(0001, F_2)$	$0(2, A_1)$	(0100, E)	$(0001, F_2)$	$5(3, F_1)$
$(0001, F_2)$	$(0001, F_2)$	$1(1, F_1)$	(0100, E)	$(0001, F_2)$	$5(3, F_2)$
$(0001, F_2)$	$(0001, F_2)$	$2(0, A_1)$	(0100, E)	$(0001, F_2)$	$5(5, F_1)$
$(0001, F_2)$	$(0001, F_2)$	2(2, E)	(0100, E)	$(0001, F_2)$	$5(5, F_1)$
$(0001, F_2)$	$(0001, F_2)$	$2(2, F_2)$	(0100, E)	$(0001, F_2)$	$5(5, F_2)$
$(0001, F_2)$	$(0001, F_2)$	$3(1, F_1)$	(0100, E)	$(0001, F_2)$	$6(2, F_2)$
$(0001, F_2)$	$(0001, F_2)$	$3(3, F_1)$	(0100, E)	$(0001, F_2)$	$6(4, F_1)$
$(0001, F_2)$	$(0001, F_2)$	$4(0, A_1)$	(0100, E)	$(0001, F_2)$	$6(4, F_2)$
$(0001, F_2)$	$(0001, F_2)$	4(2, E)	(0100, E)	$(0001, F_2)$	$6(6, F_1)$
$(0001, F_2)$	$(0001,F_2)$	$4(2, F_2)$	(0100, E)	$(0001, F_2)$	$6(6, F_2)$
$(0001, F_2)$	$(0001, F_2)$	$4(4, A_1)$	(0100, E)	$(0001, F_2)$	$6(6, F_2)$

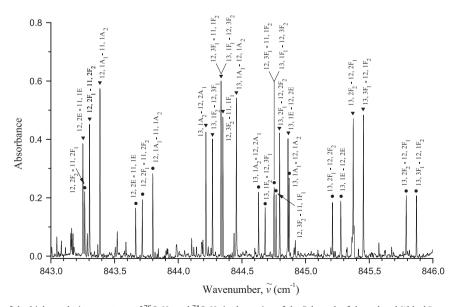
convenient, especially when one would like to make some or other changes in the codes. For example, it would be reasonable to have a possibility to analyze spectra not only "polyad by polyad" as it is provided in the XTDS program package, but (as for any other type of molecules considered in high resolution spectroscopy) for separate state (or sets of states) in higher wave length regions. In that case, of course, it is good to have an opportunity for code corrections. With the XTDS program package it is not possible just because it is a "black box". As a consequence, the SPHETOM code was made which is free of such limitation.

#### 4. Analysis of experimental data in the dyad region

GeH<sub>4</sub> is a spherical top molecule. As a consequence. only transitions from the ground to the  $F_2$ -symmetry vibrational states are allowed in absorption by the symmetry of the molecule. The  $\nu_2$  is the band of *E*-symmetry, and its ro-vibrational transitions appear in absorption only because of strong Coriolis interaction with the allowed band,  $\nu_4$ . For that reason (as is seen in Fig. 1), the irregular structure of the  $\nu_2$  band contrasts with the regular structure of the  $\nu_4$  band. In Fig. 2 one can see a small part of the experimental high resolution spectrum in the region of the R-branch of the  $\nu_4$  band. The transitions assigned to the <sup>76</sup>GeH<sub>4</sub> isotopologue are marked by dark circles. One can see also weaker lines belonging to the <sup>74</sup>GeH<sub>4</sub> isotopologue which are located about 0.4 cm<sup>-1</sup> from the corresponding lines of the <sup>76</sup>GeH<sub>4</sub> isotopologue towards the blue part of the spectrum. It should be mentioned that, as can be seen from Fig. 2, the experimental spectrum contains numerous very weak lines. To answer the question "what can it be?", we made a special set of measurements with different sample pressures. As a result we saw that the intensities of the above-mentioned very weak lines had increased proportionally to the pressure. This undoubtedly indicates that the lines belong to the sample used. We believe that they cannot be lines of the other (M=73, 72, 70) isotopologues of  $^{M}$ GeH<sub>4</sub>, because there are no characteristic line clusters in the spectrum. So, one can expect that they are lines corresponding to the "hot" dyad–pentad transitions of  $^{76}$ GeH<sub>4</sub> (the ratio of populations of the "dyad" vibrational states to the population of the ground vibrational state at room temperature changed from 0.019 for the (0001) state to 0.011 for the (0100) one). However, the correct answer to that question can be given only after the corresponding analysis of the spectra in the pentad region.

Assignments of the transitions were made simultaneously with the fit of parameters of the ground vibrational state and of the upper vibrational states, (0100, E) and (0001,  $F_2$ ). As a result, we were able to assign 1922 transitions with  $J^{max.} = 26$  to the  $^{76}\text{GeH}_4$  isotopologue and 788 transitions with  $J^{max.} = 24$  to the  $^{74}\text{GeH}_4$  isotopologue. As an illustration, a small part of experimentally recorded transitions is shown in column 1 of Table 2 together with the values of absorbance (column 4) and assignment of transitions (columns 2 and 3). Columns 6 and 7 show to which band and isotopologue ( $^{76}\text{GeH}_4$  or  $^{74}\text{GeH}_4$ ) the line belongs. Values of  $\Delta = \nu_{exp.} - \nu_{calc.}$  are listed in column 5. The recorded spectrum ("W" or "S") to which the transition belongs is specified in column 8. A complete list of assigned transitions is given in the Supplementary materials to the present paper.

As was noted above, the fit of the parameters of the effective Hamiltonian was made with the SPHETOM Fortran code. The weighted least square fit procedure was used. In this case, weights of isolated (unblended) not very weak and unsaturated lines have been taken as 100.



**Fig. 2.** Small portion of the high resolution spectrum of  $^{76}$ GeH<sub>4</sub> and  $^{74}$ GeH<sub>4</sub> in the region of the R-branch of the  $\nu_4$  band ("black" spectrum). The transitions assigned to the  $^{76}$ GeH<sub>4</sub> and  $^{74}$ GeH<sub>4</sub> isotopologues are marked by dark triangles and circles, respectively. Numerous very weak lines belong probably to the "hot" dyad–pentad bands.

O.N. Ulenikov et al. / Journal of Quantitative Spectroscopy & Radiative Transfer 144 (2014) 11-26

**Table 2** Small part of the observed transition wavenumbers of  ${}^{M}\text{GeH}_{4}$  (M = 76, 74) in the dyad region.

Wavenumber, $cm^{-1}$	J	n	γ	J'	n'	$\gamma'$	Absorb.	$\Delta$ , in $10^{-4}$ cm <sup>-1</sup>	Band	Species	Spectrum
1	2			3			4	5	6	7	8
781.42018	11	3	$A_1$	12	1	$A_2$	18.4	0.5	$\nu_4$	74	W
781.64008	12	3	$A_2$	13	1	$A_1$	42.5	-0.3	$ u_4$	76	W
781.89355	12	9	$F_2$	13	2	$F_1$	31.2	-0.3	$\nu_4$	76	W
781.96851	12	3	$A_2$	13	1	$A_1$	15.5	-0.0	$\nu_4$	74	W
781.99308	12	6	E	13	1	E	27.1	-0.4	ν4	76	W
782.22325	12	9	$F_2$	13	2	$\overline{F_1}$	13.5	0.4	$\nu_4$	74	W
782.32310	12	6	E	13	1	E	8.5	-1.0	$\nu_4$	74	W
782.70904	11	8	$F_1$	12	2	$F_2$	38.9	0.0	$\nu_4$	76	W
782.81368	13	3	$A_1$	14	1	$A_2$	35.5	0.1	$\nu_4$	76	W
782.82592	13	10	$F_1$	14	1	$F_2$	30.4	-0.4		76	W
782.83204	13	7	E E	14	1	E E	16.9	0.3	$\nu_4$	76 76	W
782.96638	11	5	E	12	2	E	27.9	-0.5	$\nu_4$	76 76	W
783.03556	11	8		12	2		27.9 14.0		$\nu_4$	76 74	W
			$F_1$			$F_2$		0.2	$\nu_4$		
783.15113	13	3	$A_1$	14	1	$A_2$	14.9	-0.2	$\nu_4$	74	W
783.16344	13	10	$F_1$	14	1	$F_2$	10.3	-0.5	$\nu_4$	74	W
783.16947	13	7	E	14	1	E	4.0	-1.0	$ u_4$	74	W
783.29417	11	5	Ε	12	2	Е	12.2	0.5	$\nu_4$	74	W
783.32624	11	1	$A_1$	11	1	$A_2$	9.2	-1.4	$\nu_4$	74	S
783.34058	11	3	$F_1$	11	2	$F_2$	4.4	− 1 <b>.</b> 7	$\nu_4$	74	S
783.58539	5	2	$F_2$	6	1	$F_1$	12.8	1.2	$ u_4$	76	S
783.87914	5	2	$F_1$	6	2	$F_2$	26.5	1.1	$ u_4$	76	S
784.14727	10	6	$F_2$	11	3	$F_1$	41.9	0.3	$\nu_4$	76	W
784.36405	10	4	Ε	11	2	Ε	31.3	-0.1	$\nu_4$	76	W
784.47003	10	6	$F_2$	11	3	$F_1$	15.4	-0.3	$\nu_4$	74	W
784.60230	11	7	$F_2$	12	2	$F_1$	37.6	-0.0	$ u_4$	76	W
784.68802	10	4	Ε	11	2	E	14.5	-0.3	$ u_4$	74	W
784.80961	10	6	$F_1$	11	3	$F_2$	38.5	-0.5	$\nu_4$	76	W
784.90444	11	9	$F_1$	12	1	$\overline{F_2}$	30.8	0.1	$\nu_4$	76	W
784.93603	11	7	$F_2$	12	2	$F_1$	13.4	-0.4	$\nu_4$	74	W
785.07487	10	1	$A_2$	10	1	$A_1$	28.0	-0.3	$\nu_4$	76	S
785.13570	10	6	F <sub>1</sub>	11	3	$F_2$	18.3	0.4	$\nu_4$	74	W
785.23962	11	9	$F_1$	12	1	$F_2$	15.3	-0.5	$\nu_4$	74	W
785.32925	12	9	F <sub>1</sub>	13	1	$F_2$	34.3	0.0		76	W
785.34826	12	10	$F_2$	13	1	$F_1$	31.3	-0.4	$\nu_4$	76	W
785.67071	12	9	F <sub>1</sub>	13	1	$F_2$	13.9	-0.4	$\nu_4$	74	W
785.68996	12	10		13	1	г <sub>2</sub> Г <sub>1</sub>	13.7	0.3	$\nu_4$	74 74	W
		7	F <sub>2</sub>						$\nu_4$		
786.19938	10		$F_2$	11	2	$F_1$	42.7	-0.2	$\nu_4$	76	W
786.53327	10	7	$F_2$	11	2	$F_1$	18.5	0.0	$\nu_4$	74	W
787.35952	10	5	E	11	2	E	4.6	-1.0	$\nu_4$	76	S
787.43820	10	5	E	11	1	E	29.5	-0.1	$\nu_4$	76 76	W
787.55322	10	7	$F_1$	11	3	$F_2$	5.9	0.1	$\nu_4$	76	S
787.62504	10	7	$F_1$	11	2	$F_2$	44.5	-1.2	$\nu_4$	76	W
787.77675	10	5	Ε	11	1	E	13.6	- 0.5	$\nu_4$	74	W
787.82842	11	6	Ε	12	1	Ε	29.1	-0.7	$ u_4$	76	W
787.84305	11	8	$F_2$	12	1	$F_1$	33.6	-0.8	$\nu_4$	76	W
787.86207	9	5	$F_1$	10	3	$F_2$	38.0	-0.4	$\nu_4$	76	W
787.87129	11	3	$A_2$	12	1	$A_1$	34.3	-0.1	$\nu_4$	76	W

