

Five number Summary

- 1) minimum
- 2) First Quartile (Q_1) 25%
- 3) Median (Q_2) 50%
- 4) Third Quartile (Q_3) 75%
- 5) maximum.

Note: Choose these 5 numbers after removing the outlier from the data by finding boundary values.

[Lower fence upper

$$LF = Q_1 - 1.5(IQR)$$

$$UF = Q_3 + 1.5(IQR)$$

$$IQR = (\text{inter quartile range})$$

$$IQR = Q_3 - Q_1$$

$$\{1, 1, 2, 3, 4, 4, 4, 5, 5, 6, 7, 7, 8, 8, 9\} \setminus \{28, 36\} = 15$$

outlier

~~LF = Q1~~

$$Q_1 = \frac{25}{100} \times 18$$

$$= 4.5 \text{ index}$$

$$Q_1 = 3$$

$$Q_3 = \frac{75}{100} \times 18$$

$$= 13.5 \text{ index}$$

$$Q_3 = 8$$

$$IQR = Q_3 - Q_1$$

$$= 8 - 3 = 5$$

$$LF = Q_1 - 1.5(IQR)$$

$$= 3 - 1.5(5)$$

$$= -4.5$$

$$UF = 8 + 1.5(5)$$

$$= 15.5$$

$y < -4.5$ and > 15.5 is outlier

minimum = 1

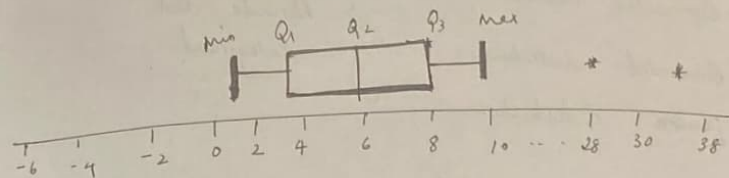
$$Q_1 = 3$$

$$Q_3 = 8$$

$$\text{median} = 5$$

$$\text{max} = 9$$

Boxplot



This graph is used to find the outlier

Different types Distribution

- To understand data patterns
- To summarise the data easily
- To calculate probability
- To make prediction and decision
- To choose right statistical test

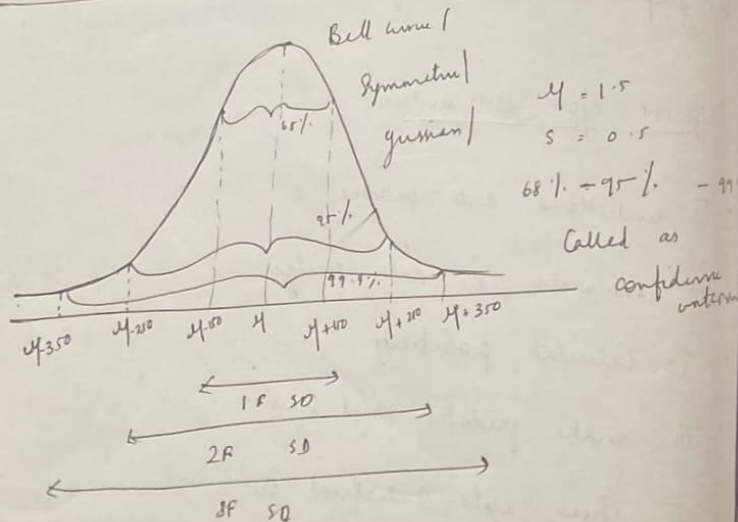
There are 2 Category

- 1) Continuous distribution (Number)
 \rightarrow Any value including decimal (measuring)
 eg. Weight = 52.8 kg, time = 4.36 Sec
- 2) Discrete distribution (Categorical distribution)
 \rightarrow Specific values - you count them.
 eg. No. of students in class = 20, 21, 22 (not 20.5)

1) Normal distribution } continuous dist
 2) Standard normal distribution } numerical

3) Bernoulli distribution } Discrete dist
 4) Binomial distribution } Categorical.
 5) Poisson distribution

1) Normal distribution

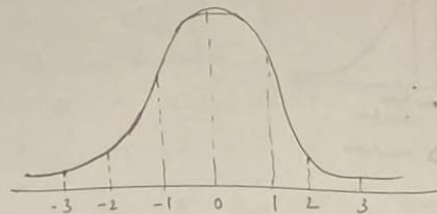


Empirical rule

- 68% of data will be present in 1SD
- 95% of data will be present in 2SD
- 99.7% of data will be present in 3SD