787.90787	10	3	$A_1$	11	1	$A_2$	37.7	0.2	$ u_4$	76	W
787.96466	10	7	$F_1$	11	2	$F_2$	16.7	-0.1	$ u_4$	74	W
788.17408	11	6	E	12	1	E	11.7	1.2	$ u_4$	74	W
788.18893	11	8	$F_2$	12	1	$F_1$	18.9	2.5	$ u_4$	74	W
788.19388	9	4	Ē	10	2	E	49.3	-2.0	$ u_4$	76	W
788.21710	11	3	$A_2$	12	1	$A_1$	24.0	1.2	$ u_4$	74	W
788.24869	10	3	$A_1$	11	1	$A_2$	24.4	-0.0	$\nu_4$	74	W
788.38981	9	1	$F_2$	9	3	$F_1$	6.1	3.4	$ u_4$	76	S
788.49855	9	6	$\overline{F_2}$	10	2	$F_1$	37.9	-1.2	$ u_4$	76	W
788.52742	9	4	E	10	2	E	15.0	0.9	$\nu_4$	74	W
788.83348	9	6	$F_2$	10	2	$F_1$	19.1	0.1	$ u_4$	74	W
789.17373	9	2	E	9	1	E	17.4	0.0	$ u_4$	76	S
789.21956	9	1	$A_2$	9	1	$A_1$	22.3	-1.0	$ u_4$	76	S
789.49558	9	3	$A_2$	10	1	$A_1$	42.2	-0.4	ν4	76	W
789.83609	9	3	$A_2$	10	1	$A_1$	23.7	-0.4	$ u_4$	74	W
790.01257	4	2	$F_2$	5	2	$F_1$	12.2	1.4	$ u_4$	74	S
790.25518	9	7	$\overline{F_2}$	10	2	$F_1$	13.4	2.7	$\nu_4$	76	S
790.31790	10	8	$\overline{F_1}$	11	1	$F_2$	37.6	-0.1	$ u_4$	76	W
790.36036	10	8	$F_2$	11	1	$\overline{F_1}$	35.4	-0.2	$ u_4$	76	W
790.61847	9	6	$\overline{F_1}$	10	2	$F_2$	45.3	-0.4	$ u_4$	76	W
790.63706	9	7	$F_2$	10	1	$\overline{F_1}$	20.8	-0.3	$ u_4$	74	W
790.66717	10	8	$\overline{F_1}$	11	1	$F_2$	19.5	-0.6	$\nu_4$	74	W
790.70983	10	8	$F_2$	11	1	$F_1$	19.4	-0.8	$ u_4$	74	W
790.96352	9	6	$F_1$	10	2	$F_2$	18.7	-1.0	$ u_4$	74	W
791.32539	8	2	$A_1$	9	1	$A_2$	47.9	-0.8	$ u_4$	76	W
791.56530	8	5	$F_1$	9	2	$F_2$	44.0	0.0	$ u_4$	76	W
791.66486	8	2	$A_1$	9	1	$A_2$	30.2	0.2	$ u_4$	74	W
791.86704	8	5	$F_2$	9	3	$F_1$	38.2	-0.3	$ u_4$	76	W
791.90593	8	5	$F_1$	9	2	$F_2$	19.0	-0.0	$ u_4$	74	W
792.20922	8	5	$F_2$	9	3	$F_1$	23.5	-0.2	$ u_4$	74	W
792.30902	8	2	$F_1$	8	1	$F_2$	16.9	1.4	$ u_4$	76	S
792.35480	8	2	$F_2$	8	2	$F_1$	15.6	-0.3	$ u_4$	76	S
792.50146	8	2	$A_2$	9	1	$A_1$	45.4	0.1	$ u_4$	76	W
792.76251	9	2	$A_1$	10	1	$A_2$	51.1	-0.1	$ u_4$	76	W
792.82893	9	7	$F_1$	10	1	$F_2$	37.6	-0.3	$\nu_4$	76	W
792.84634	8	2	$A_2$	9	1	$A_1$	24.4	-0.1	$\nu_4$	74	W
792.85897	9	5	Ε	10	1	Е	33.0	-0.5	$ u_4$	76	W
793.11543	9	2	$A_1$	10	1	$A_2$	27.0	-0.1	$ u_4$	74	W

**Table 3** Spectroscopic parameters  $Y_{\nu_{\gamma,\nu'\gamma'}}^{\Omega(K,nI')}$  of the ground vibrational state of germane (in cm<sup>-1</sup>)<sup>a,b</sup>.

$\varOmega(K,n\varGamma)$	<sup>76</sup> GeH₄	<sup>74</sup> GeH₄
1	2	3
$2(0, A_1)$ $4(0, A_1)10^4$ $4(4, A_1)10^4$ $6(0, A_1)10^8$ $6(4, A_1)10^8$ $6(6, A_1)10^8$	2.695870305(528) -0.3341682(330) -0.24753264(156) 0.114368(658) 0.1187243(333) 0.0577831(104)	2.695864734(234) -0.3341682 -0.24753264 0.114368 0.1187243 0.0577831

<sup>&</sup>lt;sup>a</sup> The  $(v\gamma) = (v'\gamma') = (0000, A_1)$  in Table 3.

**Table 4** Spectroscopic parameters  $Y_{\nu_{\gamma},\nu_{\gamma'}}^{\Omega(K,nT)}$  of the (0100,E) vibrational state of germane (in cm<sup>-1</sup>)<sup>a,b</sup>.

$\Omega(K, n\Gamma)$	<sup>76</sup> GeH₄	<sup>74</sup> GeH₄
1	2	3
$0(0, A_1)$ $2(0, A_1)$ $2(2, E)10^2$ $3(3, A_2)10^4$ $4(0, A_1)10^4$	929.9130275(120) 2.695870305 3.051146(154) 1.80944(463) -0.3382202(928)	929.9093056(153) 2.695870305 3.0515281(155) 1.80944 -0.3382202
$4(2, E)10^{6}$ $4(4, A_{1})10^{5}$ $4(4, E)10^{6}$ $6(0, A_{1})10^{8}$ $6(4, A_{1})10^{8}$ $6(6, A_{1})10^{8}$	-2.02994(673) -2.4450064(858) -1.49638(965) 0.114368 0.1187243 0.0577831	- 2.02994 - 2.4450064 - 1.49638 0.114368 0.1187243 0.0577831

<sup>&</sup>lt;sup>a</sup> The  $(v\gamma) = (v'\gamma') = (0100, E)$  in Table 4.

Saturated lines were not used at all. Weak lines were used in the fit with the weight 1. 36 parameters were fitted (6 parameters of the ground vibrational state and 30 parameters of the dyad): they are the 6, 7, and 13 parameters of the ground, (0100, E), and (0001,  $F_2$ ) vibrational states, respectively, and 10 parameters which describe the Coriolis interaction between the (0100, E) and (0001,  $F_2$ ) states. Obtained parameters are presented in column 2 of Tables 3–6 together with their  $1\sigma$  statistical confidence intervals. A set of 36 parameters reproduces the initial 1922 experimental line positions of the  $^{76}$ GeH<sub>4</sub> isotopologue with the root-mean square deviation  $d_{rms} = 1.81 \times 10^{-4}$  cm<sup>-1</sup> ( $d_{rms} = 1.76 \times 10^{-4}$  cm<sup>-1</sup> for the  $\nu_4$  band, and  $d_{rms} = 1.86 \times 10^{-4}$  cm<sup>-1</sup> for the  $\nu_2$  band), which is comparable with experimental uncertainties (see the statistical information in Table 7). Values of rotational energies of the

**Table 5** Spectroscopic parameters  $Y_{\nu_{y},\nu_{\gamma'}}^{\Omega(K,n\Gamma)}$  of the (0001, $F_2$ ) vibrational state of germane (in cm<sup>-1</sup>)<sup>a,b</sup>.

$\varOmega(K,n\varGamma)$	<sup>76</sup> GeH₄	<sup>74</sup> GeH <sub>4</sub>
1	2	3
$0(0, A_1)$	820.3270025(104)	820.7118508(732)
$1(1, F_1)$	7.38069370(334)	7.37317292(255)
$2(0, A_1)$	2.696930760(819)	2.696932024(127)
$2(2, E)10^2$	0.42000477(979)	0.42387205(143)
$2(2, F_2)10^2$	2.469295(136)	2.2469831(125)
$3(1, F_1)10^4$	-1.881200(667)	-1.879439(789)
$3(3, F_1)10^4$	-2.21249(629)	-2.21249
$4(0,A_1)10^4$	-0.3378212(812)	-0.3378212
$4(2, F_2)10^6$	-1.8768(130)	-1.8768
$4(4, A_1)10^5$	-2.6203003(742)	-2.6203003
$5(1, F_1)10^8$	1.59831(356)	1.59831
$5(3, F_1)10^8$	1.80981(380)	1.80981
$6(0, A_1)10^8$	0.118644(873)	0.118644
$6(4, A_1)10^8$	0.1187243	0.1187243
$6(6, A_1)10^8$	0.0577831	0.0577831

<sup>&</sup>lt;sup>a</sup> The  $(v\gamma) = (v'\gamma') = (0001, F_2)$  in Table 5.

**Table 6** Spectroscopic parameters  $Y_{\nu_{\gamma},\nu_{\gamma}'}^{\Omega(K,nI')}$  of the  $(0100,E)/(0001,F_2)$  Coriolis interaction (in cm<sup>-1</sup>)<sup>a,b</sup>.

$\varOmega(K,n\varGamma)$	<sup>76</sup> GeH₄	<sup>74</sup> GeH₄
1	2	3
$   \begin{array}{c}     1(1, F_1) \\     2(2, F_2) 10^2 \\     3(1, F_1) 10^3 \\     3(3, F_2) 10^4 \\     4(2, F_2) 10^6 \\     4(4, F_1) 10^6 \\     4(4, F_2) 10^6 \\     5(1, F_1) 10^8 \\     5(3, F_1) 10^8 \\     5(3, F_2) 10^9   \end{array} $	-5.19969250(157) -4.922900(411) -0.3144712(575) 0.637838(440) -1.1317(156) -1.71376(279) -1.938780(675) -1.41723(673) 1.45888(645) 6.2773(710)	- 5.20319458(664) - 4.919207(275) - 0.3144712 0.637838 - 1.1317 - 1.71376 - 1.938780 - 1.41723 1.45888 6.2773

<sup>&</sup>lt;sup>a</sup> The  $(v\gamma) = (0100, E)$  and  $(v'\gamma') = (0001, F_2)$  in Table 6.

**Table 7**Statistical information on the studied bands of germane.

Isotopomer	Band	Canter (cm <sup>-1</sup> )	J <sup>max</sup>	N <sub>tr.</sub> a	N <sub>en</sub> .b	n <sub>par.</sub> c	d <sub>rms</sub> (10 <sup>-4</sup> cm <sup>-1</sup> )
<sup>76</sup> GeH <sub>4</sub> <sup>76</sup> GeH <sub>4</sub> <sup>76</sup> GeH <sub>4</sub> <sup>74</sup> GeH <sub>4</sub> <sup>74</sup> GeH <sub>4</sub>	ν <sub>2</sub> ν <sub>4</sub> gr. ν <sub>2</sub> ν <sub>4</sub> gr.	929.91303 820.32700 929.90931 820.71185	26 27 21	1117	163	30 6 10	1.86 1.76 2.52 1.79

<sup>&</sup>lt;sup>a</sup> The  $N_{tr}$  is the number of transitions assigned to the band.

 $<sup>^{\</sup>rm b}$  Values in parentheses are  $1\sigma$  statistical confidence intervals. Parameters of  $^{74}{\rm GeH_4}$  presented without confidence intervals were constrained to the values of corresponding parameters of the  $^{76}{\rm GeH_4}$  isotopologue and were fixed in the fit.

<sup>&</sup>lt;sup>b</sup> Values in parentheses are  $1\sigma$  statistical confidence intervals. Parameters presented in column 2 without confidence intervals were constrained to their values from the ground vibrational state and were fixed in the fit. Analogously, parameters of <sup>74</sup>GeH<sub>4</sub> presented in column 3 without confidence intervals were constrained to the values of corresponding parameters of the <sup>76</sup>GeH<sub>4</sub> isotopologue and were fixed in the fit.

<sup>&</sup>lt;sup>b</sup> See footnote (b) to Table 4.

 $<sup>^{\</sup>rm b}$  Values in parentheses are  $1\sigma$  statistical confidence intervals. Parameters of  $^{74}{\rm GeH_4}$  presented without confidence intervals were constrained to the values of corresponding parameters of the  $^{76}{\rm GeH_4}$  isotopologue and were fixed in the fit.

<sup>&</sup>lt;sup>b</sup> The  $N_{en.}$  is the number of energy levels of the upper vibrational state

 $<sup>^{\</sup>rm c}$  The  $n_{par.}$  is the number of fitted parameters. For  $^{74}{\rm GeH_4}$ , the unfitted parameters were fixed to the values of corresponding parameters of  $^{76}{\rm GeH_4}$ .

19

**Table 8** Rotational energies of the ground vibrational state of  $^{76}$ GeH<sub>4</sub> and  $^{74}$ GeH<sub>4</sub> (in cm<sup>-1</sup>).

J'	n	γ	E(M=76)	E(M = 74)	J'	n'	$\gamma'$	E(M=76)	E(M = 74)
	1		2	3		1		2	3
0	1	$A_1$	0.000000	0.000000	10	2	$F_1$	296.183713	296.183100
1	1	$F_1$	5.391607	5.391596	10	1	$F_2$	296.077588	296.076975
2	1	E	16.173938	16.173904	10	2	$F_2$	296.137875	296.137262
2	1	$F_2$	16.174073	16.174040	10	3	$F_2$	296.196851	296.196238
3	1	$A_2$	32.346446	32.346379	11	1	$A_2$	355.257086	355.256350
3	1	$F_1$	32.345227	32.345160	11	1	E	355.269254	355.268519
3	1	$F_2$	32.345769	32.345702	11	2	Е	355.347845	355.347110
4	1	$A_1$	53.902153	53.902041	11	1	$F_1$	355.176351	355.175615
4	1	E	53.903778	53.903667	11	2	F <sub>1</sub>	355.305575	355.304839
4	1	$F_1$	53.903101	53.902990	11	3	F <sub>1</sub>	355.352789	355.352054
4	1	$F_2$	53.905808	53.905697	11	1	$F_2$	355.177533	355.176798
5	1	E	80.848905	80.848738	11	2	$F_2$	355.264496	355.263761
5	1	$F_1$	80.842344	80.842177	11	3	F <sub>2</sub>	355.336457	355.335721
5	2	$F_1$	80.849784	80.849617	12	1	$A_1$	419.603508	419.602639
5	1	$F_2$	80.844173	80.844006	12	2	$A_1$	419.858995	419.858126
6	1	$A_1$	113.176205	113.175971	12	1	$A_2$	419.830815	419.829946
6	1	$A_2$	113.163238	113.163004	12	1	E E	419.604925	419.604056
6	1	E E	113.159985	113.159751	12	2	E	419.782153	419.781284
6	1	$F_1$	113.174178	113.173944	12	1	F <sub>1</sub>	419.604443	419.603574
6	1		113.160793	113.160559	12	2	$F_1$	419.726051	419.725182
6	2	$F_2$			12	3			
7	1	$F_2$	113.171883	113.171649	12		$F_1$	419.852775	419.851906
7	1	A <sub>2</sub> E	150.865528 150.873651	150.865216 150.873339	12	1 2	F <sub>2</sub>	419.717041 419.789769	419.716172
7	1	_				3	$F_2$		419.788900
	-	$F_1$	150.849564	150.849252	12	3 1	$F_2$	419.844743	419.843874
7	2	$F_1$	150.878019	150.877707	13	•	$A_1$	489.508938	489.507924
7	1	$F_2$	150.851377	150.851065	13	1	$A_2$	489.628297	489.627283
7	2	$F_2$	150.870811	150.870499	13	1	E	489.496642	489.495628
8	1	$A_1$	193.903423	193.903022	13	2	E	489.689212	489.688198
8	1	E	193.906071	193.905669	13	1	$F_1$	489.348159	489.347146
8	2	Ε	193.949880	193.949479	13	2	$F_1$	489.500208	489.499194
8	1	$F_1$	193.905092	193.904691	13	3	$F_1$	489.586994	489.585980
8	2	$F_1$	193.941425	193.941024	13	4	$F_1$	489.698156	489.697142
8	1	$F_2$	193.931803	193.931402	13	1	$F_2$	489.348905	489.347892
8	2	$F_2$	193.952423	193.952022	13	2	$F_2$	489.603369	489.602355
9	1	$A_1$	242.374560	242.374059	13	3	$F_2$	489.680084	489.679070
9	1	$A_2$	242.396070	242.395568	14	1	$A_1$	564.694825	564.693655
9	1	E	242.358292	242.357791	14	1	$A_2$	564.397258	564.396088
9	1	$F_1$	242.316247	242.315745	14	1	Е	564.396404	564.395234
9	2	$F_1$	242.361508	242.361007	14	2	E	564.728314	564.727144
9	3	$F_1$	242.386903	242.386401	14	3	E	564.862565	564.861395
9	1	$F_2$	242.317962	242.317460	14	1	$F_1$	564.592940	564.591770
9	2	$\overline{F_2}$	242.392047	242.391546	14	2	$F_1$	564.715350	564.714180
10	1	$A_1$	296.164978	296.164365	14	3	$F_1$	564.850085	564.848915
10	1	$A_2$	296.079110	296.078497	14	1	$F_2$	564.396687	564.395517
10	1	E	296.076885	296.076272	14	2	$F_2$	564.586515	564.585345
10	2	E	296.189922	296.189309	14	3	$F_2$	564.773253	564.772083
10	1	$F_1$	296.145125	296.144512	14	4	$F_2$	564.869800	564.868630
15	1	$A_1$	645.335814	645.334477	18	3	E	918.421795	918.419889