2) Standard Normal distribution

$\mu = 0$
 $\sigma = 1$ } Always



$$Z \text{ score} = \frac{x_i - \mu}{\sigma} = \frac{2 - 3.86}{2}$$

Normal dist data

Standard Normal dist data

2

-0.93

1

1.57

$\mu = 0$

5

0.57

$\sigma = 0.94$

4

0.07

1

-1.43

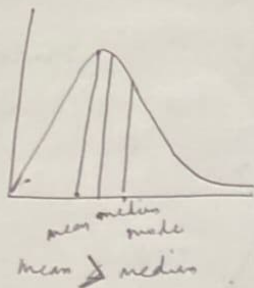
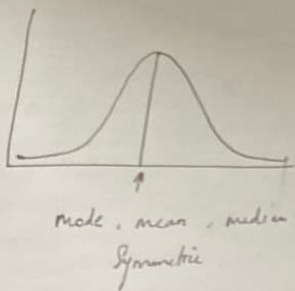
3

-0.43

0

0.57

Symmetric



Positive Skew (Right Skew)

Tail on the right side is longer most data are on the left

Negative Skew (Left Skew)

Tail on the left side is longer most data are on the right

Zero Skew (Symmetric)

The data is evenly distributed around the mean (like a normal distribution)

$$\text{Skewness} = \frac{3(\text{mean} - \text{median})}{\text{Standard deviation}}$$

If Value near to -1 then it is -ve Skew

If Value near to +1 then it is +ve Skew

If Value lies in -0.5 to 0.5 then it is Zero Skew

Kurtosis

$$K = \frac{1}{n} \sum_{i=1}^n \left(\frac{x_i - \mu}{\sigma} \right)^4$$

It measures the tailedness or peakness of a distribution

Types of kurtosis

1) Mesokurtic ($k=3$)

- Normal distribution
- No outliers
- Moderate tail and peak.

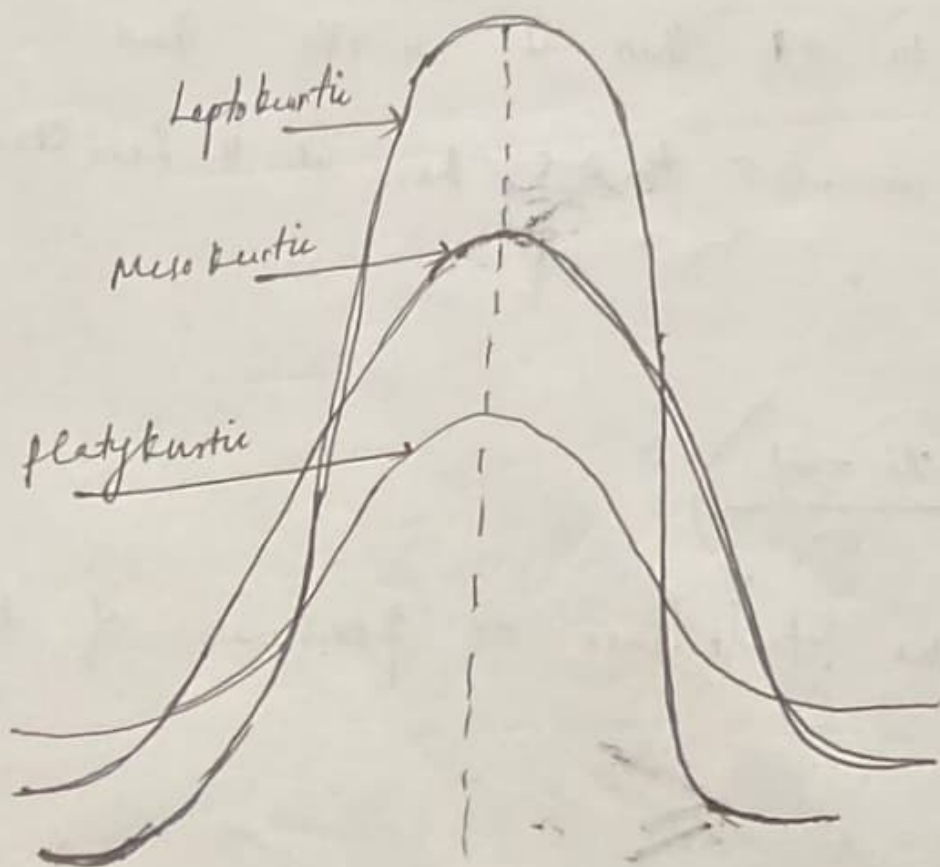
2) Leptokurtic ($k>3$)

- Heavy tails and sharp peak
- more outliers

$$P(X=x) = C(n, k) p^k (1-p)^{n-k}$$

3) platykurtic ($k<3$)

- light tail and flat peak
- fewer outliers



5) poisson distribution

It is used to model the number of event that occur in a fixed time interval or space and occur independently the parameter λ represents the avg number of event in the interval

$$P(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

how many times something happens in a fixed time or area

λ = the avg no of event
 k = no of arguments