J'	n	γ	E(M=76)	E(M=74)	J'	n'	γ'	E(M = 76)	E(M = 74)
15	1	$A_2$	644.970977	644.969640	18	1	F <sub>1</sub>	917.778534	917.77662
15	2	$A_2$	645.366892	645.365555	18	2	$F_1$	918.091110	918.08920
5	1	Ε	644,979152	644.977815	18	3	$F_1$	918.344669	918.34276
5	2	Ε	645.223164	645.221827	18	4	$F_1$	918.665042	918.66313
5	1	$F_1$	644.735295	644.733958	18	1	$F_2$	917.348806	917.3469
5	2	$F_1$	645.125763	645.124426	18	2	$F_2$	917.775678	917.7737
5	3	$F_1$	645.237194	645.235857	18	3	$F_2$	918.275431	918,2735
5	4	$F_1$	645.349299	645.347962	18	4	$F_2$	918.443862	918.4419
5	1	$F_2$	644.735719	644.734382	18	5	$F_2$	918.655314	918.6534
5	2	$F_2$	644.976266	644.974929	19	1	$A_1$	1019.924199	1019.9220
5	3	$F_2$	645.154056	645.152719	19	1	$A_2$	1019.203562	1019.2014
5	4	$F_2$	645.359004	645.357667	19	2	$A_2$	1020.092454	1020.0903
6	1	$A_1$	730,350393	730.348877	19	1	E	1019.206860	1019.2047
6	2	$A_1$	731.029578	731.028063	19	2	Е	1019.825133	1019.8230
6	1	$A_2$	730.880936	730.879421	19	3	Е	1020.335156	1020,3330
6	1	E	730.350861	730.349346	19	1	$F_1$	1018.698866	1018.6967
6	2	E	730.840933	730.839418	19	2	$F_1$	1019.577535	1019.5754
6	3	E	731.158099	731.156584	19	3	$F_1$	1019.846580	1019.8444
6	1	$F_1$	730.350704	730.349189	19	4	$F_1$	1020.017708	1020.01559
6	2	$F_1$	730.648739	730.647223	19	5	F <sub>1</sub>	1020.344419	1020.3423
6	3	$F_1$	730,999496	730.997980	19	1	$F_2$	1018.698982	1018.6968
6	4	$F_1$	731.147827	731.146312	19	2	$F_2$	1019.205746	1019.2036
6	1	$F_2$	730.644082	730.642566	19	3	$F_2$	1019.594399	1019.5922
6	2	$F_2$	730.851156	730.849641	19	4	$F_2$	1020.057197	1020.0550
6	3	F <sub>2</sub>	730.971611	730.970096	19	5	F <sub>2</sub>	1020.325474	1020.3233
.6	4	$F_2$	731.167861	731.166345	20	1	$A_1$	1125.259813	1125.2574
17	1	$A_1$	821.588940	821.587235	20	2	$A_1$	1126.774992	1126.7726
7	1	$A_2$	821.967857	821.966152	20	1	$A_2$	1126.322145	1126,31980
7	1	E E	821.583353	821.581648	20	1	E E	1125.259936	1125.2575
7	2	E E	822.040644	822.038939	20	2	E E	1126.301046	1126,2987
. 7 . 7	3	E E	822.264838	822.263134	20	3	E E	1126.914542	1126.9122
7 7	3 1		822.264838		20	3 4	E E		
	2	$F_1$		821.225314 821.583456		4 1	_	1127.277972	1127,2756
7 7	3	$F_1$	821.585161		20 20	2	$F_1$	1125.259895	1125,2575
7 7	4	$F_1$	821.831848 822.091787	821.830143 822.090083	20	3	$F_1$	1125.854751 1126.652702	1125.8524 1126.6503
7	4 5	$F_1$				3 4	$F_1$		
		$F_1$	822.273266	822.271561	20	-	$F_1$	1126.875507	1126.8731
7	1	$F_2$	821.227246	821.225541	20	5	$F_1$	1127.268030	1127.2656
7	2	$F_2$	821.851314	821.849609	20	1	$F_2$	1125.853069	1125.8507
7	3	$F_2$	822.015217	822.013513	20	2	$F_2$	1126.307597	1126.3052
7	4	$F_2$	822.253080	822.251375	20	3	$F_2$	1126.610719	1126.6083
8	1	$A_1$	918.074155	918.072249	20	4	$F_2$	1126.969200	1126.9668
8	2	$A_1$	918.673467	918.671561	20	5	$F_2$	1127.286178	1127.2838
8	1	$A_2$	917.348969	917.347064	21	1	$A_1$	1237.704836	1237.7022
8	2	$A_2$	918.643570	918.641665	21	2	$A_1$	1239.460762	1239,4581
8	1	E	917.348724	917.346819	21	1	$A_2$	1238.590763	1238.5881
8	2	E	918.101055	918.099150	21	2	$A_2$	1239.486503	1239.4839
1	1	E	1237.702945	1237.700371	23	2	$F_2$	1476.931645	1476.9285
1	2	Ε	1238.656468	1238.653894	23	3	$F_2$	1477.662249	1477.6591
1	3	Ε	1239.071932	1239.069359	23	4	$F_2$	1478.643528	1478.6404
1	1	$F_1$	1237.013333	1237.010759	23	5	$F_2$	1478.966013	1478.9629

21

21	2	$F_1$	1237.703572	1237.700998	23	6	$F_2$	1479.571893	1479.568818
21	3	$F_1$	1238.234221	1238.231648	24	1	$A_1$	1603.234252	1603.230909
21	4	$F_1$	1238.847660	1238.845086	24	2	$A_1$	1606.147713	1606.144371
21	5	$F_1$	1239.102409	1239.099835	24	3	$A_1$	1607.469790	1607.466447
21	6	F <sub>1</sub>	1239.470210	1239.467636	24	1	$A_2$	1605.112387	1605.109045
21	1	$F_2$	1237.013391	1237.010817	24	2	$A_2$	1607.449546	1607.446203
21	2	$F_2$	1238.245103	1238.242530	24	1	E	1603.234280	1603.230938
21	3	$F_2$	1238.631350	1238.628776	24	2	Ε	1605.104132	1605.100789
21	4	$F_2$	1238.993626	1238.991052	24	3	Е	1606.280425	1606.277082
21	5	$F_2$	1239,478721	1239.476148	24	4	Е	1606.825805	1606.822463
22	1	$A_1$	1355,354332	1355.351513	24	1	$F_1$	1603.234271	1603.230928
22	2	$A_1$	1356.494341	1356.491522	24	2	$F_1$	1604.270615	1604.267273
22	1	$A_2$	1353.940270	1353.937451	24	3	$F_1$	1605.771944	1605.768601
22	2	$A_2$	1356.320179	1356.317360	24	4	$F_1$	1606.230101	1606.226759
22	1	E E	1353.940210	1353.937391	24	5		1606.753619	1606.750277
							$F_1$		
22	2	E	1355.367466	1355.364647	24	6	$F_1$	1607.463398	1607.460056
22	3	Ε	1356.114094	1356.111275	24	1	$F_2$	1604.270118	1604.266776
22	4	E	1356.912872	1356.910053	24	2	$F_2$	1605.106839	1605.103496
22	1	$F_1$	1354.736448	1354.733629	24	3	$F_2$	1605.741723	1605.738380
22	2	$F_1$	1355.362945	1355.360126	24	4	$F_2$	1606.476665	1606.473322
22	3	F <sub>1</sub>	1355.856395	1355.853576	24	5	$\overline{F_2}$	1606.862701	1606.859358
22	4	$F_1$	1356.454866	1356.452047	24	6	$F_2$	1607.456667	1607.453324
22	5	$F_1$	1356.904790	1356.901971	25	1	$A_1$	1736.731639	1736.728018
	1					2	-		
22	-	$F_2$	1353.940230	1353.937411	25		$A_1$	1739.706024	1739.702403
22	2	$F_2$	1354.735518	1354.732699	25	1	$A_2$	1738.415565	1738.411943
22	3	$F_2$	1355.810365	1355.807546	25	2	$A_2$	1739.871268	1739.867647
22	4	$F_2$	1356.150734	1356.147915	25	1	Е	1736.731101	1736.727480
22	5	$F_2$	1356.407031	1356.404212	25	2	Е	1738.454045	1738.450423
22	6	$F_2$	1356.920714	1356.917895	25	3	Е	1739.327023	1739.323402
23	1	$A_1$	1478.255439	1478.252364	25	4	Е	1740.540057	1740.536436
23	1	$A_2$	1476.930964	1476.927889	25	1	F <sub>1</sub>	1735.559822	1735.556200
23	2	_	1478.766065	1478.762989	25	2	$F_1$	1736.731280	1736.727659
		$A_2$				3			
23	1	E	1476.931987	1476.928912	25	-	$F_1$	1737.684814	1737.681193
23	2	E	1478.195633	1478.192558	25	4	$F_1$	1738.952857	1738.949236
23	3	E	1479.014376	1479.011301	25	5	$F_1$	1739.381448	1739.377827
23	4	E	1479.579647	1479.576572	25	6	$F_1$	1739.779934	1739.776313
23	1	$F_1$	1476.020680	1476.017605	25	7	$F_1$	1740.546116	1740.542494
23	2	$F_1$	1477.655170	1477.652095	25	1	$F_2$	1735.559835	1735.556214
23	3	$F_1$	1478.212954	1478.209879	25	2	F <sub>2</sub>	1737.688991	1737.685370
23	4	F <sub>1</sub>	1478.572429	1478.569354	25	3	F <sub>2</sub>	1738.440384	1738.436763
23	5	F <sub>1</sub>	1479.069197	1479.066122	25	4	F <sub>2</sub>	1739.057576	1739.053955
23	6	•	1479.586622	1479.583547	25	5		1739.830043	1739.826422
		$F_1$					$F_2$		
23	1	$F_2$	1476.020708	1476.017632	25	6	$F_2$	1740.533886	1740.530264
26	1	$A_1$	1875.374429	1875.370518	27	2	$A_1$	2022.230675	2022.226463
26	2	$A_1$	1877.546368	1877.542457	27	1	$A_2$	2016.932865	2016.928653
26	1	$A_2$	1872.975628	1872.971717	27	2	$A_2$	2020.325579	2020.321367
26	2	$A_2$	1877.002574	1876.998663	27	3	$A_2$	2022.245447	2022.241236
26	1	Е	1872.975615	1872.971704	27	1	Е	2016.933141	2016.928929
26	2	Е	1875.379193	1875.375282	27	2	Е	2019.138566	2019.134354
26	3	E	1876.862351	1876.858441	27	3	E	2020.562508	2020.558296
26	4	E E	1877.964807	1877.960897	27	4	E	2020.302308	2020.538290
	-					•			
26	5	E	1878.804692	1878.800781	27	1	$F_1$	2015.459312	2015.455100
26	1	$F_1$	1874.293008	1874.289097	27	2	$F_1$	2018.155880	2018.151668
26	2	$F_1$	1875.377593	1875.373682	27	3	$F_1$	2019.147155	2019.142944

J'	и	γ	E(M = 76)	E(M = 74)	,,	n'	λ	E(M = 76)	E(M = 74)
26	3	$F_1$	1876.255926	1876.252016	27	4	$F_1$	2019.879075	2019.874863
26	4	$F_1$	1877.424620	1877.420709	27	2	$F_1$	2020.754215	2020.750003
26	2	$F_1$	1877.915012	1877.911101	27	9	$F_1$	2021.336292	2021.332081
26	9	$F_1$	1878.799028	1878.795117	27	7	$F_1$	2022.235743	2022.231532
26	1	$F_2$	1872.975619	1872.971708	27	1	$F_2$	2015.459318	2015.455107
26	2	$F_2$	1874.292750	1874.288839	27	2	$F_2$	2016.933049	2016.928837
26	3	$F_2$	1876.233741	1876.229830	27	3	$F_2$	2018.158285	2018.154073
26	4	$F_2$	1876.898914	1876.895003	27	4	$F_2$	2019.945637	2019.941426
26	2	$F_2$	1877.323508	1877.319597	27	2	$F_2$	2020.479597	2020.475386
26	9	F <sub>2</sub>	1878.015887	1878.011976	27	9	$F_2$	2021.236676	2021.232464
26	7	$F_2$	1878.810045	1878.806134	27	7	$F_2$	2022.240664	2022.236453
27	1	$A_1$	2019.165347	2019.161136					

Table 8 (continued)

ground vibrational state for the <sup>76</sup>GeH<sub>4</sub> (column 2) and <sup>74</sup>GeH<sub>4</sub> (column 3) isotopologues calculated using the parameters from Table 3 are listed in Table 8.

Some words should be said concerning the procedure of the fit. In the process of assignments of transitions we were able to obtain from the analysis of experimental data more than 100 ground state combination differences (GSCD) for the <sup>76</sup>GeH<sub>4</sub> species and more than 20 GSCD for the <sup>74</sup>GeH<sub>4</sub> one. Any of the GSCD was determined on the basis of transitions from the different ground state rotational states to the concrete upper ro-vibrational state of the (0001) or (0100) vibrational states. Of course, unlike the asymmetric or symmetric top molecules, usually only one line among transition-partners in a concrete GSCD is a strong enough "allowed transition". The others are weak "forbidden transitions". However, all of them are well pronounced in the experimental spectra, and the corresponding ground state combination differences can be determined without doubt. The obtained number of GSCD was more than enough for correct determination of six ground state rotational parameters. When speaking about parameters of the dyad (see Table 1), as was mentioned in Ref. [72] (see also Ref. [73]), there are 19 quasi-linear relationships among the 62 upper state parameters. It means that in a general case, the number of independent parameters is 43. In the present study the number of fitted parameters of upper states was 30 for the <sup>76</sup>GeH<sub>4</sub> species and only 10 for the <sup>74</sup>GeH<sub>4</sub> species (that is much less than 43).

The result of the analogous fit of transitions assigned to the <sup>74</sup>GeH<sub>4</sub> isotopologue is shown in column 3 of Tables 3–6. As the value of the  $(M_{76} - M_{74})/M_{76}$  ratio is very small, one can expect that the differences between absolute values of spectroscopic parameters of the same type of the <sup>76</sup>GeH<sub>4</sub> and <sup>74</sup>GeH<sub>4</sub> isotopologues will be nonzero only for the largest parameters. For that reason, values of the majority of parameters of the <sup>74</sup>GeH<sub>4</sub> isotopologue were fixed in the fit to the values of the corresponding parameters of <sup>76</sup>GeH<sub>4</sub> (they are presented in Tables 3-6 without confidence intervals). The final set of 11 fitted parameters (1 parameter of the ground vibrational state and 10 parameters of the dyad) is presented in column 3 of Tables 3-6 and reproduces the initial 788 transitions ( $J^{max.} = 24$ ) of the <sup>74</sup>GeH<sub>4</sub> isotopologue with  $d_{ms} = 2.05 \times 10^{-4} \text{ cm}^{-1} \ (d_{ms} = 1.79 \times 10^{-4} \text{ cm}^{-1} \text{ for the } \nu_4 \text{ band, and } d_{ms} = 2.52 \times 10^{-4} \text{ cm}^{-1} \text{ for the } \nu_2 \text{ band). It}$ should also be mentioned that the parameters of Tables 3-6 have the same sense as the parameters used in the XTDS program package with only one exception: the  $Y_{\nu_{x},\nu_{y}}^{\Omega(K,A_{1})}$  parameters in our case are real spectroscopic parameters of the corresponding vibrational state, but the analogous parameters in the XTDS program package are increments to the lower polyad parameters (see, e.g., Ref. [44]).

To give the reader a possibility to judge the quality of the results, Fig. 3 shows the fit residuals for line positions as a function of quantum number J. Fig. 4 presents the diagram of calculated reduced energy levels for the dyad of  $^{76}\text{GeH}_4$  as defined by the equation

$$E_{lny}^{red.}/hc = E_{lny}/hc - B_{gr}J(J+1) + D_{gr}J^{2}(J+1)^{2} - \cdots$$
 (11)

Fig. 5 illustrates the comparison between the experimental spectrum for the dyad (top part of Fig. 5) and the synthetic

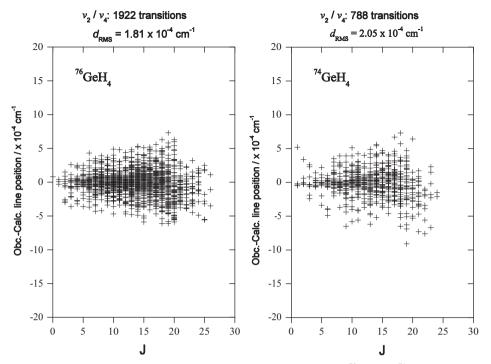
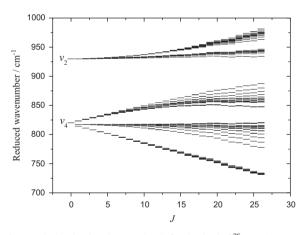


Fig. 3. Observed–calculated line positions and fit statistics for the  $\nu_2/\nu_4$  dyad of the  $^{76}\text{GeH}_4$  and  $^{74}\text{GeH}_4$  isotopologues.

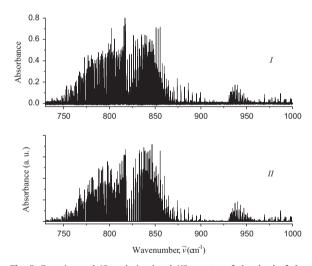


**Fig. 4.** Calculated reduced energy levels for the dyad of  $^{76}{\rm GeH_4}$  (see text for details).

spectrum (bottom part of Fig. 5) constrained on the base of the parameters derived in the present study. In all of Figs. 3–5 one can see more than satisfactory correspondence between experimental and theoretical results.

#### 5. Conclusion

We recorded the high resolution FTIR spectrum of  $^{76}\text{GeH}_4$  with a small amount of  $^{74}\text{GeH}_4$  (88.1% of  $^{76}\text{GeH}_4$  and 11.5% of  $^{74}\text{GeH}_4$  in the sample) in the region of the dyad,  $\nu_2/\nu_4$ . As the result of assignment of the experimental transitions, 1922 lines with the value of  $J^{\text{max.}} = 26$ 



**Fig. 5.** Experimental (I) and simulated (II) spectra of the dyad of the  $^{76}\text{GeH}_4$  and  $^{74}\text{GeH}_4$  isotopologues. Experimental conditions for the spectrum I: absorption path length is 20 cm; room temperature; number of scans is 1000; sample pressure is 0.4 Torr. Simulated spectrum: line positions were calculated with the parameters obtained from the fit and presented in Tables 3–6.

and 788 lines with the value of  $J^{max} = 24$  were assigned to the  $^{76}\text{GeH}_4$  and  $^{74}\text{GeH}_4$  isotopologues, respectively. Analysis of the assigned transitions was made on the basis of a specially constructed Fortran code, SPHETOM. The set of 36 spectroscopic parameters reproduces the 1922 line positions of  $^{76}\text{GeH}_4$  with the  $d_{rms.} = 1.81 \times 10^{-4} \text{ cm}^{-1}$ . Analogously, the additional set of 11 fitted parameters

reproduces the 788 line positions of  $^{74}$ GeH<sub>4</sub> with the  $d_{rms} = 2.05 \times 10^{-4} \text{ cm}^{-1}$ .

#### **Acknowledgments**

This research was supported by the Foundation of the President of the Russian Federation (Grant no. MK-4872.2014.2). Part of the work was made under the project FTI-120 of the Tomsk Polytechnic University.

### Appendix A. Rotational operators symmetrized in the SO (3) symmetry group

In accordance with Eqs. (1)–(5), the symmetrized rotational operators,  $R_n^{\Omega(K)}$  ( $0 \le \Omega \le 3$ , and  $0 \le K \le 3$ ), can be obtained in the following form:

$$R_{0}^{1(1)} = J_{0} \quad J_{0} | Jk \rangle = k | Jk \rangle$$

$$R_{+1}^{1(1)} = -J_{+} = -\frac{1}{\sqrt{2}} \left( J_{x} - iJ_{y} \right) \quad J_{+} | Jk \rangle$$

$$= \frac{1}{\sqrt{2}} (J(J+1) - k(k+1))^{1/2} | Jk + 1 \rangle$$

$$R_{-1}^{1(1)} = J_{-} = \frac{1}{\sqrt{2}} \left( J_{x} + iJ_{y} \right) \quad J_{-} | Jk \rangle$$

$$= \frac{1}{\sqrt{2}} (J(J+1) - k(k-1))^{1/2} | Jk - 1 \rangle, \tag{12}$$

$$\begin{split} R_0^{2(2)} &= \sqrt{\frac{3}{2}} J_0^2 - \frac{1}{\sqrt{6}} J^2 \\ R_{\pm 1}^{2(2)} &= \mp \frac{1}{\sqrt{2}} [J_0, J_{\pm}]_+ \\ R_{\pm 2}^{2(2)} &= J_{\pm}^2 \\ R_0^{2(0)} &= J^2, \end{split} \tag{13}$$

$$\begin{split} R_0^{3(3)} &= -\frac{3}{\sqrt{10}} J^2 J_0 + \sqrt{\frac{5}{2}} J_0^3 + \frac{1}{\sqrt{10}} J_0 \\ R_{\pm 1}^{3(3)} &= \pm \frac{3}{2\sqrt{15}} J_{\pm} J^2 \mp \frac{\sqrt{15}}{4} \left( J_{\pm} J_0^2 + J_0^2 J_{\pm} \right) \pm \frac{3}{4\sqrt{15}} J_{\pm} \\ R_{\pm 2}^{3(3)} &= \frac{\sqrt{3}}{2} \left( J_0 J_{\pm}^2 + J_{\pm}^2 J_0 \right) \\ R_{\pm 3}^{3(3)} &= \mp J_{\pm}^3 \\ R_{\pm 1}^{3(1)} &= \mp J^2 J_{\pm} \\ R_0^{3(1)} &= J^2 J_0, \end{split}$$
 (14)

Appendix B. Analytical representation of the  ${}^{(K)}G^m_{n_{T\alpha}}$ 

elements for the reduction  $T_d \leftarrow SO(3)$ 

where  $I^2 = \sum_{\alpha} I_{\alpha}^2$ 

As was shown in Ref. [53], the elements of the G-matrix for  $T_d$ -symmetry molecule can be determined from the following analytical expressions:

$${}^{J}G_{kF_{\lambda}z}^{m} = \frac{\exp(i\phi_{J})[1 - (-1)^{J}\delta_{k0}]}{2\sqrt{2}} \left[1 - (-1)^{\lambda+k/2}\right] \left[\delta_{km} - (-1)^{J}\delta_{-km}\right], \tag{15}$$

$${}^{J}G_{kF,y}^{m} = \frac{\exp(i\phi_{J})[1 - (-1)^{J}\delta_{k0}]}{2\sqrt{2}(1 + \delta_{k0})^{3/2}} \left[1 - (-1)^{\lambda + k/2}\right] (-i)^{m} \left[1 - (-1)^{m}\right] d_{km}^{J}(\pi/2), \tag{16}$$

$${}^{J}G_{kF,x}^{m} = (-1)^{\lambda+1} \frac{\exp(i\phi_{j})[1 - (-1)^{j}\delta_{k0}]}{2\sqrt{2}} \left[1 - (-1)^{\lambda+k/2}\right] \left[1 - (-1)^{m}\right] d_{km}^{J}(\pi/2),$$
(17)

$$^{J}G_{kA_{\lambda}}^{m} = \sum_{n=L}^{k} \alpha_{kn}^{JA_{\lambda}} \frac{\exp(i\chi_{J})}{2\sqrt{6}} \Big[ 1 - (-1)^{\lambda + n/2} \Big] \\
\times \{ [1 + (-1)^{m}] [1 - (-1)^{\lambda + m/2}] d_{nm}^{J}(\pi/2) - (-1)^{\lambda} \delta_{nm} \\
- (-1)^{\lambda + J} \delta_{-nm} \}.$$
(18)

and

$$^{J}G_{kE_{\lambda}}^{m} = (-1)^{\lambda+1} \sum_{n=L}^{k} \alpha_{kn}^{JE} \frac{\exp(i\chi_{J})}{4(1+2\delta_{\lambda 1})^{1/2}} \Big[ 1 + (-1)^{n/2} \Big]$$

$$\times \{ [1 + (-1)^{m}] [1 - (-1)^{\lambda+m/2}] d_{nm}^{J}(\pi/2) - 2\delta_{\lambda 1} [\delta_{nm} + (-1)^{J}\delta_{-nm}] \}.$$

$$(19)$$

In Eqs. (14)–(18)  $\lambda=1$  or 2, and the phases  $\exp(i\phi_J)$  and  $\exp(i\chi_J)$  are chosen so that  $\exp(i\phi_J)=-i\exp(i\chi_J)=1$  for odd J and  $\exp(i\phi_J)=i\exp(i\chi_J)=i$  for even J (the phases are chosen in such a way that to satisfy the relations  ${}^JG^{-m}_{k\gamma\sigma}=(-1)^m ({}^JG^{-m}_{k\gamma\sigma})^*$ ; the validity of lasts is necessary if one wants to provide the elements of the Hamiltonian matrix to be real, see, e.g., [43]). The quantities  $d^J_{km}(\pi/2)$  are known from the angular momentum theory, [47]:

$$d_{km}^{J}(\pi/2) = (-1)^{k+m} \frac{1}{2^{J}} \left( \frac{(J+k)!(J-k)!}{(J+m)!(J-m)!} \right)^{1/2}$$

$$\sum_{r} (-1)^{r} {J+m \choose r} {J-m \choose \tau+k-m}.$$
(20)

The index k in (14)–(18) takes the values 0, 2, 4,..., J (or J-1) only. In Eqs. (17) and (18) n=L,L+4,L+8,...,k and L=0 for  $\Gamma=A_1$  or E, L=2 for  $\Gamma=A_2$ . The coefficients  $\alpha_{kn}^{IT}$  can be obtained from simple recurrence relations:

$$(\alpha_{kk}^{I\Gamma})^{-1/2} = 1 + \delta_{k0}(-1)^{J} + [4(-1)^{\Gamma} - 6\delta_{\Gamma E}]d_{kk}^{J}(\pi/2)$$

$$- \sum_{l=L}^{K-4} \sum_{i \le l, j \le l} \alpha_{li}^{J\Gamma} \alpha_{lj}^{J\Gamma} [4(-1)^{\Gamma} - 6\delta_{\Gamma E}]^{2} d_{ki}^{J}(\pi/2) d_{kj}^{J}(\pi/2),$$
(21)

and

$$\alpha_{kn}^{J\Gamma} = -\alpha_{kk}^{J\Gamma} \sum_{i>n}^{k-4} \sum_{j< i} \alpha_{ij}^{J\Gamma} \alpha_{in}^{J\Gamma} [4(-1)^{\Gamma} - 6\delta_{\Gamma E}] d_{kj}^{J}(\pi/2). \tag{22}$$

In Eqs. (20) and (21) the numbers k, n, i, j, and l are multiples of 4 when  $\Gamma = A_1$  or E, and are even but not multiples of 4 when  $\Gamma = A_2$ .

## Appendix C. Nonzero $3\Gamma$ -symbols of the $T_d$ symmetry group

The nonzero  $3\Gamma$ -symbols of the  $T_d$  symmetry group, which are reproduced here from Ref. [49], have the following form:

$$\begin{pmatrix} A_1 & \gamma & \gamma' \\ & s & s' \end{pmatrix} = \frac{1}{\sqrt{|\gamma|}} \delta_{\gamma\gamma'} \delta_{ss'} \quad \text{where } \gamma \text{ and } s \text{ are arbitrary};$$

$$\begin{pmatrix} A_{2} & E & E \\ & 1 & 2 \end{pmatrix} = \frac{1}{\sqrt{2}}; \quad \begin{pmatrix} A_{2} & F_{1} & F_{2} \\ & \alpha & \beta \end{pmatrix} = \frac{1}{\sqrt{3}} \delta_{\alpha\beta}, \alpha, \beta = x, y, z;$$

$$\begin{pmatrix} E & E & E \\ 1 & 1 & 1 \end{pmatrix} = -\begin{pmatrix} E & E & E \\ 1 & 2 & 2 \end{pmatrix} = -\frac{1}{2};$$

$$\begin{pmatrix} E & F_{1} & F_{1} \\ 1 & z & z \end{pmatrix} = \begin{pmatrix} E & F_{2} & F_{2} \\ 1 & z & z \end{pmatrix} = -\frac{1}{\sqrt{3}};$$

$$\begin{pmatrix} E & F_1 & F_1 \\ 1 & x & x \end{pmatrix} = \begin{pmatrix} E & F_1 & F_1 \\ 1 & y & y \end{pmatrix} = \begin{pmatrix} E & F_2 & F_2 \\ 1 & x & x \end{pmatrix}$$

$$= \begin{pmatrix} E & F_2 & F_2 \\ 1 & y & y \end{pmatrix} = \frac{1}{2\sqrt{3}};$$

$$\begin{pmatrix} E & F_1 & F_1 \\ 2 & x & x \end{pmatrix} = -\begin{pmatrix} E & F_1 & F_1 \\ 2 & y & y \end{pmatrix} = \begin{pmatrix} E & F_2 & F_2 \\ 2 & x & x \end{pmatrix}$$

$$= -\begin{pmatrix} E & F_2 & F_2 \\ 2 & y & y \end{pmatrix} = -\frac{1}{2};$$

$$\begin{pmatrix} E & F_1 & F_2 \\ 1 & x & x \end{pmatrix} = -\begin{pmatrix} E & F_1 & F_2 \\ 1 & y & y \end{pmatrix} = -\frac{\sqrt{3}}{2} \begin{pmatrix} E & F_1 & F_2 \\ 2 & z & z \end{pmatrix}$$

$$= \sqrt{3} \begin{pmatrix} E & F_1 & F_2 \\ 2 & x & x \end{pmatrix} = \sqrt{3} \begin{pmatrix} E & F_1 & F_2 \\ 2 & y & y \end{pmatrix} = -\frac{1}{2};$$

$$\begin{pmatrix} F_1 & F_1 & F_1 \\ x & y & z \end{pmatrix} = \begin{pmatrix} F_2 & F_2 & F_2 \\ x & y & z \end{pmatrix} = \begin{pmatrix} F_1 & F_1 & F_2 \\ x & y & z \end{pmatrix} = \begin{pmatrix} F_1 & F_1 & F_2 \\ x & y & z \end{pmatrix}$$

$$= \begin{pmatrix} F_1 & F_1 & F_2 \\ z & x & y \end{pmatrix} = \begin{pmatrix} F_2 & F_2 & F_1 \\ x & y & z \end{pmatrix}$$

$$= \begin{pmatrix} F_2 & F_2 & F_1 \\ z & x & y \end{pmatrix} = -\frac{1}{\sqrt{6}}.$$

In this case, the following relations are valid for the nonzero  $3\Gamma$ -symbols:

$$\begin{pmatrix} \gamma_1 & \gamma_2 & \gamma_3 \\ s_1 & s_2 & s_3 \end{pmatrix} = \begin{pmatrix} \gamma_3 & \gamma_1 & \gamma_2 \\ s_3 & s_1 & s_2 \end{pmatrix} = \begin{pmatrix} \gamma_2 & \gamma_3 & \gamma_1 \\ s_2 & s_3 & s_1 \end{pmatrix}$$

$$= (-1)^{\gamma_1 + \gamma_2 + \gamma_3} \begin{pmatrix} \gamma_2 & \gamma_1 & \gamma_3 \\ s_2 & s_1 & s_3 \end{pmatrix},$$

where  $(-1)^{A_1} = -(-1)^{A_2} = (-1)^E = -(-1)^{F_1} = (-1)^{F_2} = 1$ .

#### Appendix D. Supplementary data

Supplementary data associated with this article can be found in the online version at http://dx.doi.org/10.1016/j.jqsrt.2014.03.025.

#### References

- Haller EE. Germanium: from its discovery to SiGe devices. Mater Sci Semicond Process 2006:9:408–22.
- [2] Chen F, Judge DL, Wu CYR, Caldwell J, White HP, Wagener R. Highresolution, low-temperature photoabsorption cross sections of C<sub>2</sub>H<sub>2</sub>, PH<sub>3</sub>, AsH<sub>3</sub>, and GeH<sub>4</sub>, with application to Saturn's atmosphere. J Geophys Res 1991;96:17519–27.
- [3] Atreya SK, Mahaffy PR, Niemann HB, Wong MH, Owen TC. Composition and origin of the atmosphere of Jupiter—an update, and implications for the extrasolar giant planets. Planet Space Sci 2003;51:105–12.
- [4] Lodders K. Jupiter formed with more tar than ice. Astrophys | 2004;611:587–97.
- [5] Lodders K. Atmospheric chemistry of the gas giant planets. Geochemical Society; Geochemical News 142 - Jan 2010. (http://www. geochemsoc.org/publications/geochemicalnews/gn142jan10/atmo sphericchemistryoftheg/).
- [6] Steward WB, Nielsen HH. The infrared absorption spectrum of germane. Phys Rev 1935;48:861–4.
- [7] Lee E, Sutherland GBBM. A peculiarity in the infra-red absorption spectrum of germane. Math Proc Camb Philos Soc 1939;35:341-2.
- [8] Murphy GM. Coriolis perturbations in the spectra of silane and germane. J Chem Phys 1940;8:71–8.
- [9] Tindal CH, Straley JW, Nielsen HH. The infra-red spectra of SiH<sub>4</sub> and GeH<sub>4</sub>. Proc Natl Acad Sci US 1941;27(4):208–12.

- [10] Straley JW, Tindal CH, Nielsen HH. The vibration–rotation spectrum of GeH<sub>4</sub>. Phys Rev 1942;62:161–5.
- [11] Wilkinson GR, Wilson MK. Infrared spectra of some MH<sub>4</sub> molecules. J Chem Phys 1966;44:3867–74.
- [12] Levin IW. Infrared intensities of the fundamental vibrations of GeH<sub>4</sub> and GeD<sub>4</sub>. J Chem Phys 1965;42:1244–51.
- [13] Chalmers AA, McKean DC. Infra-red intensities in GeH<sub>4</sub>. Spectrochim Acta 1965;21:1941–5.
- [14] Corice Jr. J, Fox K, Fletcher WH. Studies of absorption spectra of GeH<sub>4</sub> in the 2– $17\mu$  region. J Mol Spectrosc 1972;41:95–104.
- [15] Kattenberg HW, Gabes W, Oskam A. Infrared and laser Raman gas spectra of GeH<sub>4</sub>. J Mol Spectrosc 1972;44:425–42.
- [16] Ozier IO, Rosenberg A. The forbidden rotational spectrum of  $GeH_4$  in the Ground Vibronic State. Can J Phys 1973;51(17):1882–95.
- [17] Curl RF, Oka T, Smith DS. The observation of a pure rotational Q-branch transition of methane by infrared-radio frequency double resonance. J Mol Spectrosc 1973;46:518–20.
- [18] Curl Jr. RF. Infrared-radio frequency double resonance observations of pure rotational Q-branch transitions of methane. J Mol Spectrosc 1973;48:165–73.
- [19] Kreiner WA, Oka T. Infrared-radio-frequency double resonance observations of  $\Delta J=0$  "forbidden" rotational transitions of SiH<sub>4</sub>. Can J Phys 1975;53:2000–6.
- [20] Kreiner WA, Andresen U, Oka T. Infrared-microwave double resonance spectroscopy of GeH<sub>4</sub>. J Chem Phys 1977;66:4662–5.
- [21] Kreiner WA, Orr BJ, Andresen U, Oka T. Measurement of the centrifugal-distortion dipole moment of GeH<sub>4</sub> using a CO<sub>2</sub> laser. Phys Rev A 1977:15:2298–304.
- [22] Kagann RH, Ozier I, Gerry MCL. The centrifugal distortion dipole moment of silane. J Chem Phys 1976;64:3487–8.
- [23] Lepage P, Brégier R, Saint-Loup R. La bande  $\nu_3$  du germane. C R Acad Sci Ser B 1976;283:179–80.
- [24] Kagann RH, Ozier I, McRae GA, Gerry MCL. The distortion moment spectrum of GeH<sub>4</sub>: the microwave Q branch. Can J Phys 1979;57: 593–600.
- [25] Daunt SJ, Halsey GW, Fox K, Lovell RJ, Gailar NM. High-resolution infrared spectra of  $\nu_3$  and  $2\nu_3$  of germane. J Chem Phys 1978;68: 1319–21.
- [26] Fox K, Halsey GW, Daunt SJ, Kennedy RC. Transition moment for  $\nu_3$  of  $^{74}$ GeH $_4$ . J Chem Phys 1979;70:5326–7.
- [27] Kreiner WA, Magerl G, Furch B, Bonek E. IR laser sideband observations in GeH<sub>4</sub> and CD<sub>4</sub>. J Chem Phys 1979;70:5016–20.
- [28] Magerl G, Schupita W, Bonek E, Kreiner WA. Observation of the isotope effect in the  $\nu_2$  fundamental of germane. J Chem Phys 1980;72:395–8.
- [29] Kreiner WA, Opferkuch R, Robiette AG, Turner PH. The ground-state rotational constants of germane. J Mol Spectrosc 1981;85:442–8.
- [30] Lepage P, Champion JP, Robiette AG. Analysis of the  $\nu_3$  and  $\nu_1$  infrared bands of GeH<sub>4</sub>. J Mol Spectrosc 1981;89:440–8.
- [31] Cheglokov AE, Kuritsin YuA, Snegirev EP, Ulenikov ON, Vedeneeva GV. High-resolution spectroscopy of the ν<sub>2</sub> Q branch of GeH<sub>4</sub>, with a computer-assisted, pulsed-diode laser spectrometer. J Mol Spectrosc 1984;105:385–96.
- [32] Cheglokov AE, Kuritsin YuA, Snegirev EP, Ulenikov ON, Vedeneeva GV. Study of the  $\nu_2$  infrared band of GeH<sub>4</sub>: Q-branch. Mol Phys 1984;53:287–94.
- [33] Schaeffer RD, Lovejoy RW. Absolute line strengths of  $^{74}$ GeH $_4$  near 5  $\mu$ m. J Mol Spectrosc 1985;113:310–4.
- [34] Zhu Q, Thrush BA, Robiette AG. Local mode rotational structure in the (3000) Ge–H stretching overtone ( $3\nu_3$ ) of germane. Chem Phys Lett 1988:150:181–3.
- [35] Zhu Q, Thrush BA. Rotational structure near the local mode limit in the (3000) band of germane. J Chem Phys 1990;92:2691–7.
- [36] Zhu Q, Qian H, Thrush BA. Rotational analysis of the (2000) and (3000) bands and vibration-rotation interaction in germane local mode states. Chem Phys Lett 1991;186:436–40.
- [37] Campargue A, Vetterhöffer J, Chenevier M. Rotationally resolved overtone transitions of <sup>70</sup>GeH<sub>4</sub> in the visible and near-infrared. Chem Phys Lett 1992;192:353–6.
- [38] Zhu Q, Campargue A, Vetterhöffer J, Permogorov D, Stoeckel F. High resolution spectra of GeH<sub>4</sub> v=6 and 7 stretch overtones. The perturbed local mode vibrational states. J Chem Phys 1993;99: 2359–64.
- [39] Sun F, Wang X, Liao J, Zhu Q. The (5000) local mode vibrational state of germane: a high-resolution spectroscopic study. J Mol Spectrosc 1997:184:12–21.
- [40] Chen XY, Lin H, Wang XG, Deng K, Zhu QS. High-resolution Fourier transform spectrum of the (4000) local mode overtone of GeH<sub>4</sub>: local mode effect. J Mol Struct 2000;517–518:41–51.

- [41] Maki AG, Wells JS, Wavenumber calibration tables from heterodyne frequency measurements (version 1.3). Gaithersburg, MD: NIST; 1998. Available online: (http://www.nist.gov/pml/data/wavenum/ spectra.cfm).
- [42] Moret-Bailly J. Sur l'interprétation des spectres de vibration-rotation des molécules à symmétrie tétraédrique ou octaédrique. Cah Phys 1961;15:238–314.
- [43] Champion JP, Pierre G, Michelot F, Moret-Bailly J. Composantes cubiques normales des tenseurs spheriques. Can J Phys 1977;55: 512–20
- [44] Champion JP. Developpement complet de l'hamiltonien de vibration-rotation adapté à l'étude des interactions dans les molécules toupies sphériques. Application aux bandes ν<sub>2</sub> et ν<sub>4</sub> de <sup>12</sup>CH<sub>4</sub>. Can I Phys 1977:55:1802–28.
- [45] Fano U, Racah G. Irreducible tensorial sets. New York: Academic Press; 1959.
- [46] Wigner EP. Quantum theory of angular momentum. New York: Academic Press; 1965.
- [47] Varshalovitch DA, Moskalev AN, Khersonsky VK. Quantum theory of angular momentum. Leningrad: Nauka; 1975.
- [48] Boudon V, Champion JP, Gabard T, Loëte M, Rotger M, Wenger Ch. Spherical top theory and molecular spectra. In: Quack M, Merkt F, editors. Handbook of high-resolution spectroscopy, vol. 3. Chichester: Wiley; 2011. p. 1437–60.
- [49] Makushkin YuS, Ulenikov ON, Cheglokov AE. Symmetry and its applications to the problems of molecular vibration-rotation spectroscopy, Parts I and II. Tomsk; Tomsk State University Press; 1990.
- [50] Ulenikov ON, Bekhtereva ES, Fomchenko AL, Litvinovskaya AG, Leroy C, Quack M. On the "expanded local mode" approach applied to the methane molecule: Isotopic substitution CH<sub>3</sub>D←CH<sub>4</sub> and CHD<sub>3</sub>←CH<sub>4</sub>. Mol Phys, 2014, in press.
- [51] Moret-Bailly J, Gautier L, Montagutelli J. Clebsch-Gordan coefficients adapted to cubic symmetry. J Mol Spectrosc 1965;15:355-77.
- [52] Rey M, Boudon V, Wenger Ch, Pierre G, Sartakhov B. Orientation of O(3) and SU(2) ⊗ C<sub>1</sub> representation in cubic point groups (O<sub>h</sub>, T<sub>d</sub>) for application to molecular spectroscopy. J Mol Spectrosc 2003;219: 313–25.
- [53] Cheglokov AE, Ulenikov ON. On determination of the analytical formulas for reduction matrices of tetrahedral-symmetry molecules. J Mol Spectrosc 1985;110:53–64.
- [54] Ulenikov ON, Bekhtereva ES, Albert S, Bauerecker S, Niederer HM, Quack M. Survey of the high resolution infrared spectrum of methane (<sup>12</sup>CH<sub>4</sub> and <sup>13</sup>CH<sub>4</sub>): partial vibrational assignment extended towards 12000 cm<sup>-1</sup>. J Chem Phys, 2014, submitted for publication.
- [55] Ulenikov ON, Bekhtereva ES, Albert S, Bauerecker S, Hollenstein H, Quack M. High resolution infrared spectroscopy and global vibrational analysis for the CH<sub>3</sub>D and CHD<sub>3</sub> isotopomers of methane. Mol Phys 2010;108:1209–40.
- [56] Nielsen HH. The vibration–rotation energies of molecules. Rev. Mod. Phys. 1951;23:90.
- [57] Papousek D, Aliev MR. Molecular vibrational–rotational spectra. Amsterdam, Oxford, New York: Elsevier Scientific Publishing Company; 1982.

- [58] Ulenikov ON, Sun F-G, Wang X-G, Zhu Q-S. High resolution spectroscopic study of arsine:  $3\nu_3$  and  $2\nu_1+\nu_3$  dyad the tendency of symmetry reduction. J Chem Phys 1996;105:7310–5.
- [59] Han J-X, Ulenikov ON, Yurchinko S, Hao L-Y, Wang X-G, Zhu Q-S. High resolution photoacoustic spectrum of AsH<sub>3</sub> (600A<sub>1</sub>/E) bands. Spectrochim Acta A 1997;53:1705–12.
- [60] Hai L, Ulenikov ON, Yurchinko S, Wang X-G, Zhu Q-S. High resolution spectroscopic study of the (310) local mode combination band system of AsH<sub>3</sub>, I Mol Spectrosc 1998;187:89–96.
- [61] Ülenikov ON, Bekhtereva ES, Kozinskaia VA, Zheng J-J, He S-G, Hu S-M, et al. On the study of resonance interactions and splittings in the PH<sub>3</sub> molecule:  $\nu_1$ ,  $\nu_3$ ,  $\nu_2 + \nu_4$  and  $2\nu_4$  bands. J Mol Spectrosc 2002;215:295–308.
- [62] Ulenikov ON, Malikova AB, Li H-F, Qian H-B, Zhu Q-S, Thrush BA. High-resolution spectroscopic study of  $2\nu_1$ ,  $2\nu_3$ , and  $\nu_1+\nu_2$  stretching states: the local mode effects of H<sub>2</sub>Se. J Chem Soc Faraday Trans 1995;91:13–6.
- [63] Zhou Z-Y, Wang X-H, Zhou Z-P, Ulenikov ON, Onopenko GA, Zhu Q-S. High resolution spectroscopic study of H<sub>2</sub>Se (40<sup>+</sup>, 0) A<sub>1</sub> and (40<sup>-</sup>, 0) B<sub>2</sub> stretching states: normal mode and local mode analysis. Mol Phys 1997;92:1073–81.
- [64] Wang X-H, Ulenikov ON, Onopenko GA, Bekhtereva ES, He S-G, Hu S-M, et al. High resolution study of the first hexad of  $D_2O$ . J Mol Spectrosc 2000;200:25–33.
- [65] Hu S-M, Ulenikov ON, Onopenko GA, Bekhtereva ES, He S-G, Wang X-H, et al. High-resolution study of strongly interacting vibrational bands of HDO in the region 7600–8100 cm<sup>-1</sup>. J Mol Spectrosc 2000;203:228–34.
- [66] Ulenikov ON, Bekhtereva ES, Onopenko GA, Sinitsin EA, Bürger H, Jerzembeck W. Isotopic effects in XH<sub>3</sub> molecules: the lowest vibrational bands of PH<sub>2</sub>D reinvestigated. J Mol Spectrosc 2001;208: 236–48.
- [67] Ulenikov ON, Hu S-M, Bekhtereva ES, Onopenko GA, He S-G, Wang X-H, et al. High-resolution Fourier transform spectrum of D<sub>2</sub>O in the region near 0.97 μm. | Mol Spectrosc 2001;210:18–27.
- [68] Ulenikov ON, Gromova OV, Bekhtereva ES, Bolotova IB, Konov IA, Horneman VM, et al. High resolution analysis of the SO<sub>2</sub> spectrum in the 2600–2900 cm<sup>-1</sup> region:  $2\nu_3$ ,  $\nu_2 + 2\nu_3 \nu_2$  and  $2\nu_3 + \nu_2$  bands. J Quant Spectrosc Radiat Transf 2012;113:500–17.
- [69] Ulenikov ON, Gromova OV, Aslapovskaya YuS, Horneman VM. High resolution spectroscopic study of C<sub>2</sub>H<sub>4</sub>: re-analysis of the ground state and ν<sub>4</sub>, ν<sub>7</sub>, ν<sub>10</sub>, and ν<sub>12</sub> vibrational bands. J Quant Spectrosc Radiat Transf 2013;118:14–25.
- [70] Wenger C, Boudon V, Champion JP, Pierre G. Highly-spherical top data system (HTDS) software for spectrum simulation of octahedral XY<sub>6</sub> molecules. J Quant Spectrosc Radiat Transf 2000;66:1–16.
- [71] Wenger C, Boudon V, Rotger M, Sanzharov M, Champion JP. XTDS and SPVIEW: graphical tools for the analysis and simulation of highresolution molecular spectra. J Mol Spectrosc 2008;251:102–13.
- [72] Champion JP, Hilico JC, Wenger C, Brown LR. Analysis of the  $\nu_2/\nu_4$  dyad of  $^{12}\text{CH}_4$  and  $^{13}\text{CH}_4$ . J Mol Spectrosc 1989;133:256–72.
- [73] Ulenikov ON. On the determination of the reduced rotational operator for polyatomic molecules. J Mol Spectrosc 1986;119: 144–52.